

# Low $x$ Hadronic Final State Studies at H I

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# Overview

- Quick Introduction to the low  $x$  issue.
- New results from H1.
- Implications for the LHC.

# Parton Evolution

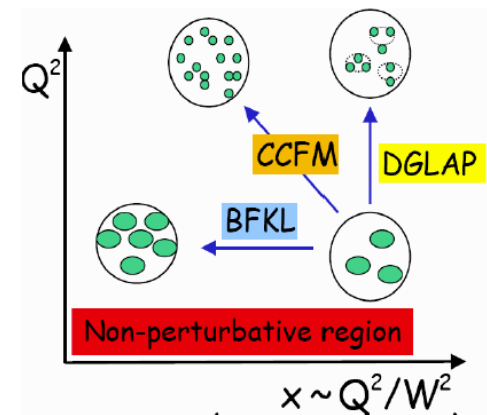
Standard DGLAP approximation, large  $Q^2$ :  
sums terms  $\sim \alpha_s \log Q^2$ , strong ordering in  $k_T$  of  
parton emission (collinear factorisation).

non DGLAP effects  
expected to produce a  
significant enhancement  
of gluon radiation

BFKL evolution equation, low  $x$ :  
sums terms  $\sim \alpha_s \log(1/x)$ , strong ordering in  $x_i$ ,  
no ordering in  $k_T$ , ( $k_T$  factorisation).

Inclusive F2 measurement not  
able to discriminate between  
different QCD approaches.  
Study Hadronic final state.

CCFM equation applicable at all  $x$  and  $Q^2$ :  
includes both  $\alpha_s \log Q^2$  and  $\alpha_s \log(1/x)$  terms.  
implements angular ordering resulting from  
QCD interference effects

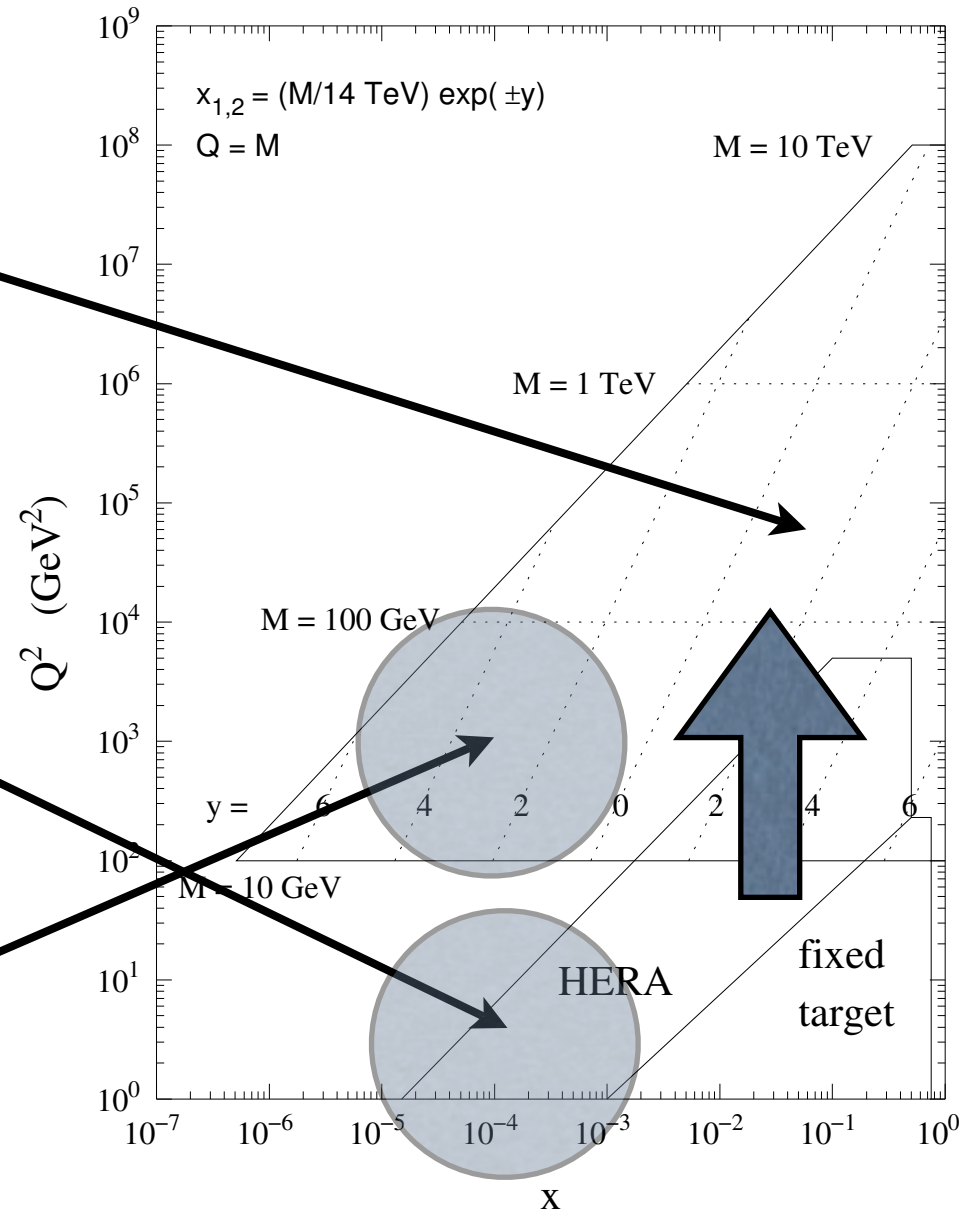


# Low x Domain

Conventional DGLAP  
QCD approach  
evolves with Q

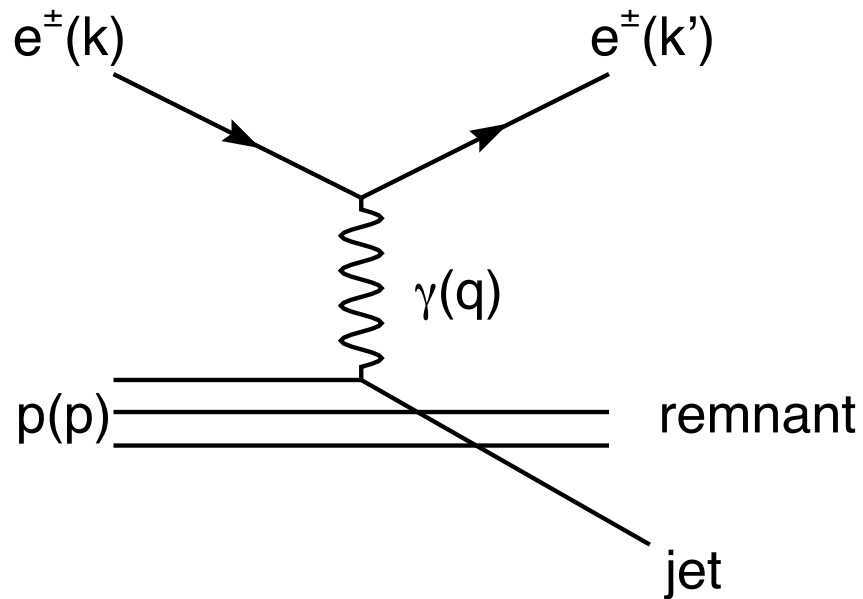
Possibility of non DGLAP  
behaviour of the parton  
evolution at HERA

What does this mean  
for the LHC?



# DIS and HERA

## Kinematic Variables:



$$Q^2 = -q^2 = -(k - k')^2 \quad \text{Momentum transfer}$$

$$x = \frac{Q^2}{2p \cdot q}$$

Fraction of the proton's momentum that participates in the hard scatter

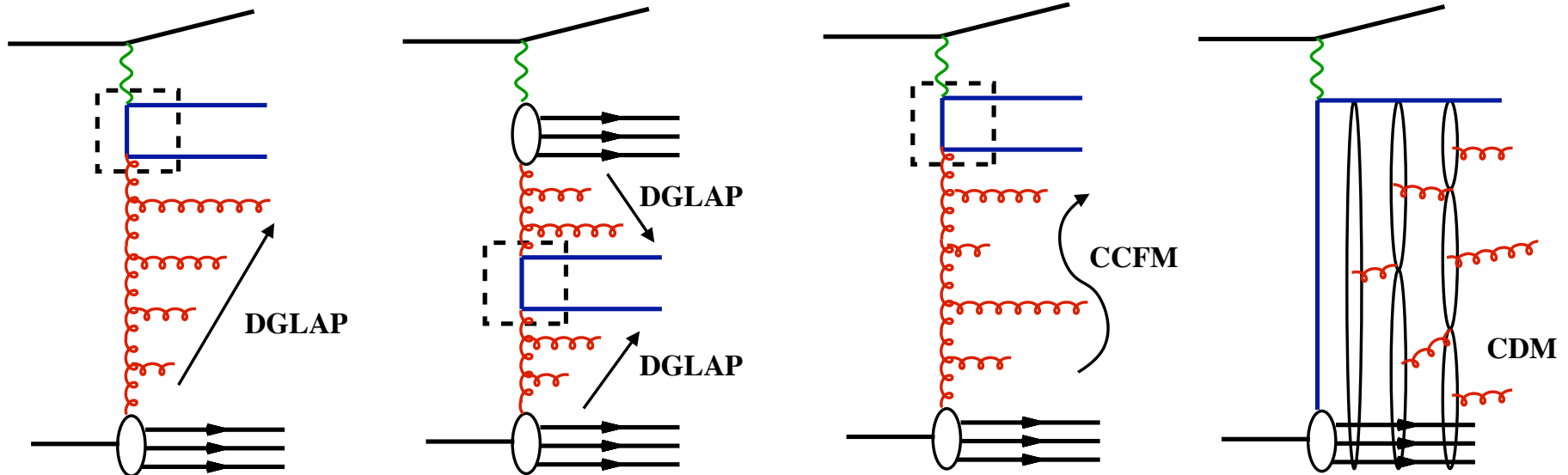
$$y = \frac{p \cdot q}{p \cdot k}$$

Fraction of the electron's energy available in the proton's rest frame

$$Q^2 = sxy$$

$s$  = center of mass energy squared

# Monte Carlos for DIS



Rapgap  
(dir)

Rapgap  
(dir+res)

Cascade

Ariadne

Strong ordering in  $k_t$   
of emitted partons

CCFM resumes both  
 $\log(Q^2)$  and  $\log(1/x)$   
angular ordering

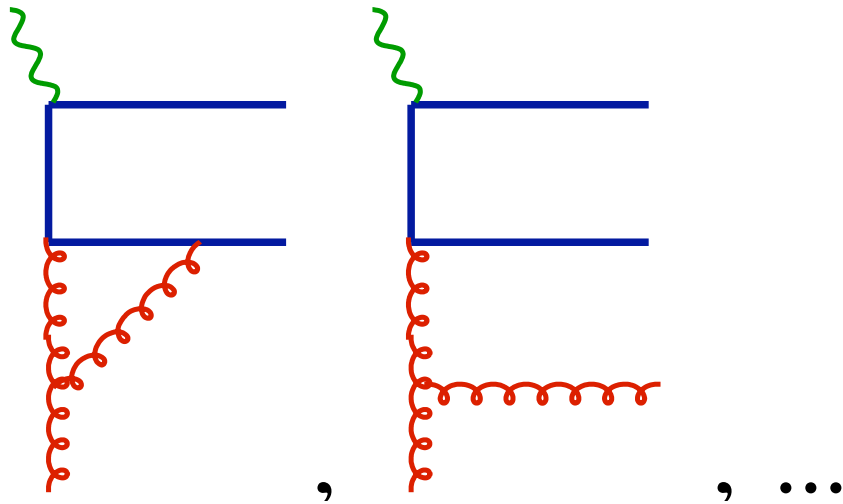
Dipoles radiate  
independently

as is PYTHIA and HERWIG

# NLO QCD Calculations

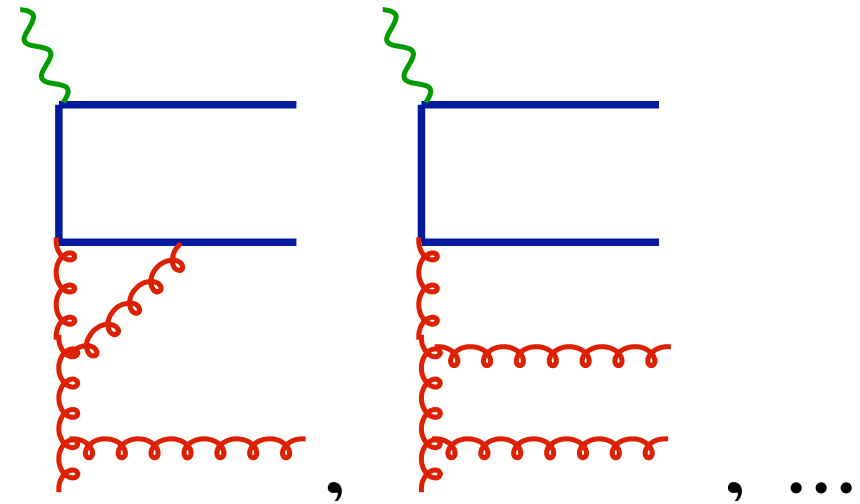
NLOJET++,  
DISENT

NLO 2-jet



NLOJET++

NLO 3-jet



Scale  $\mu_r = \mu_f = Q$  or  $E_t$  or some similar combination

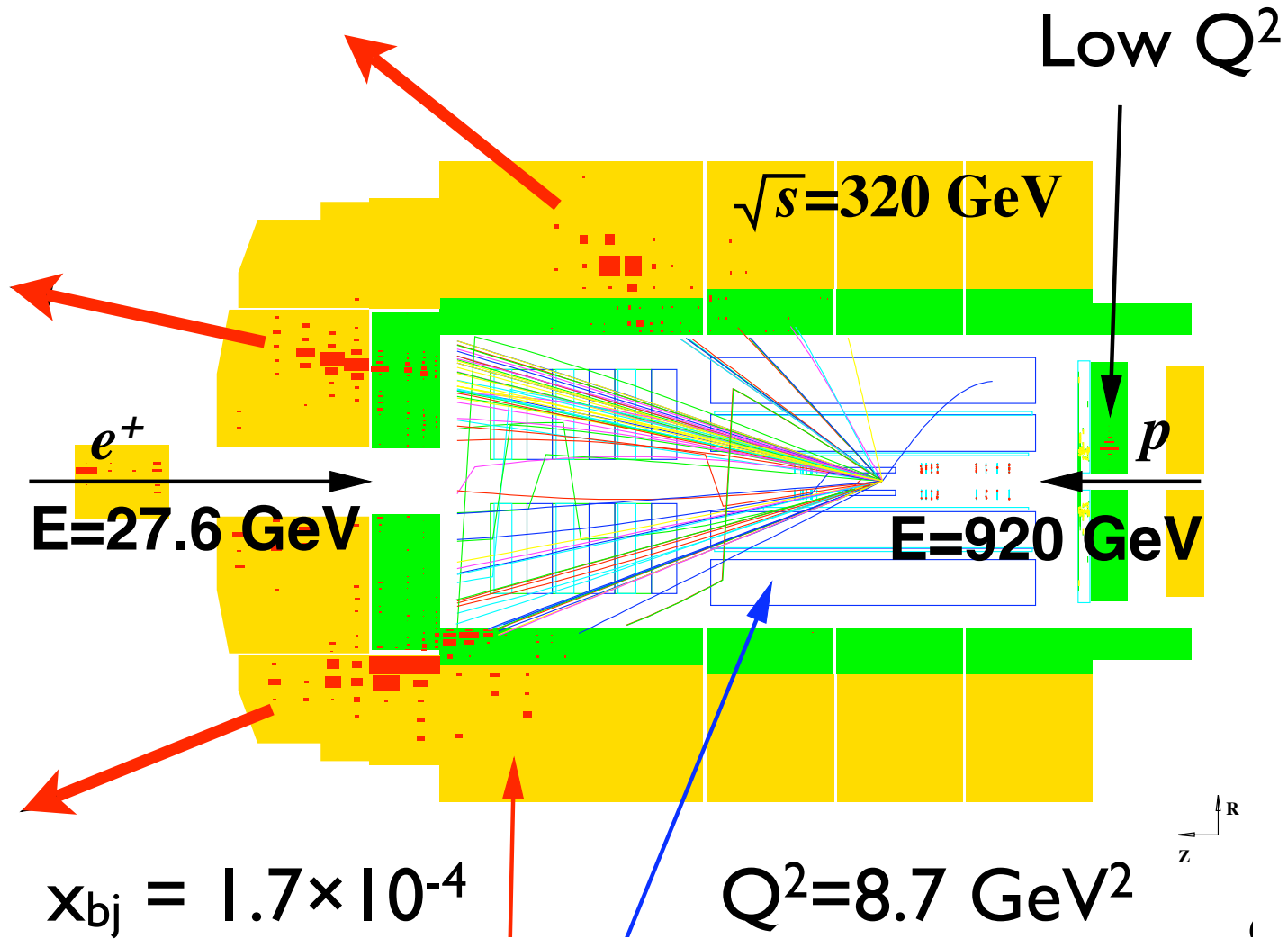
Scale Uncertainty  $1/2 \mu_{r,f} < \mu_{r,f} < 2\mu_{r,f}$ , changing both scales simultaneously

PDF : CTEQ, MRST, HI, ZEUS

Hadronisation correction from Monte Carlo



# HI

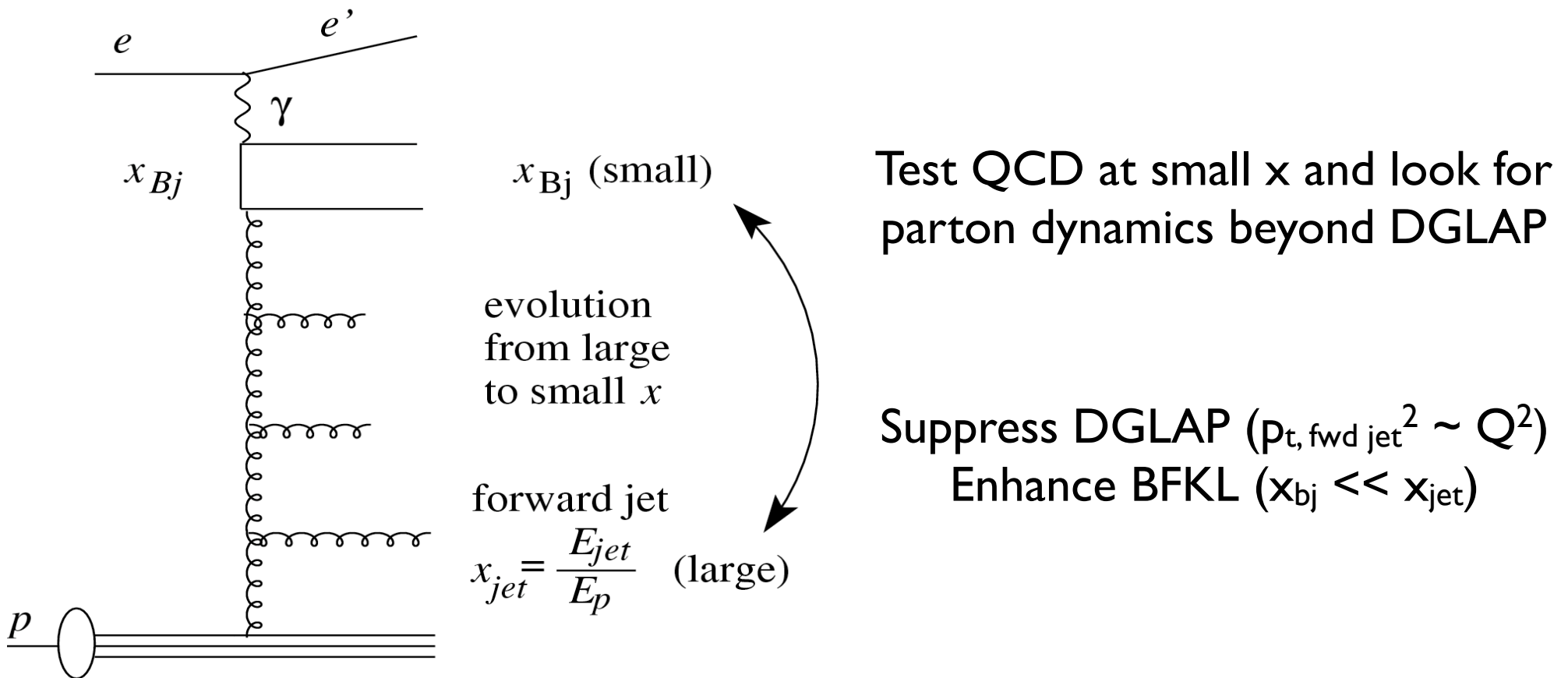


Jets measured by tracking and calorimeters

$$-1 < \eta_{\text{jet}} < 2.8$$

# Forward Jets in DIS

# Forward Jet Production



Forward jets = jets away from hard interaction.

DGLAP (ordered  $kt$ ) - soft parton emissions

BFKL (non-ordered  $kt$ ) - more (harder) jets

# Forward Jet Production

Kinematic selection:

$$5 < Q^2 < 85 \text{ GeV}^2$$

$$0.1 < y < 0.7$$

$$0.0001 < x_{bj} < 0.004$$

1997 data  $L=13.7 \text{ pb}^{-1}$

$$E_p=820, E_e=27.6$$

$$\sqrt{s} \approx 300 \text{ GeV}$$

Forward jet selection:

Inclusive kt-algorithm in Breit frame

$$1.75 < \eta_{\text{jet}} < 2.8$$

$$P_{t,\text{jet,lab}} > 3.5 \text{ GeV}$$

$$x_{\text{jet}} = E_{\text{jet}}/E_p > 0.035$$

$$0.5 < p_{t,\text{jet}}^2/Q^2 < 5$$

if  $N_{\text{jet}} > 1$ , choose highest  $\eta_{\text{jet}}$

# Forward Jet Production

DISENT LO ( $\alpha_s$ ) and NLO ( $\alpha_s^2$ ):

$$\mu_r^2 = p_t^2$$

$$\mu_f^2 = \langle p_{t,\text{fwdjet}}^2 \rangle = 45 \text{ GeV}^2$$

$$0.25\mu_{r,f}^2 < \mu_{r,f}^2 < 4\mu_{r,f}^2$$

$$(1 + \delta_{\text{HAD}})$$

NLO below data

LO  $\ll$  NLO

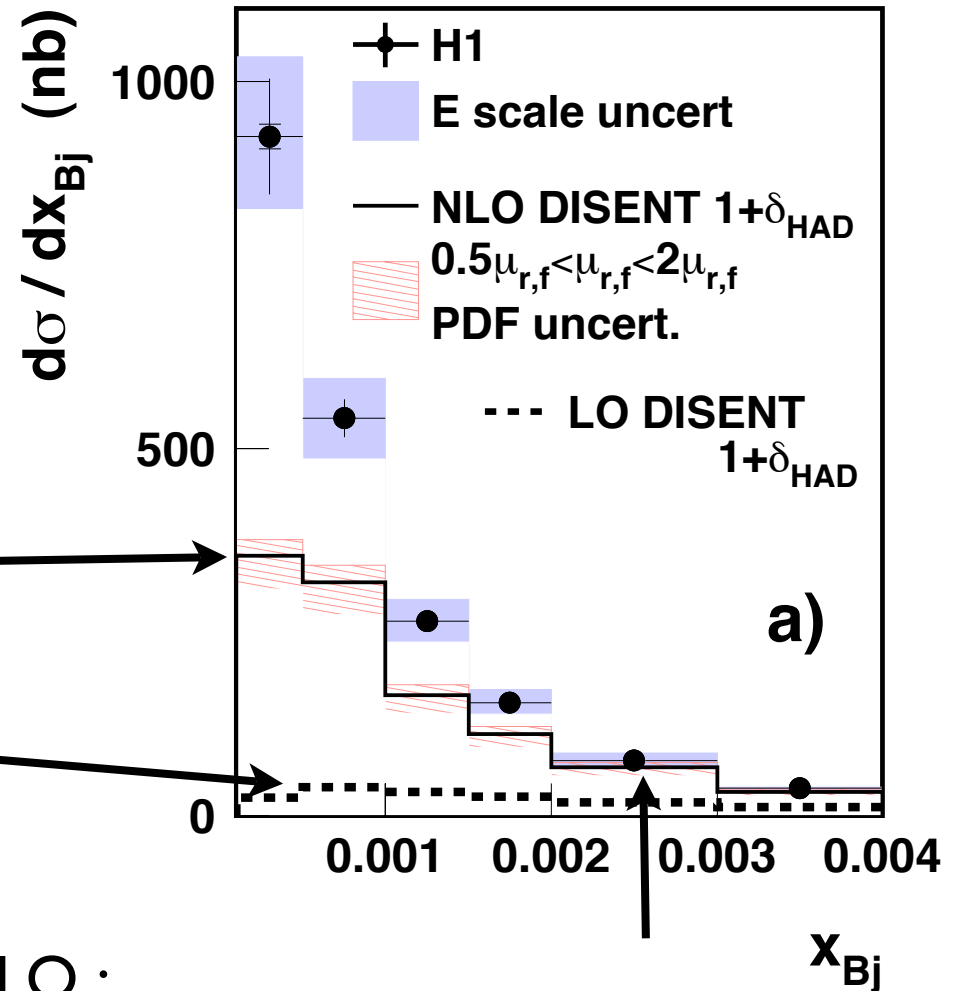


large difference between LO and NLO :

scale error underestimated?

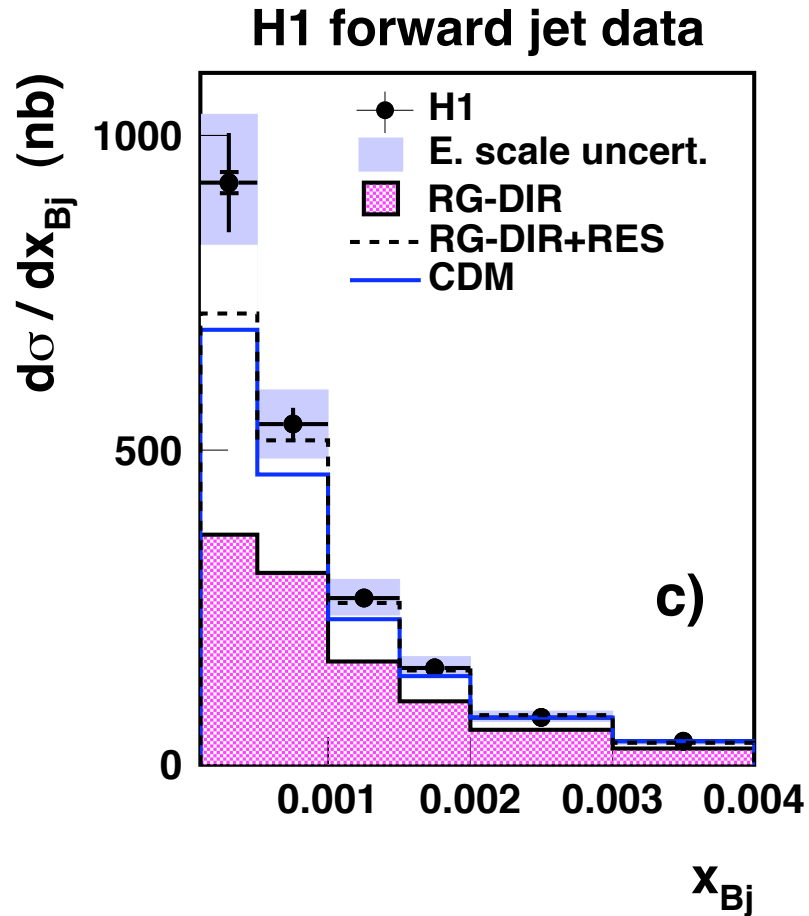
Is this really an inclusive cross section?

H1 forward jet data

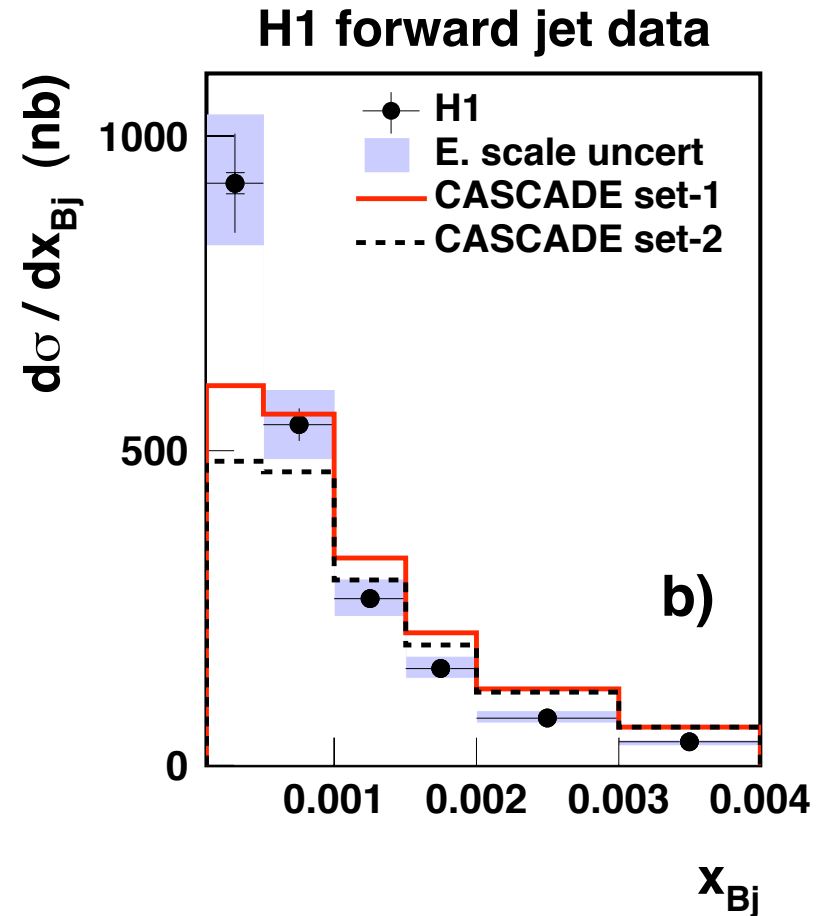


NLO better here

# Forward Jet Production



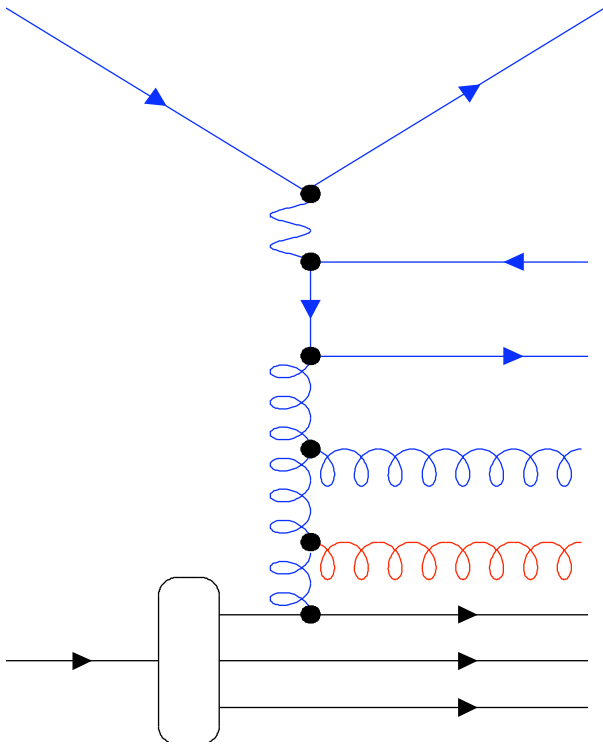
RAPGAP direct fails,  
 addition of resolved photon  
 processes improves description.  
 CDM prediction also better.



CASCADE fails to describe spectrum.  
 Differences between different updfs.  
 Harder spectrum  
 (only gluon initiated processes?)

Three Jets in DIS

# Three Jet Production



For events with three or more jets, at least one jet should come from gluon radiation

Should be sensitive to the dynamics of gluon radiation

Provides a more testing environment to compare with theory



# Three Jet Production

Kinematic selection:

$$10^{-4} \leq x_{bj} \leq 10^{-2}$$

$$5 \leq Q^2 \leq 80 \text{ GeV}^2$$

$$0.1 < y < 0.7$$

99/2000 data  $L = 44.2 \text{ pb}^{-1}$

$$E_p = 920, E_e = 27.6$$

$$\sqrt{s} \approx 318 \text{ GeV}$$

Three Jet Selection:

Inclusive kt-algorithm in  $\gamma^*p$  rest frame

$$E_{\perp, \text{jet}} > 4 \text{ GeV}$$

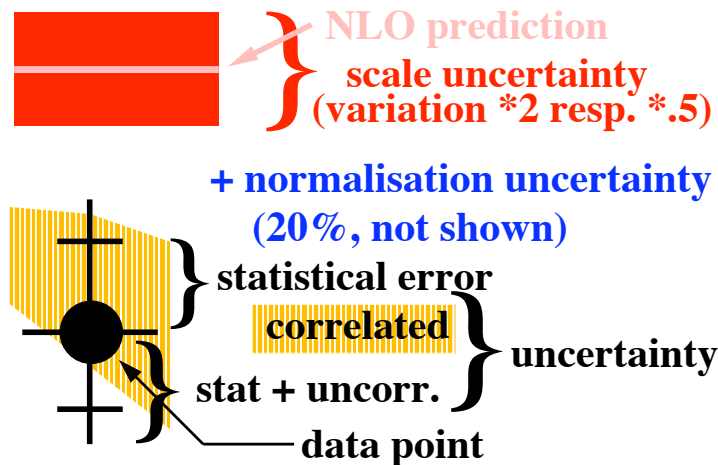
$$-1 < \eta_{\text{jet,lab}} < 2.5$$

$$N_{\text{jet}} \geq 3$$

$$E_{\perp 1} + E_{\perp 2} > 9 \text{ GeV}$$

one jet in range  $-1 < \eta_{\text{jet,lab}} < 1.3$

# Three Jet Production



$$O(\alpha^2) \rightarrow O(\alpha^3)$$

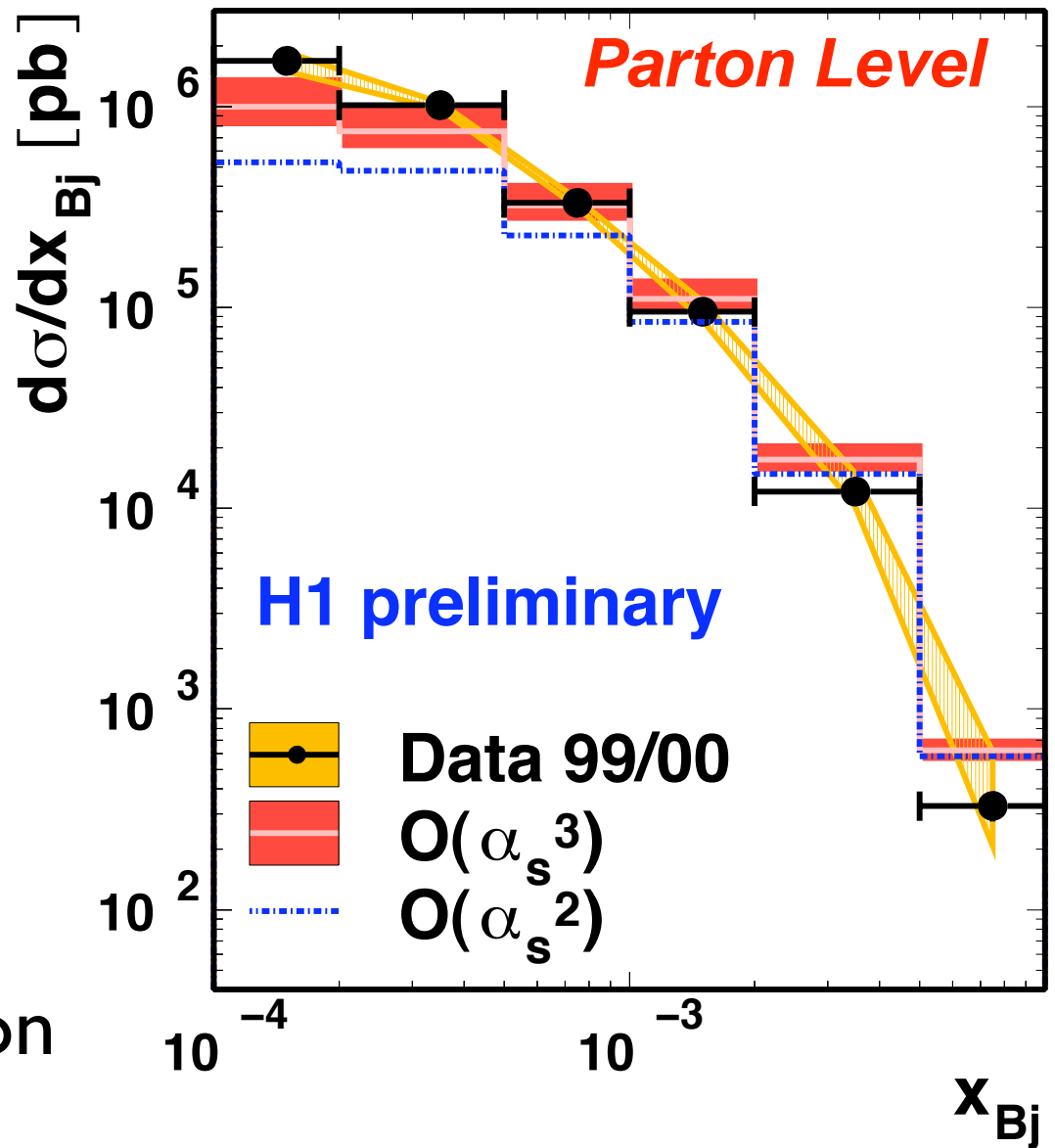
up to 3 jets

up to 4 jets

$\times 3.3$

$\times 1.7$

at low  $x$



Improvement in description especially at low  $x_{bj}$

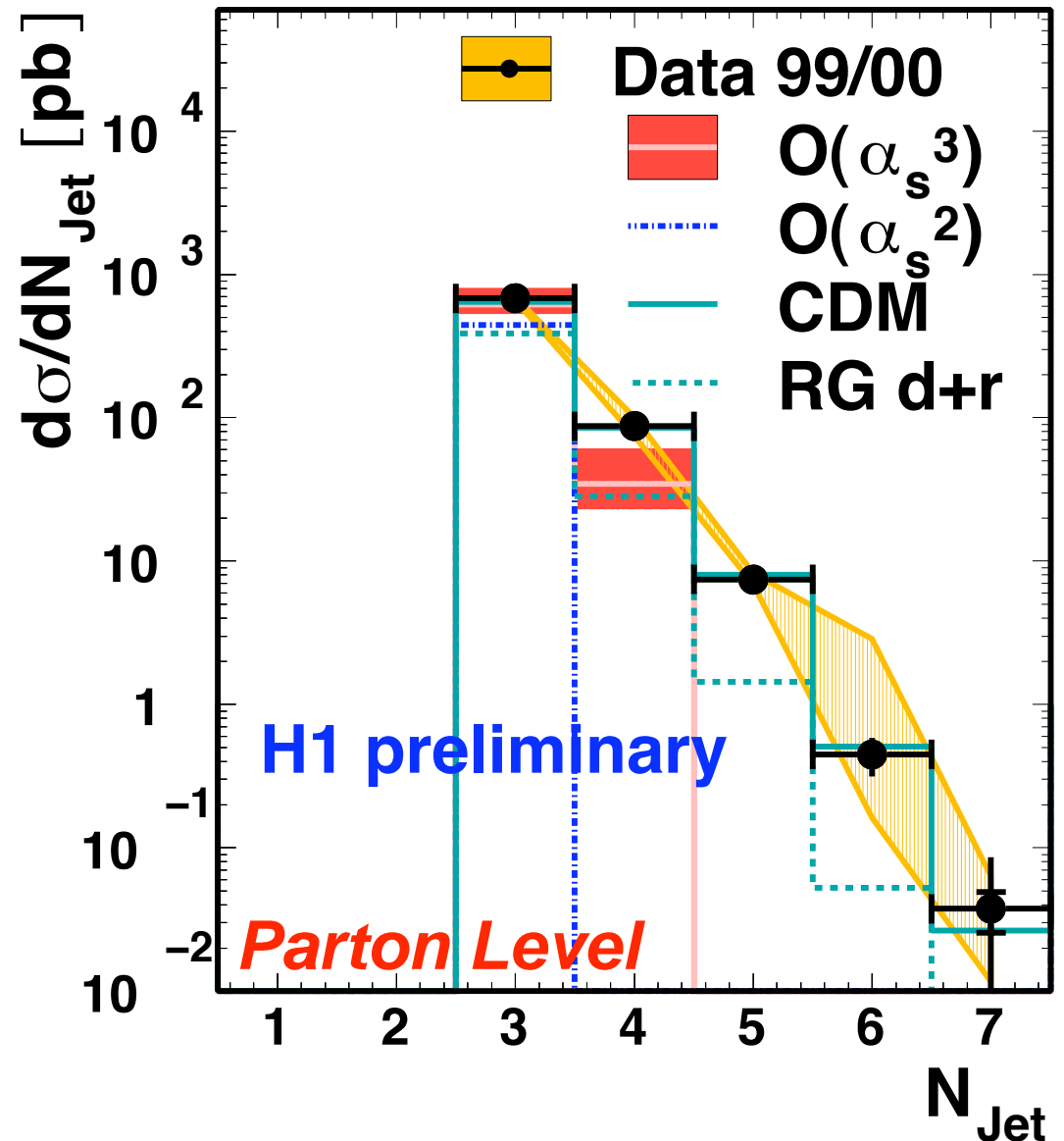
# Three Jet Production

For 3 jets  $\mathcal{O}(\alpha^3)$  = data

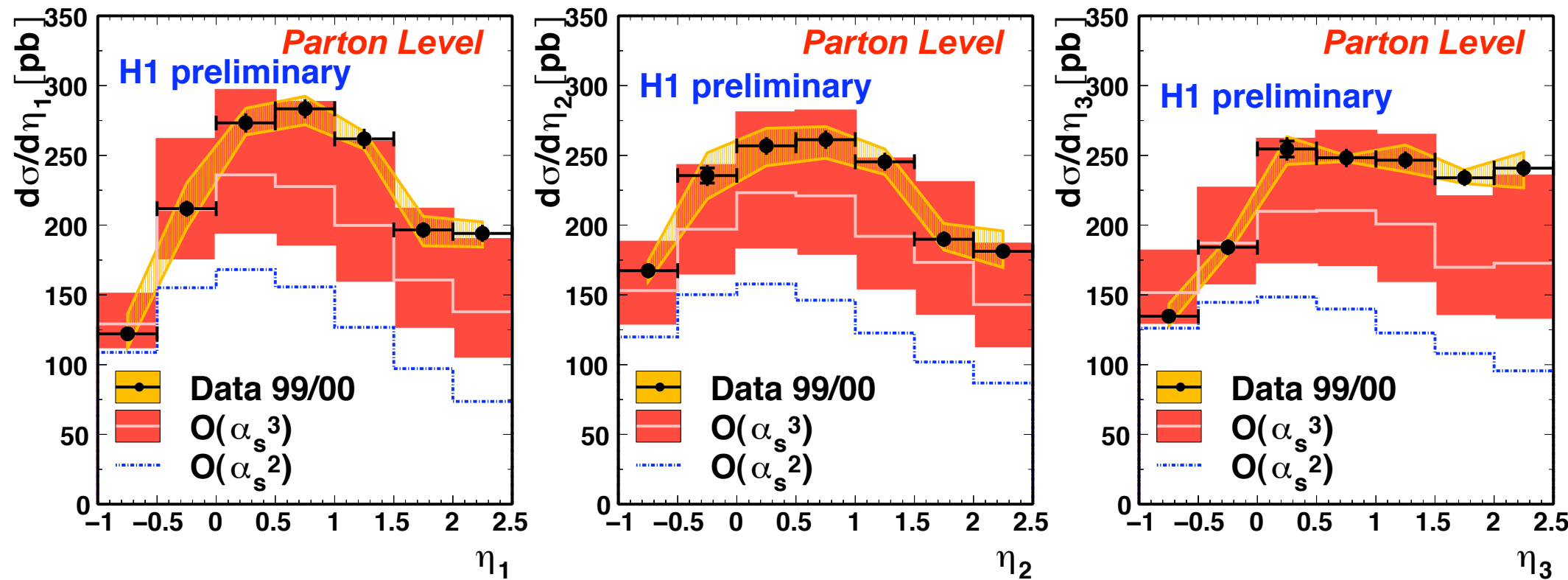
$\mathcal{O}(\alpha^3)$  misses ~20% of events with 4 or more jets

**CDM** gives excellent description

**RAPGAP** fails even for 3 jets



# Three Jet Production

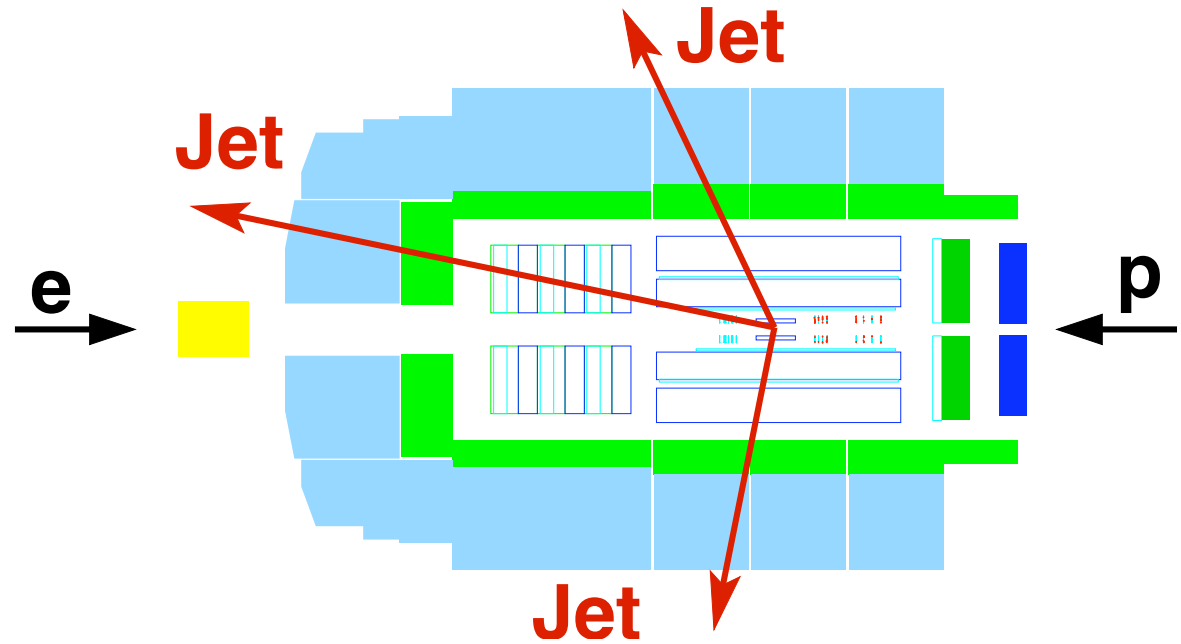


Main discrepancies at low  $x$  and large  $\eta$  (forward region)

Other distributions are well described apart from  $\sim 20\%$  normalisation difference

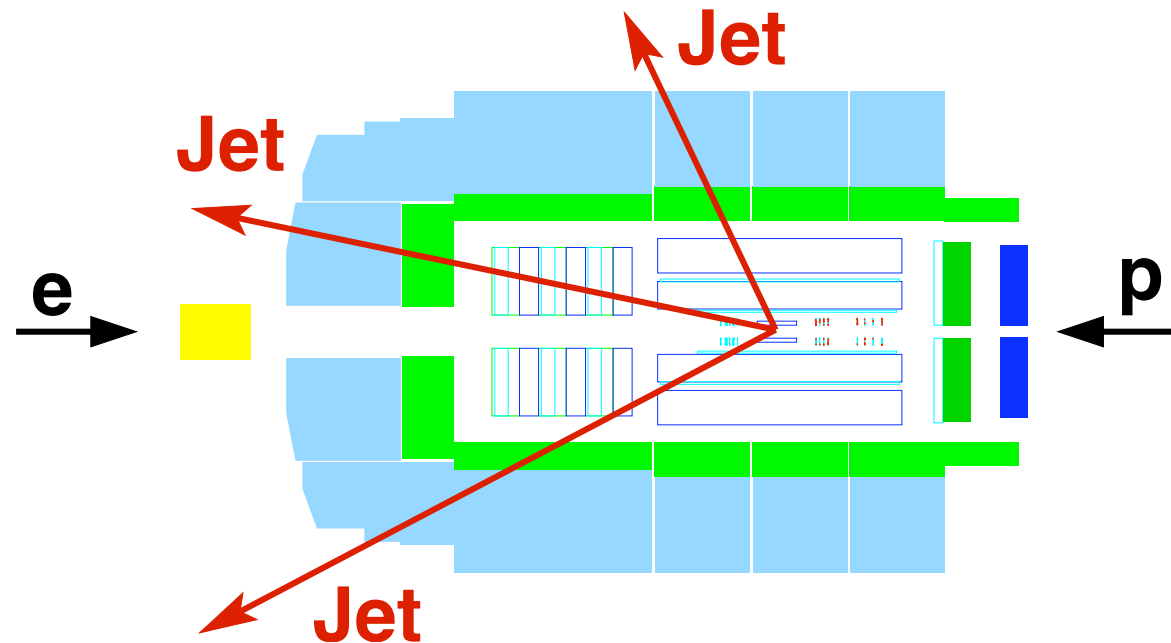
# Three Jet Production

Two central jets

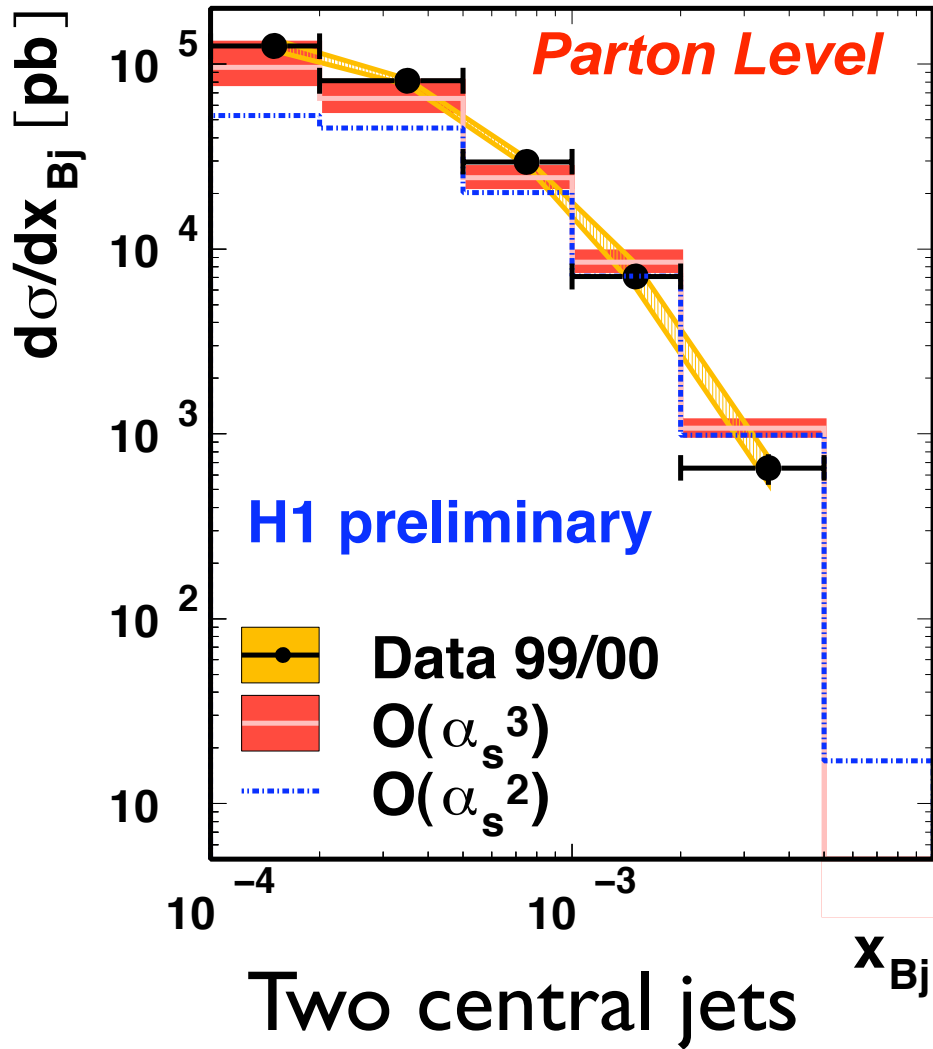


Forward jet selection:  
 $\eta_{\text{jet}} > 1.75, x_{\text{jet}} > 0.035$

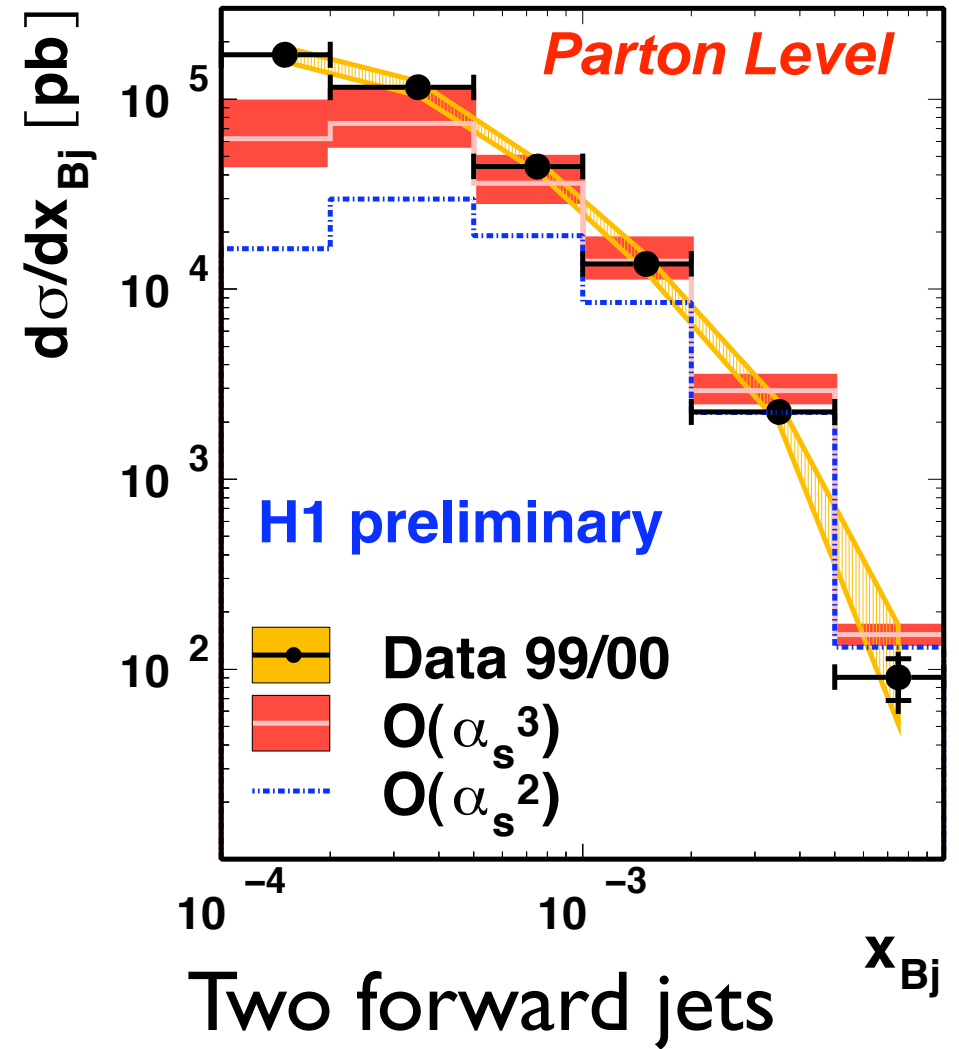
Two forward jets



# Three Jet Production



reasonably well described



Data =  $O(\alpha^2) \times 10$

Data =  $O(\alpha^3) \times 3.5$

at low  $x$

# Three Jet Production

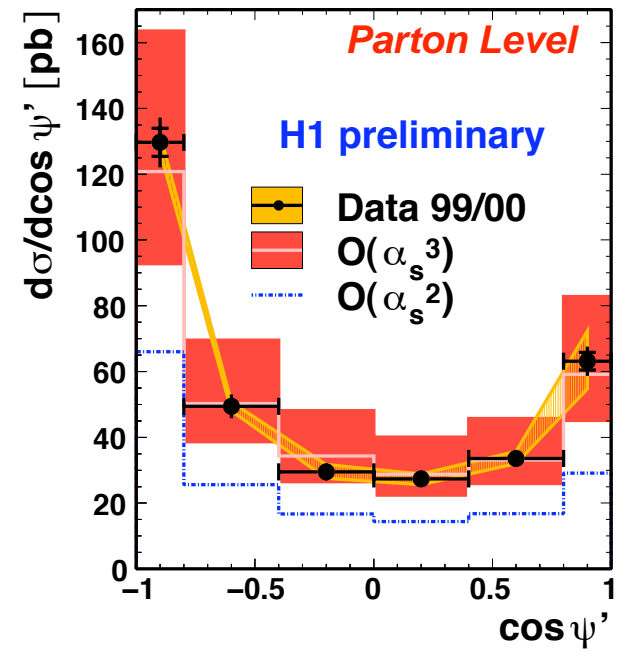
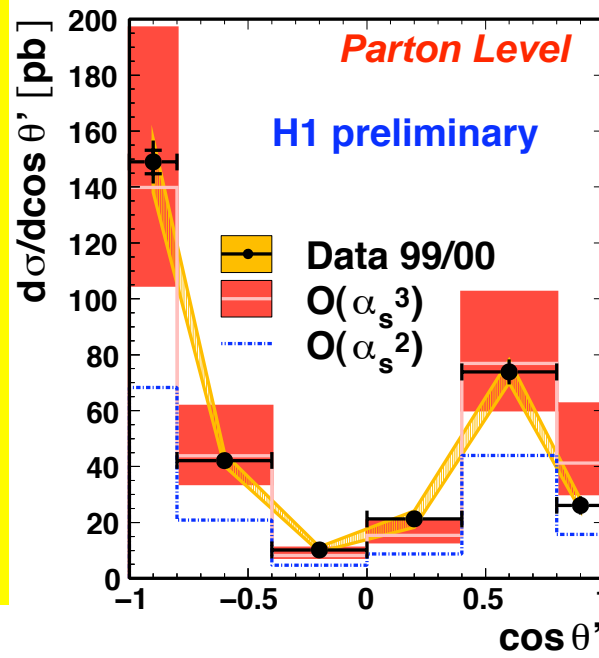
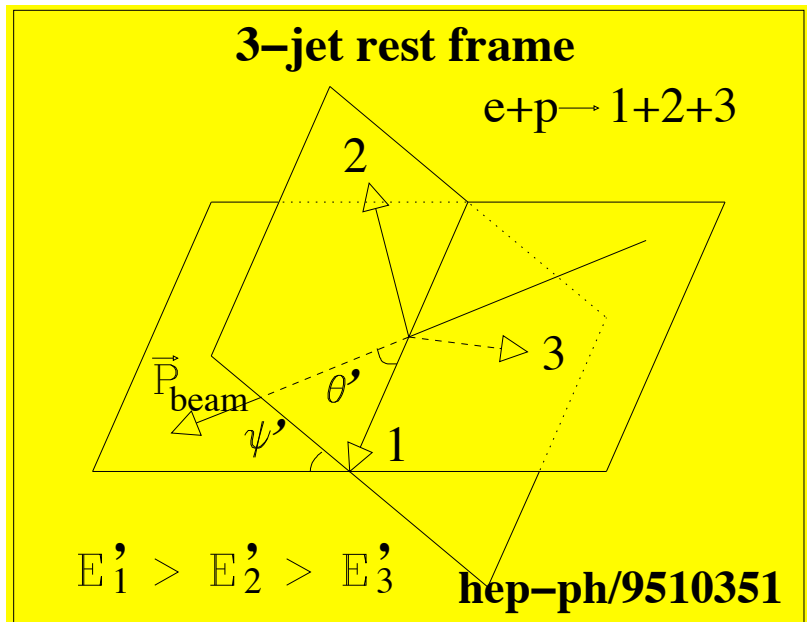
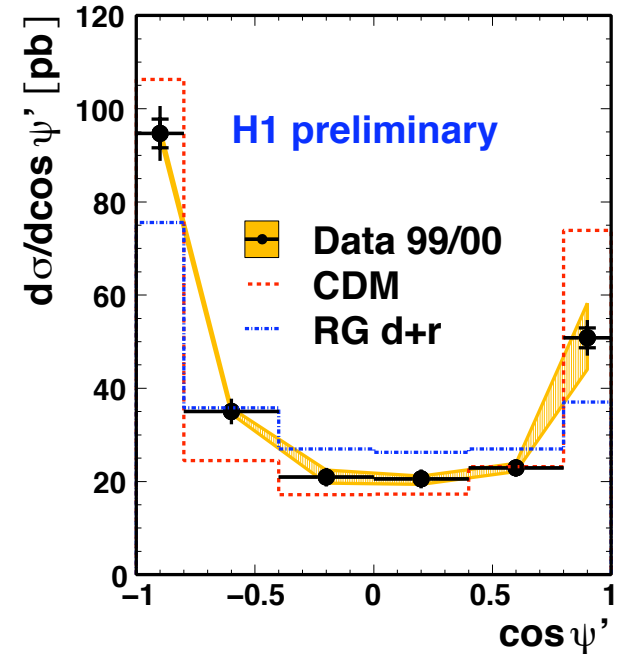
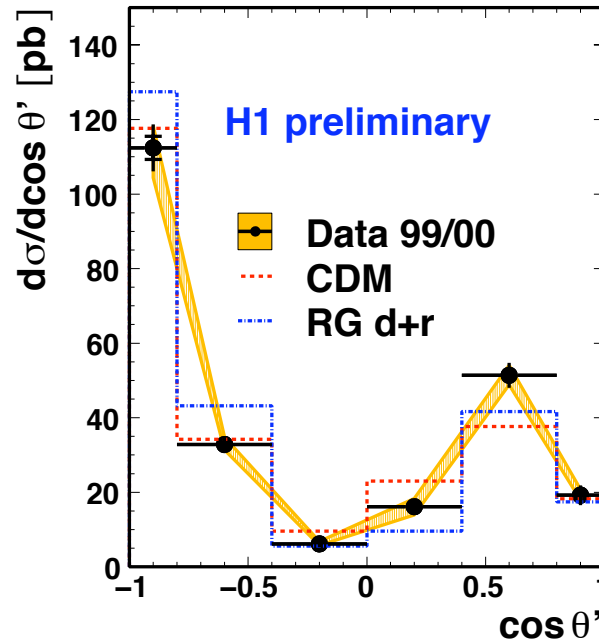
Two forward jets

compare shapes:

$O(\alpha^2)$ ,  $O(\alpha^3) \times 1.34$

Rapgap  $\times 1.74$

CDM  $\times 1.08$



# Dijet Azimuthal Correlations in DIS



# Dijet Azimuthal Correlations

DGLAP:

In LO gluon collinear with proton  
 $k_{t,g}=0$ , Jets back-to-back in HCM,  $\Delta\phi^*=180^\circ$

Higher order QCD radiation

$k_{t,g}\neq 0$ ,  $\Delta\phi^* < 180^\circ$

Gluon emissions ordered in virtuality

$k_{t,g}$  ordered

BFKL, CCFM:

unordered  $k_{t,g}$

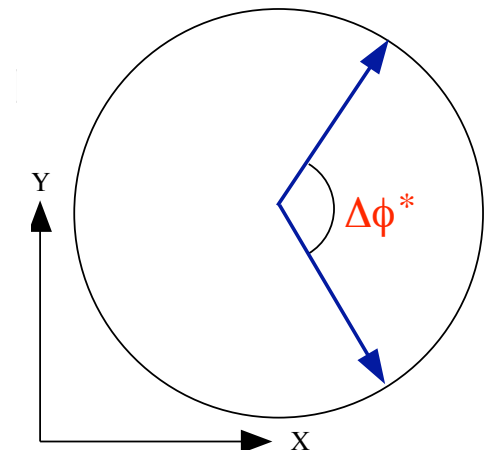
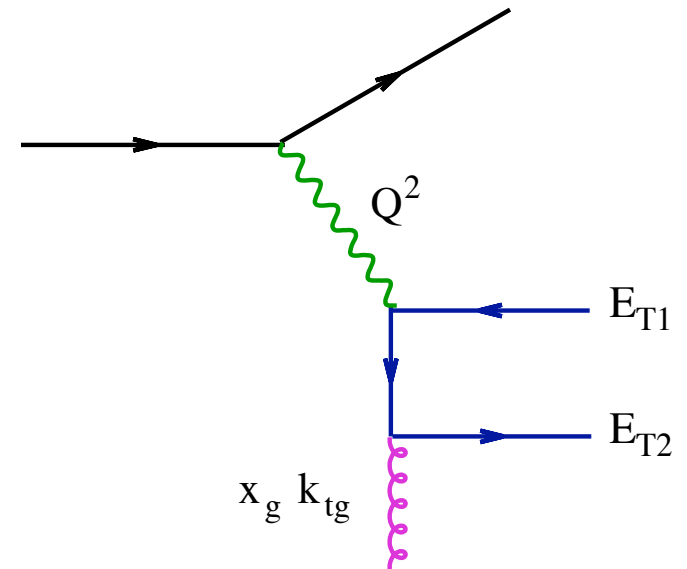
Broader  $\Delta\phi^*$  compared to DGLAP

sensitive to unintegrated (u)PDF

$\Delta\phi^* < 180^\circ$  at LO!

Sensitive to different parton dynamics

Sensitive to unintegrated gluon density

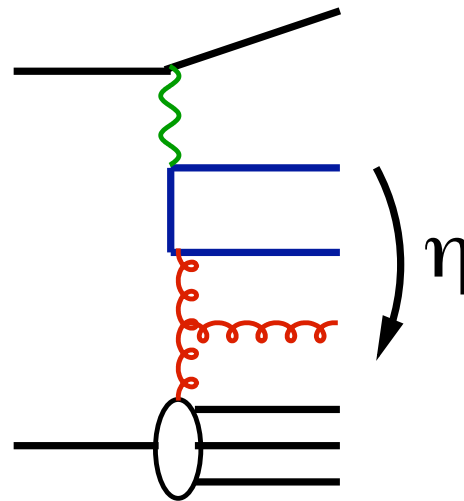


# Dijet Azimuthal Correlations

Kinematic Selection:  
 $5 < Q^2 < 100 \text{ GeV}^2$   
 $0.1 < y < 0.7$

99/2000 data  $L = 64.3 \text{ pb}^{-1}$   
 $E_p = 920, E_e = 27.6$   
 $\sqrt{s} \approx 318 \text{ GeV}$

Dijet Selection:  
Inclusive Kt-algorithm  
 $E_{\perp \text{jet}}^* > 5 \text{ GeV}$   
 $-1 < \eta_{\text{lab}} < 2.5$



Two jets closest in  $\eta$  to the scattered electron chosen as the dijet system

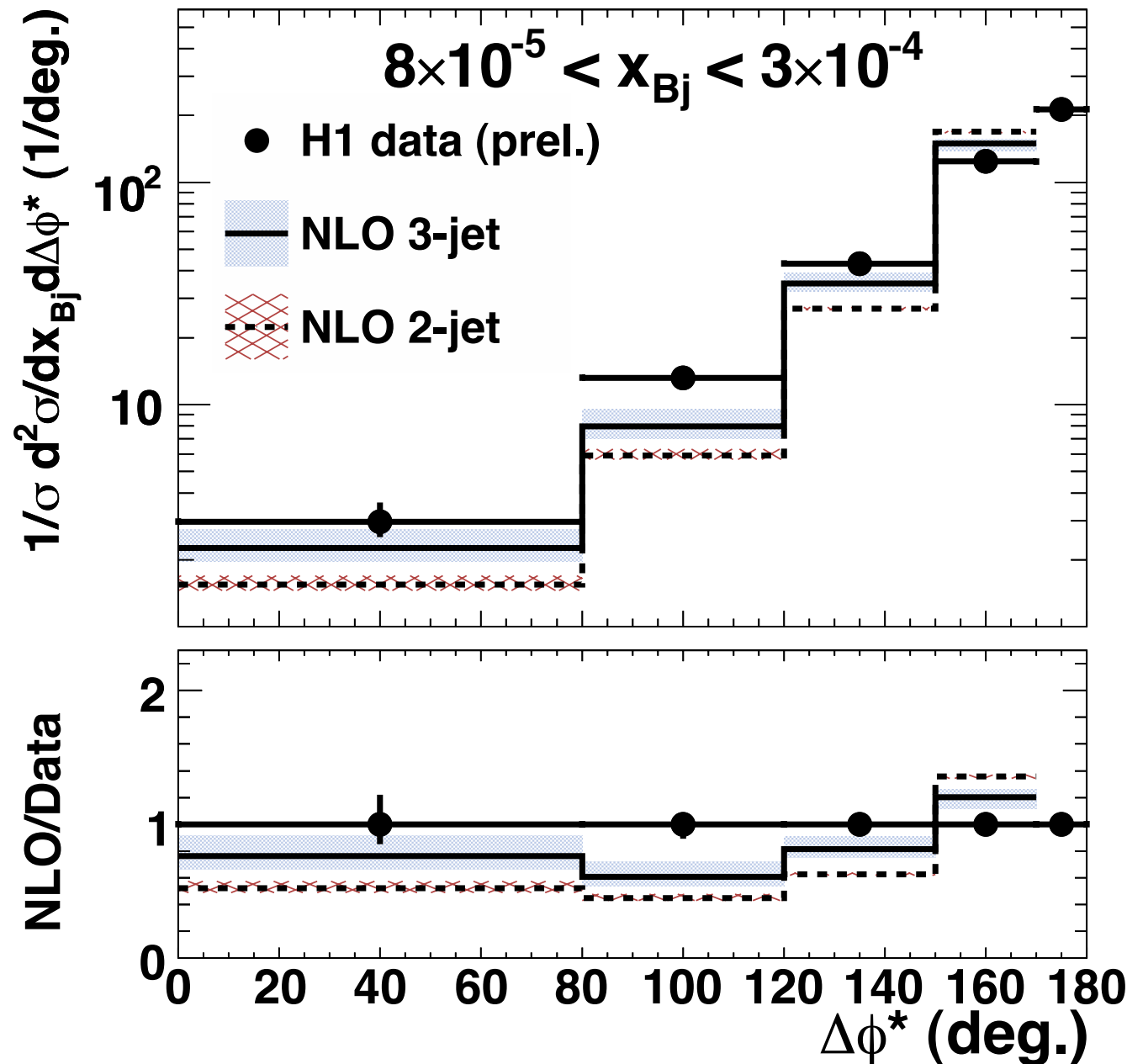
# Dijet Azimuthal Correlations

Infrared sensitivity, no NLO  
for  $\Delta\phi^* \sim 180^\circ$

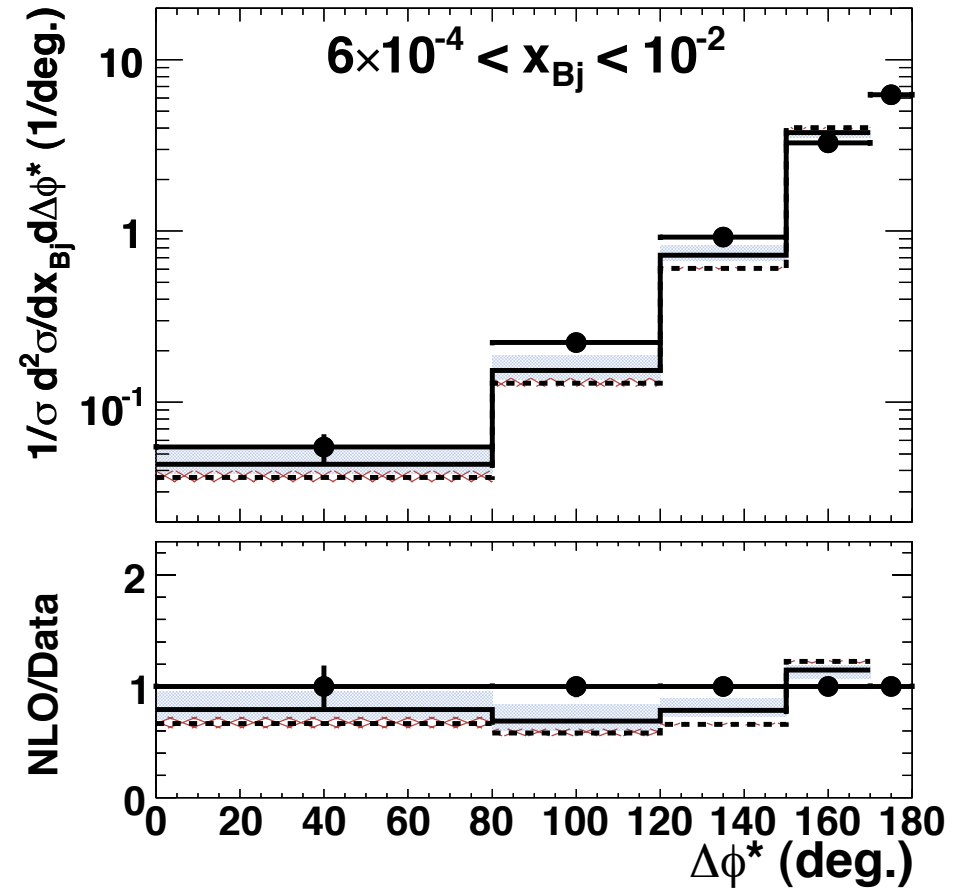
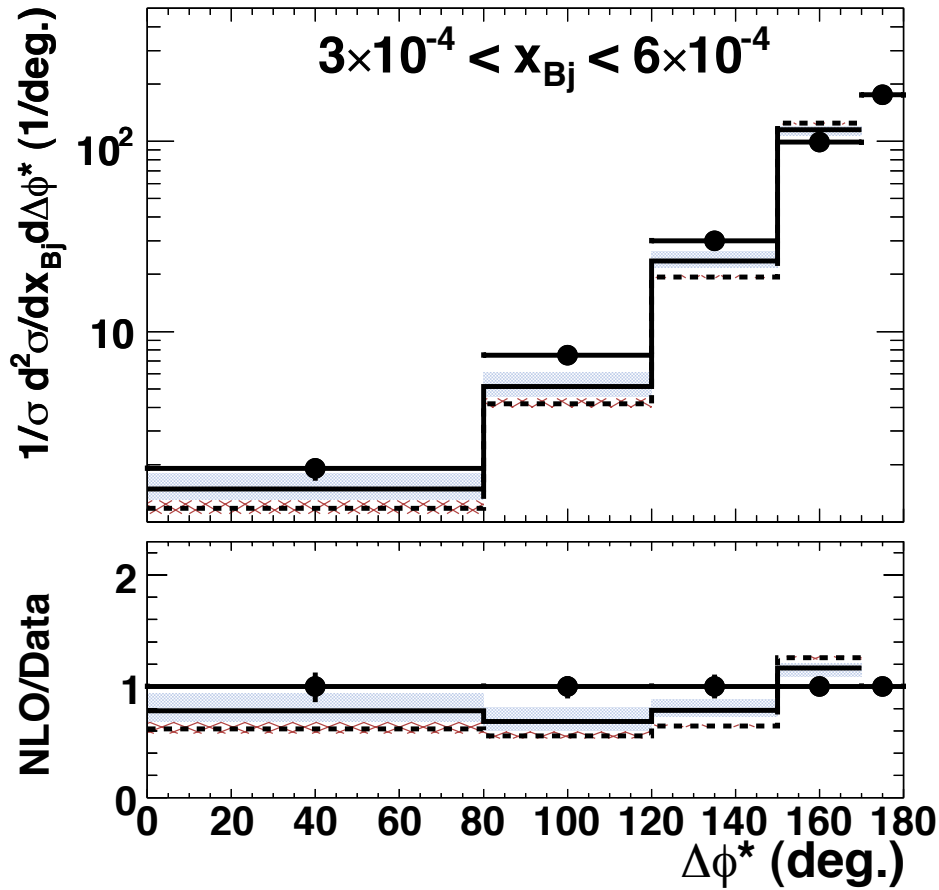
Normalise to visible cross  
section to reduce scale  
uncertainties (<20%)

NLO 2 jet ( $\alpha_s^2$ ) fails  
~ effectively LO

NLO 3 jet ( ) better  
but still systematically  
below data for  
 $\Delta\phi^* < 160^\circ$

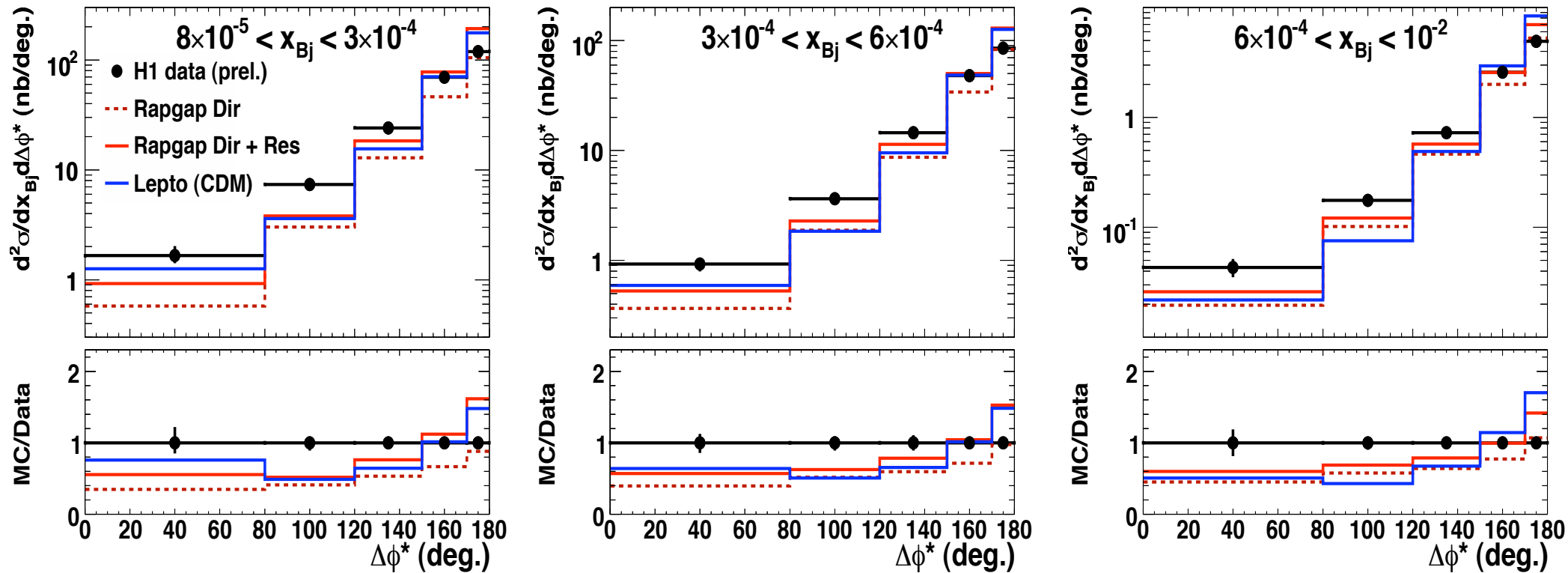


# Dijet Azimuthal Correlations



Similar story at higher  $x_{bj}$ !

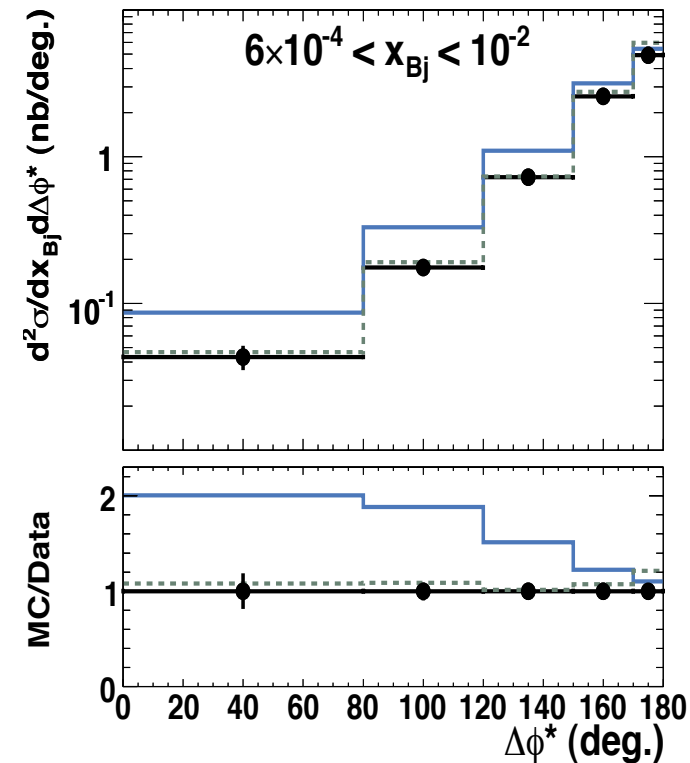
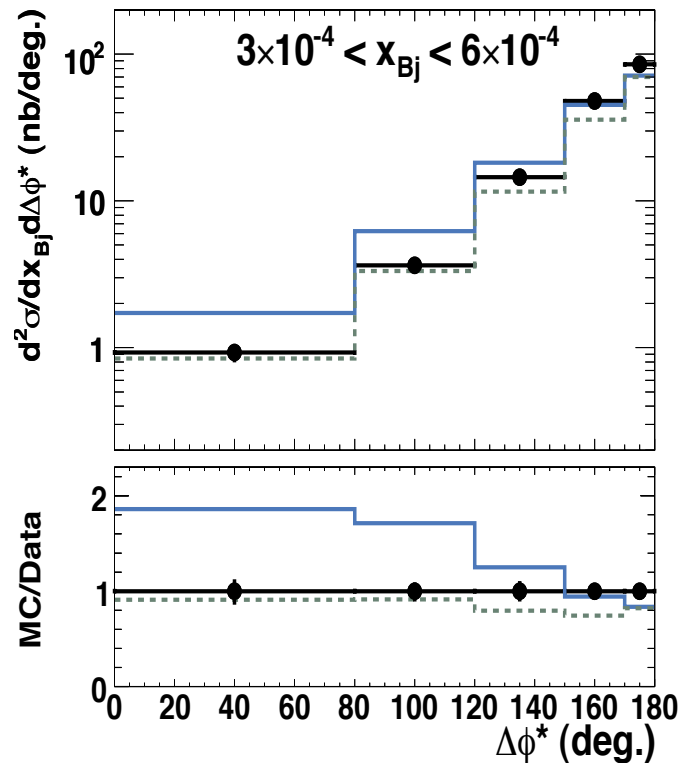
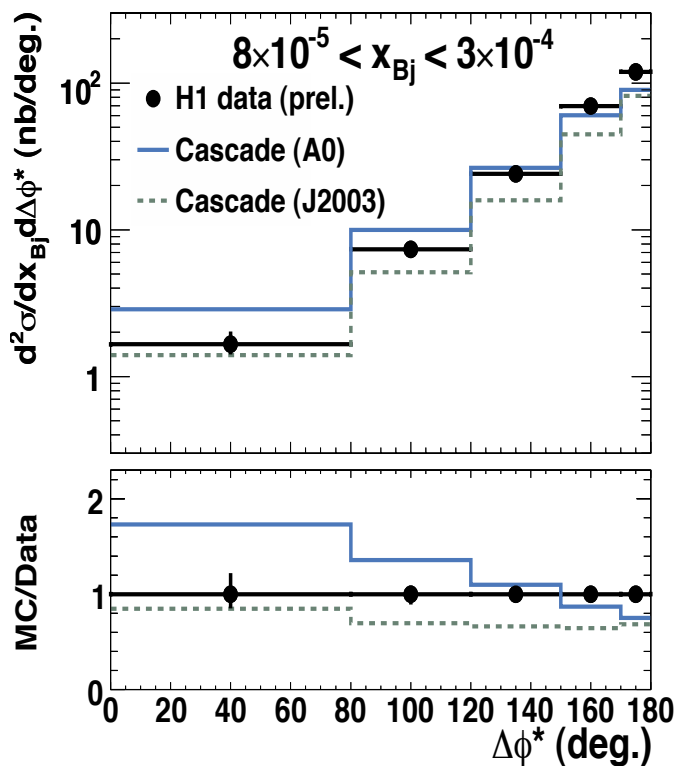
# Dijet Azimuthal Correlations



Rapgap (direct) describes back-to-back ( $\Delta\phi^* = 180^\circ$ ) jets

Rapgap (dir+res) and CDM give too many back-to-back jets and too few small  $\Delta\phi$  dijets

# Dijet Azimuthal Correlations



Sensitivity to unintegrated gluon density

Cascade J2003 much better than A0 (too hard)

Cascade + J2003 gives best description of any model

# Summary

- $O(\alpha^3)$  huge improvement compared to  $O(\alpha^2)$  predictions.
- Rapgap (direct fails)  $\rightarrow$  ordered gluon radiation.
- Rapgap (direct + resolved) is better but it still fails  $\rightarrow$  ordered gluon radiation.
- In general CDM gives best description of the data (even in normalisation)  $\rightarrow$  unordered gluon radiation.
- Cascade expect improvements with new updf fits including new data.
- Non DGLAP dynamics clearly favoured by hadronic final state measurements at low  $x$ .

# Results in full

- Measurement of Dijet Production at Low  $Q^2$  at HERA (H1 Collab., A. Aktas et al., Eur. Phys. J. C37 (2004) 141-159). [hep-ex/0401010](#)
- Inclusive Dijet Production at Low Bjorken- $x$  in Deep Inelastic Scattering (H1 Collab., A. Aktas et al., Eur. Phys. J. C33 (2004) 477). [hep-ex/0310019](#)
  - See also: QCD Analysis of Dijet Production at Low  $Q^2$  at HERA (J. Chýla et al., [hep-ph/0501065](#)).
- Forward  $\pi^0$  Production and Associated Transverse Energy Flow in Deep-Inelastic Scattering at HERA (H1 Collab., A. Aktas et al., Eur. Phys. J. C36 (2004) 441-452). [hep-ex/0404009](#)
  - See also: B.A. Kniehl, G. Kramer and M. Maniatis, Nucl. Phys. B711, 345 (2005); B720, 231(E) (2005). 8.A. and Daleo, D. de Florian and R. Sassot, Phys. Rev. D71, 034013 (2005).
- Forward Jet Production in Deep Inelastic Scattering at HERA (H1 Collab., A. Aktas et al., Eur. Phys. J. C46 (2006) 27-42). [hep-ex/0508055](#)
  - See also: Forward jet production in deep inelastic ep scattering and low- $x$  parton dynamics at HERA (ZEUS Collaboration; S. Chekanov et al. Letters B 632 (2006) 13-26).
- 3-jet cross sections at low  $x$  and  $Q^2$  (H1prelim-06-034). DIS06
- Azimuthal correlations in dijet events at low  $Q^2$  DIS (H1prelim-06-032). DIS06

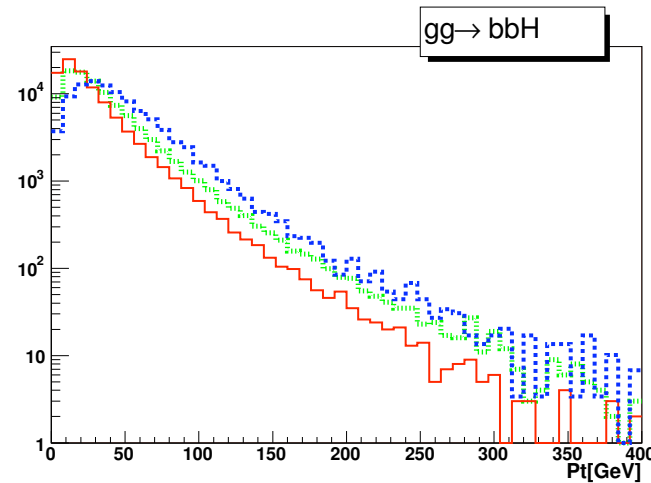
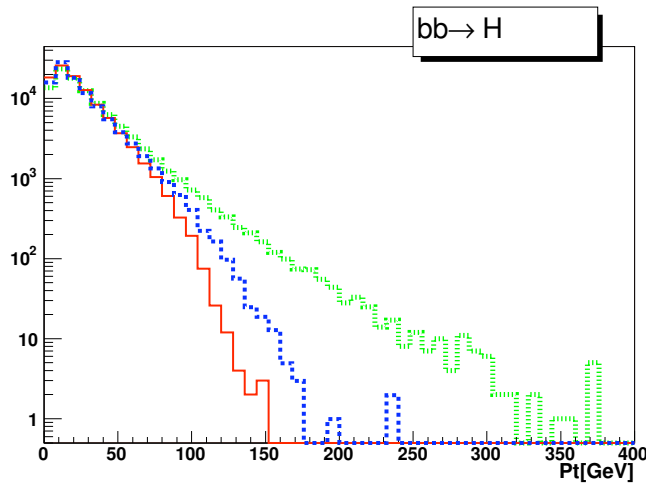
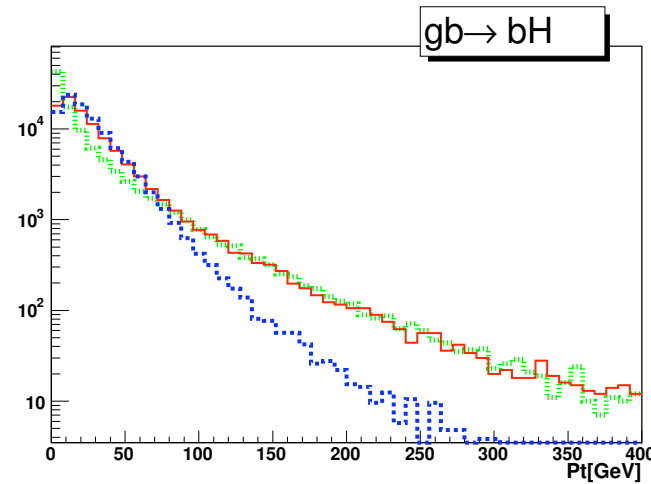
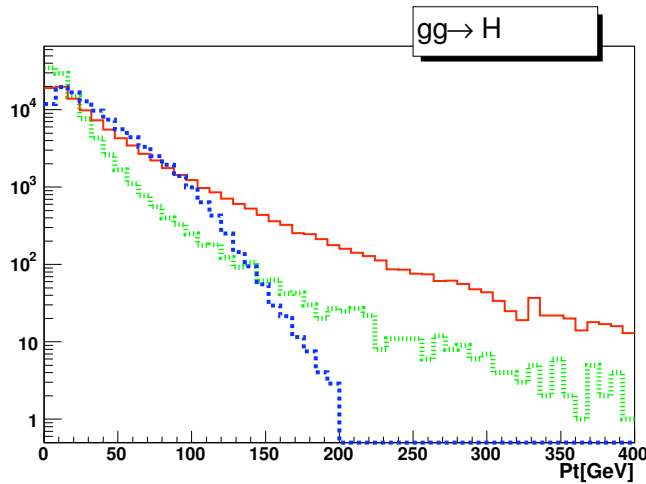


**Implications for LHC?**

- Use best models at HERA for LHC. But....
- Cascade only includes gluon processes. This limits present use for LHC. Can compare with like processes in Pythia ( $fg \rightarrow fg$ ,  $gg \rightarrow ff$ ,  $gg \rightarrow gg$ ).
- Unintergrated pdfs need to be better constrained (useful results presented here).
- Ariadne missing splitting kernel  $g \rightarrow qq$  (see contribution by Leif Lönnblad “ARIADNE at HERA and at the LHC” from HERA/LHC workshop proceedings for more details).
- Improvements expected, part of HERA/LHC program

# Multi-Jet Production and Multi-Scale QCD

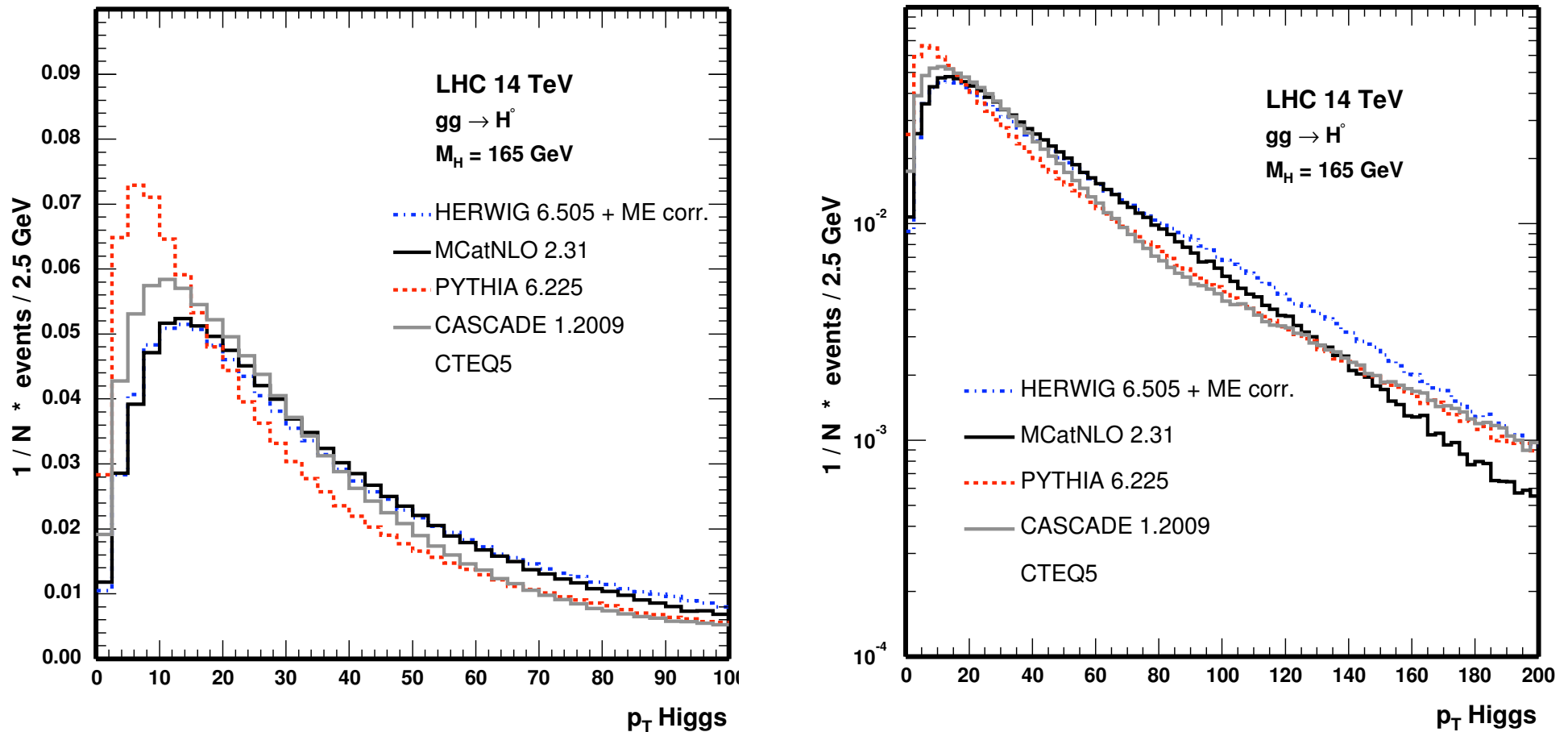
PYTHIA  
ARIADNE  
HERWIG



HERA/LHC  
workshop  
proceeding  
CERN-2005-014

**Fig. 1:** The transverse momenta of the Higgs boson,  $p_T^{\text{Higgs}}$  for 3 different shower models for each production mechanism. The red solid line represents PYTHIA, the dashed green line ARIADNE and the dotted blue line HERWIG events. The vertical scale gives the number of events per bin, and a total of  $10^5$  events have been generated with each program.

# Multi-Jet Production and Multi-Scale QCD

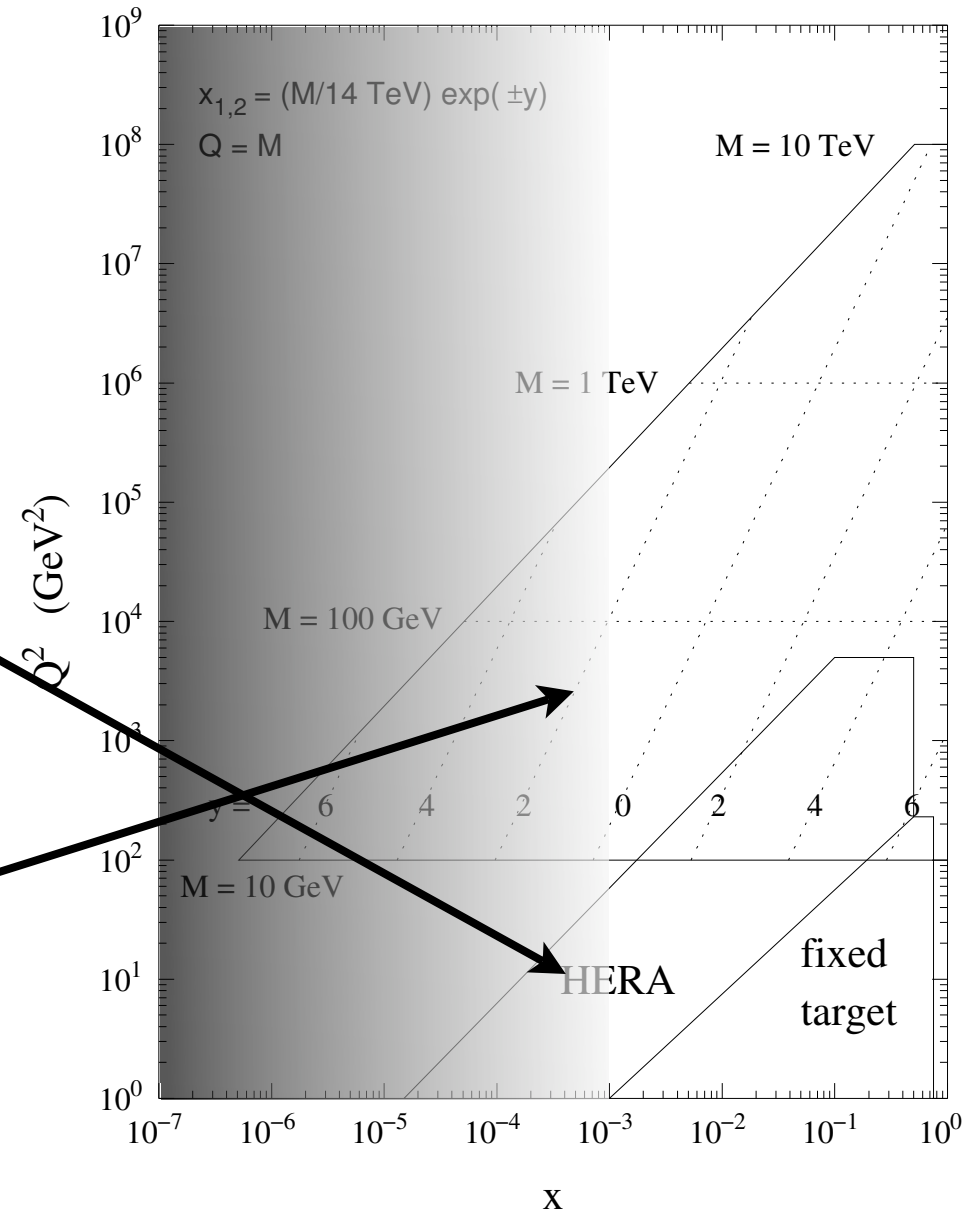


**Fig. 7:**  $p_T^{\text{Higgs}}$  Higgs of PYTHIA, HERWIG + ME Corrections, MC@NLO and CASCADE, linear and logarithmic scale.

# Low x Summary

Strong evidence of non DGLAP behaviour of the parton evolution at HERA ( $x < 0.001$ )

What does this mean for the LHC?



Backup

$$S = \frac{\int_0^{2\pi/3} N_{Dijet}(\Delta\phi^*, x, Q^2) d\Delta\phi^*}{\int_0^\pi N_{Dijet}(\Delta\phi^*, x, Q^2) d\Delta\phi^*}$$

- Data show significant increase towards low  $x$
- Study effect of higher orders:
  - LO predictions [ $O(\alpha_s)$ ]
    - at most 3 jets in final state
    - completely fails to describe data
  - NLO calculations [up to  $O(\alpha_s^3)$ ]
    - 3 or 4 jets in final state
    - reasonable description at large  $x$ ,  $Q^2$
    - but still too low at small  $x$ ,  $Q^2$

Luminosity:  $21\text{pb}^{-1}$

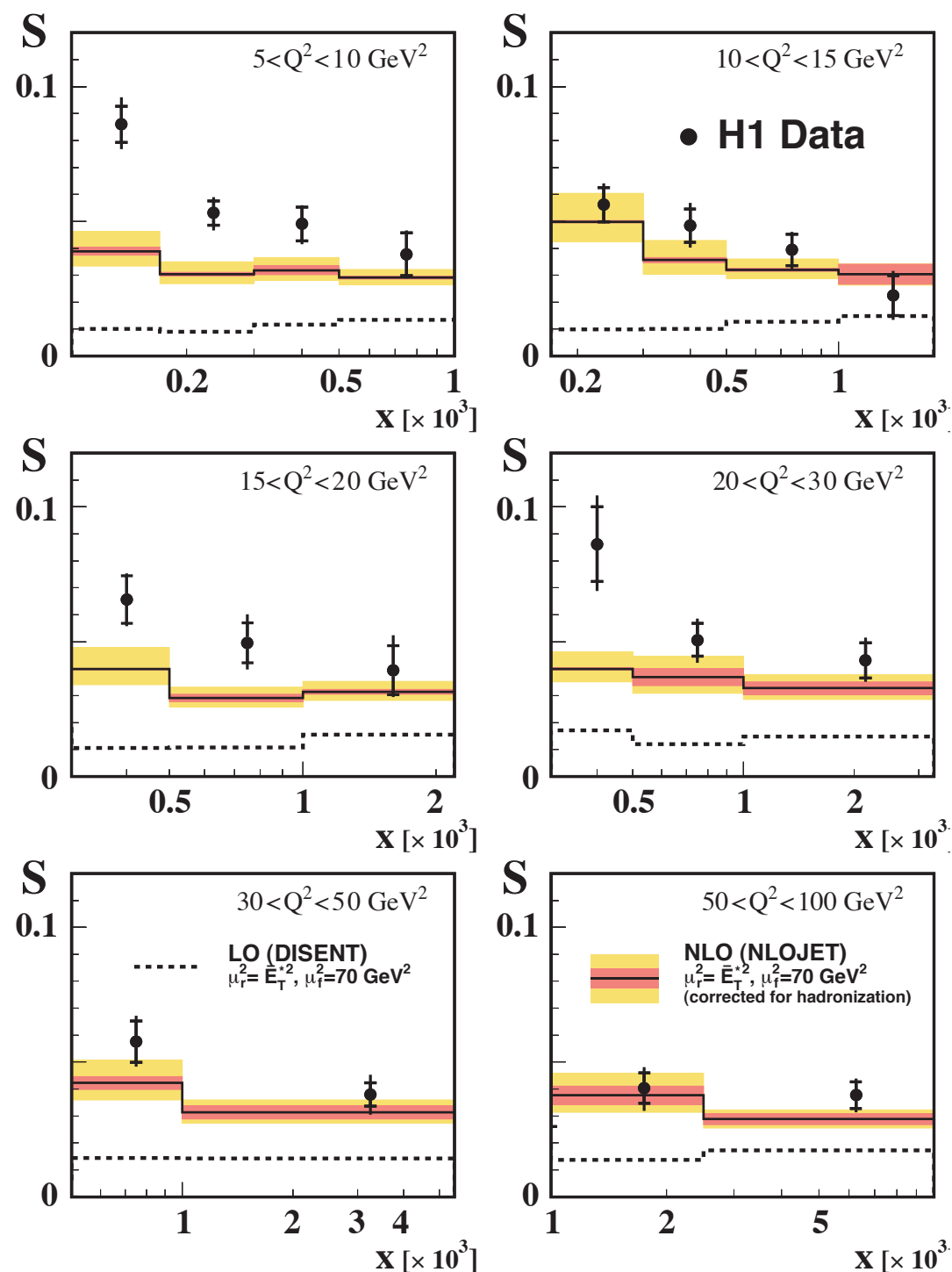
$5 < Q^2 < 100 \text{ GeV}^2$

$0.1 < y < 0.7$

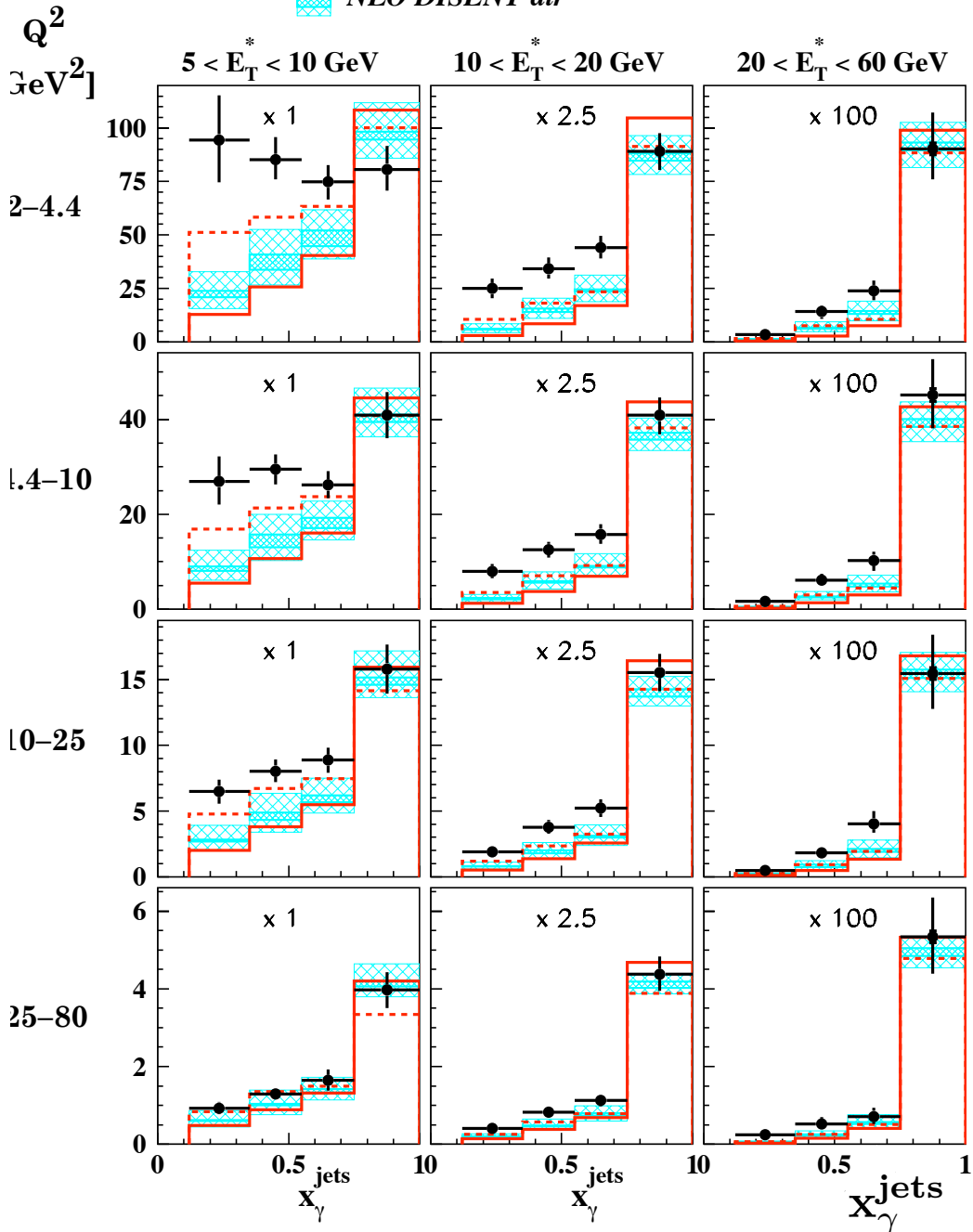
$E_{T,1}^* > 7 \text{ GeV}$

$E_{T,2}^* > 5 \text{ GeV}$

$-1 < \eta < 2.5$



- *H1 data*
- *NLO JETVIP dir*
- *NLO JETVIP dir+res<sub>T</sub>*
- ▨ *NLO DISENT dir*



**H1** (57 pb<sup>-1</sup>, 1999-2000)

$\sqrt{s} = 318$  GeV

$2 < Q^2 < 80$  GeV<sup>2</sup>

$0.1 < y < 0.85$

$E_{T1}^* > 7$  GeV

$E_{T2}^* > 5$  GeV

$-2.5 < \eta_{1,2}^* < 0$

longitudinally invariant  $k_{\perp}$  jet algorithm,  $\gamma^*p$  CMS

*Eur. Phys. J. C37 (2004) 141-159*

- Estimate fraction of photon four momentum carried by parton in hard interaction:

$$x_{\gamma}^{jets} = \frac{\sum_{j=1,2} (E_j^* - p_{z,j}^*)}{\sum_{hadrons} (E^* - p_z^*)}$$

- **direct** part ( $x_{\gamma}^{jets} > 0.75$ ) well described
- **resolved** fraction ( $x_{\gamma}^{jets} < 0.75$ ) increases

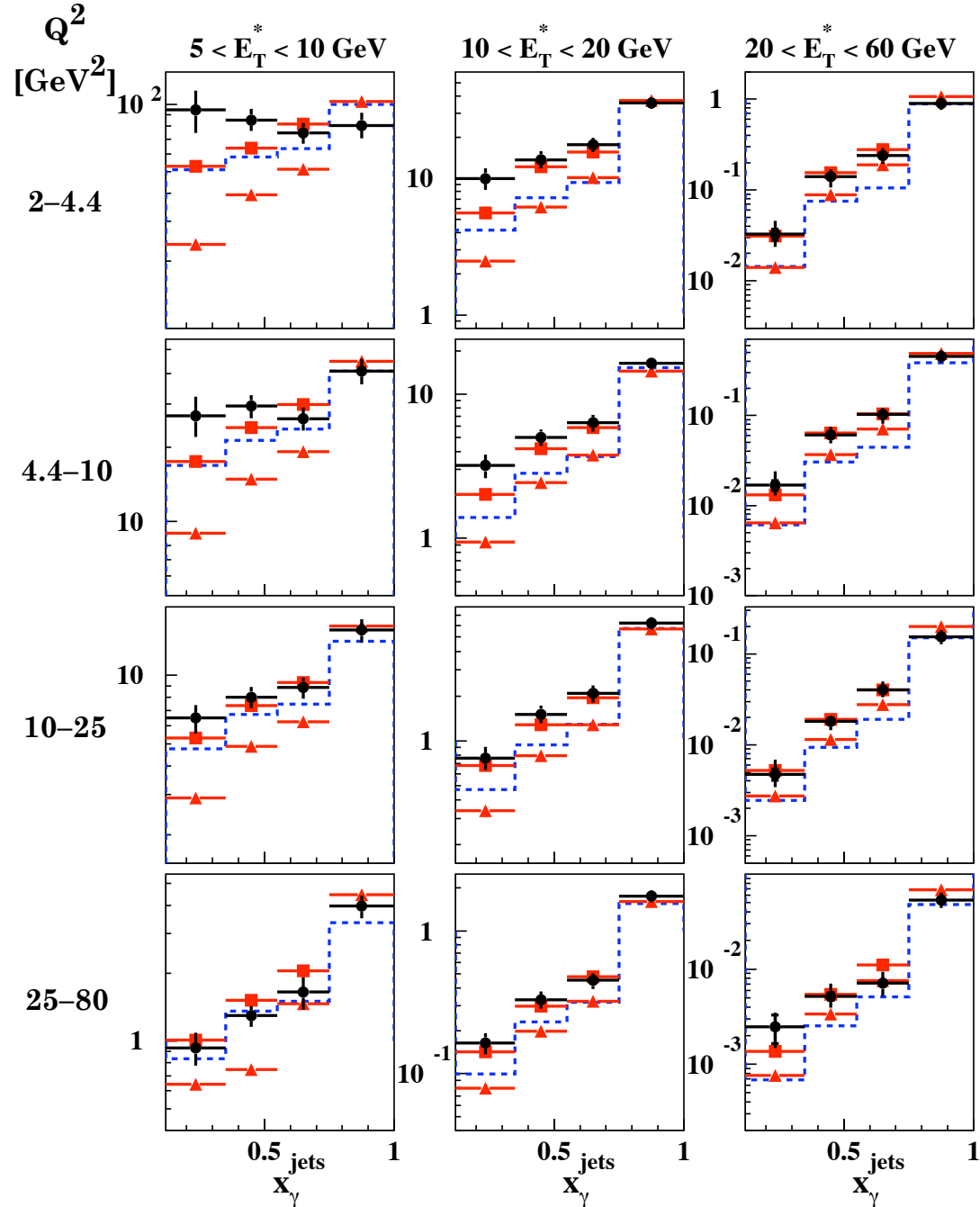
at smaller  $Q^2$

- data significantly above NLO calculations when using direct photon only
- excess decreases with increasing  $Q^2$

- JETVIP including  $\gamma_T^*$  improves description but excess for  $x_{\gamma}^{jets} < 0.75$  remains

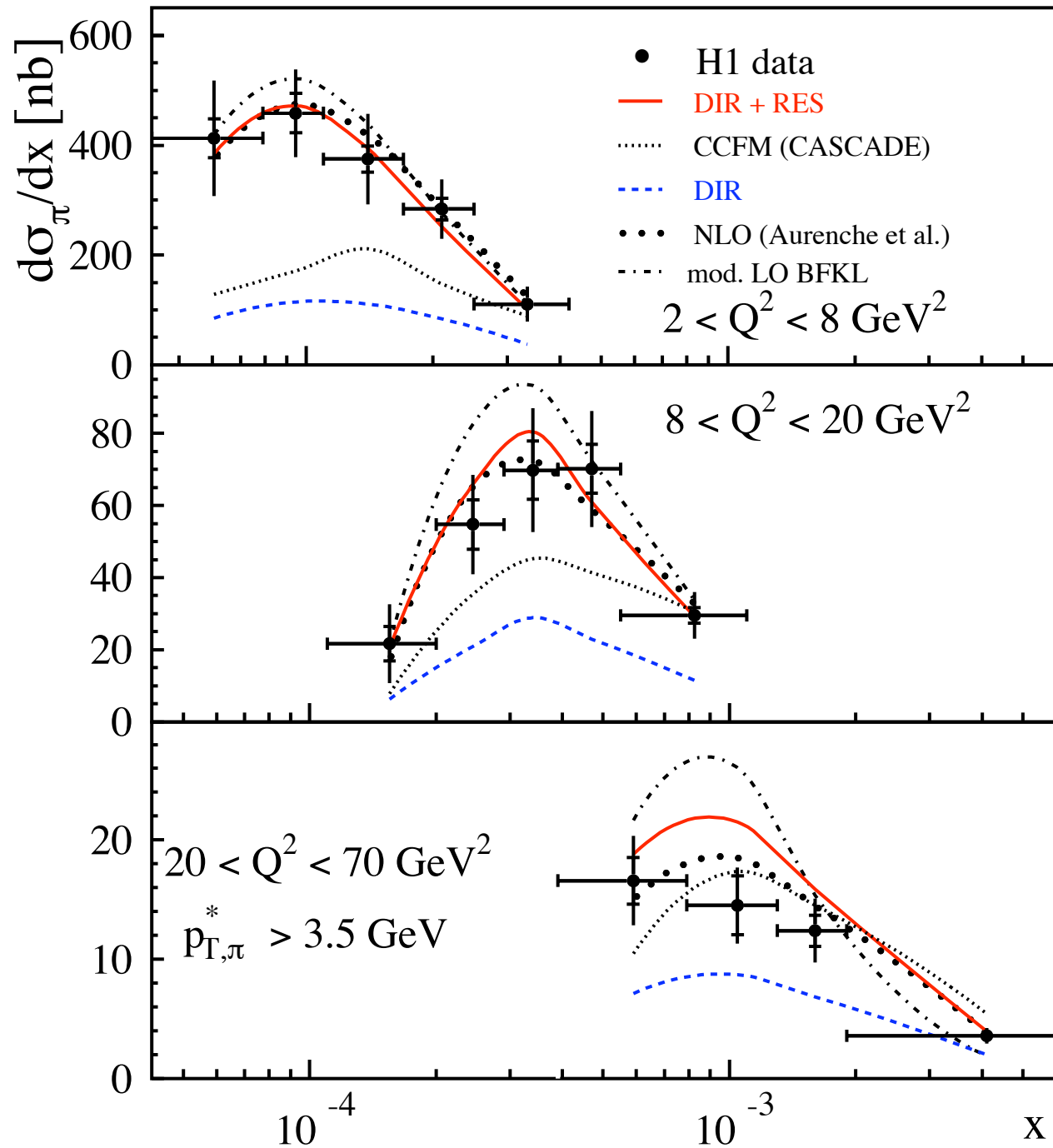


- H1 data
- Jetvip full
- NLOJET for 2 jets
- NLOJET for 3 jets



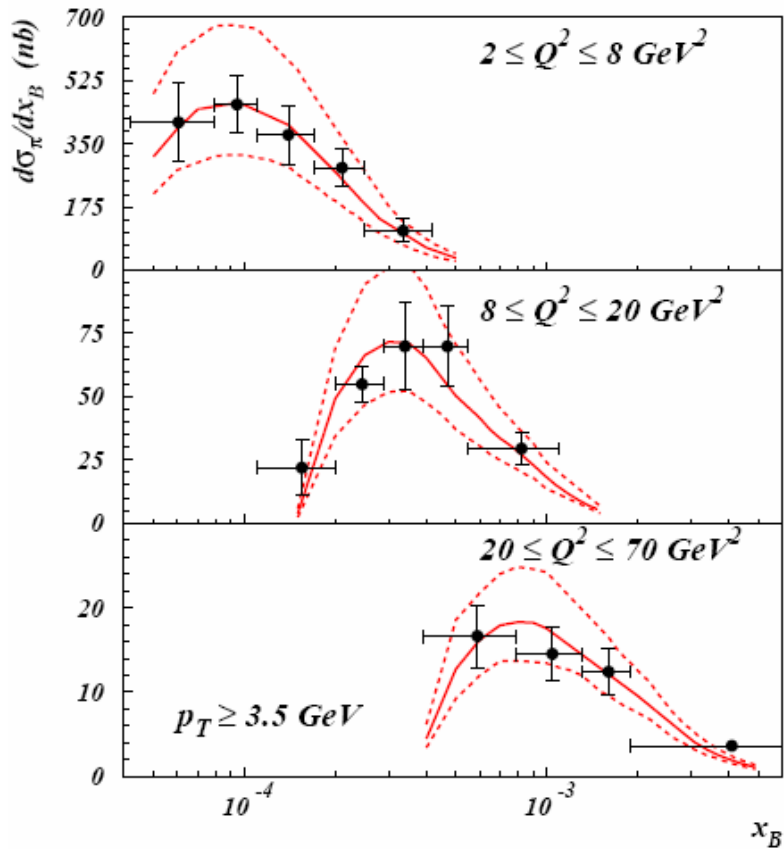
- NLOJET++ results in 3-jet mode significantly closer to data than those of 2-jet mode
  - have to cut out region  $x_\gamma \sim 1$
  - no resolved photon
- largest corrections at small  $x_\gamma$  and  $Q^2$
- remaining gap between data and NLOJET++ 3-jet also most pronounced for small  $x_\gamma$  and low  $Q^2$ 
  - there is need for further higher order QCD corrections

# Forward $\pi^0$ -meson production

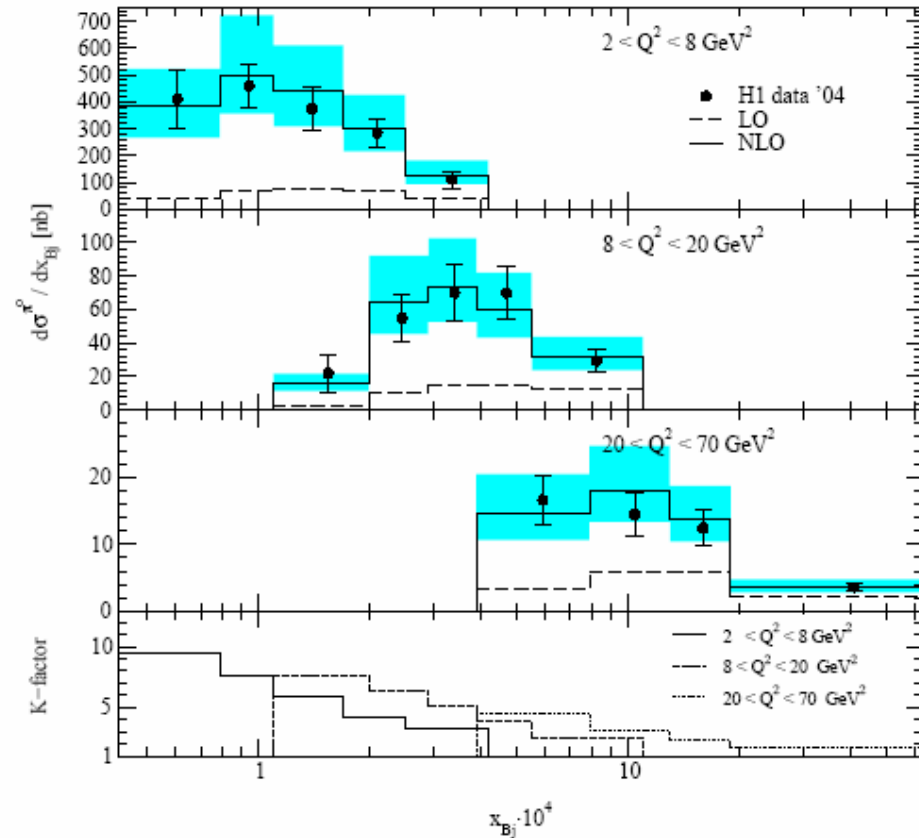


# Forward $\pi^0$ -meson production

Daleo et al.

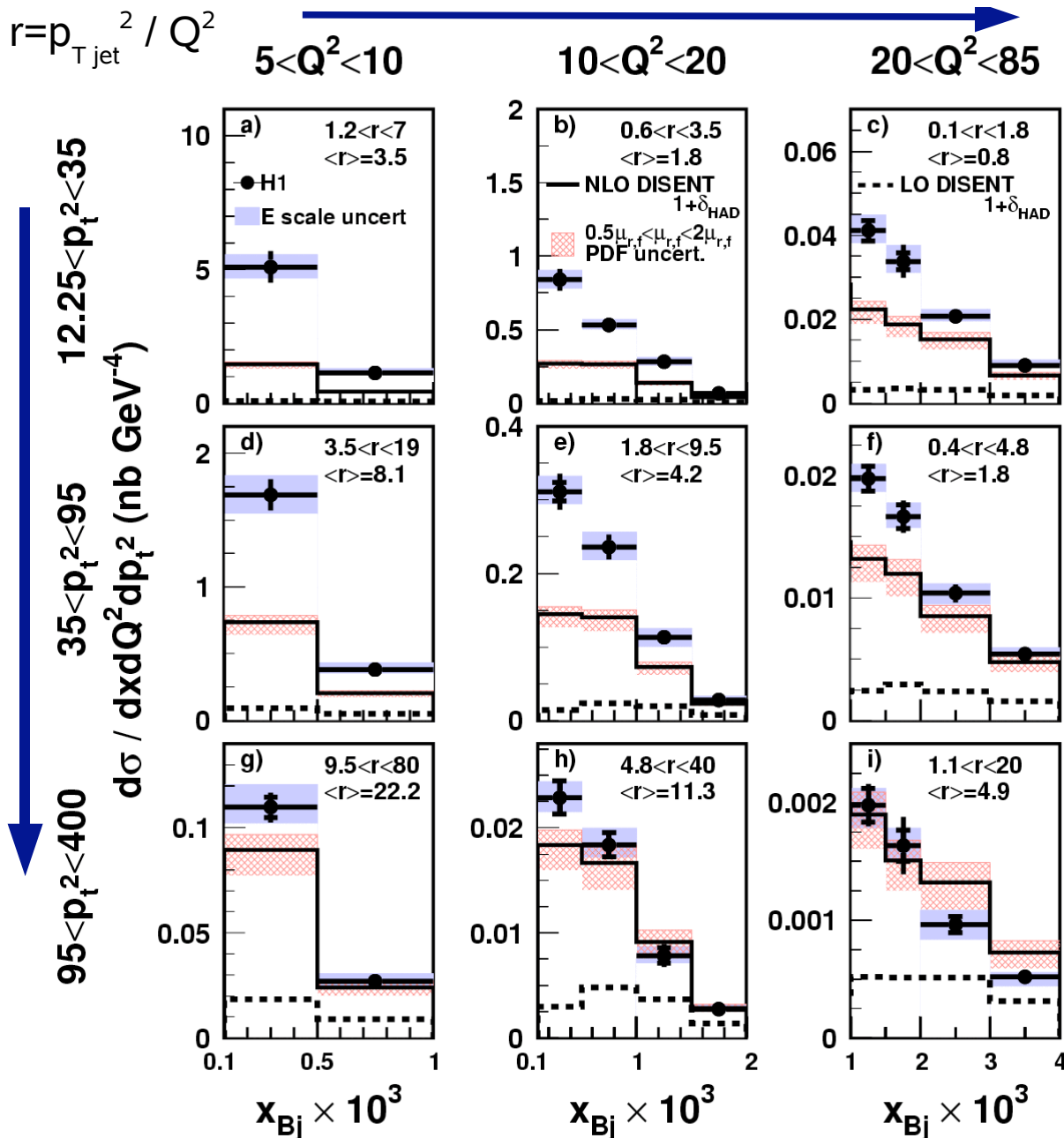


Kniehl et al.



NLO predictions in good agreement with the H1 data  
Large K factors and theoretical uncertainties  
Need for NNLO analysis

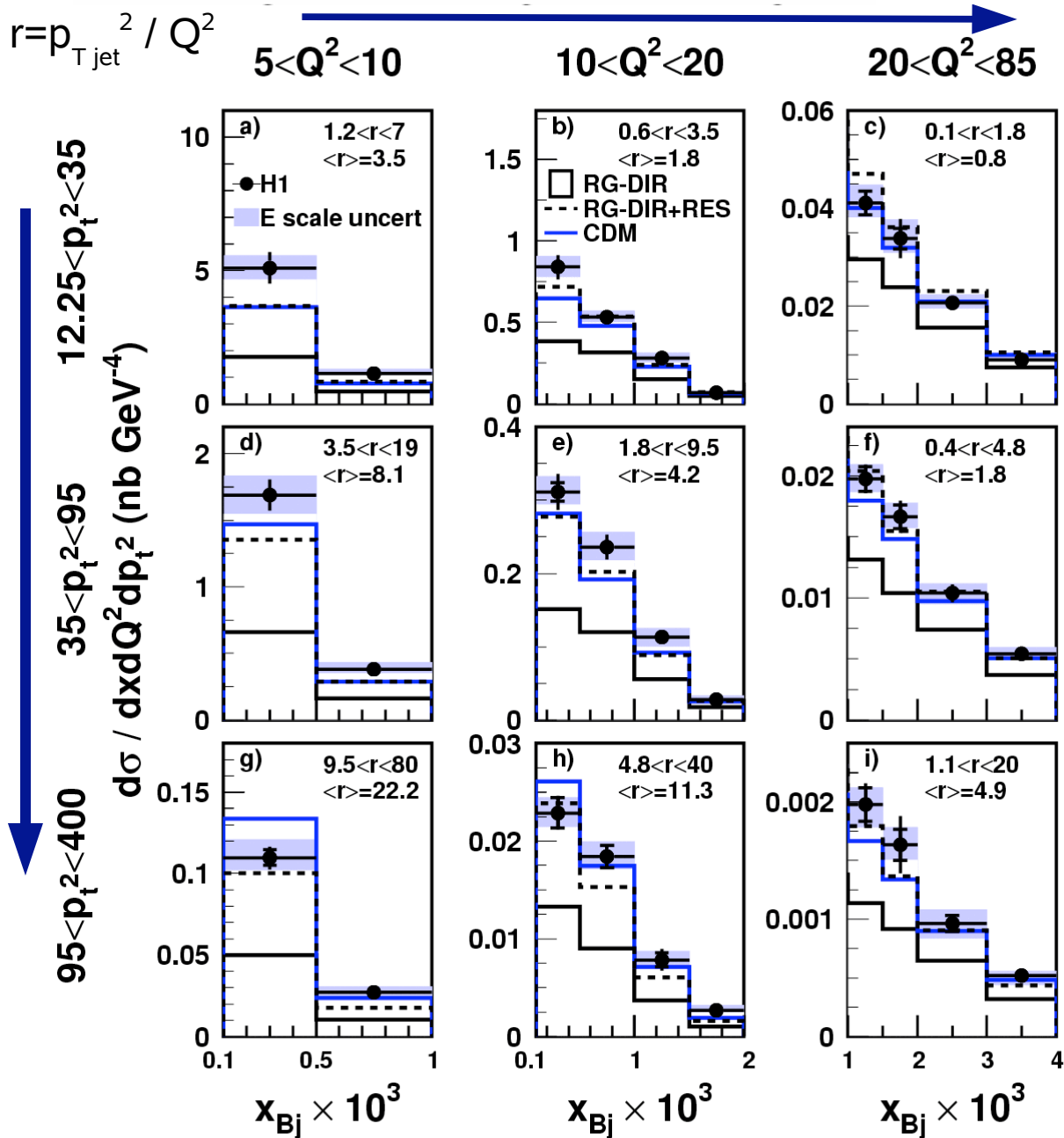
# H1 forward jets: triple differential cross section



Cross Section as fct. of  $x_{bj}$  in 3x3  $p_T^2$ - $Q^2$  bins (no  $p_{T \text{ jet}}^2 / Q^2$  cut)

$d^3\sigma / dx_{bj} dQ^2 dp_T^2$ :  
 best description: RG-DIR+RES  
 or CDM  
 RG-DIR below data, best at  $r \sim 1$   
 DISENT better at larger  
 $x_{bj}, Q^2, p_T^2$   
 CASCADE as single diff  $\sigma$   
 too hard  $x_{bj}$  spectra

# H1 forward jets: triple differential cross section



Cross Section as fct. of  $x_{bj}$  in  $3 \times 3$   $p_T^2$ - $Q^2$  bins (no  $p_{Tjet}^2 / Q^2$  cut)

**Comparison with RAPGAP and CDM**

3 kinematic regions: