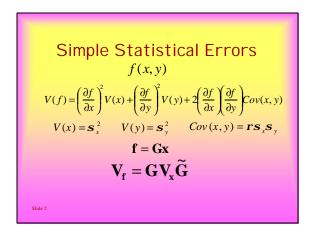
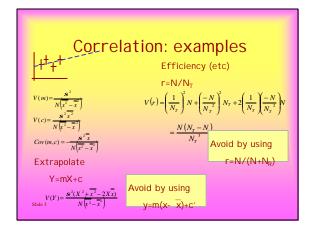
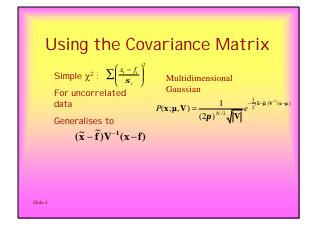
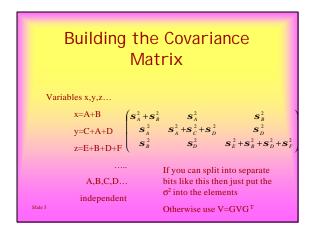
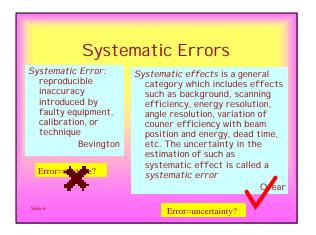
# Statistics for HEP Roger Barlow Manchester University Lecture 5: Errors











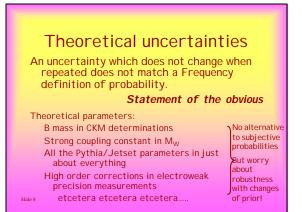
### **Experimental Examples**

- Energy in a calorimeter E=aD+b
  - a & b determined by calibration expt
- Branching ratio  $B=N/(\eta N_T)$ 
  - η found from Monte Carlo studies
- Steel rule calibrated at 15C but used in warm lab

If not spotted, this is a mistake If temp. measured, not a problem

If temp. not measured guess  $\rightarrow$ uncertainty

Repeating measurements doesn't help



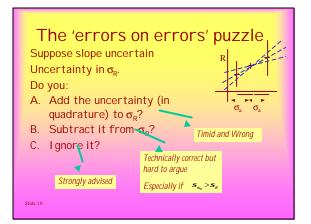
# Numerical Estimation

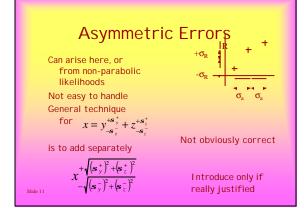
Theory(?) parameter a affects your result R

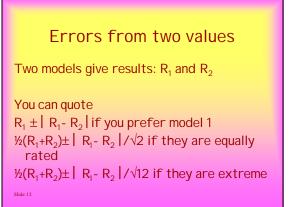
 $\sigma_{R}$   $\sigma_{R}$   $\sigma_{R}$   $\sigma_{R}$   $\sigma_{A}$   $\sigma_{A}$   $\sigma_{A}$ 

a is known only with some precision  $\sigma_a$  Propagation of errors impractical as no algebraic form for R(a)

Use data to find dR/da and  $\sigma_a$  dR/da Generally combined into one step







### Alternative: Incorporation in the Likelihood

Analysis is some enormous likelihood maximisation Regard a as 'just another parameter': include  $(a-a_0)^2/2\sigma_a^2$ as a chi squared contribution



Can choose to allow a to vary. This will change the result and give a smaller error. Need strong

If nerves not strong just use for errors Not clear which errors are 'systematic' and which are 'statistical' but not important

## The Traditional Physics **Analysis**

- 1. Devise cuts, get result
- 2. Do analysis for statistical errors
- 3. Make big table
- 4. Alter cuts by arbitrary amounts, put in table
- 5. Repeat step 4 until time/money exhausted
- 6. Add table in quadrature
- 7. Call this the systematic error
- If challenged, describe it as 'conservative'

### Systematic Checks

- Why are you altering a cut?
- To evaluate an uncertainty? Then you know how much to adjust it.
- To check the analysis is robust? Wise move. But look at the result and ask 'Is it OK?

Eg. Finding a Branching Ratio...

- · Calculate Value (and error)
- Efficiency goes up but so does background. Re-evaluate them
- · Re-calculate Branching Ratio (and error).
- Check compatibility

### When are differences 'small'?

- It is OK if the difference is 'small' compared to what?
- Cannot just use statistical error, as samples share data
- 'small' can be defined with reference to the difference in quadrature of the two errors

12±5 and 8 ±4 are OK. 18±5 and 8±4 are not

# When things go right

### DO NOTHING

Tick the box and move on Do NOT add the difference to your systematic error estimate

- I t's illogical
- I t's pusillanimous
- It penalises diligence

### When things go wrong

- 1. Check the test
- 2. Check the analysis
- 3. Worry and maybe decide there could be an effect
- 4. Worry and ask colleagues and see what other experiments did
- 99. Incorporate the discrepancy in the systematic

### The VI commandments

Thou shalt never say 'systematic error' when thou meanest 'systematic effect' or 'systematic mistake'

Thou shalt not add uncertainties on uncertainties in quadrature. If they are larger than chickenfeed, get more Monte Carlo data Thou shalt know at all times whether thou art performing a

check for a mistake or an evaluation of an uncertainty
Thou shalt not not incorporate successful check results into thy total systematic error and make thereby a shield behind which to hide thy dodgy result

Thou shalt not incorporate failed check results unless thou art truly at thy wits' end
Thou shalt say what thou doest, and thou shalt be able to justify it out of thine own mouth, not the mouth of thy supervisor, nor thy colleague who did the analysis last time, nor thy mate down the pub.

Do these, and thou shalt prosper, and thine analysis likewise

## **Further Reading**

R Barlow, Statistics. Wiley 1989

G Cowan, Statistical Data Analysis. Oxford 1998

L Lyons, Statistics for Nuclear and Particle Physicists, Cambridge 1986

B Roe, Probability and Statistics in Experimental Physics, Springer 1992 A G Frodesen et al, Probability and Statistics in Particle Physics, Bergen-Oslo-

Tromso 1979 W T Eadie et al; Statistical Methods in Experimental Physics, North Holland

M G Kendall and A Stuart; "The Advanced Theory of Statistics". 3+ volumes, Charles Griffin and Co 1979

Darrel Huff "How to Lie with Statistics" Penguin

CERN Workshop on Confidence Limits. Yellow report 2000-005

Proc. Conf. on Adv. Stat. Techniques in Particle Physics, Durham, IPPP/02/39

http://www.hep.man.ac.uk/~roger

