Physics of shower simulation at LHC, at the example of GEANT4.

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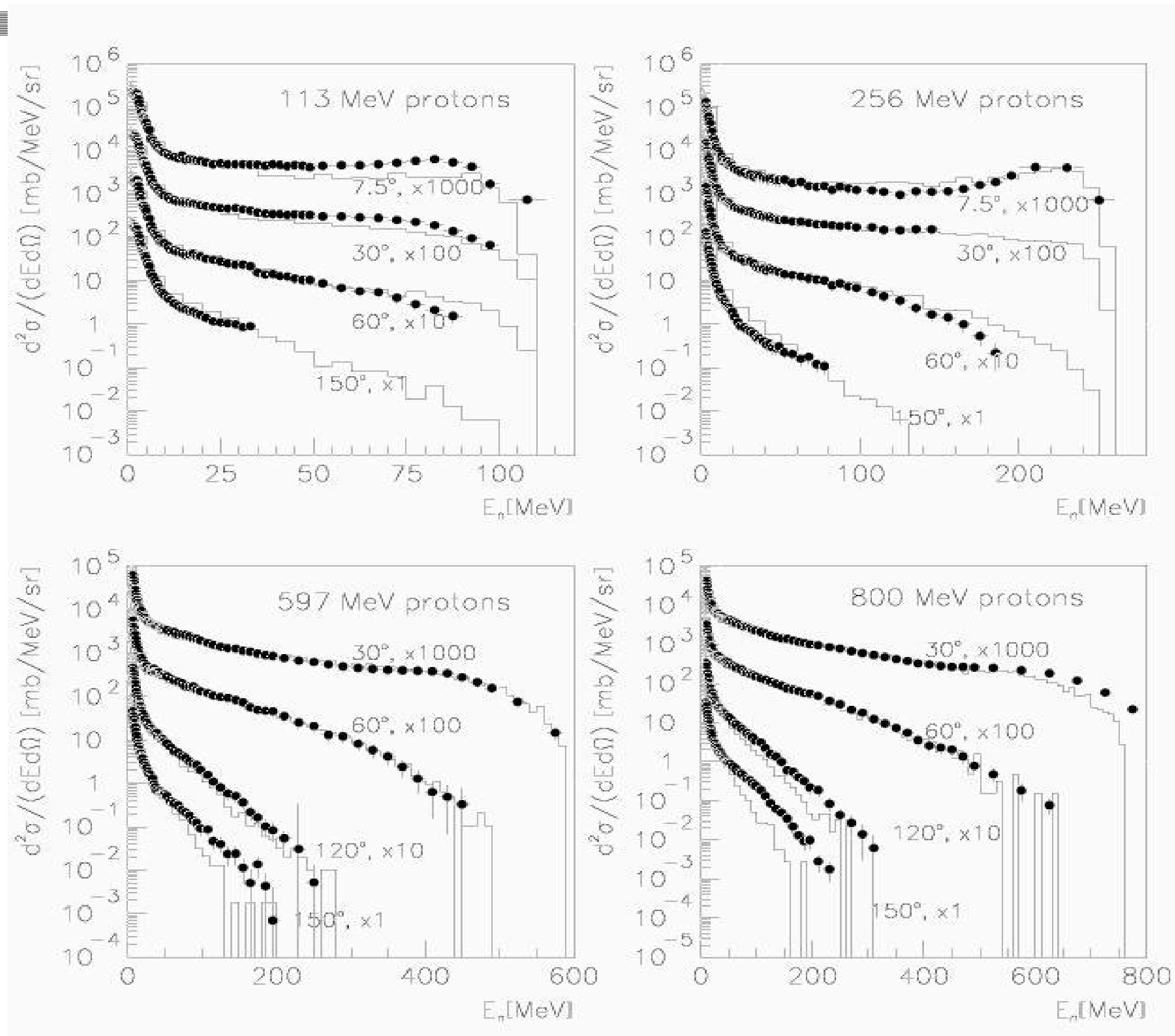
The Monte Carlo Roadmap

- Part 1: Introduction
  - LHC related use cases - LCG.
  - Analyzing showers and their development in matter.
  - Brief overview of hadronic models in geant4
- Part 2: Hadronic showers in bulk matter.
  - Selected topics on hadronic shower simulation:
    - Theory driven modeling of inelastic reactions.
- Part 3: ghad – how good is it really?
- Part 4: Modeling electromagnetic showers.
  - Examples of electromagnetic showers.
  - Selected topics on electromagnetic shower physics.

Pre-equilibrium decay

- Example: Griffin’s Exciton model
  - Phys.Rev.Lett. 17, 9 (1966)

Scattering off lead at various angles and energies



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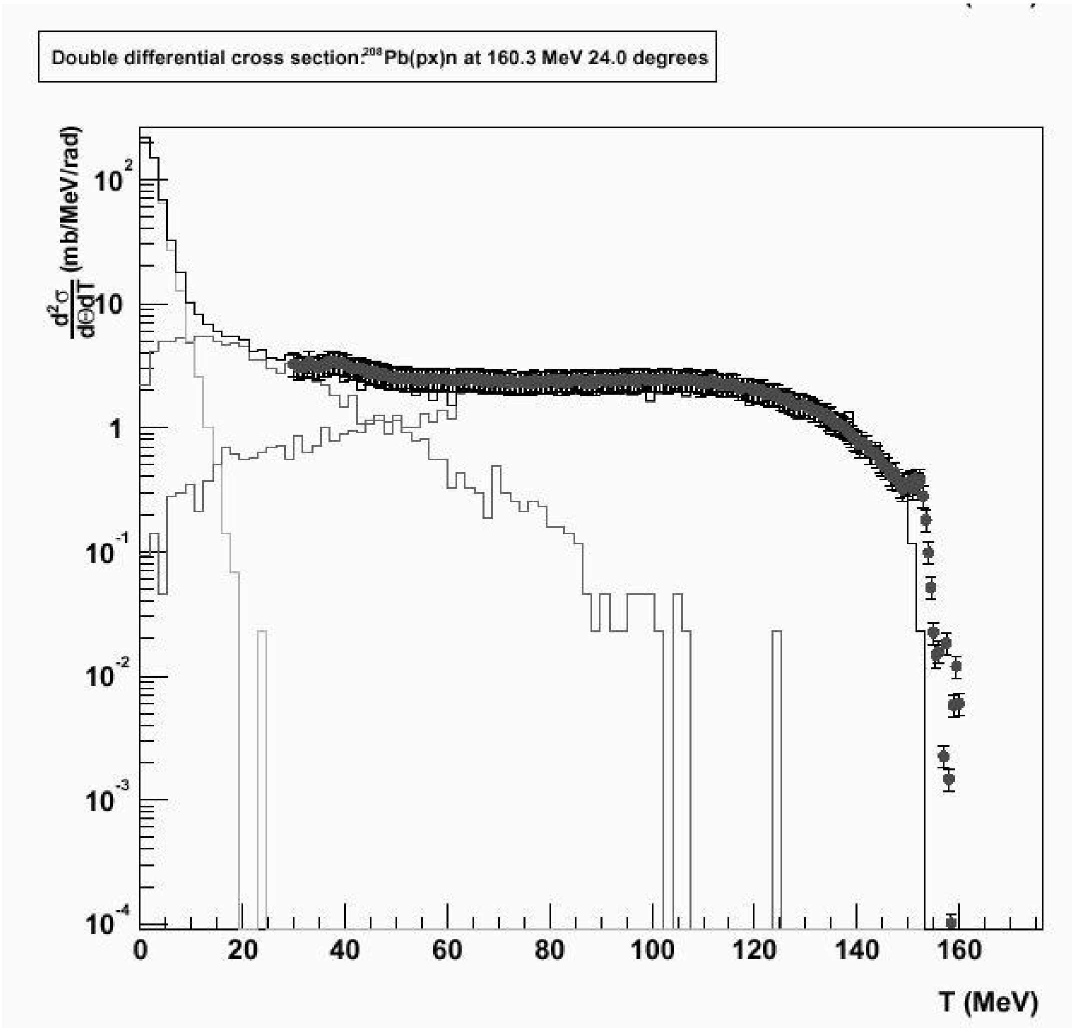
Contributions of the model components to the neutron spectrum



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Exciton pre-compound model

- In this model, the pre-compound nucleus is viewed as falling apart onto two parts.
  - A system of excitons that carry the excitation energy and the momentum of the excited system
  - A nucleus, that itself is otherwise undisturbed (Bogolubov’s transformation diagonal, excitons as quasi-particles)

- The initial state of pre-equilibrium decay consists of
  - A, Z of the pre-compound nucleus,
  - The number pf excitons (n)
  - The number of holes (h)
  - The number of charged excitons (c)
  - The momentum and mass of the exciton system

- This system is allowed to evolve, and collisions between excitons (Δn=0,-2), as well as collisions of excitons with nucleons (Δn=2) are put into competition with particle or fragment emission.
- The pre-compound transitions and emissions are iterated, until the residual system corresponds to an equilibrated nucleus.

Transition probabilities

- The probability of changing the exciton number by Δn is defined by the matrix element of the allowed transitions, and the density of accessible final states

Level densities

- For further calculation, assumptions have to be made about the level densities.
- If we assume an equidistant scheme of single particle levels with level density where *a* is the level density parameter, we can derive the density of states for n excitons as a function of the excitation energy as

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- Where the densities of the accessible final states can be written as (Nucl.Phys.A205, 545 (1973))

- With

- To estimate the matrix element, we assume that the creation probability for 2 excitons is the scattering probability of nucleon-nucleon scattering

- Where we can estimate

- with λ being the De Broglie wave length, corresponding to a relative velocity
- Here m is the nucleon mass, and .

- Assuming the the averaging of velocity and cross-section factorizes, and taking the cross-section as

- We have all informartion to calculate the transition probabilities.

Emission probabilities

- In geant4, these are similar to the emission probabilities of the Weisskopf evaporation model.
- We calculate the probability to emit a nucleon in the energy interval

Fragment emission

- To justify fragment production, we need to assume that the nucleons in the nucleus condense into fragments with a certain probability γ. We write for the probability to find a fragment with nucleon contents N in the nucleus as

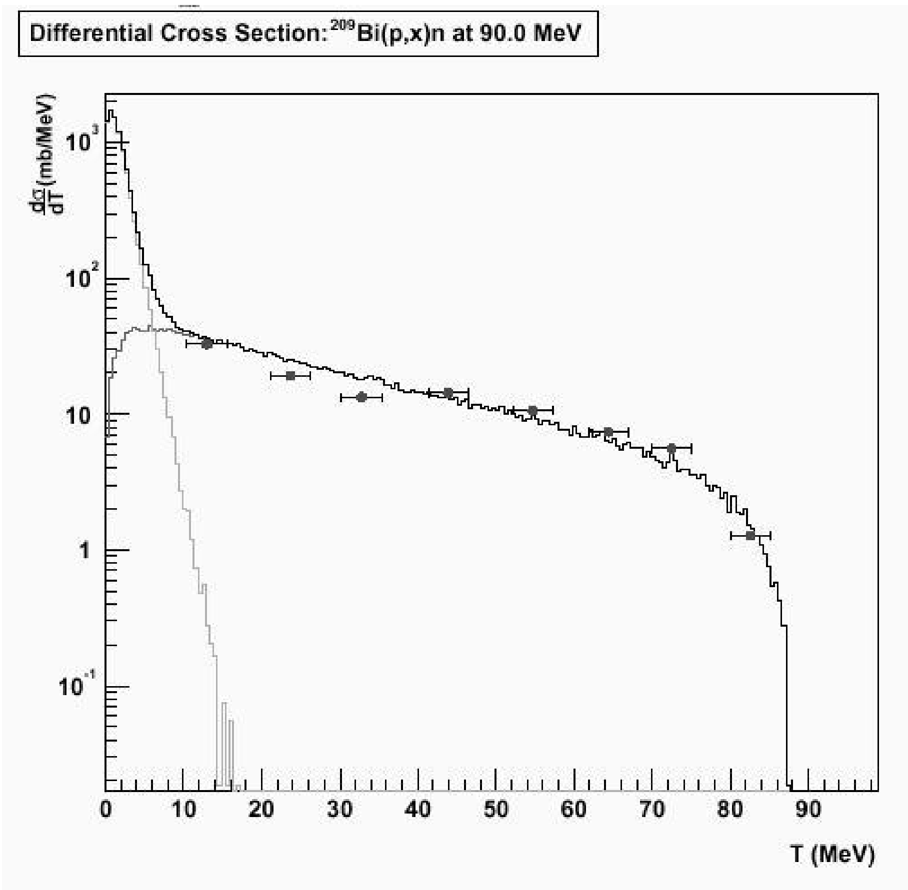
Emission probabilities

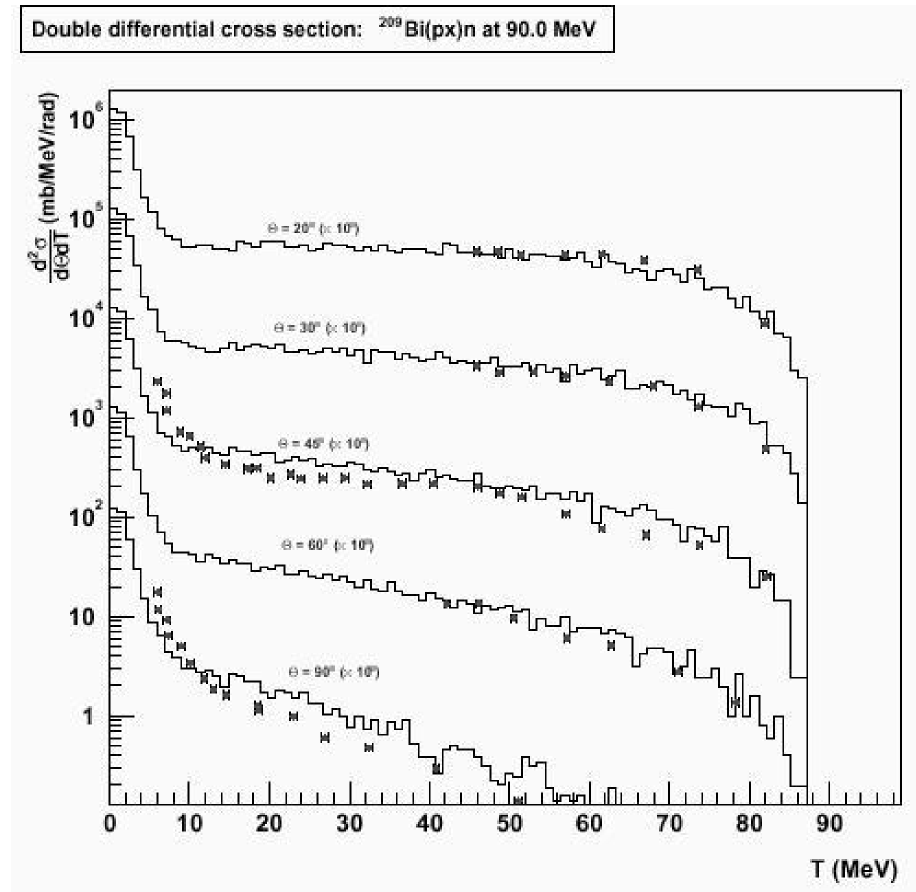
- The emission probabilities are identical in structure to the nucleon emission probabilities, except for the condensation probability and a level density factor for the fragment

Thermalization

- In statistical equilibrium, the transition probabilities (ω) for creating ($\Delta n=+2$) or destroying ($\Delta n=-2$) excitons are equal.
- Hence the equilibrium number of excitons can be found from
- To be

90 MeV protons scattering off Bismuth





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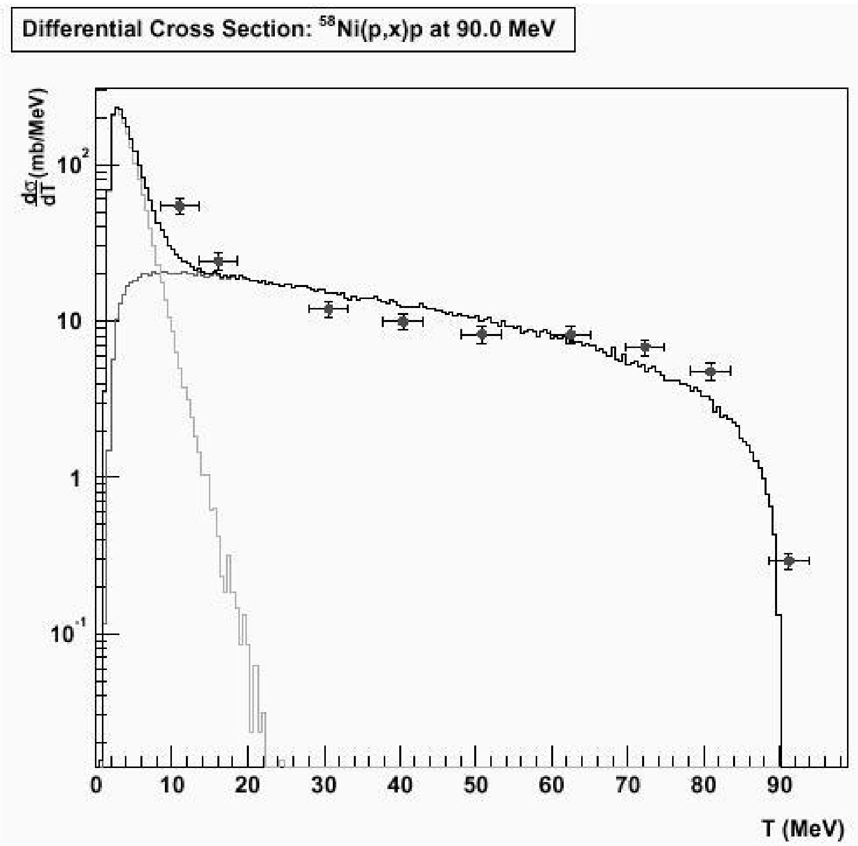
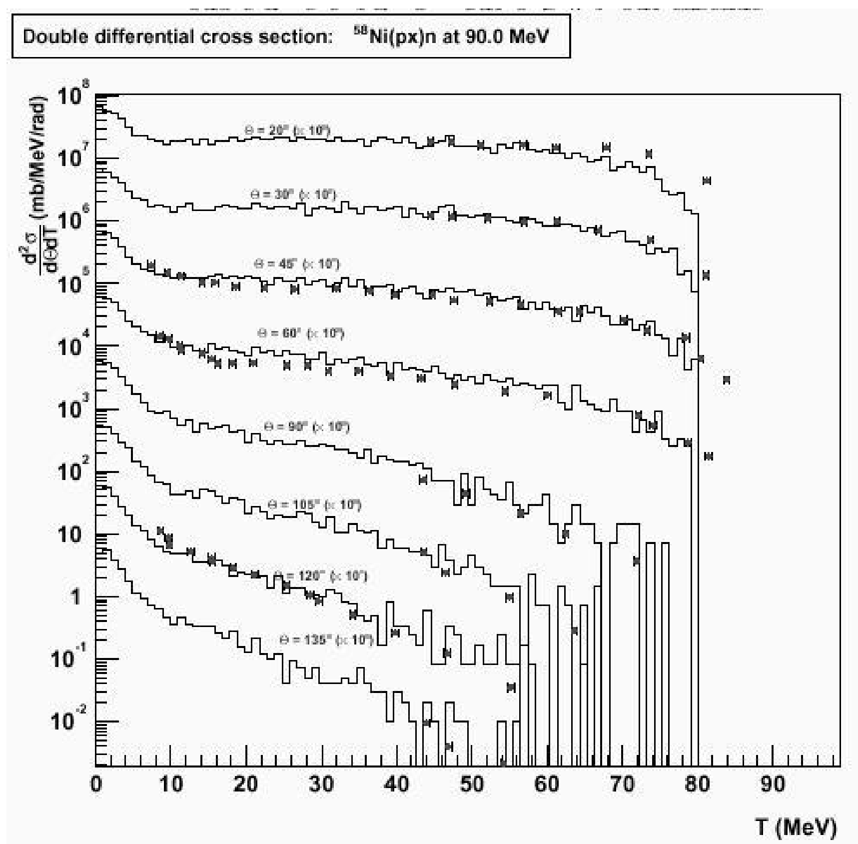
90 MeV protons scattering off Nickel





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Statistical evaporation models.

- Weisskopf-Ewing evaporation
- Furihata's generalized evaporation model
- Fission
- Photon evaporation
- Fermi-breakup
- Multifragmentation

- Notes on evaporation
  - Treats excited nuclear system in equilibrium
  - Evaporation produces most of the neutrons in a hadronic shower
  - It defines to a large extent the isotope that is left after the reaction, and may activate the detector material

The Weisskopf Ewing model

- Weisskopf's treatment is based on the principle of detailed balance
- Since the probability , is proportional to the cross-section of the inverse reactions, we can write the probability of a nucleus with excitation energy U to emit a particle j with kinetic energy T in its ground state as

- In general, we take Dostrovsky's cross-section for the inverse reactions

- With

- For neutrons, and use Shapiro's tabulation (PhysRev 90, 171 (1953)) for α and β=-'coulomb barrier' for charged particles

- The coulomb barrier calculated from electrostatics is not directly applicable, but needs correction for various effects, for example for tunneling through the barrier.
- To keep the probability distributions in an integrable form, a tabulated coefficient (also from Shapiro) can be used

- For the contact radius, please see A.S.Iljinov, et. al Intermediate Energy Nuclear Physics, CRC press, 1994

- The simplest and widely used level densities are based on those of Weisskopf, based on a completely degenerate Fermi gas.

- We use this with a level density parameter of

- With parameters taken from Ilijof at al (NPA 543, 517 (1992)), and nuclear shell corrections from Truran, Cameron, and Hilf.

It can be more sophisticated…

- Furihata's general evaporation model (NIM,B171,251(2000)
  - with parameters from Matuse, et al (Phys.Rev.C26,2338)
  - Based on the Fermi gas model, the level density functions can be written as

- With
- the nuclear temperature

- and

- Substituting this into the formula for the emission probabilities, we get the width for fragment emission

- here

- 60 nuclids up to Mg(28) are considered, including their quasi-stable excited states with half-lives

Summary

- We have looked at inelastic hadron nuclear reactions and some of the modeling possibilities realized in geant4.
- In doing so, we covered about 20% of the geant4 hadronic models (8 of 37 packages).
- For the remaining majority, please refer to the physics reference manual.

Part 3

Trying to answer the question:

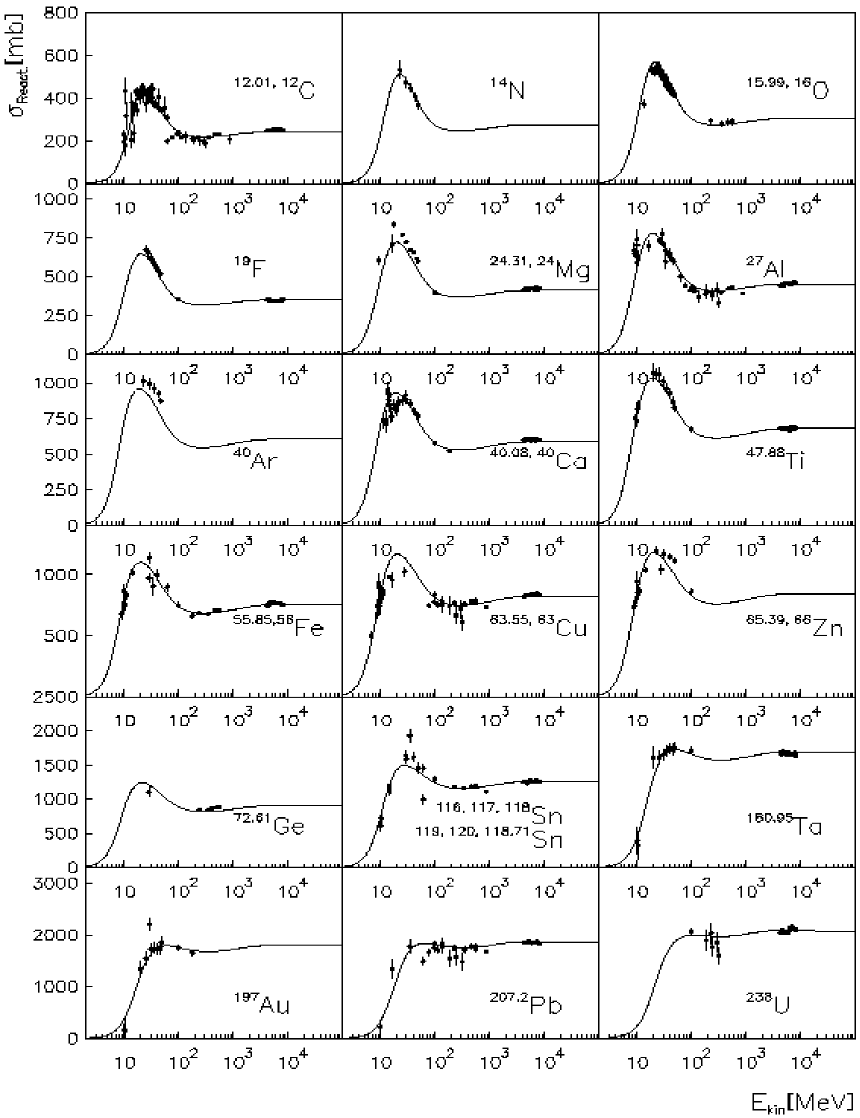
How good is it really?

Verification – grouped into sections

- The verification effort of the geant4 hadronic working group is grouped into several sections:
  - Inclusive cross-sections
  - Thin target comparisons
  - Verification of model components
  - Code comparisons (least effective)
  - Complete application tests
  - Robustness.
- I give a few examples of each in the following slides.

A few total cross-section examples

Proton reaction cross-section:



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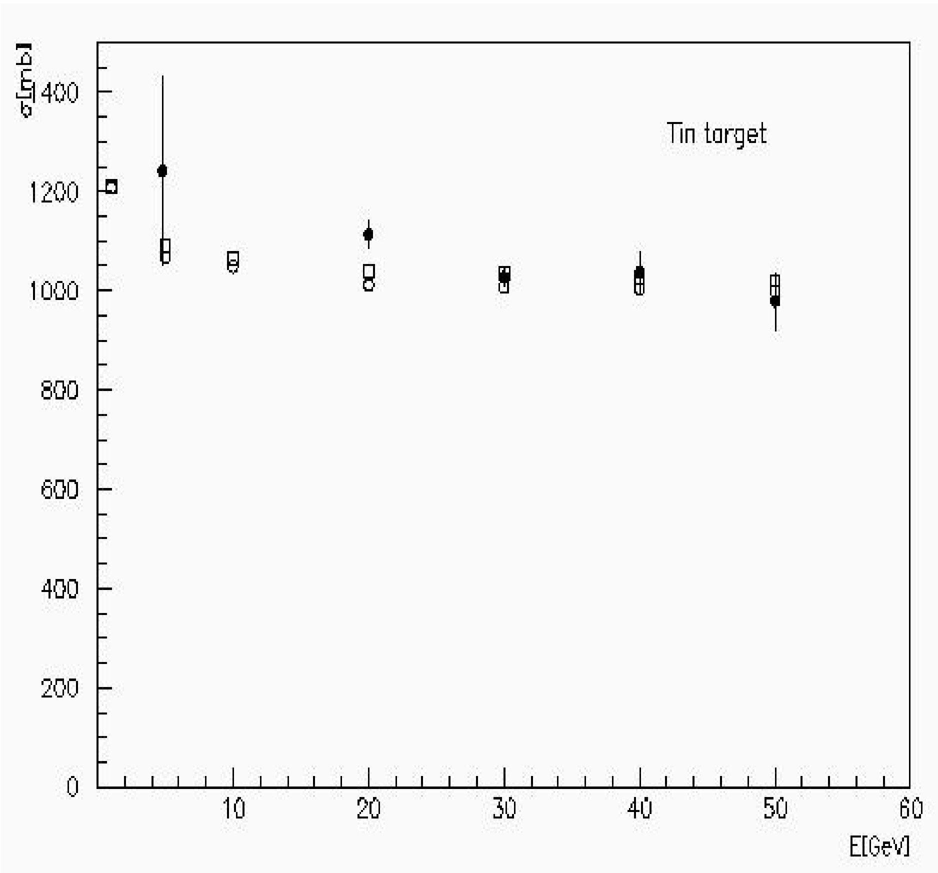
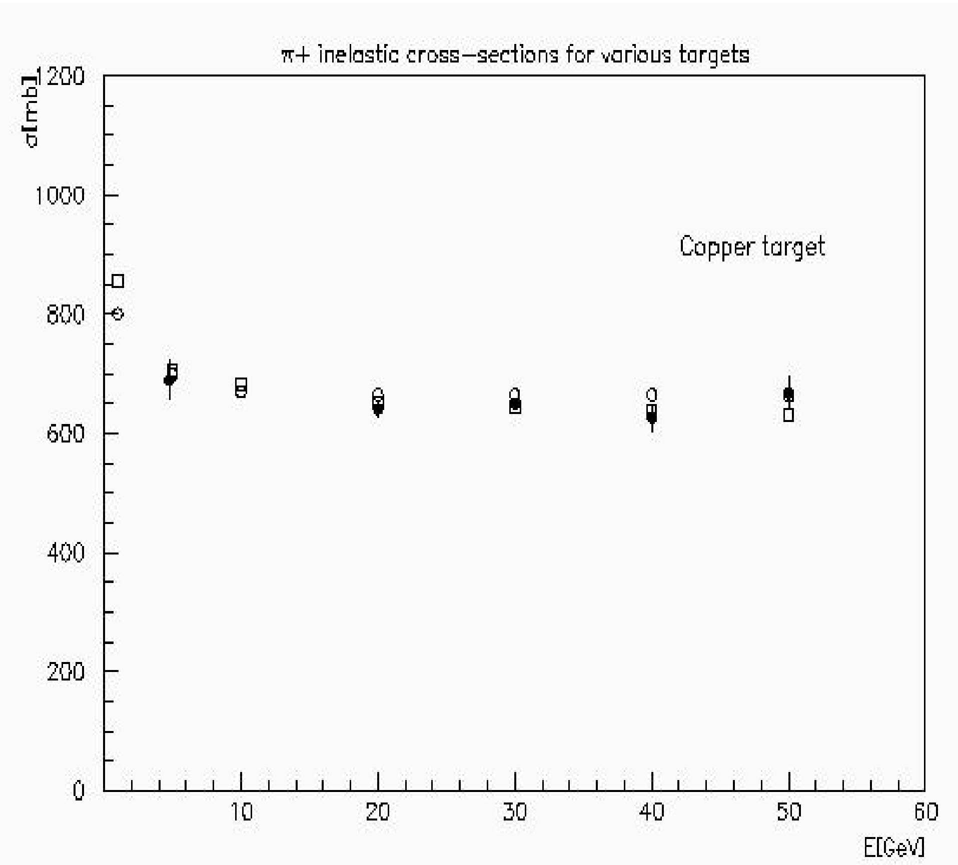
Pi+ reaction cross-sections: dots: data, open symbols: two different parametrization





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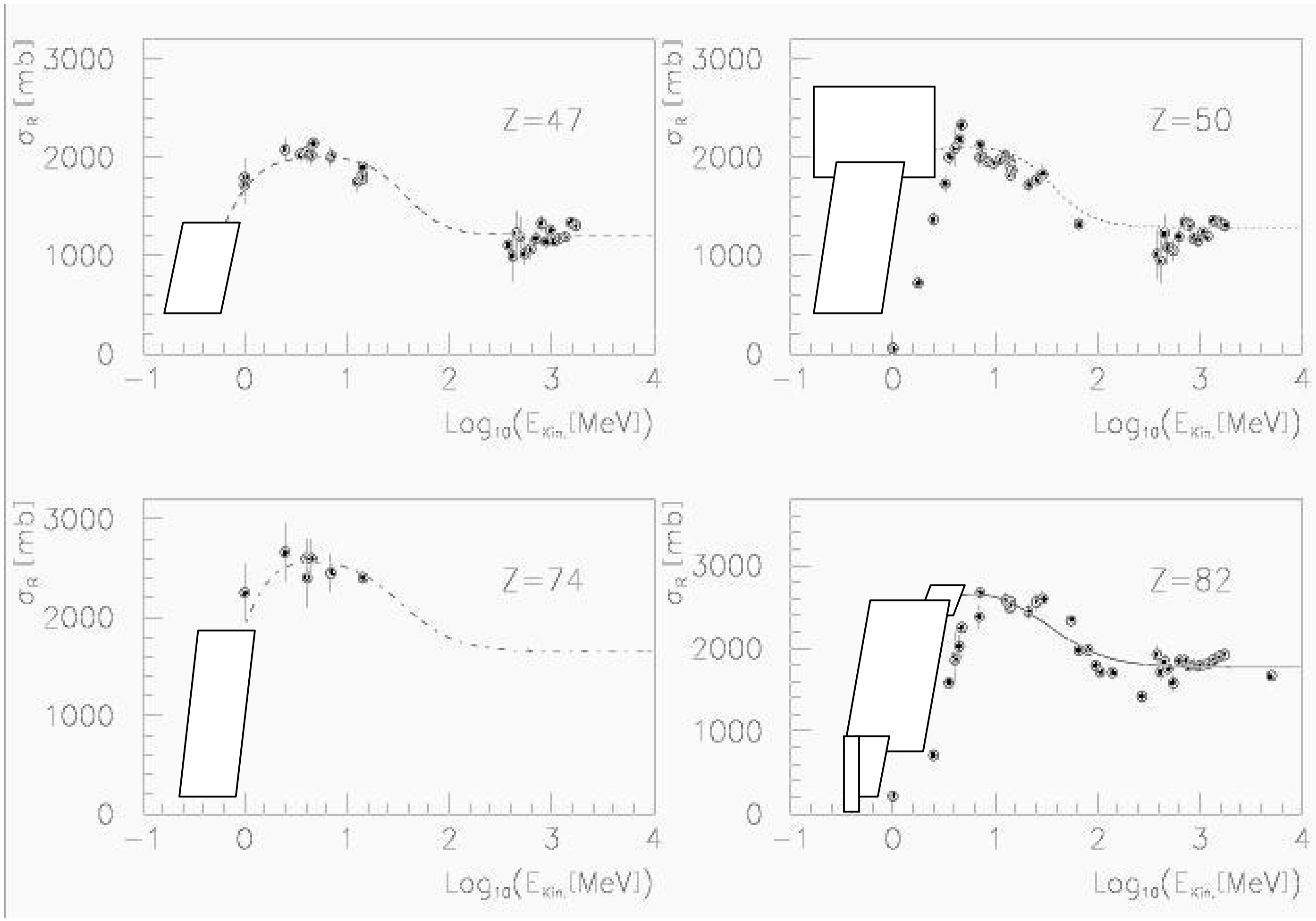
neutron-nuclear reaction cross-sections at high energies



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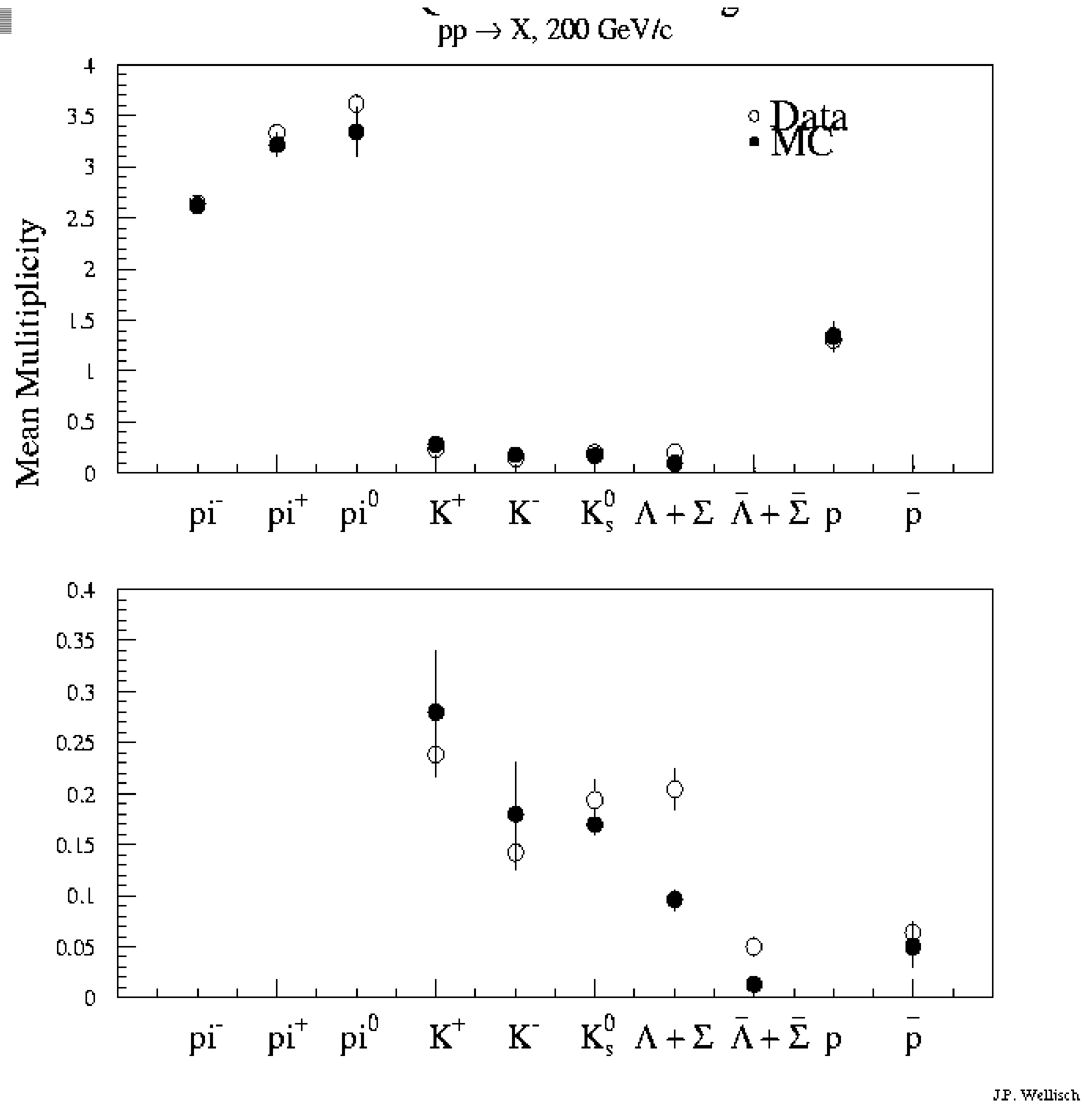
A few examples of thin target comparisons

Particle multiplicities, QGS model

(dots are data, circles are MC)



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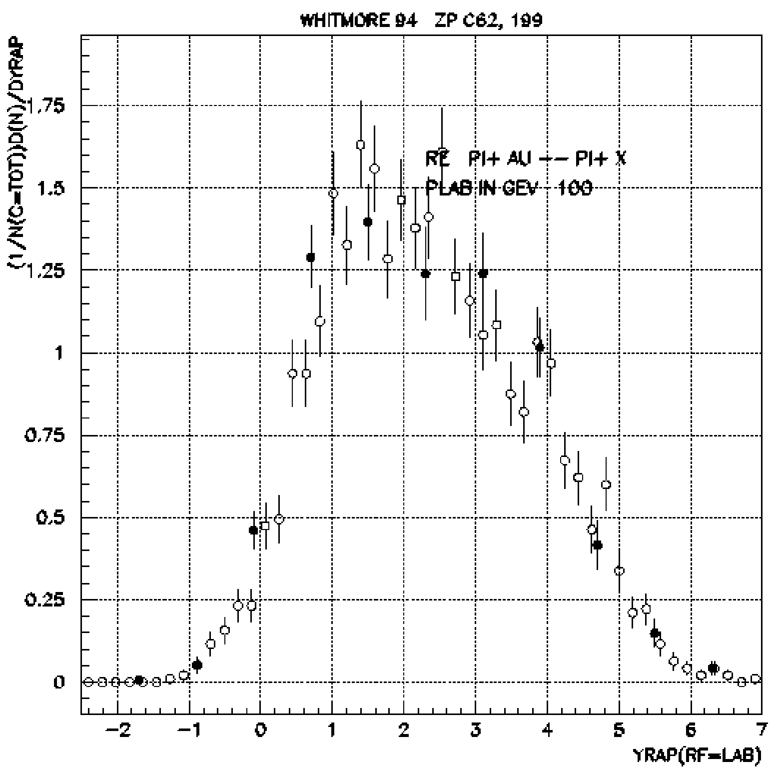
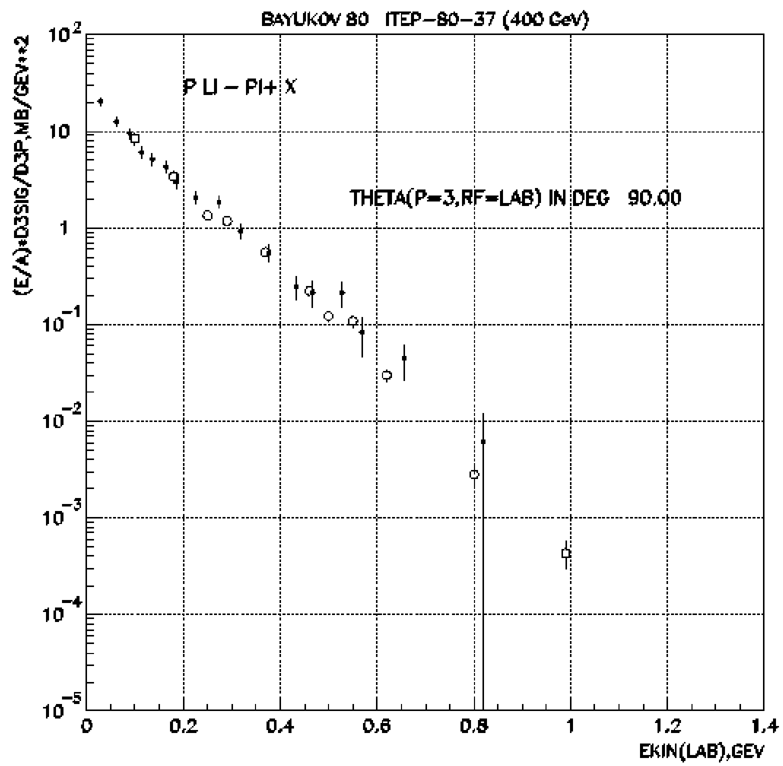
Pion production examples, QGS:

Rapidity distributions and invariant cross-section predictions in quark gluon string model



100 GeV pi+ on Gold



400GeV protons on Lithium

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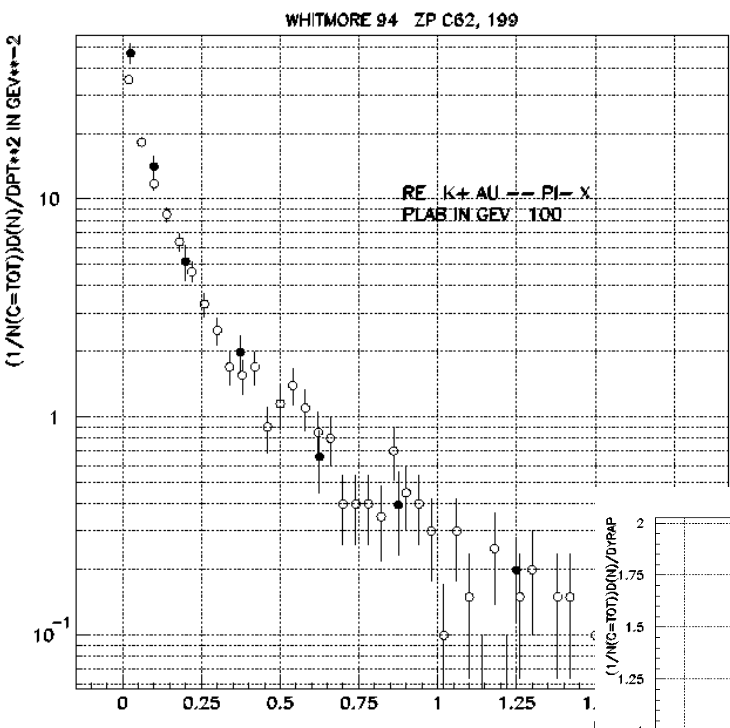
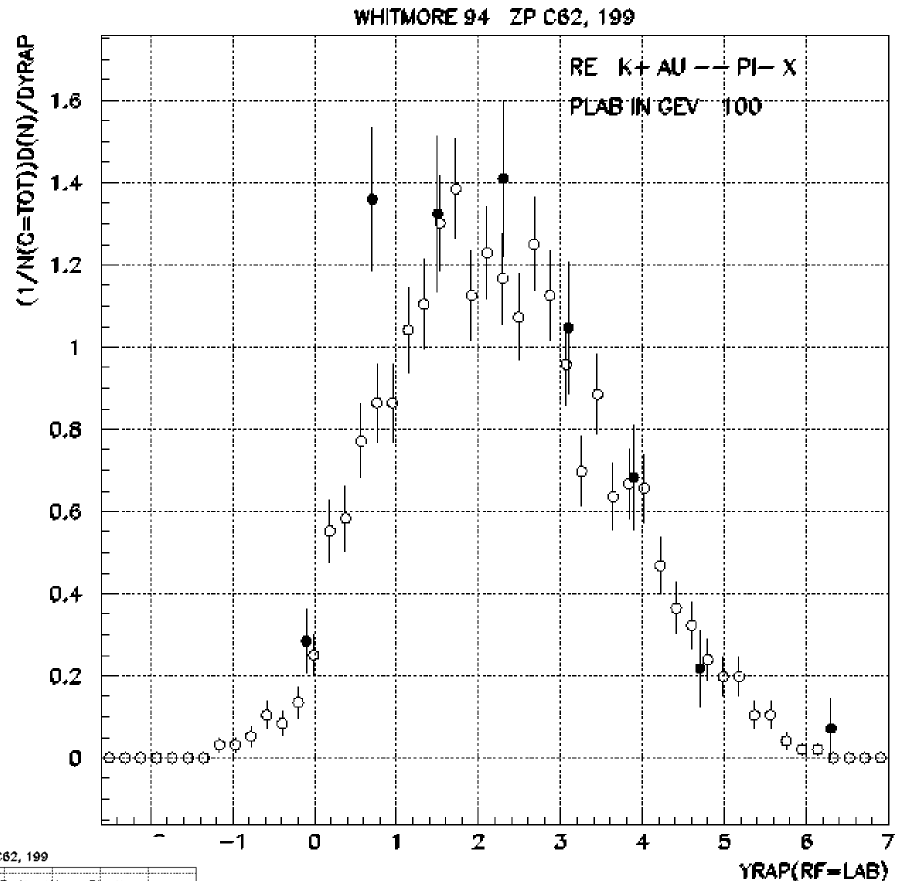
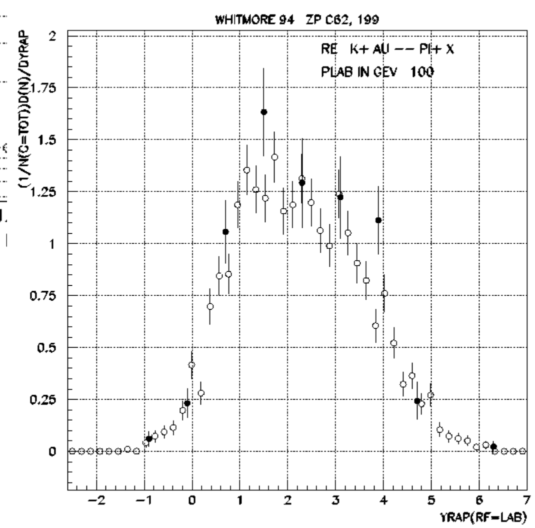
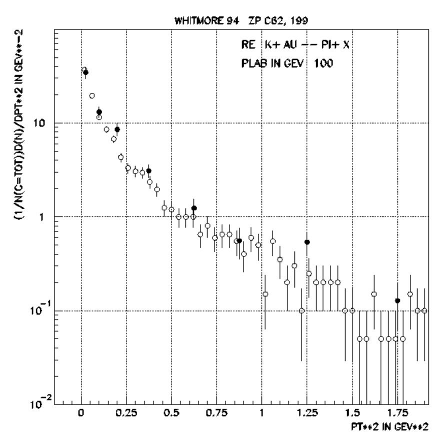
QGS Model
K+ scattering off Gold









Distributions of eta
And transverse momentum.

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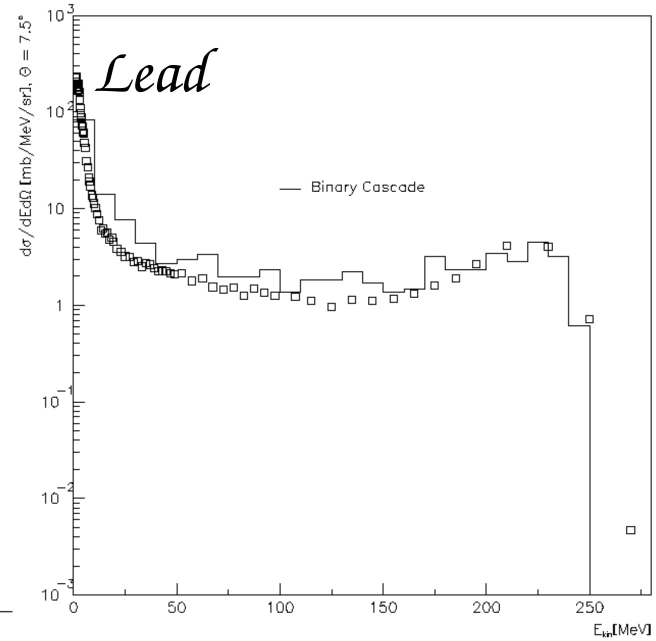
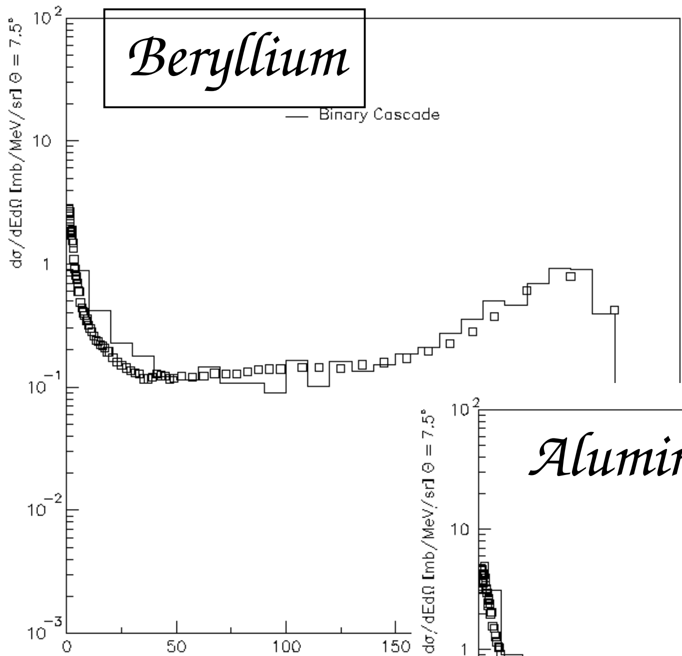
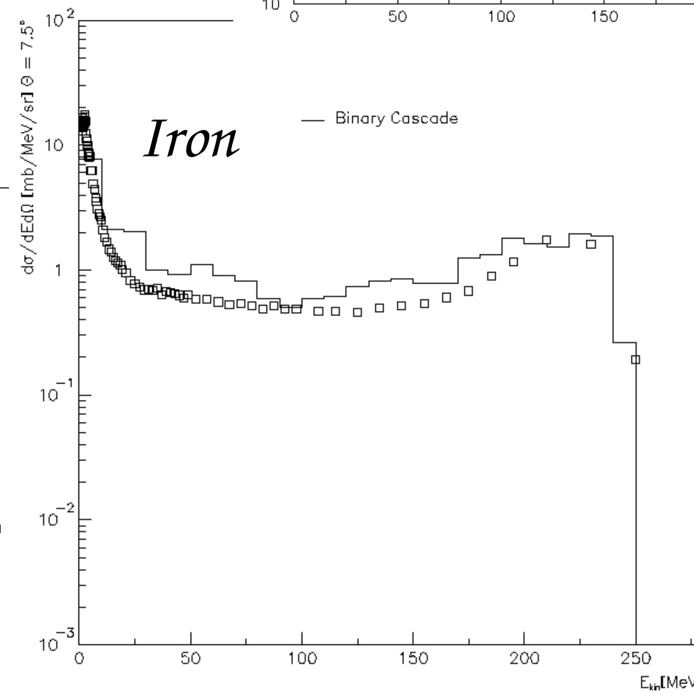
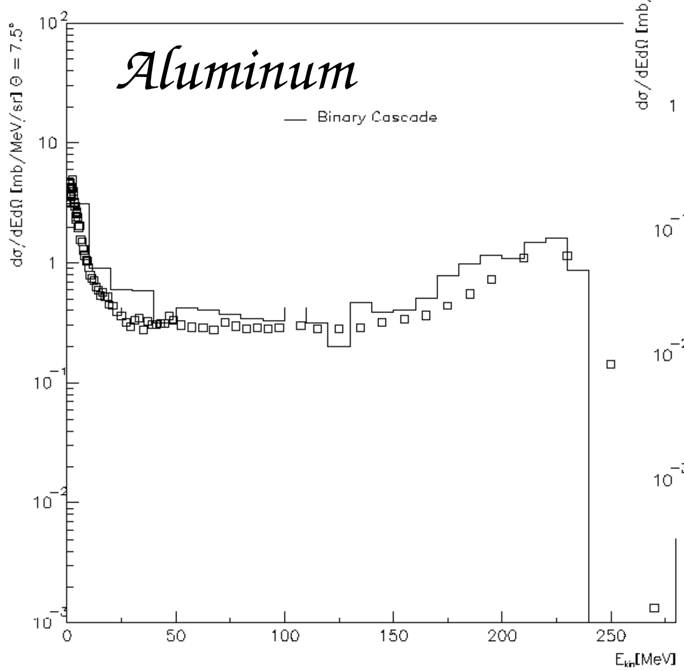
Forward peaks in proton induced neutron production





256 MeV data
Neutrons at 7.5deg.





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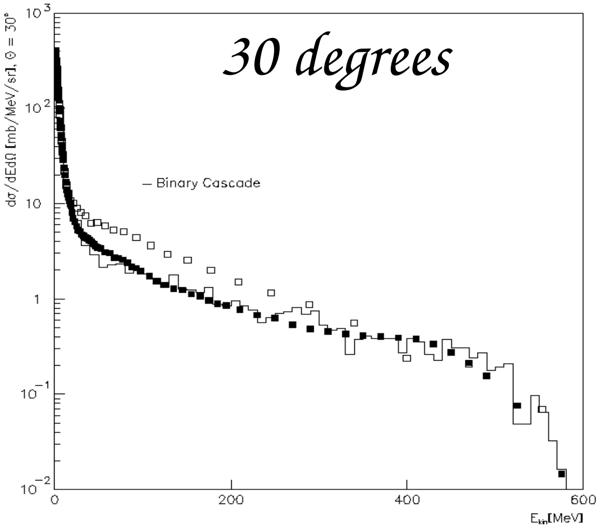
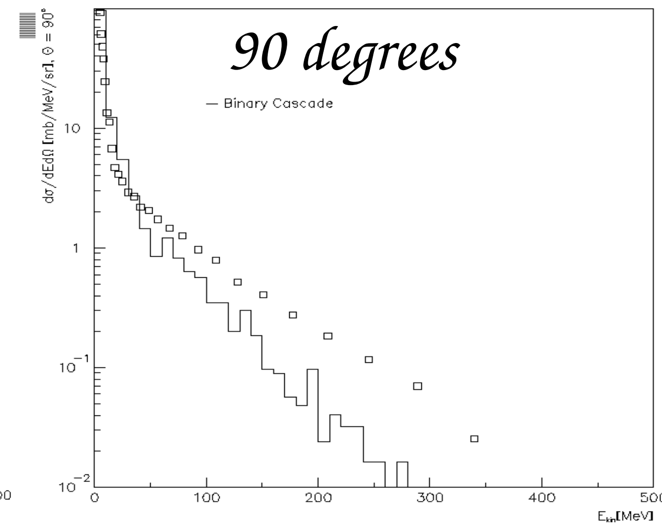
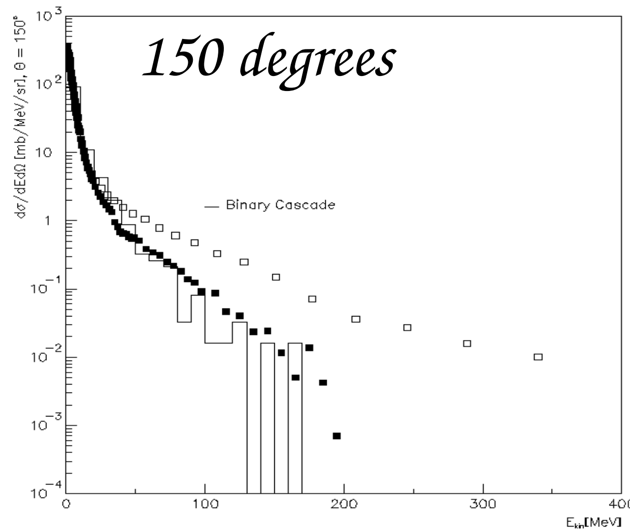
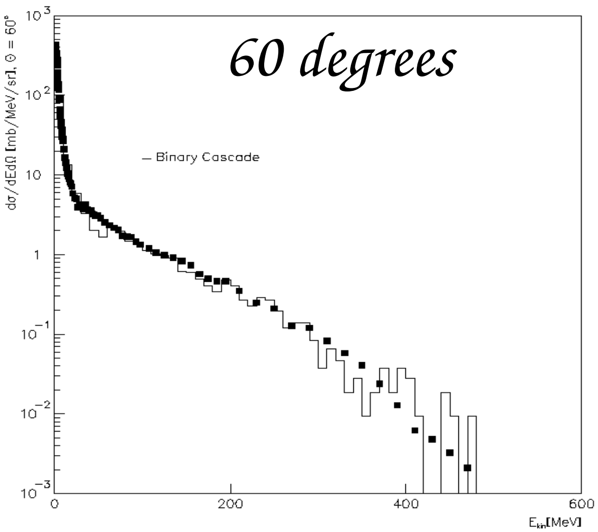
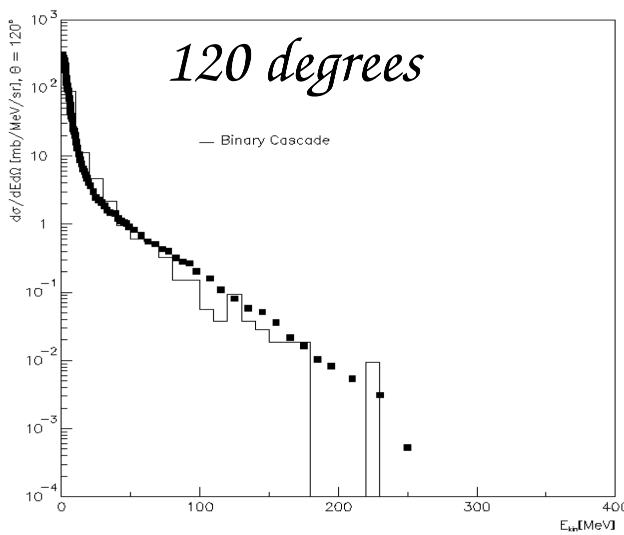
Binary cascade: Neutrons from 597 MeV p on Pb (PRC 22, p1184)











Neutron production
At 30, 60, 90, 120
And 150 degrees

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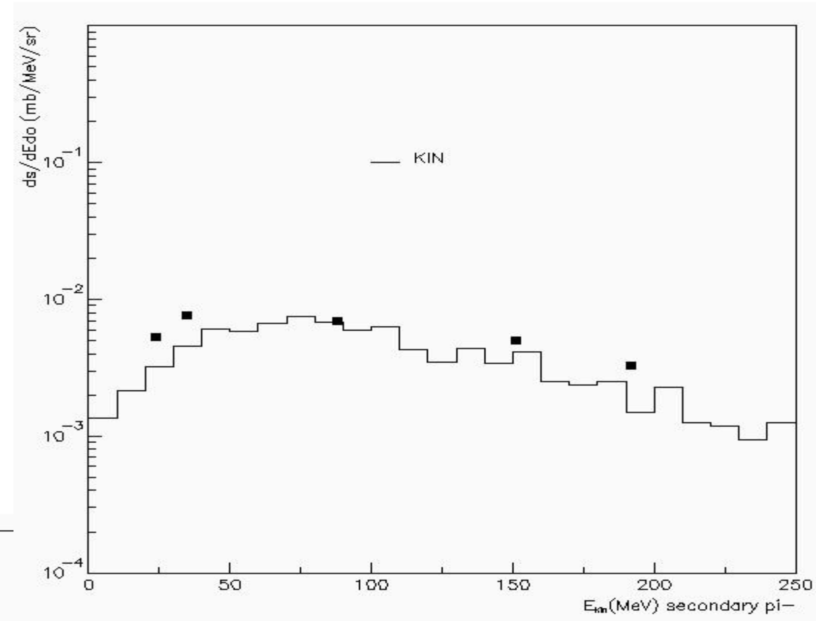
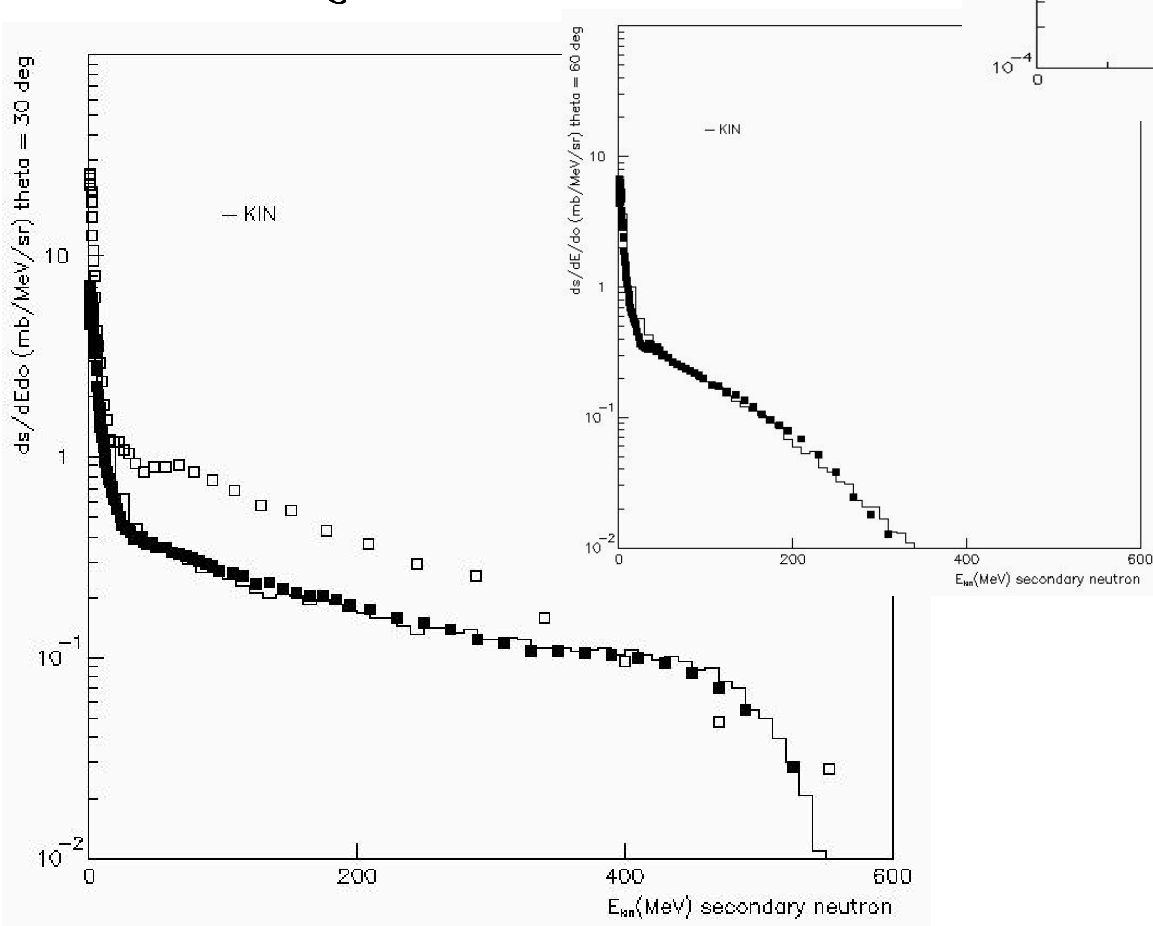
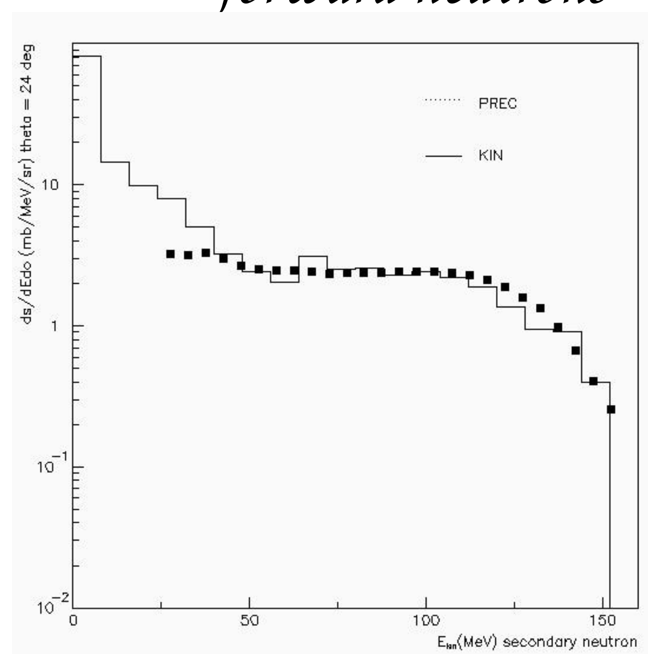
Binary cascade

585MeV p on Al, forward And backward n and π

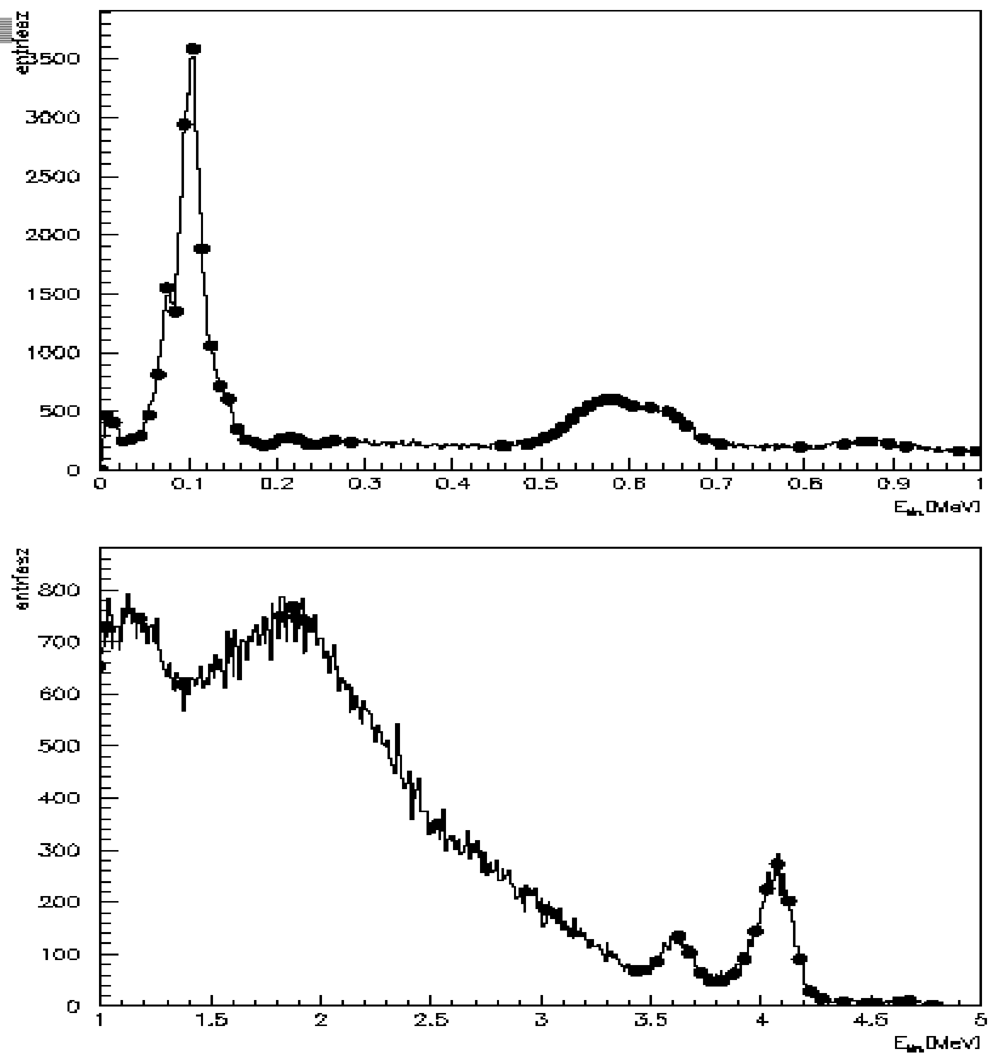




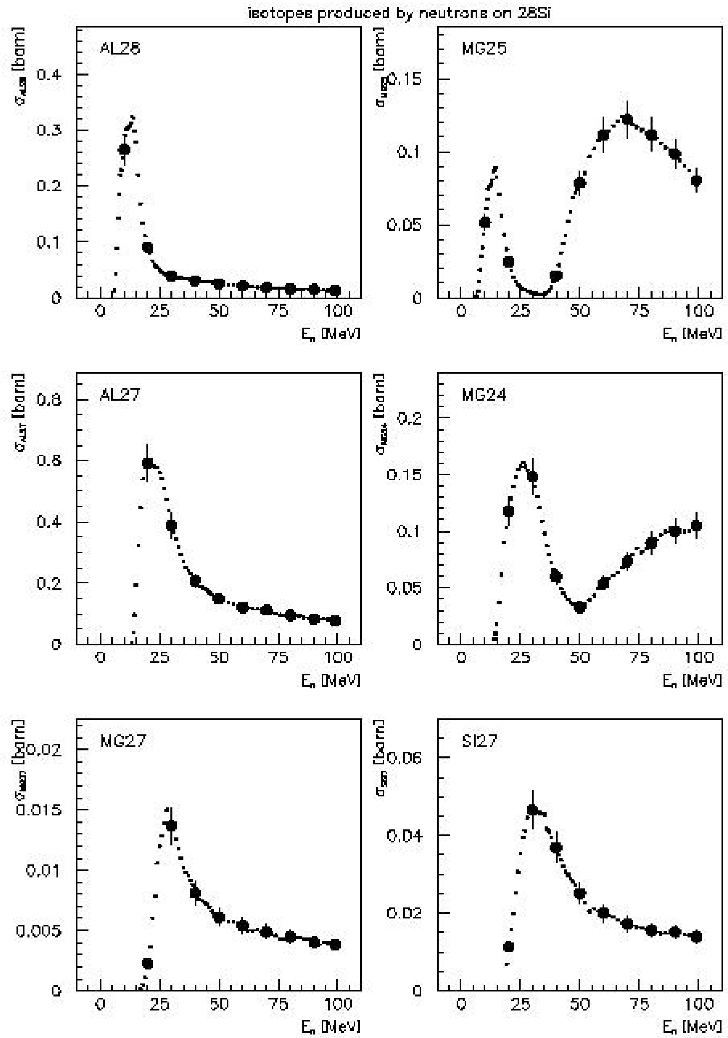
160 MeV p on Pb, forward neutrons



Low energy neutron capture:
gammas from 14 MeV capture on Uranium



Neutron induced isotope production



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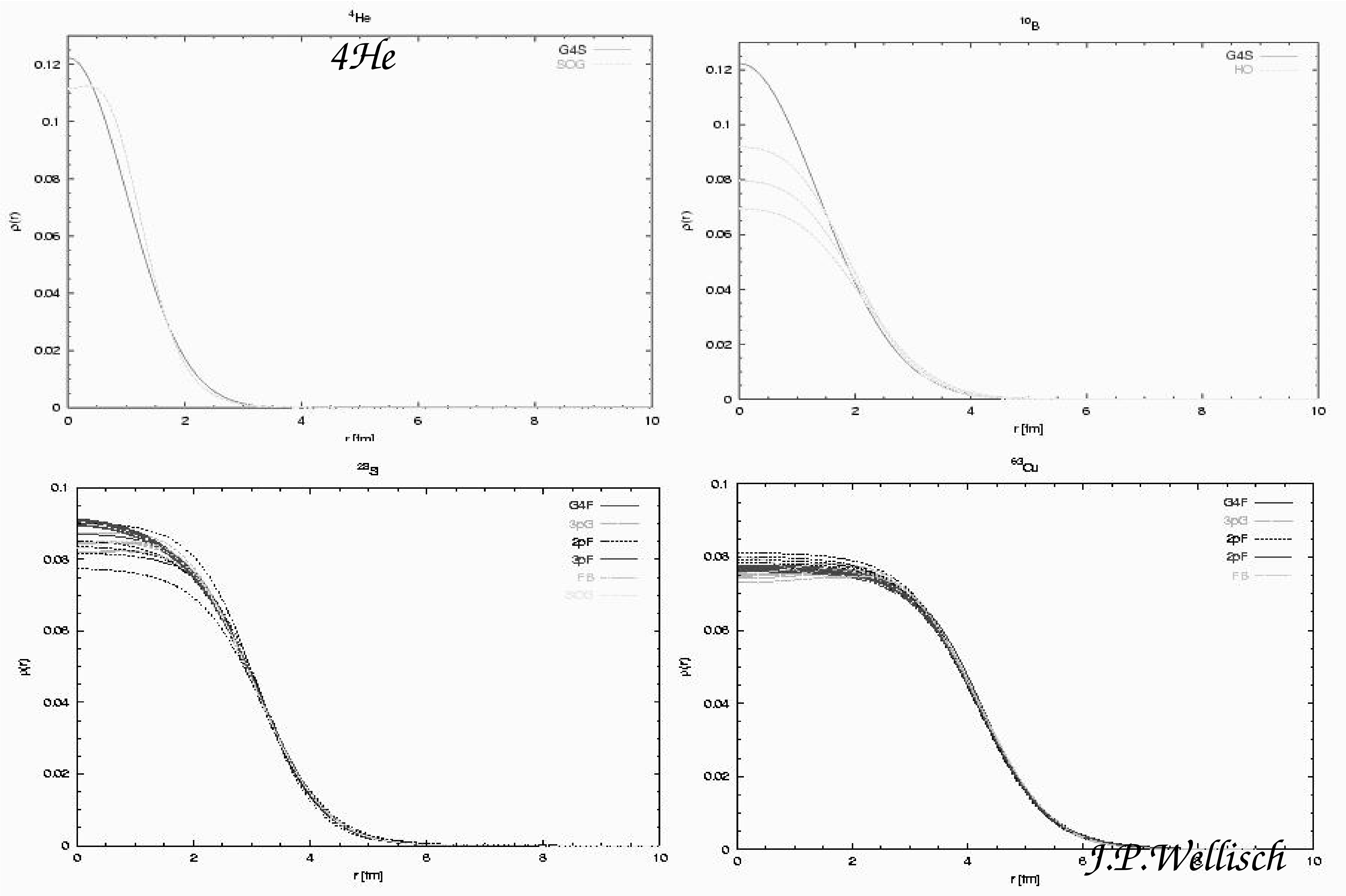
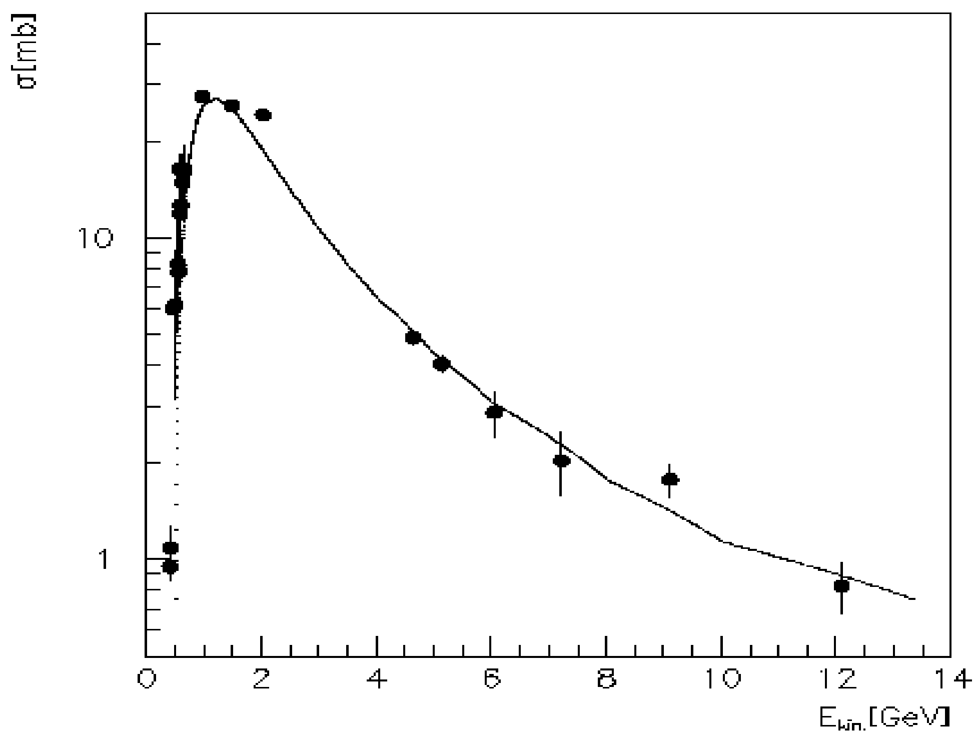
A few verification plots for model components

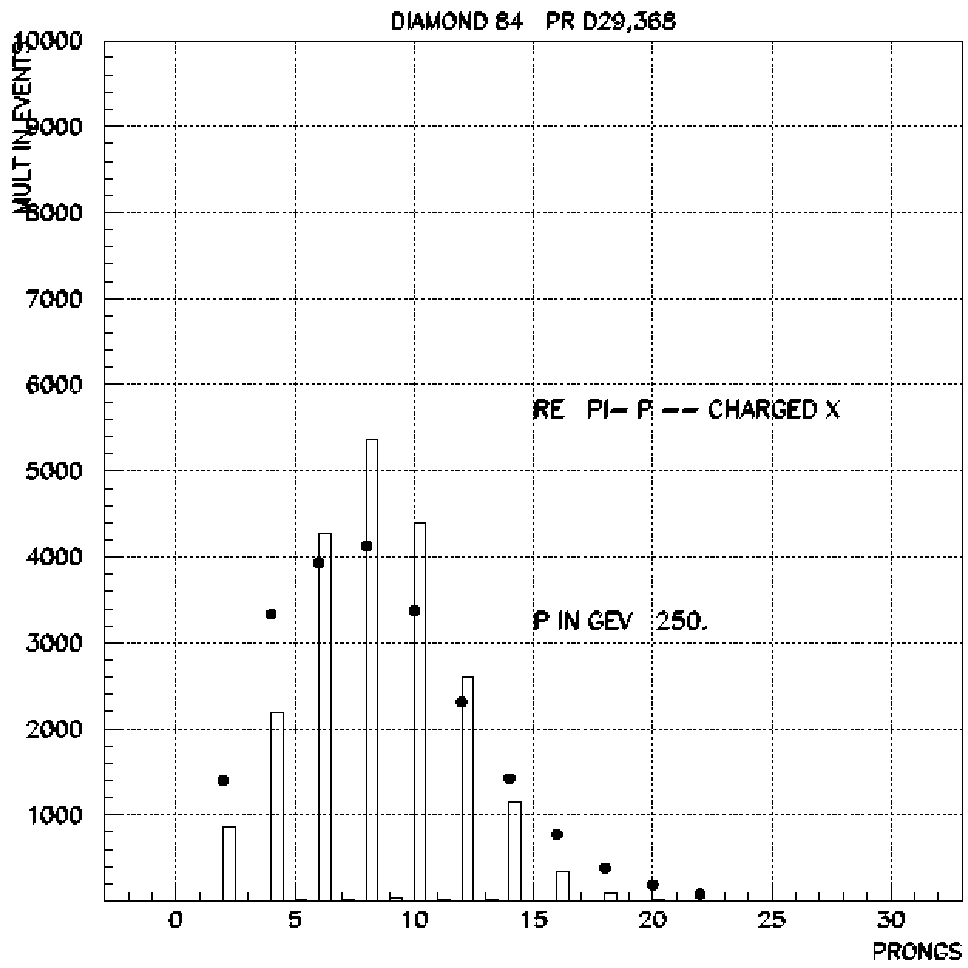
Nuclear densities: Ex. 4He, 10B, 28Si, and 63Cu



Predicting the Delta production cross-section in pp scattering by binary casacde



prongs prediction in QGS model , single pomeron exchange approximation.



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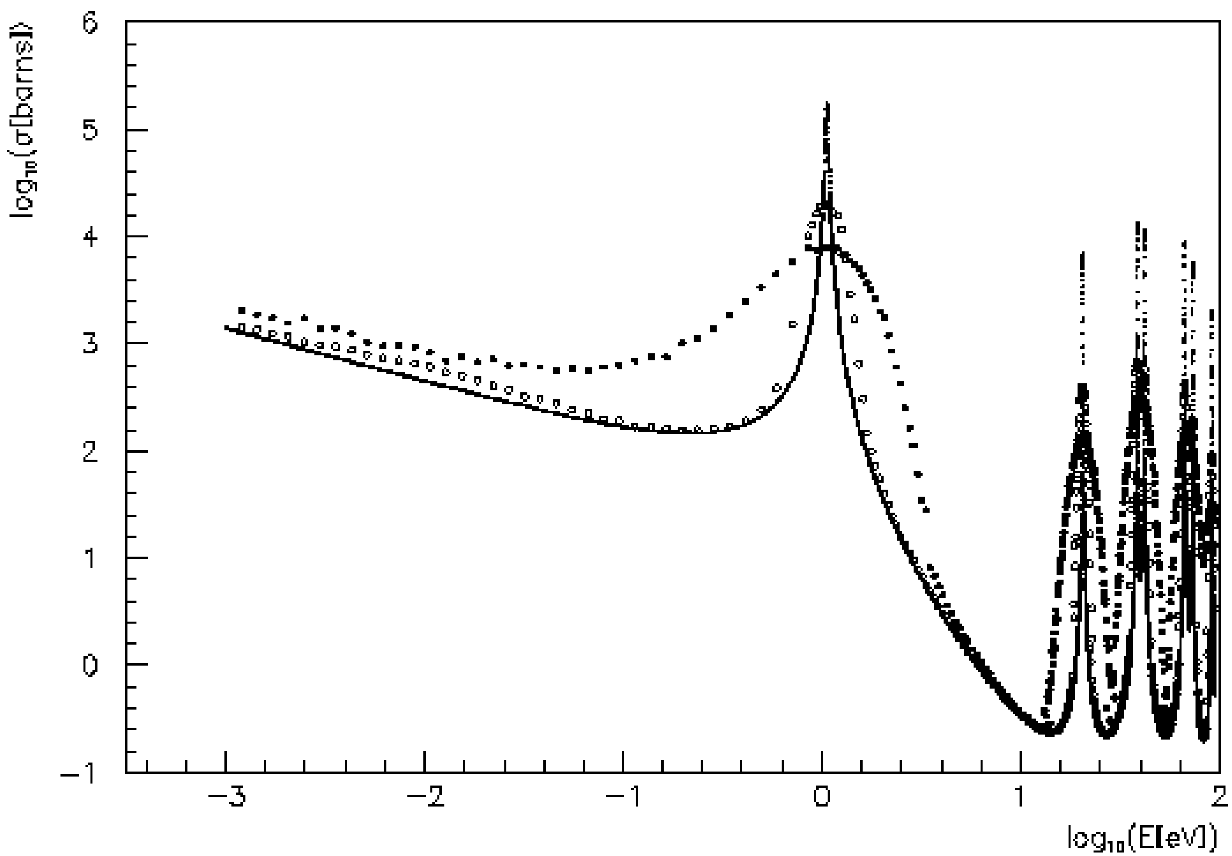
Doppler broadening (low energy neutrons)



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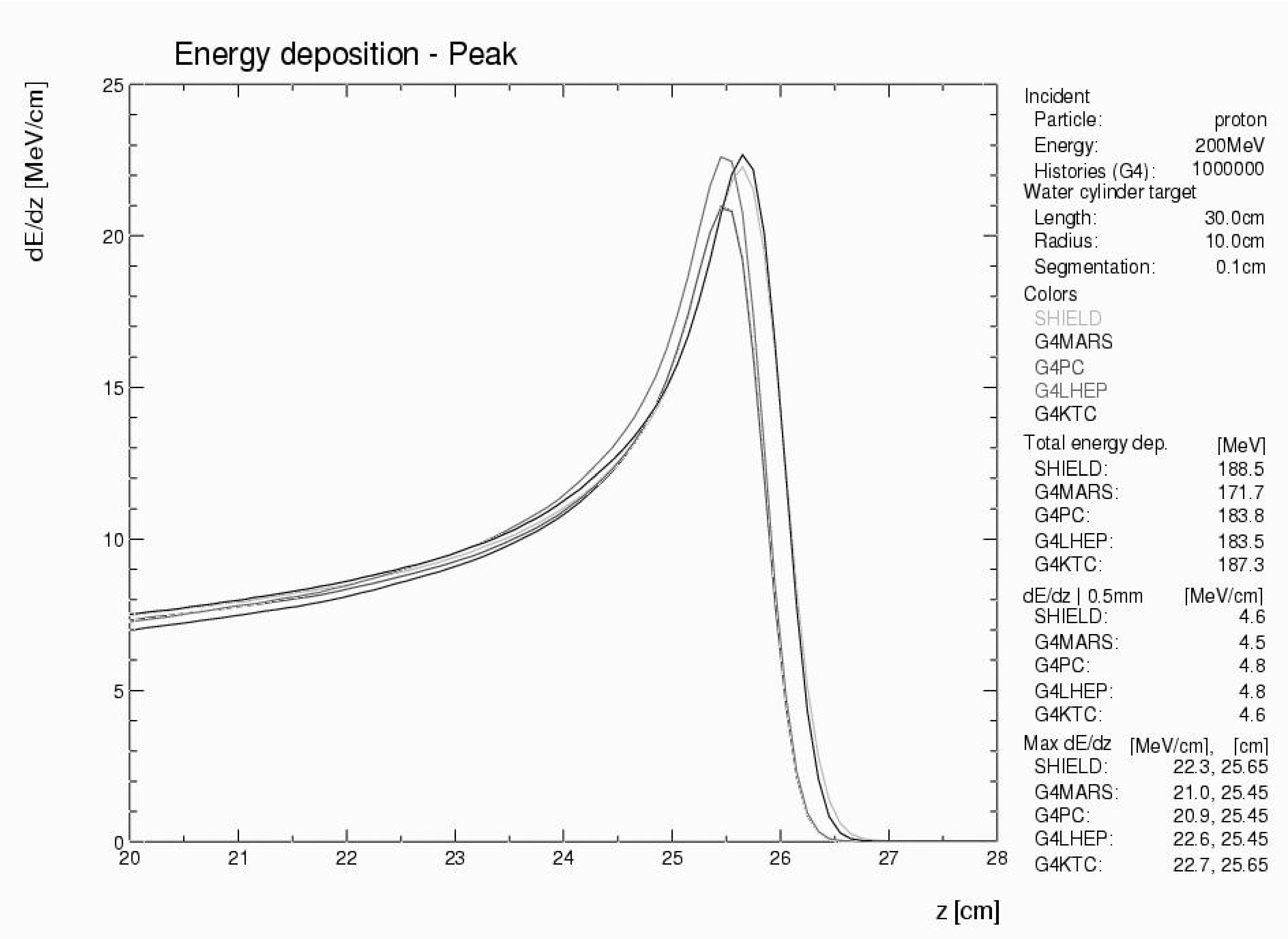
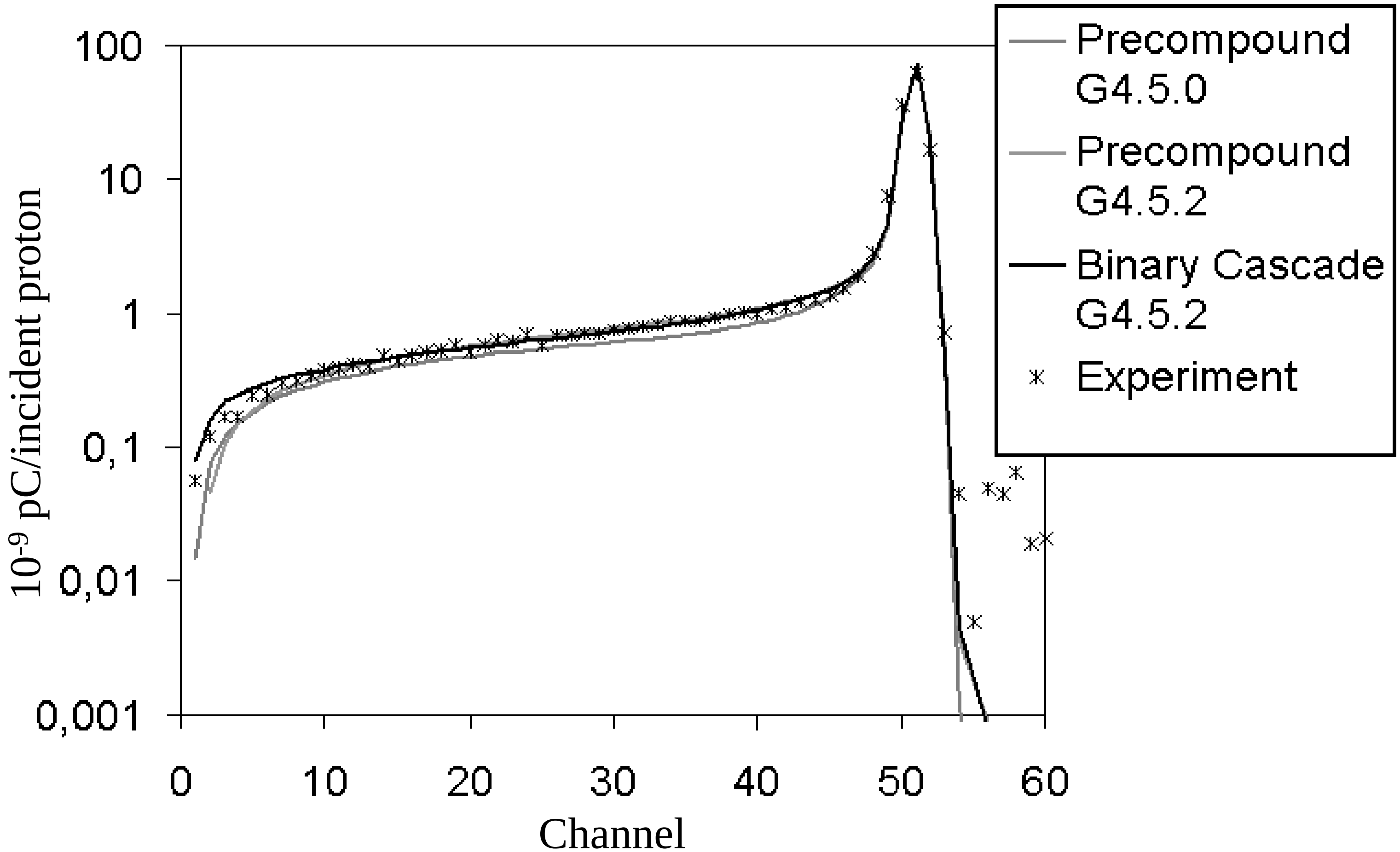
A few code comparisons

Gammas and conversion electrons in ^{57}Co: geant4 vs. RADLIST

	RADLIST (BNL)		Geant4	
Radiation	Energy (keV)	Intensity (100dks)	Energy (keV)	Intensity (100dks)
CE K	7.301	71.00 (6.0)	7.301	70.55 (1.88)
CE			12.899	10.00 (0.70)
CE L	13.567	7.40 (0.6)	13.562	5.95 (0.54)
CE			13.687	0.35 (0.13)
CE			14.315	0.85 (0.21)
CE			14.405	0.45 (0.19)
CE K	114.949	1.83 (0.14)	114.949	1.95 (0.31)
CE			120.497	5.70 (0.53)
CE L	121.215	0.19 (0.020)		
CE M+	121.968	0.03 (0.005)		
CE K	129.361	1.30 (0.16)	129.362	1.25 (0.25)
CE			134.910	0.25 (0.11)
γ	14.413	9.16 (0.15)	14.413	10.05 (0.71)
γ	122.061	85.60 (0.17)	122.061	86.05 (2.07)
γ	136.474	10.68 (0.08)	136.474	10.05 (0.71)
γ	692.410	0.15 (0.01)	692.030	0.15 (0.09)


Energy deposition - Peak
dE/dz [MeV/cm]
z [cm]
Incident
Particle: proton
Energy: 200MeV
Histories (G4): 1000000
Water cylinder target
Length: 30.0cm
Radius: 10.0cm
Segmentation: 0.1cm
Colors
SHIELD
G4MARS
G4PC
G4LHEP
G4KTC
Total energy dep. [MeV]
SHIELD: 188.5
G4MARS: 171.7
G4PC: 183.8
G4LHEP: 183.5
G4KTC: 187.3
dE/dz | 0.5mm [MeV/cm]
SHIELD: 4.6
G4MARS: 4.5
G4PC: 4.8
G4LHEP: 4.8
G4KTC: 4.6
Max dE/dz [MeV/cm], [cm]
SHIELD: 22.3, 25.65
G4MARS: 21.0, 25.45
G4PC: 20.9, 25.45
G4LHEP: 22.6, 25.45
G4KTC: 22.7, 25.65

Nuclear interactions with Geant4 versus experiment (G4 5.2 results by Soukup, et al.)



Phantom and experimental results from *H.Paganetti, B.Gottschalk, Medical physics Vol. 30, No.7, 2003*

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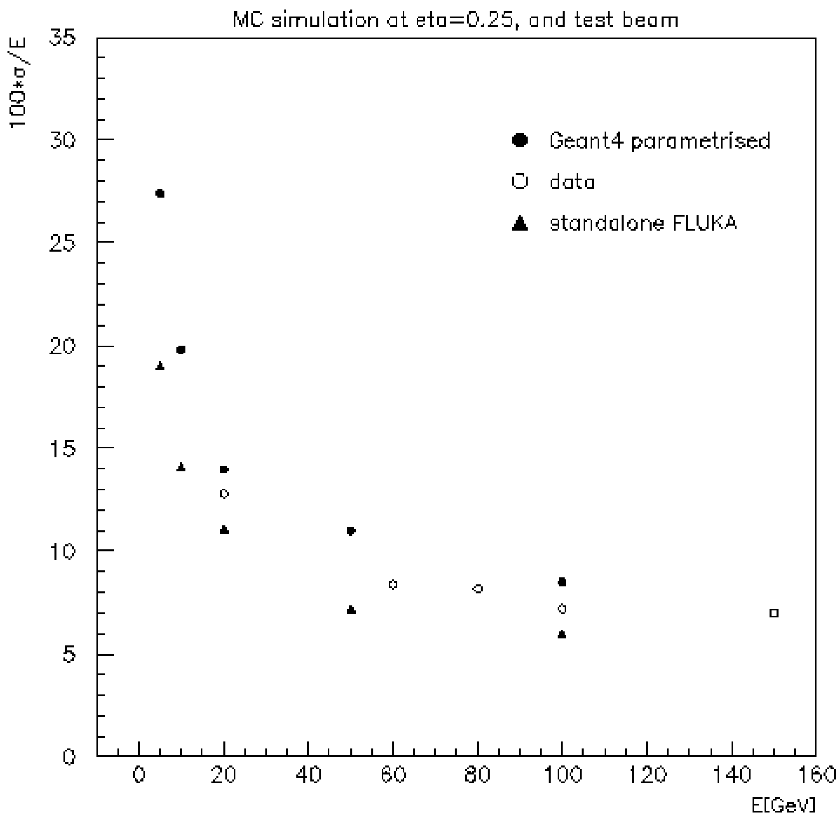
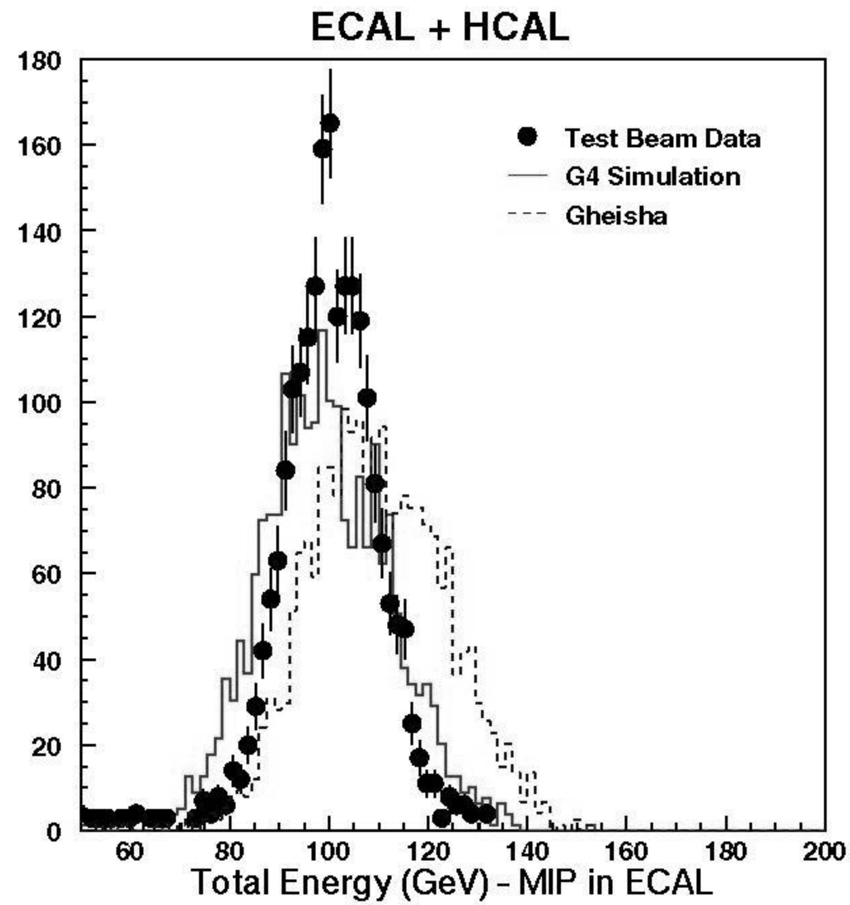
Test-beam sample result,
(a courtesy of the ATLAS and CMS detector groups)



ATLAS TILE prelim.



CMS combined prelim.

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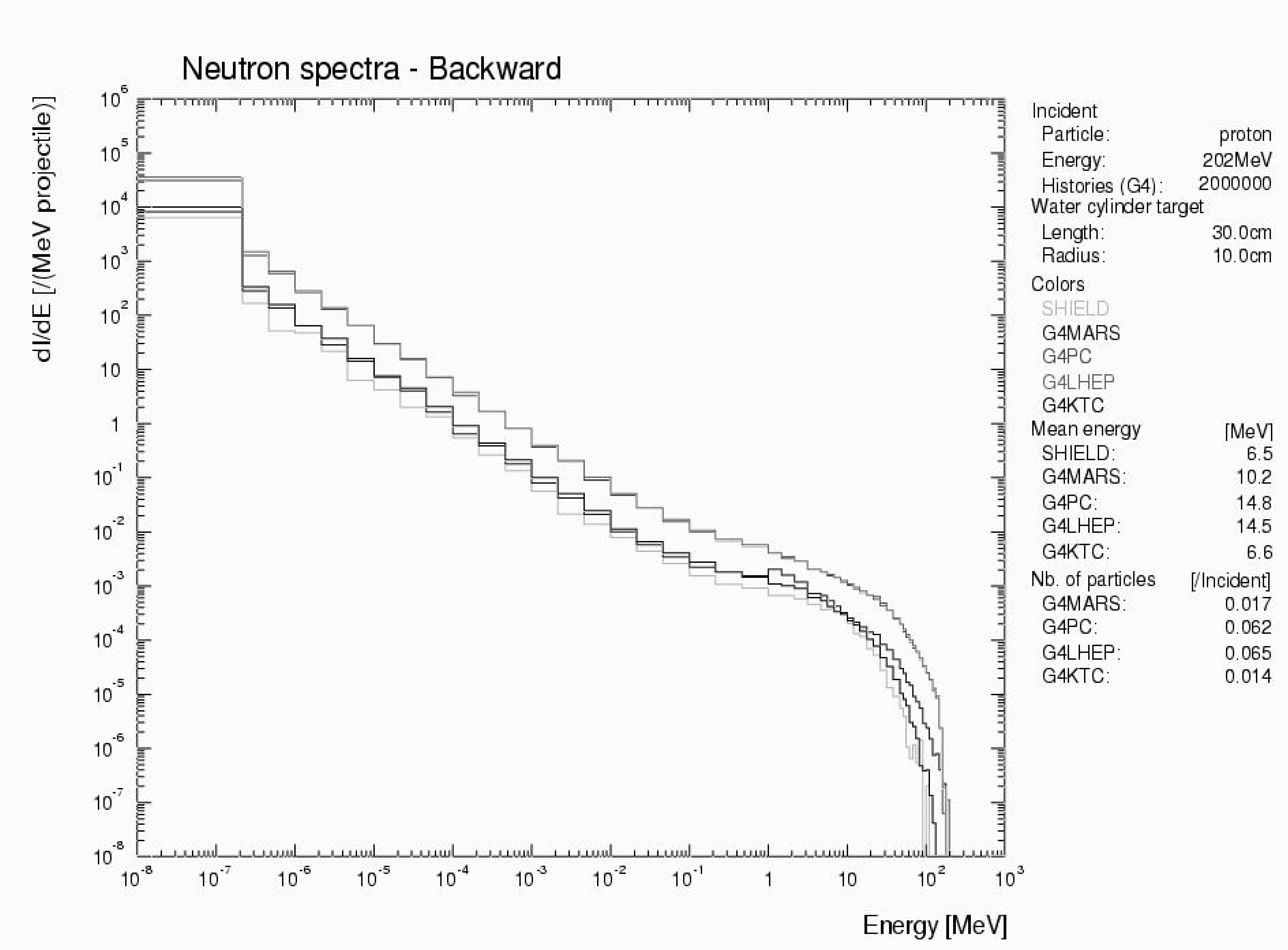
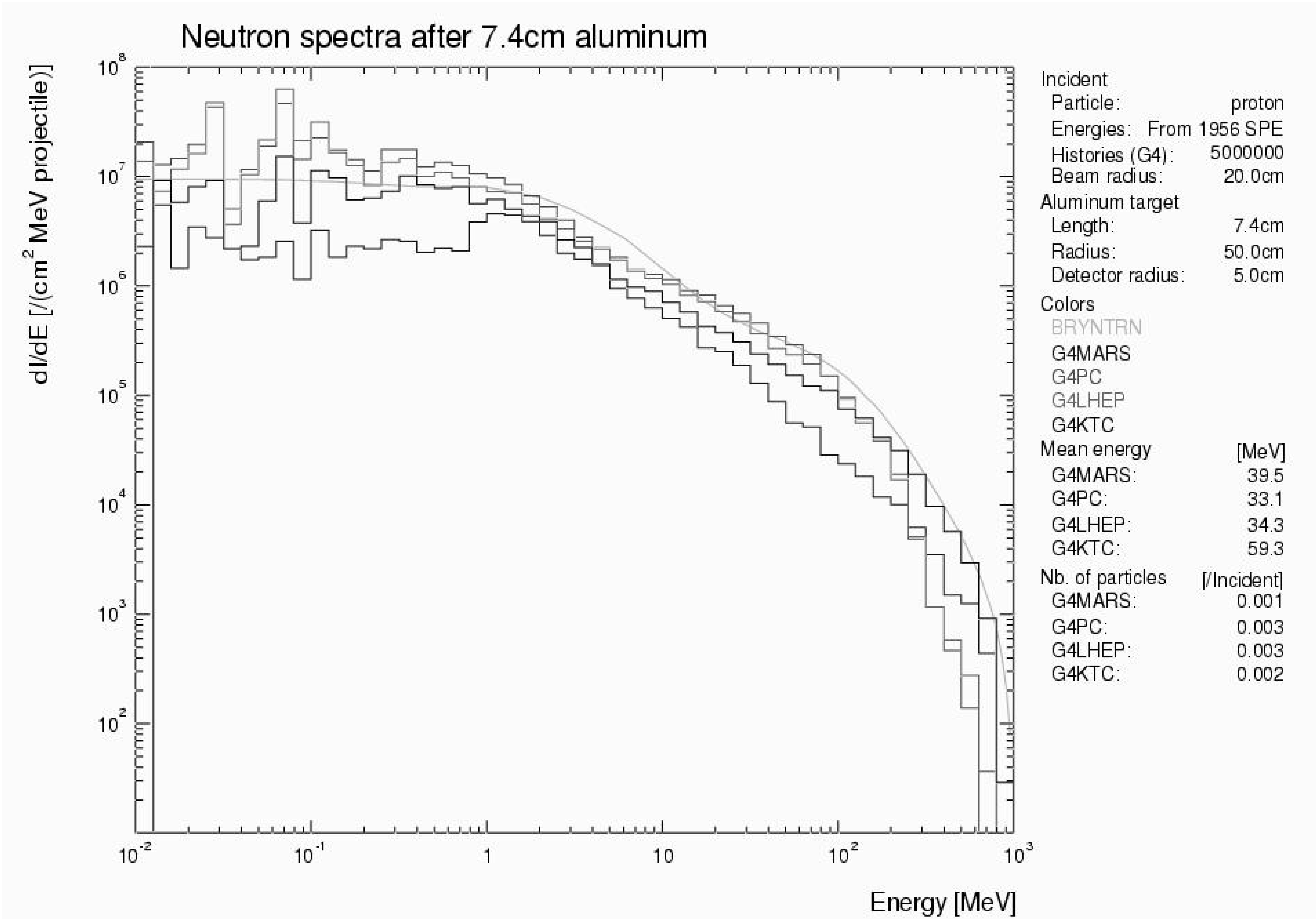
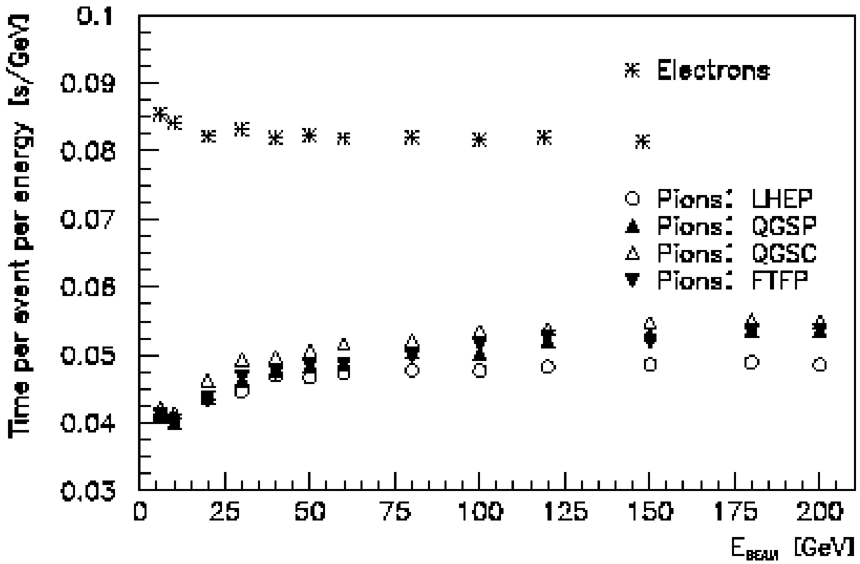

Neutron spectra - Backward
dI/dE [/(MeV projectile)]
Energy [MeV]
Incident
Particle: proton
Energy: 202MeV
Histories (G4): 2000000
Water cylinder target
Length: 30.0cm
Radius: 10.0cm
Colors
SHIELD
G4MARS
G4PC
G4LHEP
G4KTC
Mean energy [MeV]
SHIELD: 6.5
G4MARS: 10.2
G4PC: 14.8
G4LHEP: 14.5
G4KTC: 6.6
Nb. of particles [/Incident]
G4MARS: 0.017
G4PC: 0.062
G4LHEP: 0.065
G4KTC: 0.014

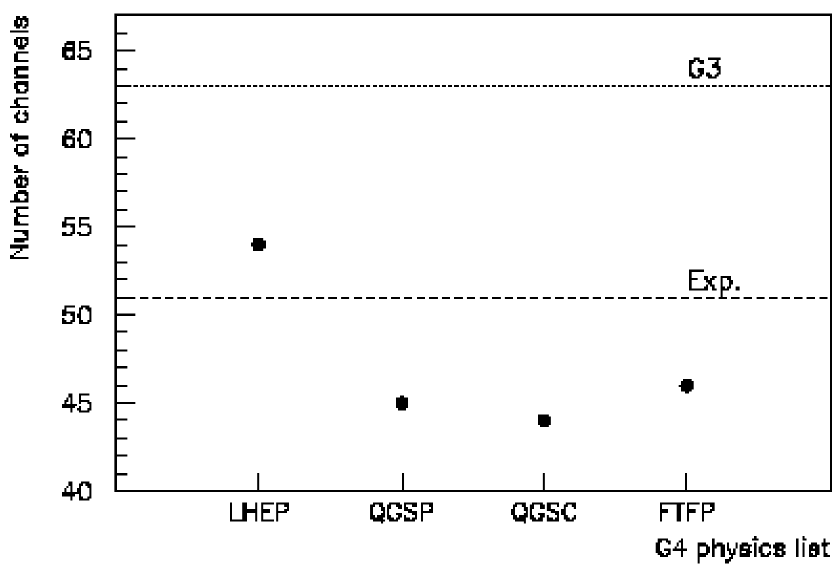

Neutron spectra after 7.4cm aluminum
dI/dE [/(cm^2 MeV projectile)]
Energy [MeV]
Incident
Particle: proton
Energies: From 1956 SPE
Histories (G4): 5000000
Beam radius: 20.0cm
Aluminum target
Length: 7.4cm
Radius: 50.0cm
Detector radius: 5.0cm
Colors
BRYNTRN
G4MARS
G4PC
G4LHEP
G4KTC
Mean energy [MeV]
G4MARS: 39.5
G4PC: 33.1
G4LHEP: 34.3
G4KTC: 59.3
Nb. of particles [/Incident]
G4MARS: 0.001
G4PC: 0.003
G4LHEP: 0.003
G4KTC: 0.002

A few calorimeter simulation comparisons



Time of different G4 simulations

Courtesy of
The ATLAS
HEC community



Size of a pion cluster

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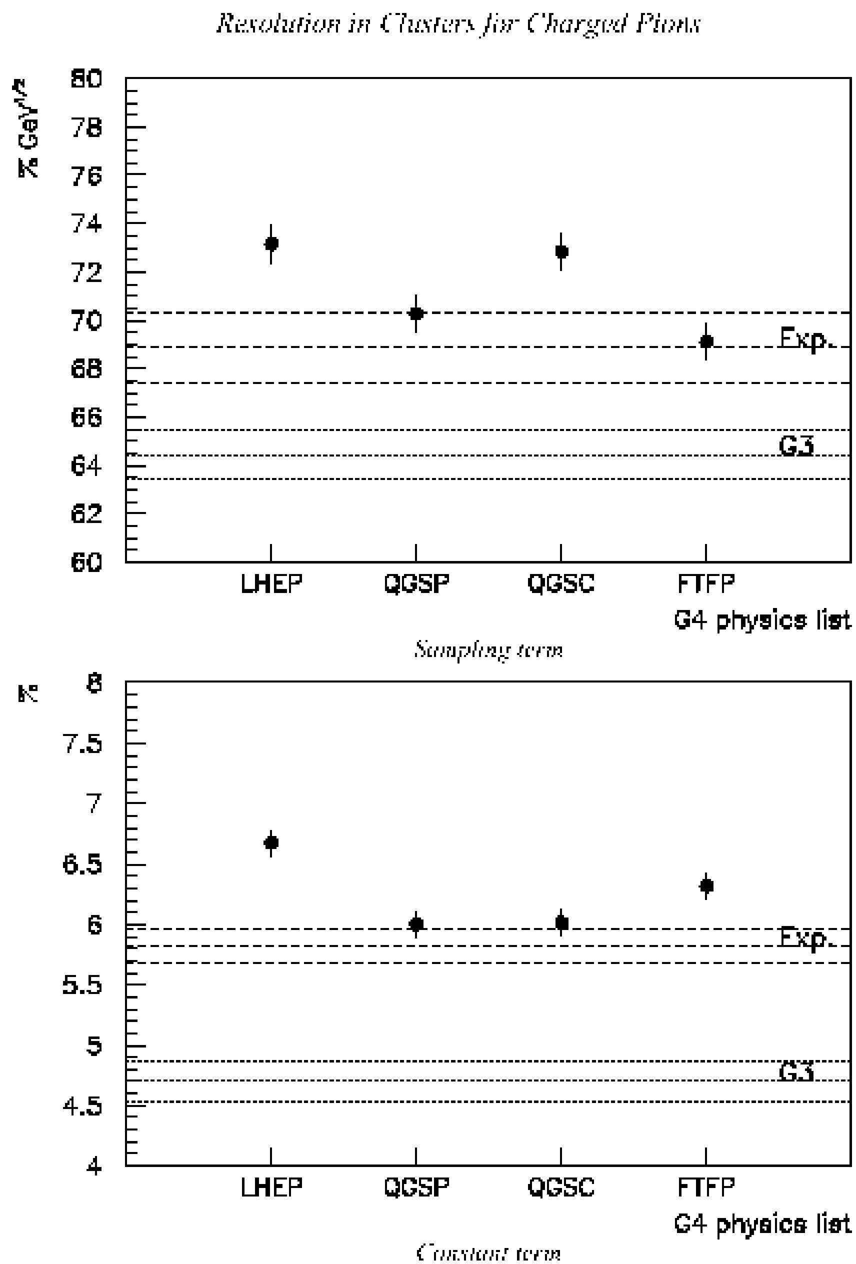
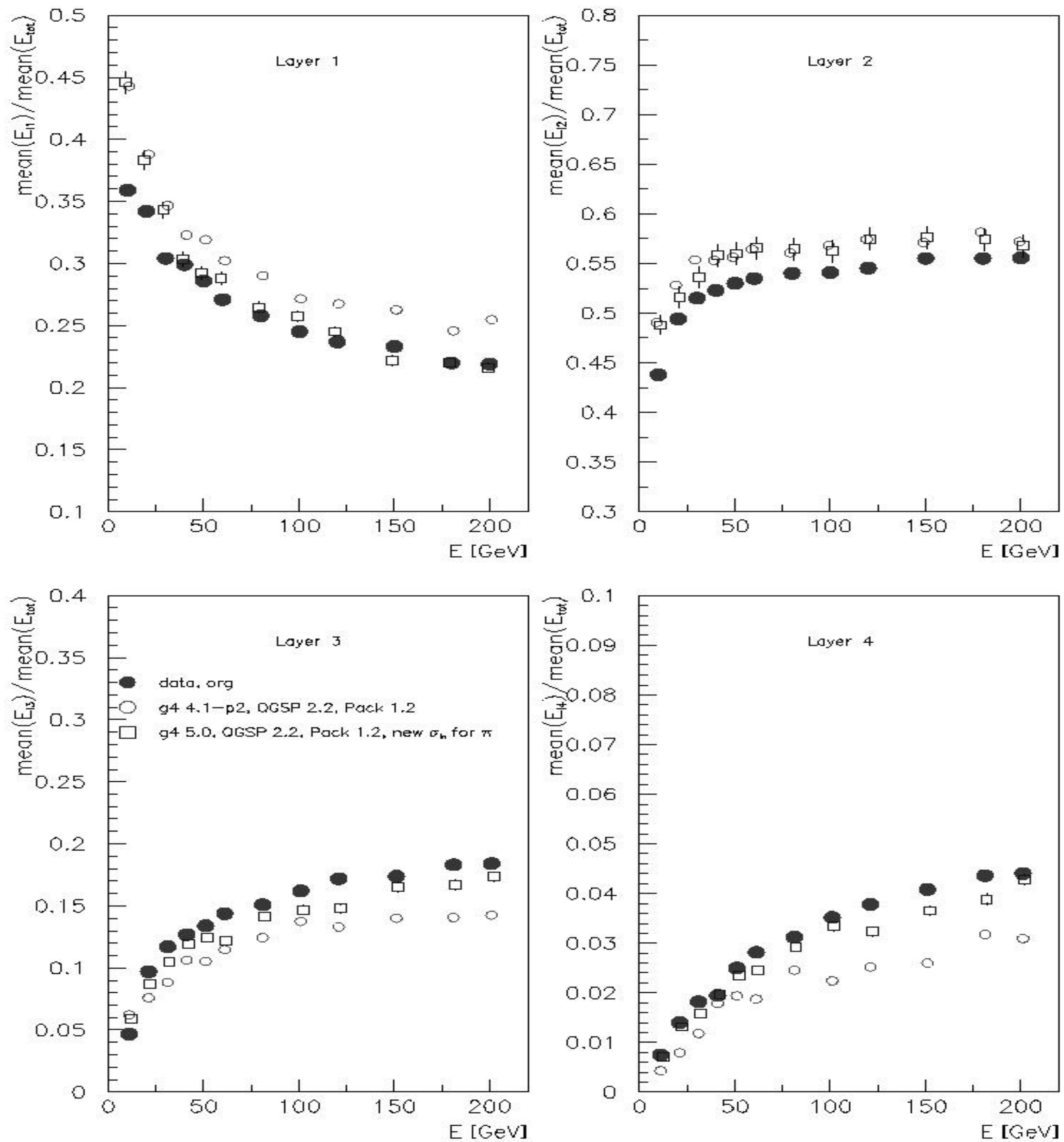


Courtesy of
The ATLAS
HEC community

J.P. Wellisch,
CERN/PH

HEC shower shapes G4 5.0 (true geometry, my toy analysis)

data from NIM, A482,94ff.



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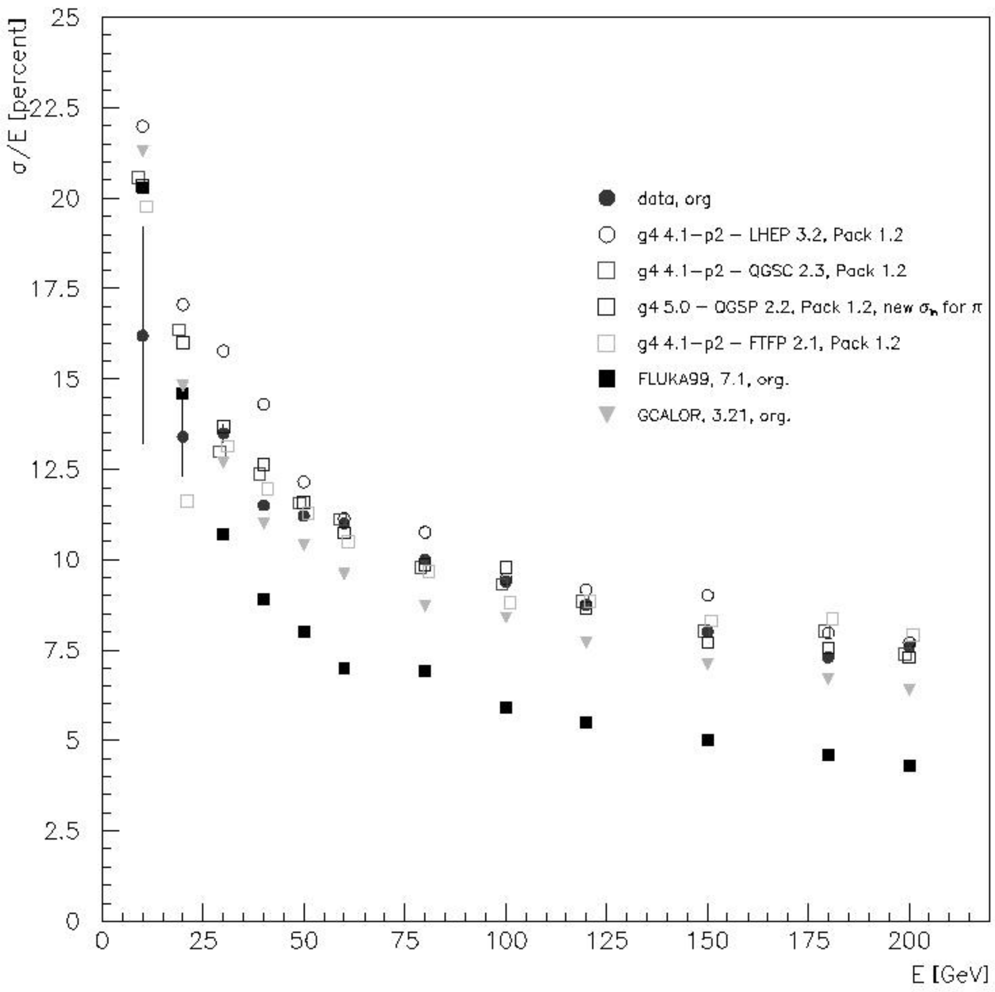
HEC G4 5.0 (true geometry, my toy analysis) data from NIM, A482,94ff.



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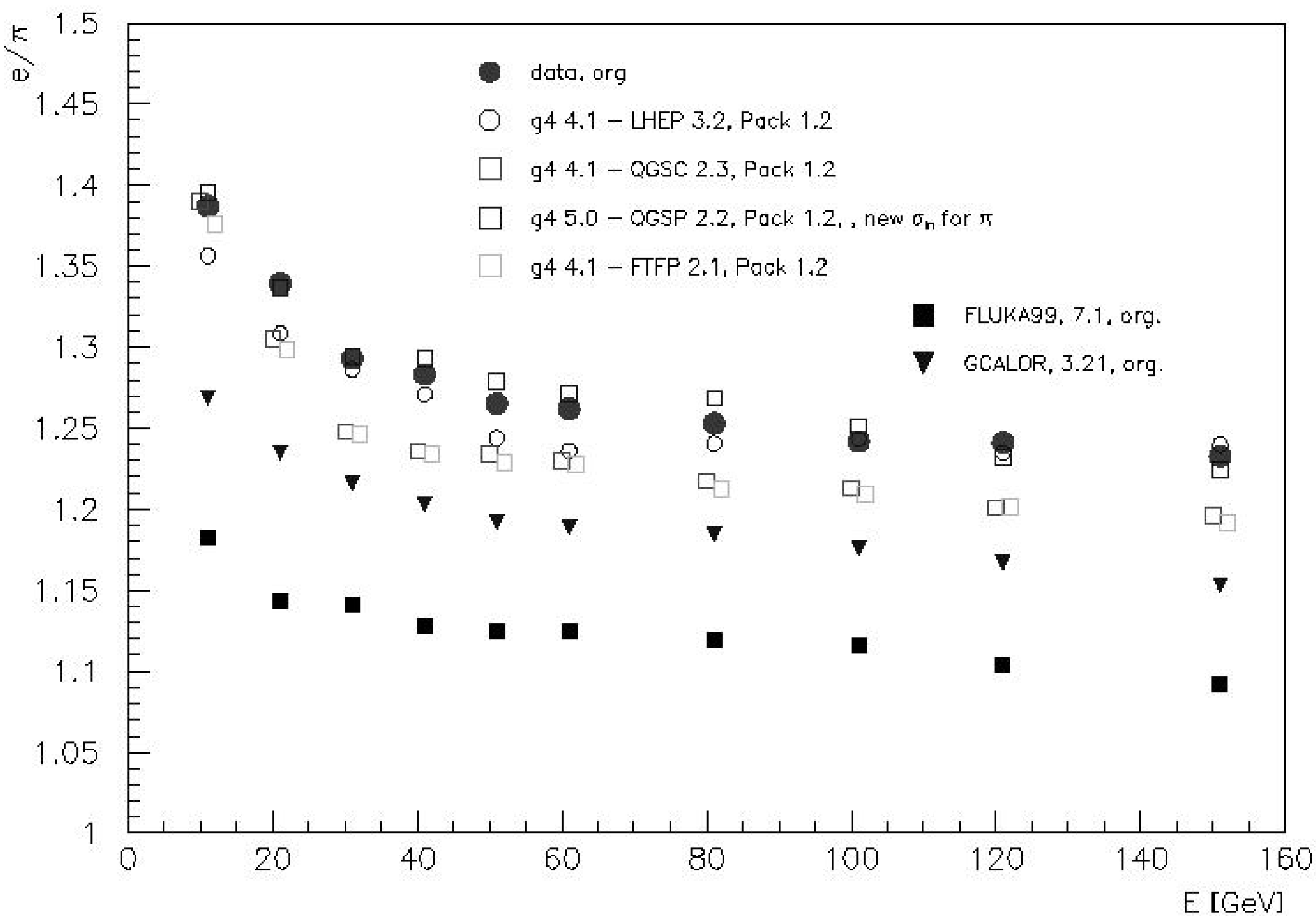
ATLAS HEC G4 5.0 (true geometry, my toy analysis) data from NIM, A482,94ff.



The END?

Tomorrow

- Selected topics of electromagnetic physics
- Some complete calorimeter simulations
  - A courtesy of the validation project, and the detector groups

The END.