

# Determinazione accurata delle masse dei bosoni di Higgs supersimmetrici

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# The Minimal Supersymmetric Standard Model

- Superfield Content:  $\begin{cases} G^a, W^a, B & \text{(vector)} \\ L, Q, E^c, U^c, D^c, H_1, H_2 & \text{(chiral)} \end{cases}$

- MSSM superpotential [ SU(3)×SU(2)×U(1) + R-parity ]

$$W = \mu H_1 H_2 + h^E H_1 L E^c + h^D H_1 Q D^c + h^U H_2 Q U^c$$

- Supersymmetry must be broken without introducing quadratic divergences  $\rightarrow$  “soft” SUSY-breaking terms:

$$-\mathcal{L}_{\text{soft}} = \frac{1}{2} \sum_A M_A \bar{\lambda}_A \lambda_A + \sum_i m_i^2 |\phi_i|^2 + B H_1 H_2 + h^E A^E H_1 L E^c + h^D A^D H_1 Q D^c + h^U A^U H_2 Q U^c$$

- $m_i^2, A^E, A^U, A^D$  are matrices in generation space

$\rightarrow$  the MSSM contains **105** new parameters !!!

- The MSSM phenomenology becomes extremely complex unless we adopt some simplifying assumptions.

## The Higgs sector of the MSSM at tree-level

- Two  $SU(2) \times U(1)$  doublets:  $H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix}$ ,  $H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix}$

$$H_i^0 = \frac{v_i + S_i + i P_i}{\sqrt{2}} \quad \tan \beta = \frac{v_2}{v_1}$$

- The soft SUSY-breaking mass terms for  $H_1^0$  and  $H_2^0$  are responsible for electroweak symmetry breaking (EWSB):

$$V_{\text{tree}} = (m_{H_1}^2 + \mu^2) |H_1^0|^2 + (m_{H_2}^2 + \mu^2) |H_2^0|^2 \\ + B (H_1^0 H_2^0 + \text{h.c.}) + \frac{1}{8} (g^2 + g'^2) (|H_1^0|^2 - |H_2^0|^2)^2$$

- Five physical states:  $h$ ,  $H$ ,  $A^0$ ,  $H^+$ ,  $H^-$

- Tree-level mass matrix for the CP-even sector:

$$(\mathcal{M}_S^2)^{\text{tree}} = \begin{pmatrix} m_Z^2 c_\beta^2 + m_A^2 s_\beta^2 & -(m_Z^2 + m_A^2) s_\beta c_\beta \\ -(m_Z^2 + m_A^2) s_\beta c_\beta & m_Z^2 s_\beta^2 + m_A^2 c_\beta^2 \end{pmatrix}$$

→  $m_h$  and  $m_H$  are predicted in terms of  $m_Z$ ,  $m_A$  and  $\tan \beta$

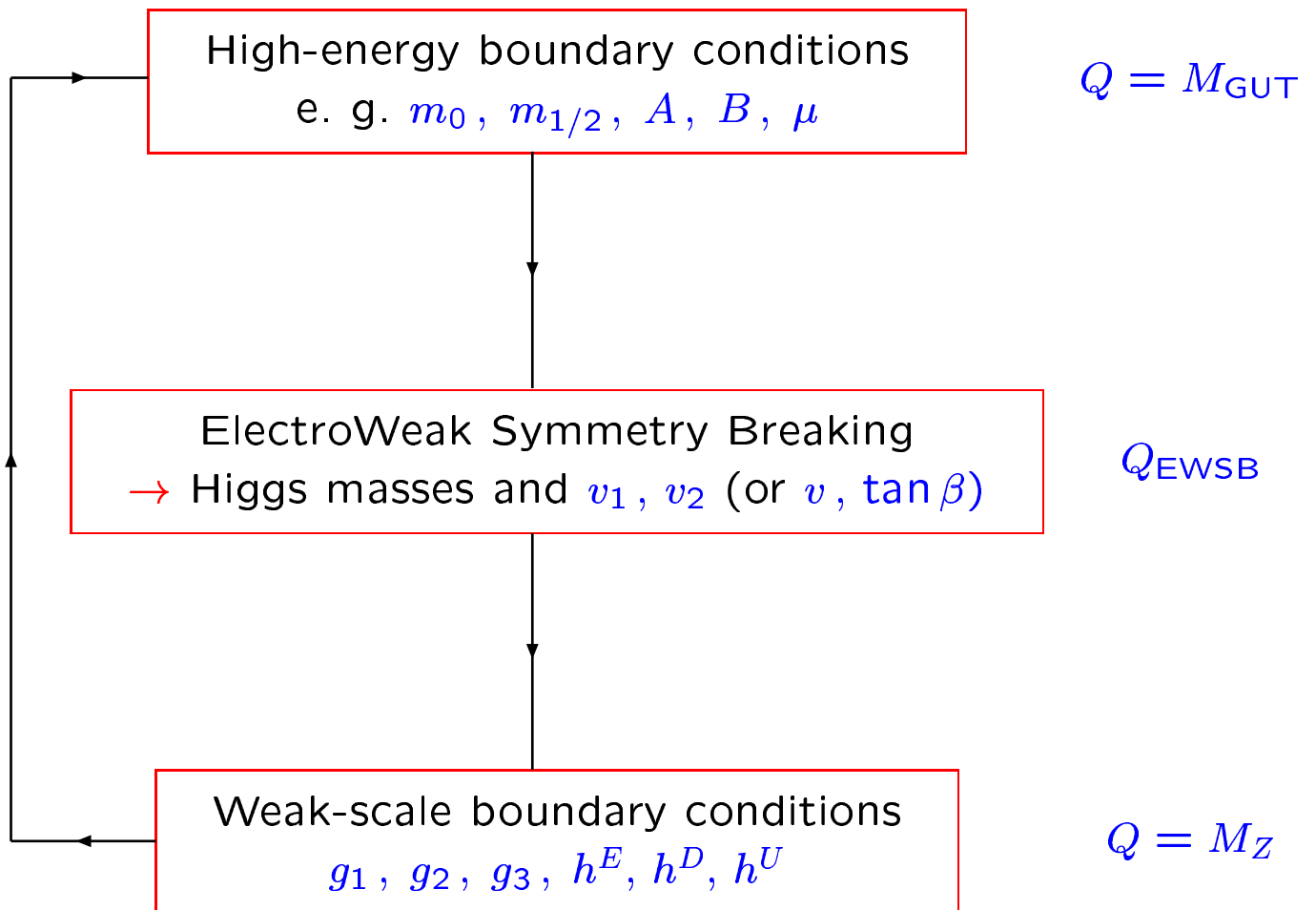
- Tree-level mass relation:  $m_h^2 \leq \cos^2 2\beta m_Z^2$  !!!

- Radiative corrections can push  $m_h$  well above the tree-level bound (e.g.  $m_h \leq 135$  GeV for typical parameter choices) and introduce a dependence on many MSSM parameters.

# High-energy boundary conditions and RG evolution

- Determining the MSSM mass spectrum becomes feasible if at some high-energy scale  $Q = M_{\text{GUT}}$  the structure of the soft SUSY-breaking terms is dictated by an underlying theory, e. g. :
  - **mSUGRA**:  $m_0, m_{1/2}, A, B, \mu$
  - **GMSB**:  $\Lambda, M_{\text{mess}}, N_{\text{mess}}, B, \mu$
  - **AMSB**:  $m_{3/2}, m_0, B, \mu$
- The gauge couplings  $g_i$  and the Yukawa couplings  $h^E, h^D, h^U$  are given as input at  $Q = M_Z$ . They are computed from the known values of the fermion masses and of the SM parameters  $G_F, M_Z, \alpha_{\text{em}}, \alpha_s$ .
- The  $\overline{\text{DR}}$ -renormalized parameters of the MSSM at the weak scale are obtained by Renormalization Group (RG) evolution.
- The EWSB conditions are imposed at the weak scale and the masses and VEVs of the Higgs fields are computed (as well as the other MSSM particle masses).

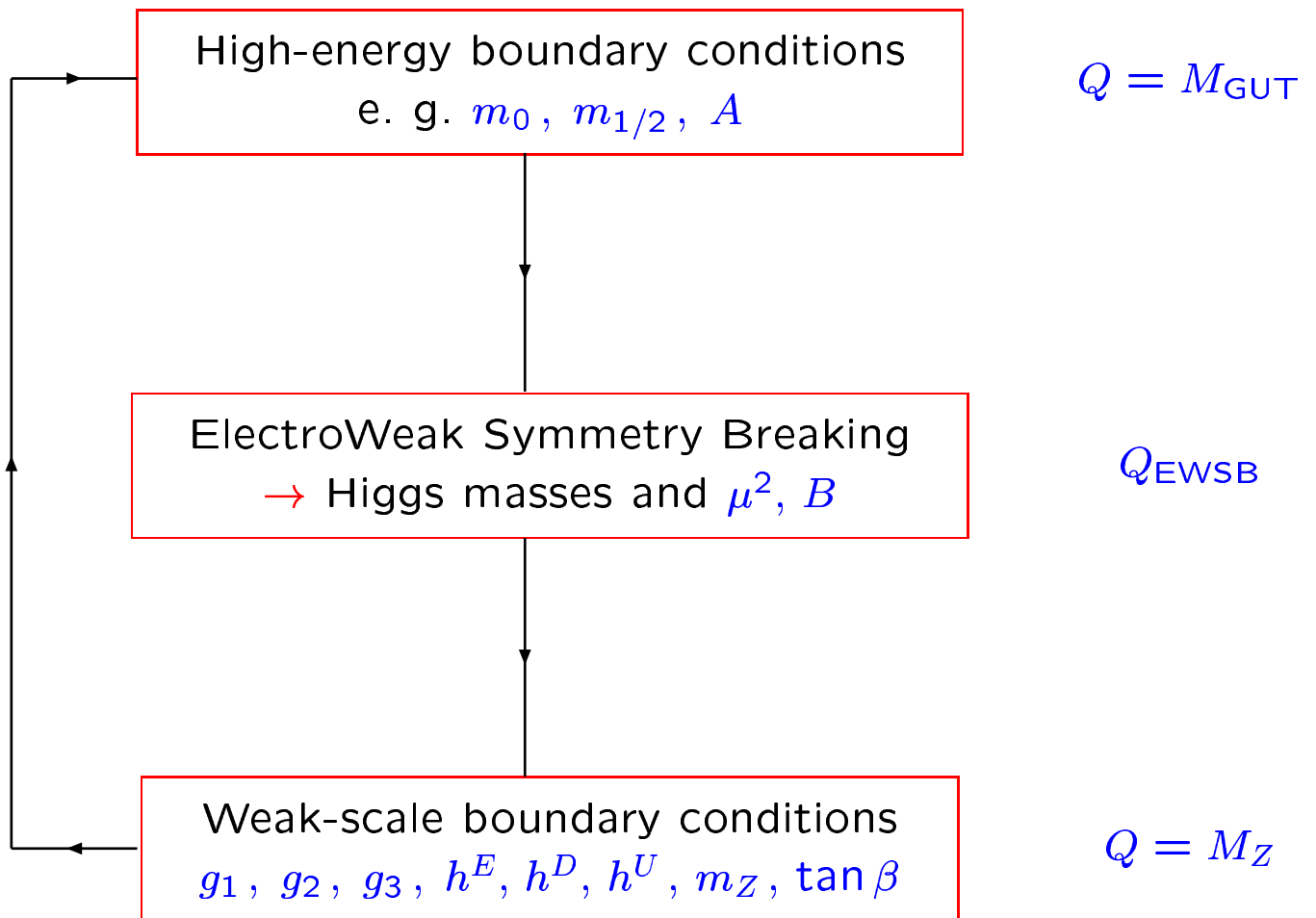
## RG evolution between different energy scales



- The physical Higgs masses should not depend on  $Q_{\text{EWSB}}$ , which can be anywhere between  $M_Z$  and the TeV scale.
- A choice of high-energy boundary conditions is satisfactory if the resulting VEVs  $v_1, v_2$  reproduce the correct value of the running Z-boson mass:

$$m_Z^2 = M_Z^2 + \text{Re} \Pi_{ZZ}^T(M_Z^2) = \frac{1}{4} (g^2 + g'^2) (v_1^2 + v_2^2)$$

## A phenomenological approach



- **Assume** successful EWSB and take  $v_1$  and  $v_2$  (or  $m_Z$  and  $\tan \beta$ ) as input parameters at  $Q = M_Z$ .
- The EWSB conditions now allow to determine  $\mu^2$  and  $B$ .
- $\text{sign}(\mu)$  is an extra (scale-independent) input parameter.

## EWSB conditions and Higgs boson masses

- The EWSB conditions allow to determine  $\mu^2$  and  $B$ :

$$\mu^2 = -\frac{m_Z^2}{2} - \frac{1}{2} \tan 2\beta \left[ \left( m_{H_1}^2 - \frac{t_1}{v_1} \right) \cot \beta - \left( m_{H_2}^2 - \frac{t_2}{v_2} \right) \tan \beta \right]$$

$$B = -\frac{m_Z^2}{2} \sin 2\beta - \frac{1}{2} \tan 2\beta \left( m_{H_1}^2 - \frac{t_1}{v_1} - m_{H_2}^2 + \frac{t_2}{v_2} \right)$$

- The CP-odd and charged Higgs boson masses are:

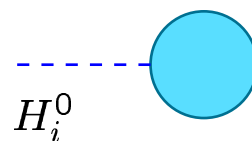
$$M_A^2 = 2B / \sin 2\beta - \text{Re} \Pi_{AA}(M_A^2) + s_\beta^2 \frac{t_1}{v_1} + c_\beta^2 \frac{t_2}{v_2}$$

$$M_{H^\pm}^2 = m_A^2 + M_W^2 + \text{Re} [\Pi_{AA}(M_A^2) - \Pi_{H^+H^-}(M_{H^\pm}^2) + \Pi_{WW}^T(M_W^2)]$$

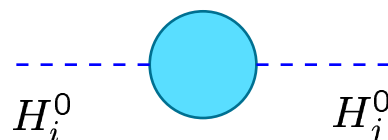
- The CP-even mass matrix is:

$$\mathcal{M}^2 = \begin{pmatrix} m_Z^2 c_\beta^2 + m_A^2 s_\beta^2 - \Pi_{11} + t_1/v_1 & -(m_Z^2 + m_A^2) s_\beta c_\beta - \Pi_{12} \\ -(m_Z^2 + m_A^2) s_\beta c_\beta - \Pi_{12} & m_Z^2 s_\beta^2 + m_A^2 c_\beta^2 - \Pi_{22} + t_2/v_2 \end{pmatrix}$$

$t_i \equiv$  tadpole :

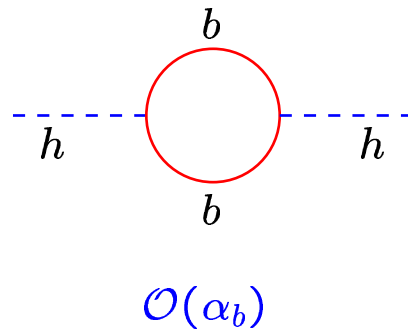
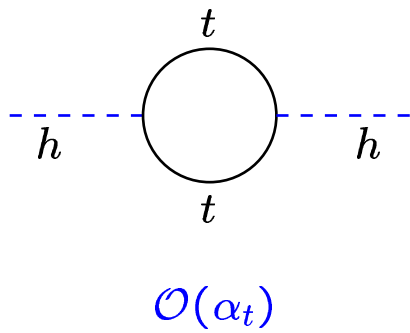


$\Pi_{ij} \equiv$  self-energy :

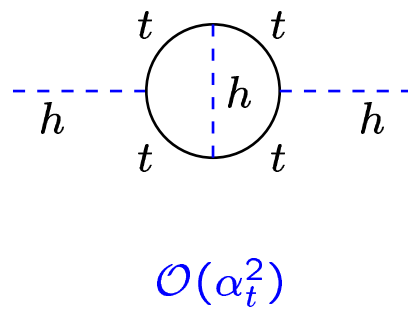
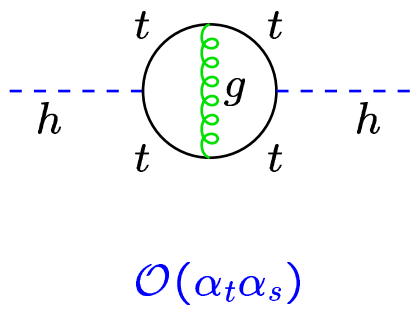


# Summary of the leading Higgs mass corrections

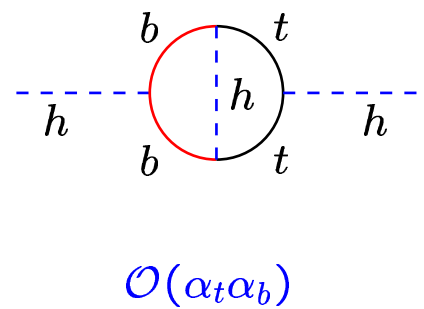
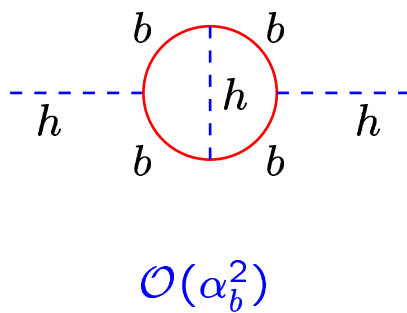
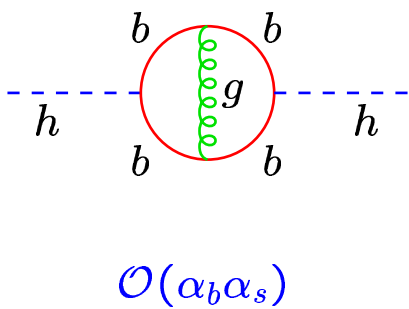
- Leading one-loop:



- Leading two-loop (top):



- Leading two-loop (bottom):





## Programs computing the MSSM mass spectrum

- We present the new versions of three public programs for the computation of the MSSM mass spectrum:
  - [SuSpect 2.3](#) (A.Djouadi, J.L.Kneur and G.Moultaka)
  - [SoftSusy 1.8](#) (B.Allanach)
  - [SPheno 2.2](#) (W.Porod)
- In the latest versions, all the codes include a two-loop computation of the Higgs masses and EWSB conditions performed in the  $\overline{\text{DR}}$  renormalization scheme.
- The full one-loop corrections are taken from [Pierce-Bagger-Matchev-Zhang \(PBMZ\) 1996](#).
- The leading two-loop corrections in the limit of zero external momentum in the self-energies are taken from [Brignole-Dedes-Degrassi-Slavich-Zwirner \(BDDSZ\) 2001-2003](#).

## Benchmark scenarios

- *Snowmass* points: six (out of ten) representative choices for the input parameters (see hep-ph/0202233)

mSUGRA:	$m_0$ (GeV)	$m_{1/2}$ (GeV)	$A$ (GeV)	$\tan \beta$	$\text{sign}(\mu)$
SPS1a	100	250	-100	10	+
SPS2	1450	300	0	10	+
SPS4	400	300	0	50	+
SPS5	150	300	-1000	5	+

GMSB:	$\Lambda$ (TeV)	$M_{\text{mess}}$ (TeV)	$N_{\text{mess}}$	$\tan \beta$	$\text{sign}(\mu)$
SPS8	100	200	1	15	+

AMSB:	$m_{3/2}$ (TeV)	$m_0$ (GeV)	$\tan \beta$	$\text{sign}(\mu)$
SPS9	60	450	10	+

## Results for the Higgs masses

- Light CP-even Higgs boson mass  $m_h$ :

	SPS1a	SPS2	SPS4	SPS5	SPS8	SPS9
<i>SoftSusy</i>	111.0	115.3	112.9	114.2	113.9	116.2
<i>SPheno</i>	111.1	115.6	113.1	114.7	114.3	116.5
<i>SuSpect</i>	111.0	115.4	112.9	114.1	113.9	116.2

- Heavy CP-even Higgs boson mass  $m_H$ :

	SPS1a	SPS2	SPS4	SPS5	SPS8	SPS9
<i>SoftSusy</i>	401.7	1523.1	335.5	692.4	542.8	1064.7
<i>SPheno</i>	401.2	1524.6	340.3	691.3	541.1	1059.4
<i>SuSpect</i>	401.3	1521.4	334.4	692.1	539.1	1064.1

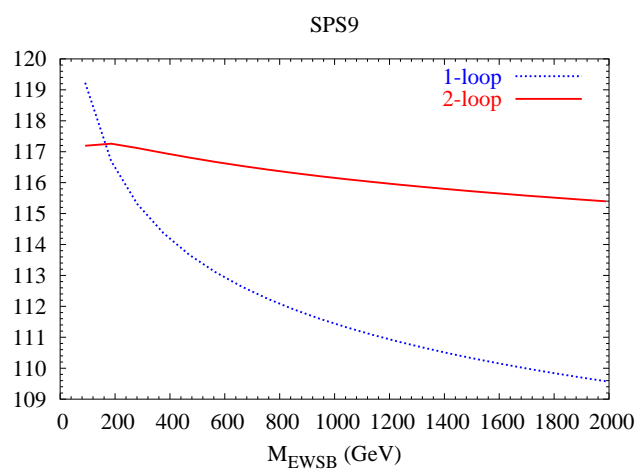
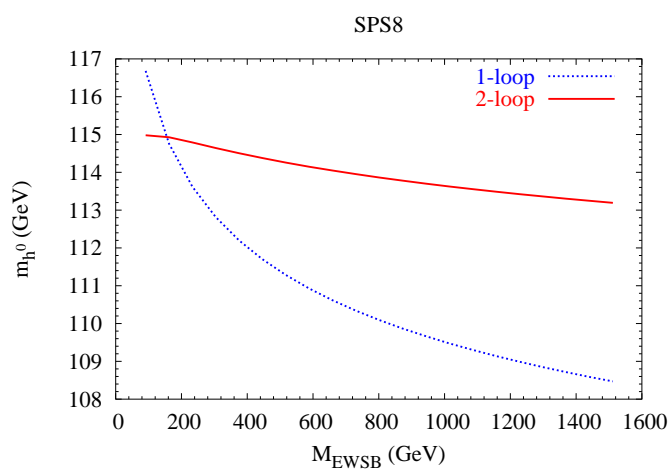
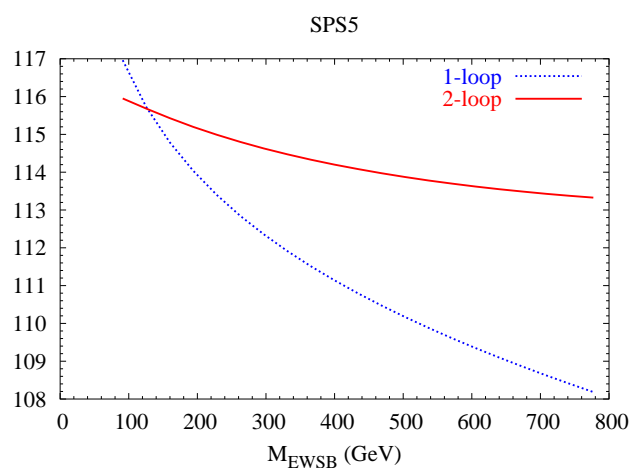
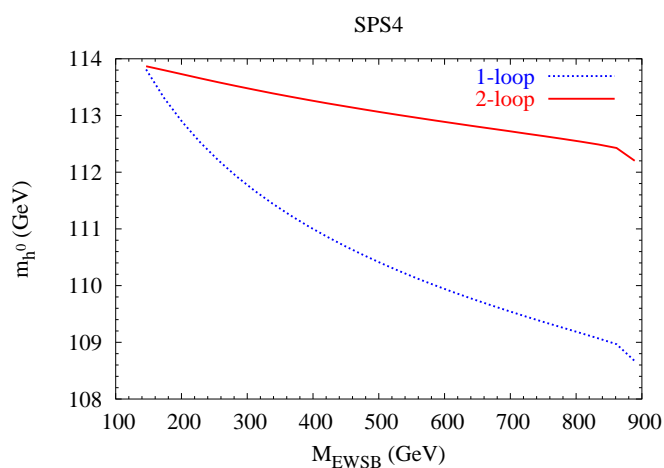
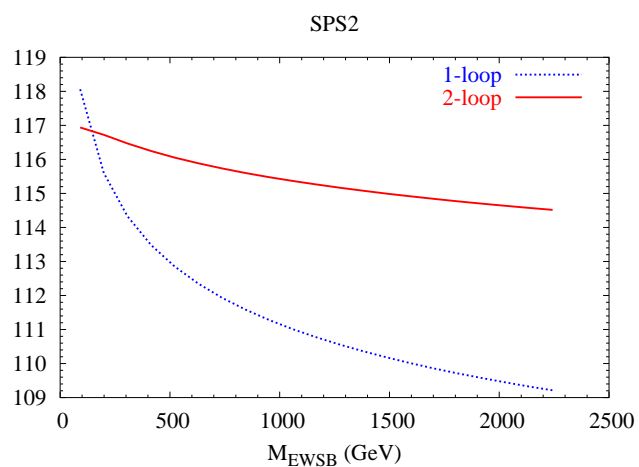
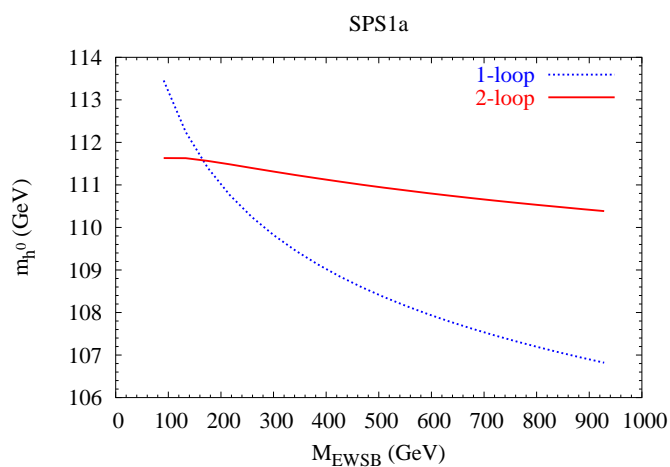
- CP-odd Higgs boson mass  $m_A$ :

	SPS1a	SPS2	SPS4	SPS5	SPS8	SPS9
<i>SoftSusy</i>	401.4	1523.0	335.5	692.3	542.5	1064.5
<i>SPheno</i>	400.8	1524.5	340.3	691.5	540.8	1059.2
<i>SuSpect</i>	401.0	1521.3	334.4	692.1	538.8	1063.9

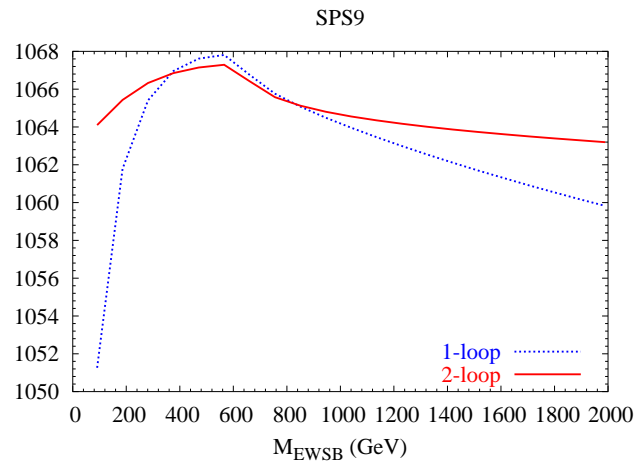
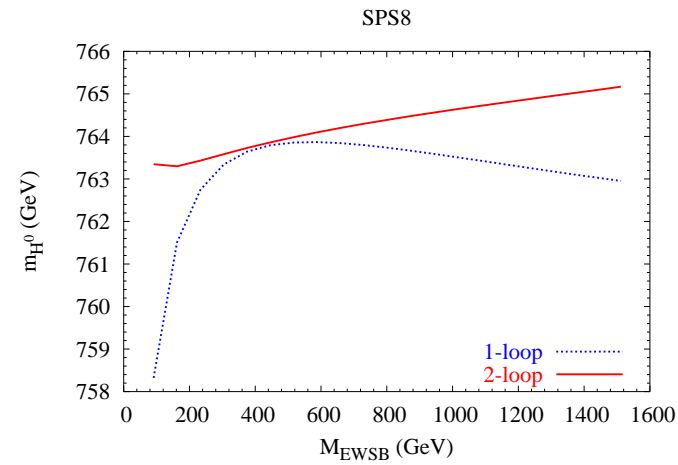
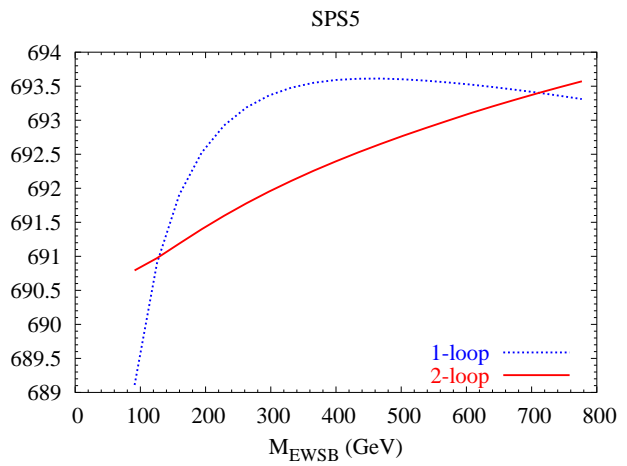
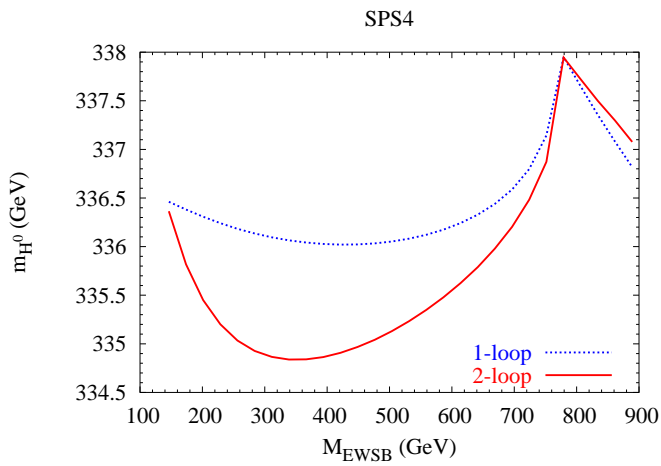
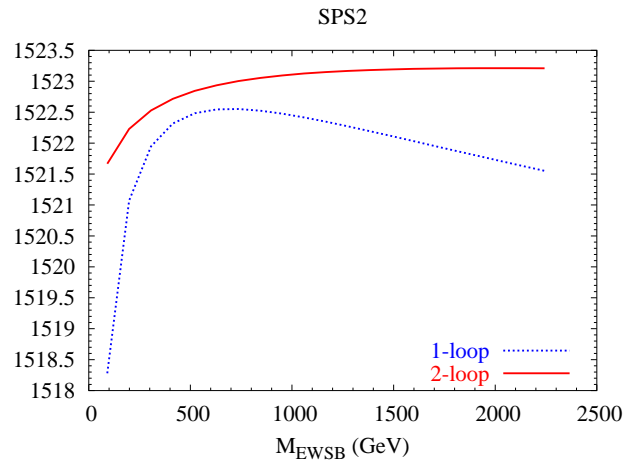
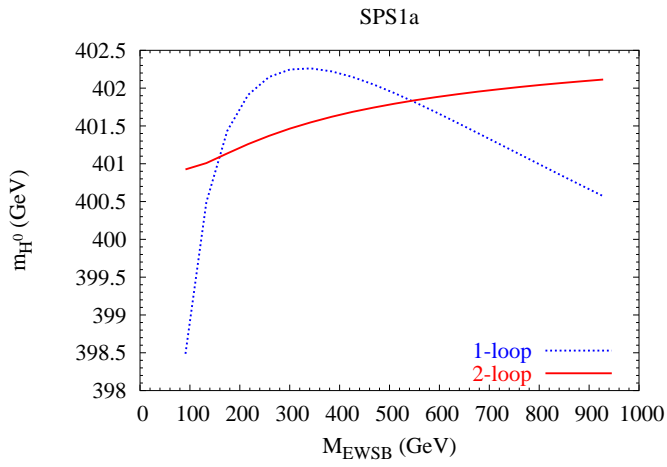
- Superpotential Higgs mass parameter  $\mu$ :

	SPS1a	SPS2	SPS4	SPS5	SPS8	SPS9
<i>SoftSusy</i>	359.6	503.9	399.5	637.0	430.6	1020.0
<i>SPheno</i>	359.0	505.3	400.2	636.1	428.5	1014.6
<i>SuSpect</i>	359.7	500.2	399.1	636.7	428.0	1019.8

# Renormalization scale dependence of $m_h$



# Renormalization scale dependence of $m_H$



## Comparing the $\overline{\text{DR}}$ and OS calculations

- In the two-loop results implemented in *SoftSusy*, *SPheno* and *SuSpect* the MSSM parameters are expressed in the  $\overline{\text{DR}}$  scheme (as they come naturally from the RG evolution).
- In alternative, we might express the MSSM input parameters in terms of physical (On-Shell) masses and mixing angles.
- The code *FeynHiggs* (S.Heinemeyer *et al.*) includes all the leading two-loop corrections in the OS renormalization scheme.
- The differences between the  $\overline{\text{DR}}$  and OS calculations measure the uncertainty coming from higher-order corrections.
- Comparing the light CP-even Higgs boson mass  $m_h$ :

	SPS1a	SPS2	SPS4	SPS5	SPS8	SPS9
<i>SuSpect</i>	111.0	115.4	112.9	114.1	113.9	116.2
<i>FeynHiggs</i> *	112.6	116.7	114.7	116.4	115.6	116.8

- Comparing the heavy CP-even Higgs boson mass  $m_H$ :

	SPS1a	SPS2	SPS4	SPS5	SPS8	SPS9
<i>SuSpect</i>	401.3	1521.4	334.4	692.1	539.1	1064.1
<i>FeynHiggs</i> *	401.4	1521.4	333.9	691.9	539.1	1064.1

- \* The MSSM input parameters for *FeynHiggs*, including  $m_A$ , are taken from the output of *SuSpect*.

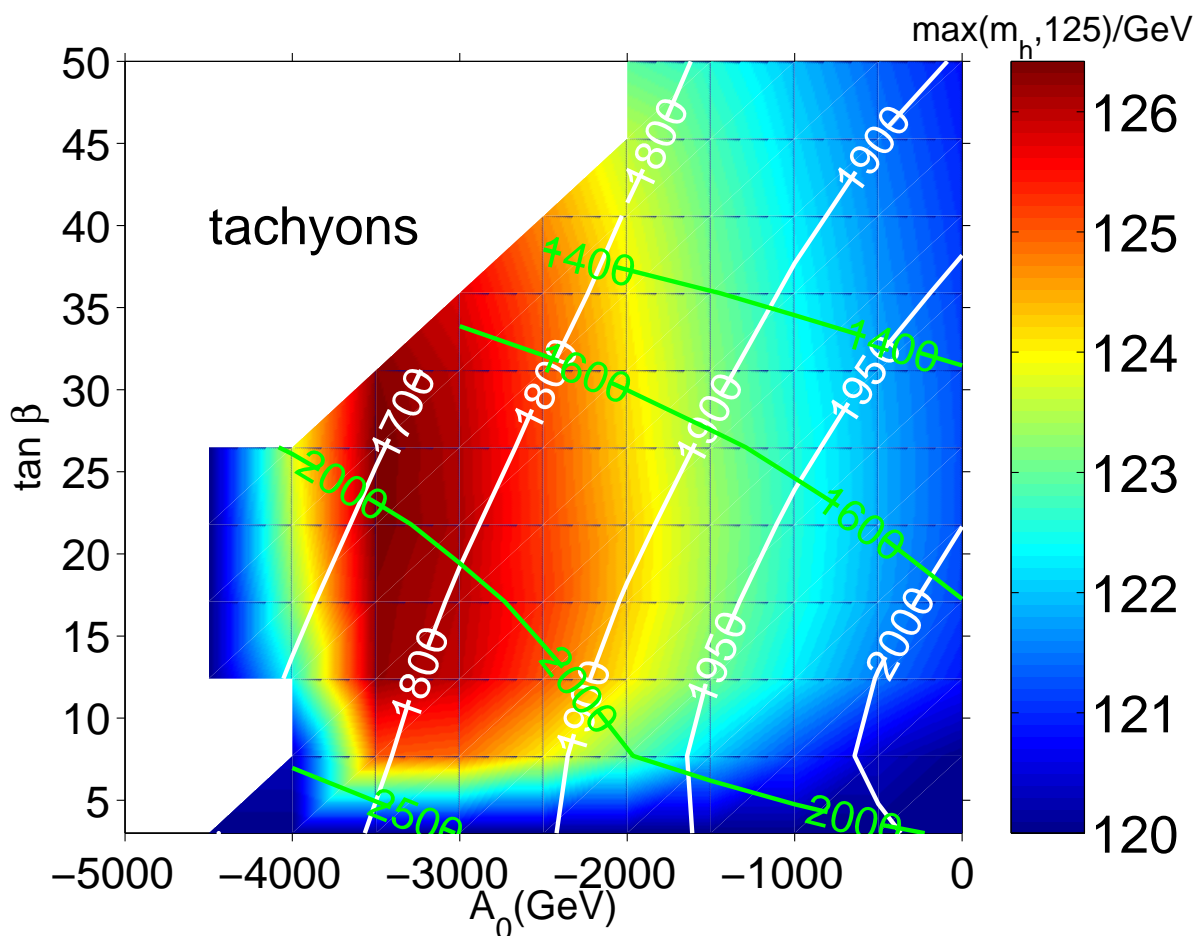
## Summary

- *SuSpect 2.3*, *SoftSusy 1.8* and *SPheno 2.2* now include a fully consistent two-loop  $\overline{\text{DR}}$  computation of the Higgs tadpoles and masses, and agree well for several choices of the MSSM boundary conditions at the GUT scale. The small residual differences are due to higher-order effects and they are understood.
- The inclusion of the two-loop corrections clearly improves the renormalization scale dependence of the Higgs masses. The residual  $\sim 2\text{--}3$  GeV variation in  $m_h$  is a measure of the unknown higher-order effects.
- The  $\sim 2$  GeV difference in  $m_h$  w.r.t. the two-loop On-Shell computation of *FeynHiggs 1.5.1* is another measure of the higher-order effects (compare with  $\Delta m_h^{\text{theory}} \simeq 3$  GeV).
- Still in progress:
  - Bounds on  $m_h$ ,  $\tan\beta$  etc. in the general MSSM;
  - implications for various SUSY-breaking mechanisms (mSUGRA, GMSB, AMSB);
  - Estimate of the remaining uncertainties (both theoretical and parametric).
- Stay tuned...

## Maximal value of $m_h$

- Look for the mSUGRA parameter choice that maximizes  $m_h$ :

$$m_0 = m_{1/2} = 1 \text{ TeV}, \quad \mu > 0, \quad M_t = 175 \text{ GeV}$$



- The maximal  $m_h$  depends on the chosen range for the squark masses (*is 3 TeV less natural than 2 TeV?*)
- The maximal  $m_h$  depends critically on the measured  $M_t$ .