IFAE, Torino, 14 aprile 2004

Probing oscillations into sterile neutrinos with astrophysics, cosmology and experiments...

"Sterile Neutrinos in all sauces"

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Introduction and Purpose

We want to study Sterile Neutrinos

- i.e. (light) spin 1/2 fermions,
 - neutral under all SM forces,
 - have a mixing with active v.

Oscillations into v_s are now excluded as the dominant solution in solar and atmospheric neutrinos:

solar:
$$v_{\mu} \rightarrow v_{s}$$
? no, $v_{e} \rightarrow v_{\mu,\tau}$ (SNO) (details...)
atmo: $v_{\mu} \rightarrow v_{s}$? no, $v_{\mu} \rightarrow v_{\tau}$ (SK, Macro) (details...)

Now the **relevant issues** become:

- which **subdominant** role is still possible for v_s ?
- where can we **detect** the v_s ?
- how can we detect the v_s ?

Perform a complete analysis:

for any possible v_{e,μ,τ} - v_s mixing pattern
 including the established v_e-v_{μ,τ} and v_μ-v_τ mixing (= in a full 4v mixing formalism)
 study *all* neutrino sources (experiments, astrophysics, cosmology)

- look for sterile evidence in present data. None.
- set present **bounds**
- identify future signals



Are sterile neutrinos still interesting at all?

• Yes, "light neutral fermions" in so many Beyond the SM constructions...

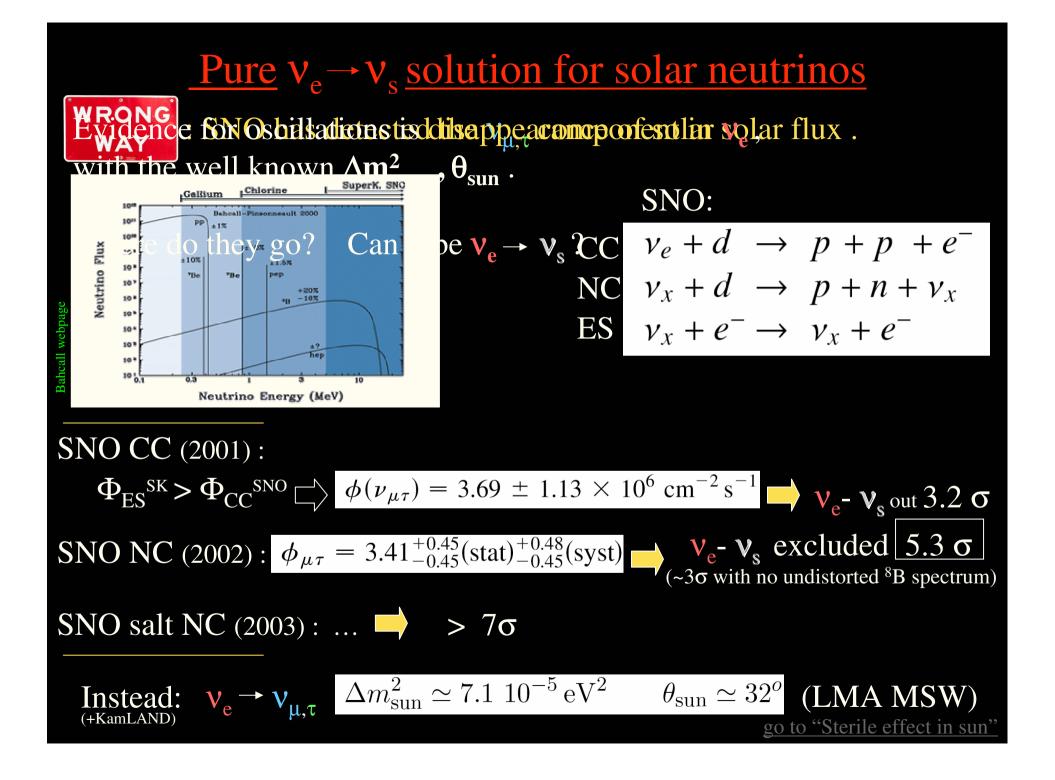
-behave effectively as v_s -parameterize with θ_s , Δm_s^2 right-handed neutrino axino goldstino majorino branino dilatino radino familino modulino mirror fermions

. . .

• Yes, sterile neutrinos invoked for so many "puzzles" ... (EMERGENCY ?)

pulsar kicks r-process nucleosynthesis Dark Matter galactic ionization

• ...LSND

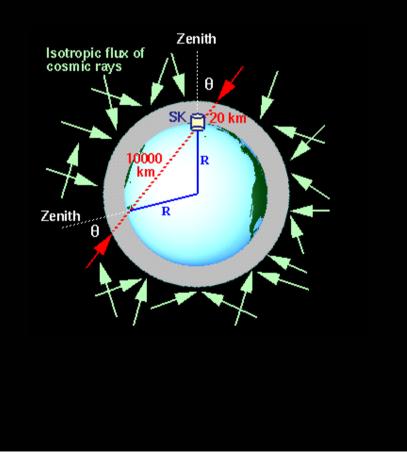


<u>Pure</u> $v_{\mu} \rightarrow v_{s}$ <u>solution for atmospheric neutrinos</u>

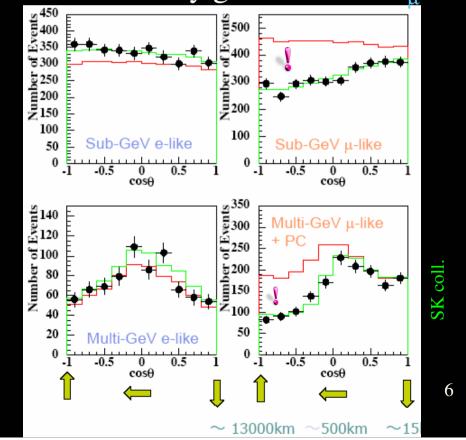


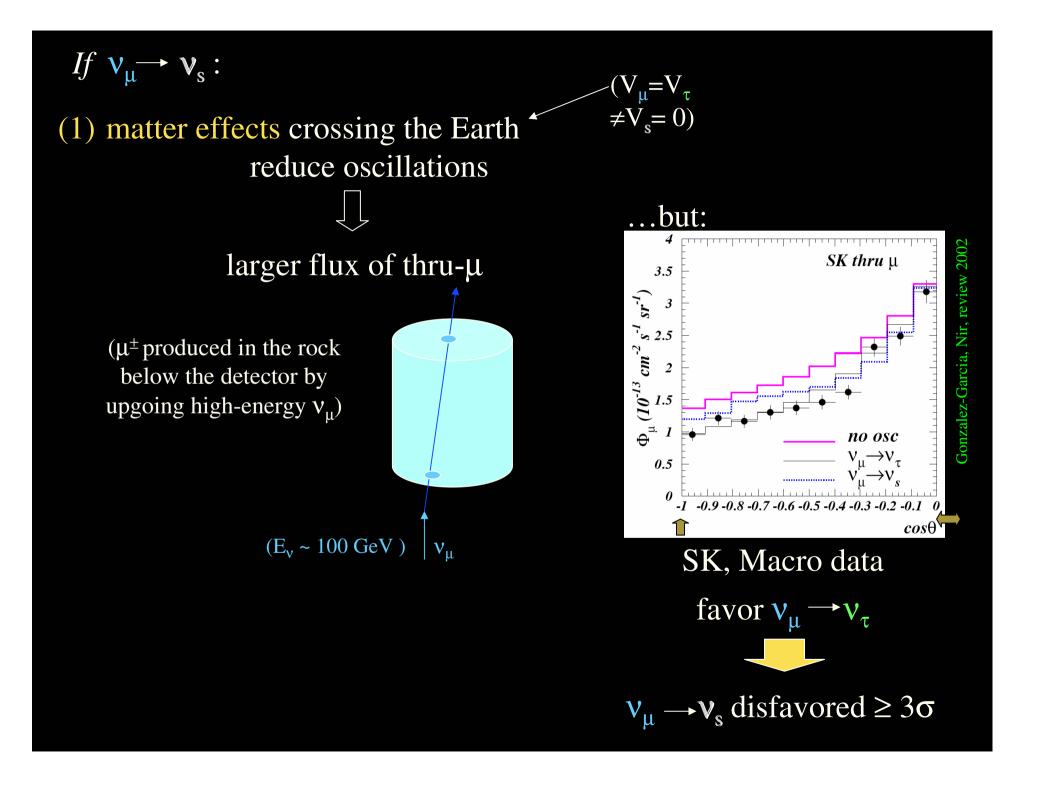
: matter effects and NC favor v_{τ} vs to v_{s} .

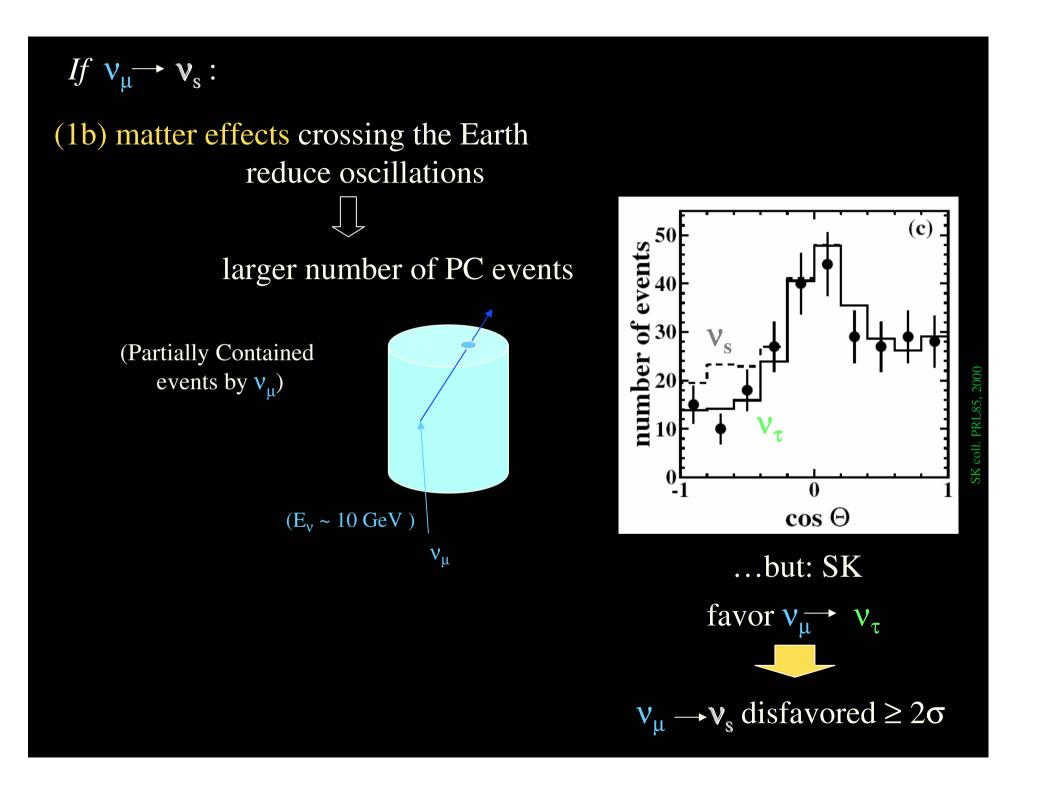
Basics:



Evidence for oscillations is disappearance of v_{μ} "from below", with the well known $\Delta m_{atm}^2, \theta_{atm}$. Where do they go? Can it be $v_{\mu} \rightarrow v_s$?

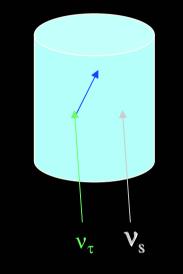




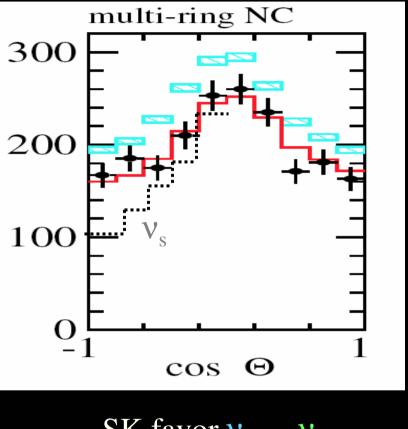


If
$$v_{\mu} \rightarrow v_{s}$$
:

(2) less NC events upward



...but:



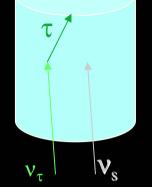
Kearns, 2002 (adapted)

SK favor
$$v_{\mu} \rightarrow v_{\tau}$$

 $v_{\mu} \rightarrow v_{s}$ disfavored ~ 2σ

If
$$\mathbf{v}_{\mu} \rightarrow \mathbf{v}_{s}$$
:

(3) τ appearance from below



but: small statistics...



not used

Global Analysis excludes
$$v_{\mu} \rightarrow v_{s}$$
 at $\sim 7 \sigma$

Instead:
$$v_{\mu} \rightarrow v_{\tau}$$
 $\Delta m_{\rm atm}^2 \simeq 2.6 \ 10^{-3} \, {\rm eV}^2$ $\theta_{\rm atm} \simeq 45^o$

(+Macro +Soudan2 +K2K)

10 go to "Sterile effects in atmo neutrinos"

<u>4v mixing formalism</u>

Present bounds are computed in a limited 2v formalism: $v_l \rightarrow cos \theta_s v_l' + sin \theta_s v_s$. We want instead a full 4v formalism.



more details

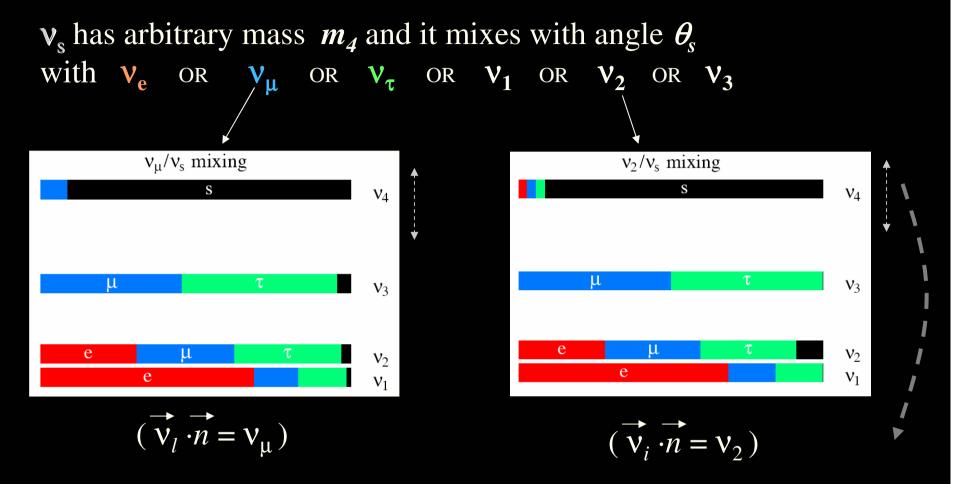
define a complex unit 3-versor \vec{n}

 \overline{n} identifies an arbitrary combination of active v :

 $\vec{n} \cdot \vec{\nu} = n_e \nu_e + n_\mu \nu_\mu + n_\tau \nu_\tau = n_1 \nu_1 + n_2 \nu_2 + n_3 \nu_3$

which mixes with $\mathbf{v}_{\mathbf{s}}$ with a single angle $\theta_{\mathbf{s}}$

In the following:



Also: take best-fit values for θ_{sun} and θ_{atm} , choose $\theta_{13} = 0$, Normal Hierarchy.

Full 4v mixing formalism

Present bounds are computed in a limited 2v formalism: $v_l \rightarrow \cos\theta_s v_l' + \sin\theta_s v_s$. We want a full 4v formalism.

$$\begin{array}{l} \textbf{3 neutrinos:} \quad \nu_{e} \, \nu_{\mu} \, \nu_{\tau} \leftrightarrow \nu_{1} \, \nu_{2} \, \nu_{3} \\ \textbf{3 angles } \theta_{12} \, \theta_{23} \, \theta_{13} \\ (and 1 \, phase \, \delta) \end{array} \qquad \begin{array}{l} \nu_{\ell} = U_{\ell i} \, \nu_{i} \\ U_{li} = U_{23} \, U_{13} \, U_{12} \\ \uparrow / / \\ \textbf{3 arotations in } ij) \end{array}$$

$$\begin{array}{l} U_{li} = U_{23} \, U_{13} \, U_{12} \\ \uparrow / / \\ \textbf{3 arotations in } ij) \end{array}$$

4 neutrinos:
$$v_e v_\mu v_\tau v_s \leftrightarrow v_1 v_2 v_3 v_4$$
 $v_{e,\mu,\tau,s} = V \cdot v_{1,2,3,4}$
add 3 angles $\theta_{14} \theta_{24} \theta_{34}$ R_{14}, R_{24}, R_{34}
(and add 2 phases) $\theta_{14} \theta_{24} \theta_{34}$ N_{14}, R_{24}, R_{34}
(4x4 rotations in ij)
• v_s mixes with the flavor eigenstates $V = R_{34}R_{24}R_{14} U_{\ell i}$
(e.g. θ_{14} mixes $v_e v_s, \theta_{24}$ mixes $v_\mu v_s...$)
 $v_\ell = U_{\ell i}v_i$
• v_s mixes with the matter eigenstates $V = U_{\ell i}R_{34}R_{24}R_{14}$
(e.g. θ_{14} mixes $v_1 v_s, \theta_{24}$ mixes $v_2 v_s...$)

A simple parametrization:

define a complex unit 3-versor \vec{n} (\checkmark 3 angles + 2 phases)

 \vec{n} identifies an arbitrary combination of active v :

 $\vec{n} \cdot \vec{\nu} = n_e \nu_e + n_\mu \nu_\mu + n_\tau \nu_\tau = n_1 \nu_1 + n_2 \nu_2 + n_3 \nu_3$

which mixes with $\mathbf{v}_{\mathbf{s}}$ with a single angle $\theta_{\mathbf{s}}$

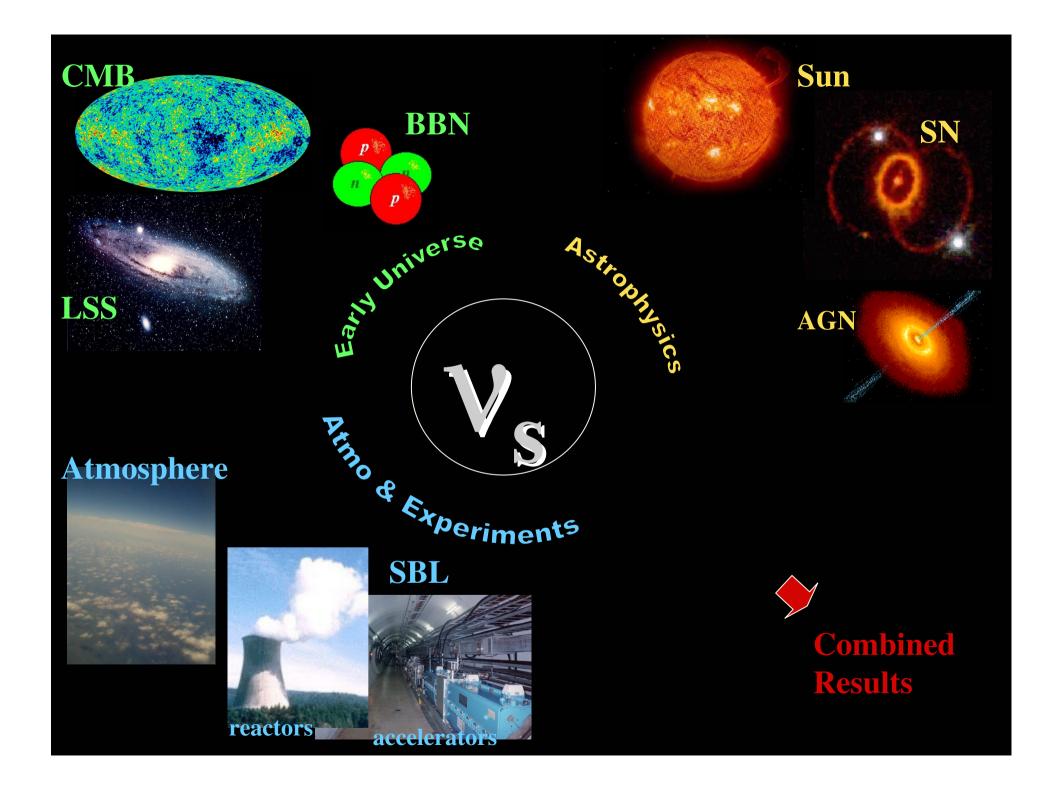
Explicitly:

$$V = \frac{\nu_{\ell}}{\nu_{\rm s}} \begin{pmatrix} U_{\ell i} - n_i n_{\ell}^* (1 - \cos \theta_{\rm s}) & n_{\ell}^* \sin \theta_{\rm s} \\ -n_i \sin \theta_{\rm s} & \cos \theta_{\rm s} \end{pmatrix}$$

In the following:

 v_s has arbitrary mass m_4 and it mixes with angle θ_s with v_e or v_μ or v_τ or v_1 or v_2 or v_3 $v_{\rm u}/v_{\rm s}$ mixing v_2/v_s mixing S S v_4 v_4 u μ v_3 v_3 u v_2 ν_2 e ν_1 e v_1 $(\overrightarrow{\mathbf{v}_l}, \overrightarrow{\mathbf{n}} = \mathbf{v}_u)$ $(\overrightarrow{\mathbf{v}}_i \cdot \overrightarrow{n} = \mathbf{v}_2)$

Also: take best-fit values for θ_{sun} and θ_{atm} , choose $\theta_{13} = 0$, Normal Hierarchy.



<u>Sterile effects</u> <u>in the Early Universe</u>

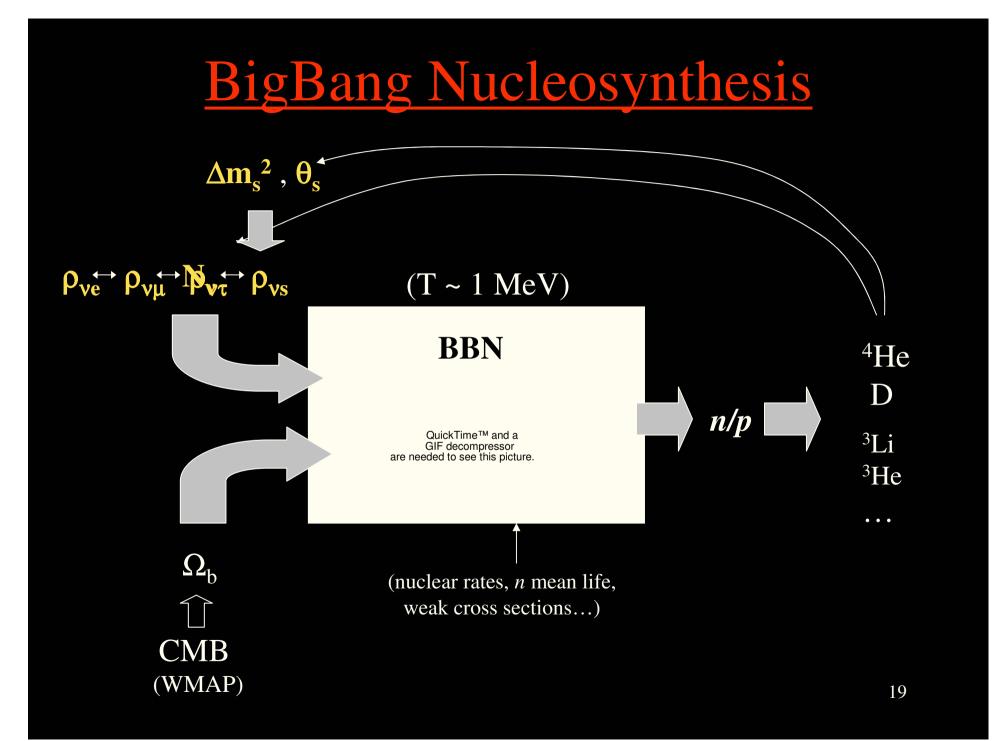
Neutrinos in the Early Universe are:

(1) a lot (as abundant as photons)

(2) the main component of the (relativistic) energy density that sets the expansion rate

(3) trapped in the dense early plasma \Box non trivial matter effects (4) important for the outcoming chemical composition

An extra v_s can make a big difference.



Roadmap (= What we do)

```
For every choice of \Delta m_s^2, \theta_s,
for T >> MeV \longrightarrow 0.07 MeV follow:
```

(BBN ends, les jeux sont fait) iii kinetic equ.s for neutrino densities $\rho_{ve}(T)$, $\rho_{vu}(T)$, $\rho_{v\tau}(T)$, $\rho_{vs}(T)$

- equation for *n/p*
- 3
- equations of light nuclei (4He, D) production

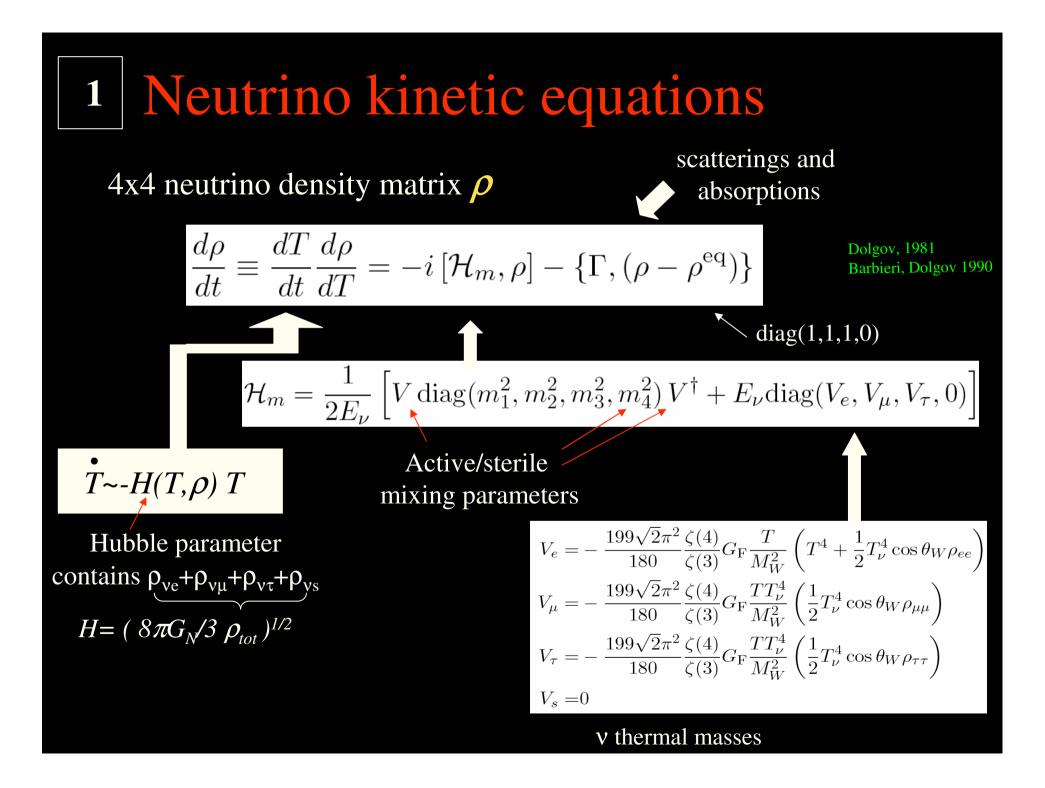


(⁴He, D) observations

Assumptions:

- no large lepton asymmetries
- neglect spectral distortions

Where does a v_s enter the BBN game? (A) v_s production \Rightarrow larger total energy density \Rightarrow faster expansion (B) mixing $v_e - v_s \Rightarrow$ depletion of $v_e \Rightarrow$ effect on $n \leftrightarrow p$ reactions



What happens:

- for T >> MeV, matter effects suppress mixing $\rho_{vs} = 0$
- as $T \rightarrow$, at a certain point oscillations $v_{active} \leftrightarrow v_s$ can begin $\rho_{vs} > 0$ when & how depend on $\Delta m_s^2, \theta_s$
- + redistribution $v_{active} \rightarrow v_{active}$
- meanwhile: v decouple at $T \sim \text{few MeV}$, e^+e^- annihilate
- Output: $\rho_{ve}(T)$, $\rho_{v\mu}(T)$, $\rho_{v\tau}(T)$, $\rho_{vs}(T)$

2 **n/p ratio**

$$\dot{r} \equiv \frac{dT}{dt} \frac{dr}{dT} = \Gamma_{p \to r}(1 - r) - \Gamma_{n \to p} \qquad r = \frac{n_n}{n_n + n_p}$$

$$\vec{r} = \frac{dT}{dt} \frac{dr}{dT} = \Gamma_{p \to r}(1 - r) - \Gamma_{n \to p} \qquad r = \frac{n_n}{n_n + n_p}$$
rates of weak interactions:

$$n \longleftrightarrow p + e^- + \bar{\nu}_e$$

$$n + \nu_e \longleftrightarrow p + e^-$$

$$n + e^+ \longleftrightarrow p + \bar{\nu}_e.$$
depend on ρ_{ve}, ρ_{ve}

Bottom line: where does a v_s enter the game? (A) total energy density \Rightarrow expansion parameter (B) depletion of v_e density \Rightarrow weak rates

3 Light elements production

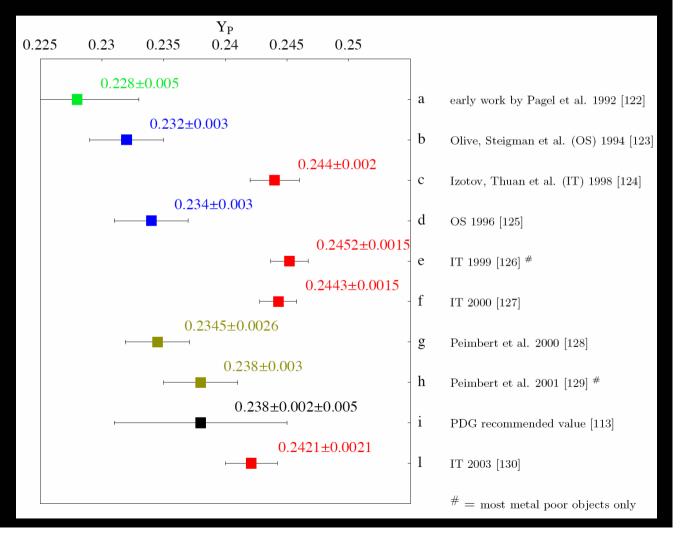
A network of Boltzman equations with up-to-date nuclear rates...

4 **Observations**

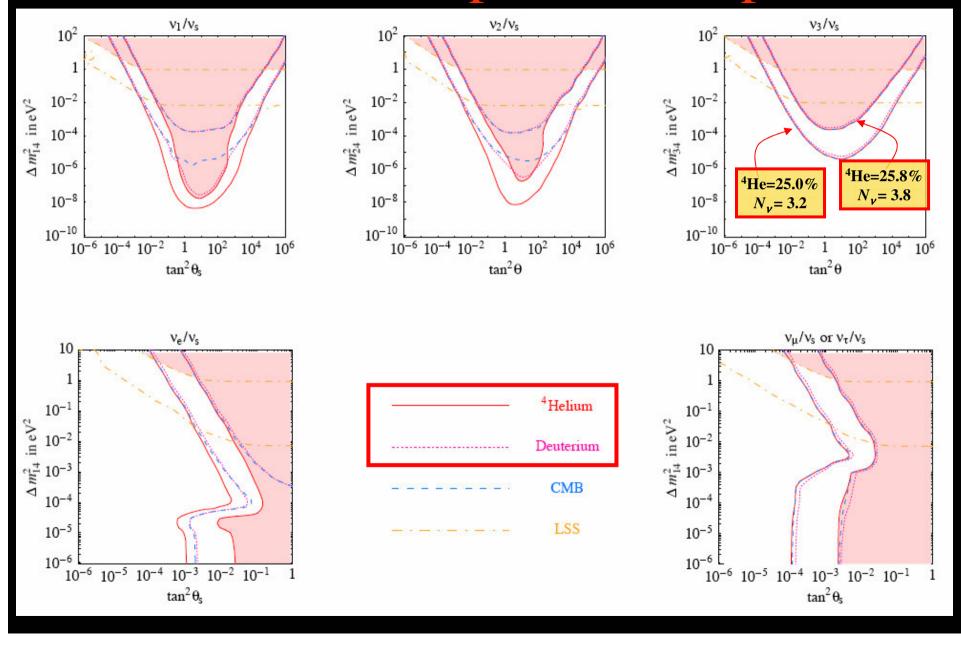
Determinations of primordial ⁴He are controversial. Very conservatively: $Y_{4He} = (24 \pm 1)\%$

Determinations of primordial D are still imprecise.

Conservatively: $Y_D = (2.8 \pm 0.5) \ 10^{-5}$



Bounds in the parameter space



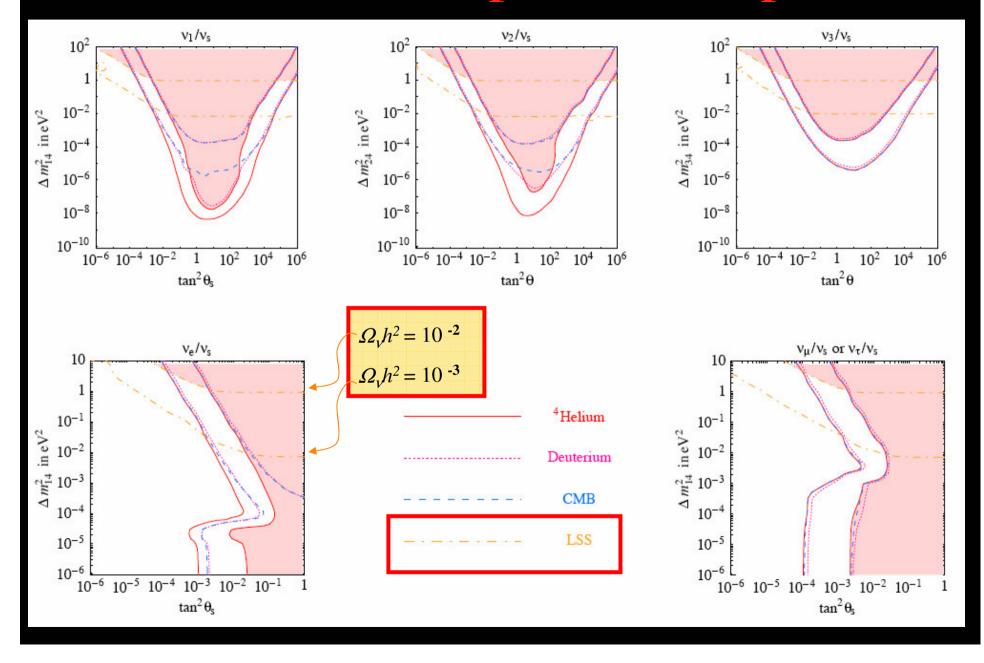
Large Scale Structure

The primordial free streaming of massive neutrinos *affects* the LSS power spectrum observed today.

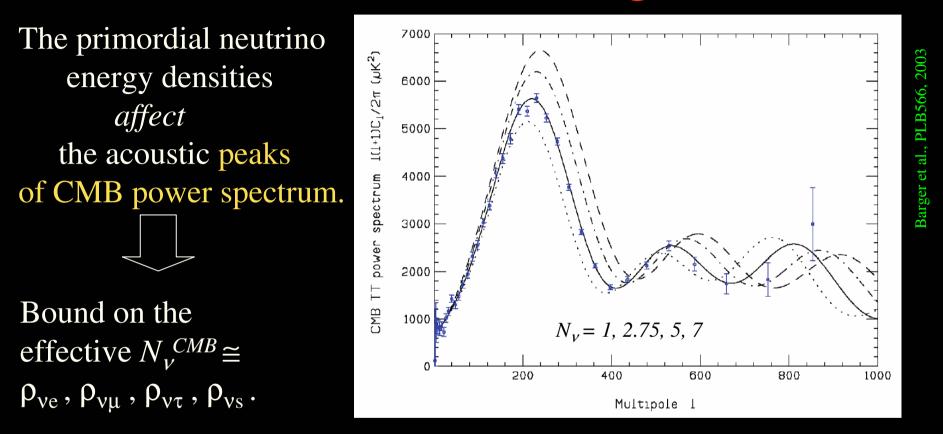
Upper bound on: $\Omega_{\nu}h^{2} = \frac{\operatorname{Tr}[m \cdot \rho]}{93.5 \,\mathrm{eV}} \quad v_{1,2,3} \,\mathrm{and} \, v_{s}$ $2dF + WMAP : \Omega_{\nu}h^{2} < 0.76 \,10^{-2}$

 \mathbf{v}_{s} contribute to $\Omega_{v} \Rightarrow$ **bound on m**_s i.e. Δm_{s}^{2} . *but*: if \mathbf{v}_{s} do not fully thermalize $\Rightarrow \rho_{vs} \ll 1 \Rightarrow$ weaker bound

Bounds in the parameter space



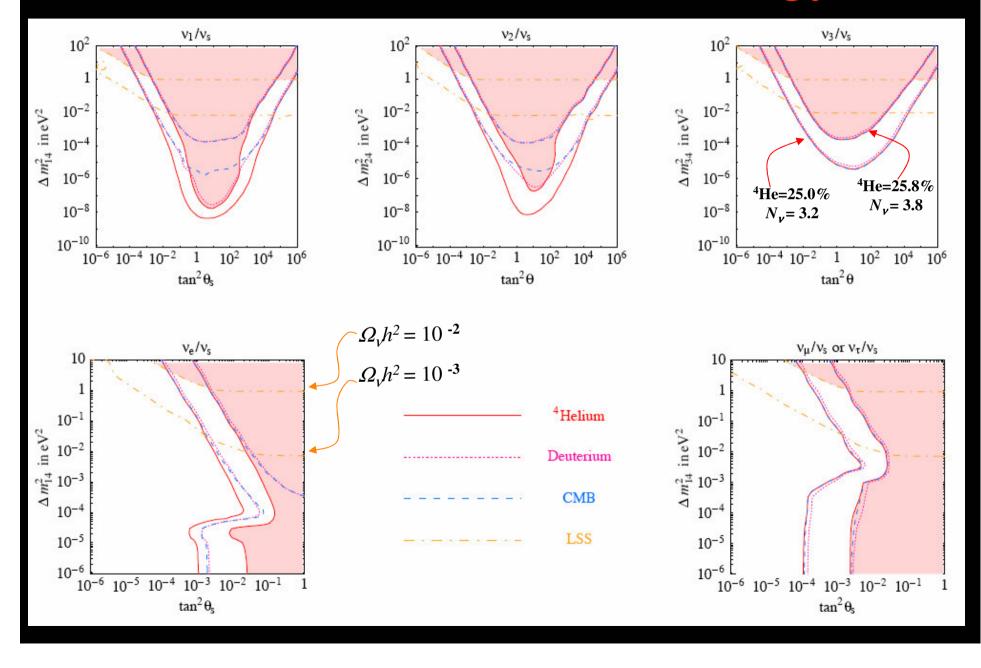
Cosmic Microwave Background



At present:
$$N_v^{CMB} = 3\pm 2$$

Bound on the Δm_s^2 , θ_s (that determine the ρ_{vs}).

All bounds from cosmology



LSND: in or out?

LSND claims evidence for $\overline{v_{\mu}} \rightarrow \overline{v_{e}}$ with Requires a new (= sterile) neutrino:

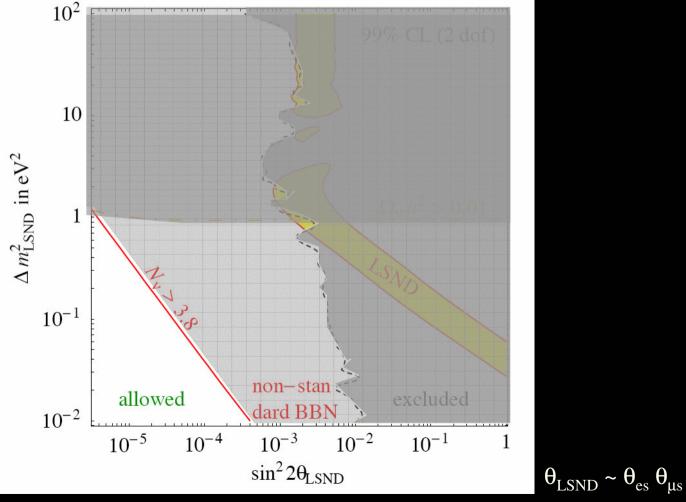
$$\Delta m^2 \neq \Delta m^2_{sun, atm}$$

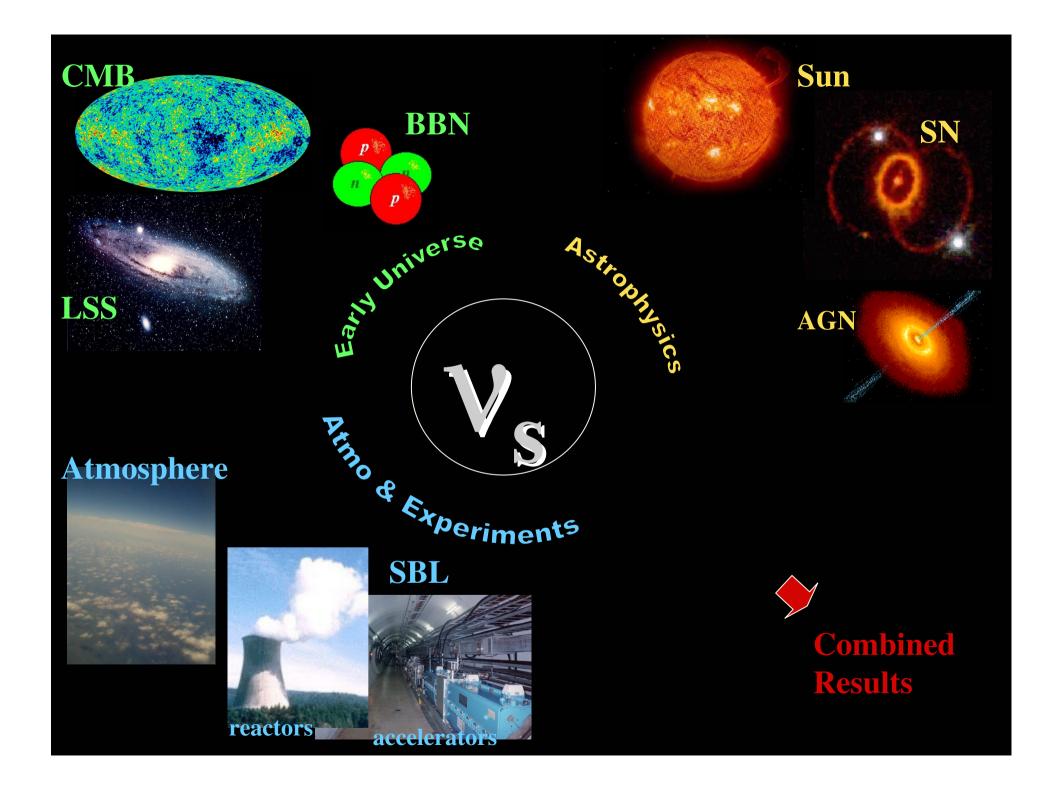
$$\overline{\mathbf{v}}_{\mu} \longrightarrow \overline{\mathbf{v}}_{s} \longrightarrow \overline{\mathbf{v}}_{e}$$

(if oscillations)

30

How does the LSND v_s fit in cosmology?



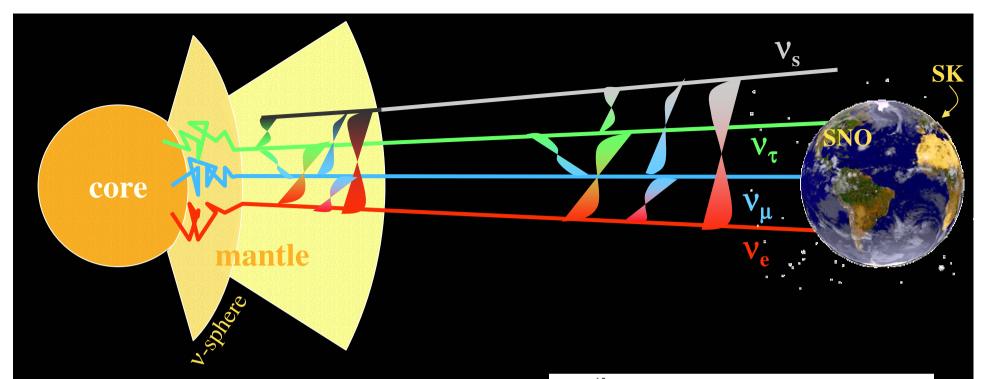


Sterile effects in SN

Neutrinos from SN:
(1) are a lot (99% of emitted energy)
(2) undergo "extreme" matter effects
(3) come from very far away (~10 kpc)
(4) have the right energy (~10 MeV) for present detectors

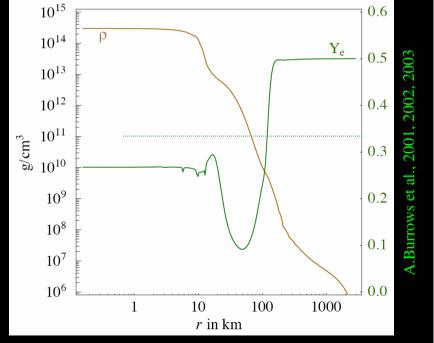
An extra v_s can make a big difference.

Overall picture confirmed by SN1987a \square Set present bounds Thousands of events from future SN \square Propose future probes



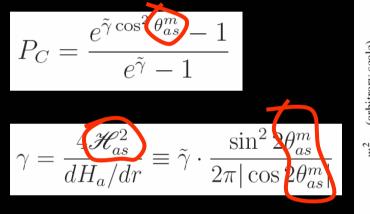
Matter oscillations in the star mantle:

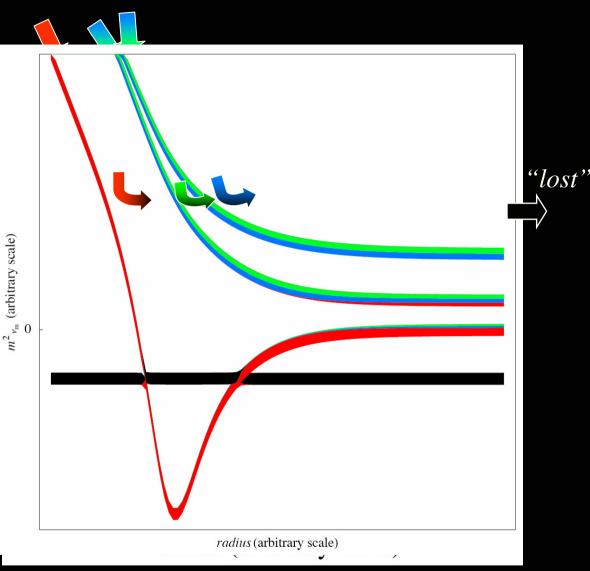
$$V_{e} = \sqrt{2}G_{F}n_{B}(3Y_{e}-1)/2, \qquad V_{\tau} = V_{\mu} + V_{\mu\tau}, V_{\mu} = \sqrt{2}G_{F}n_{B}(Y_{e}-1)/2, \qquad V_{s} = 0,$$



Matter eigenstates in the mantle:

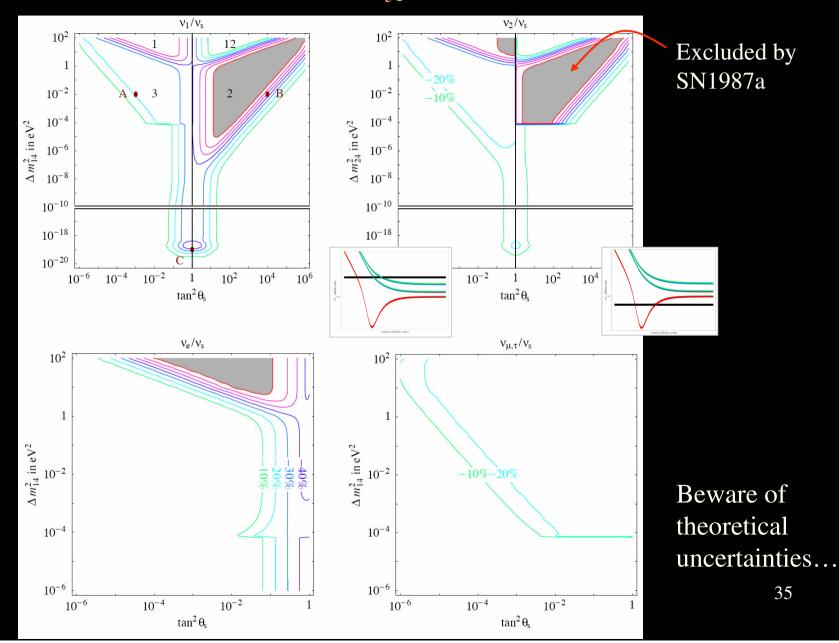
At each crossing there is a crossing probability



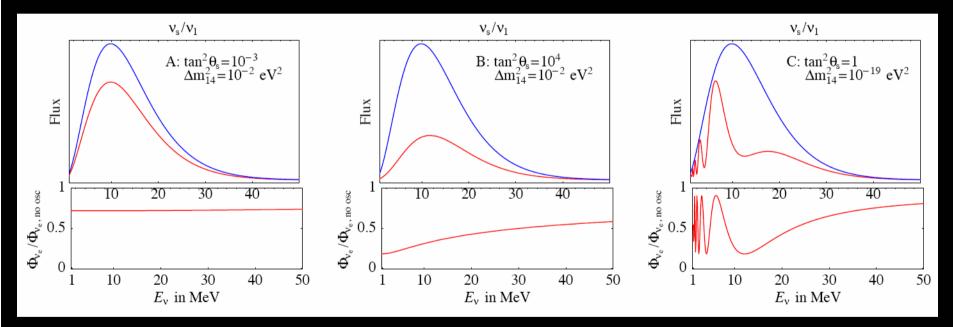


Output: final fluxes of v_e , v_μ and v_τ on Earth .

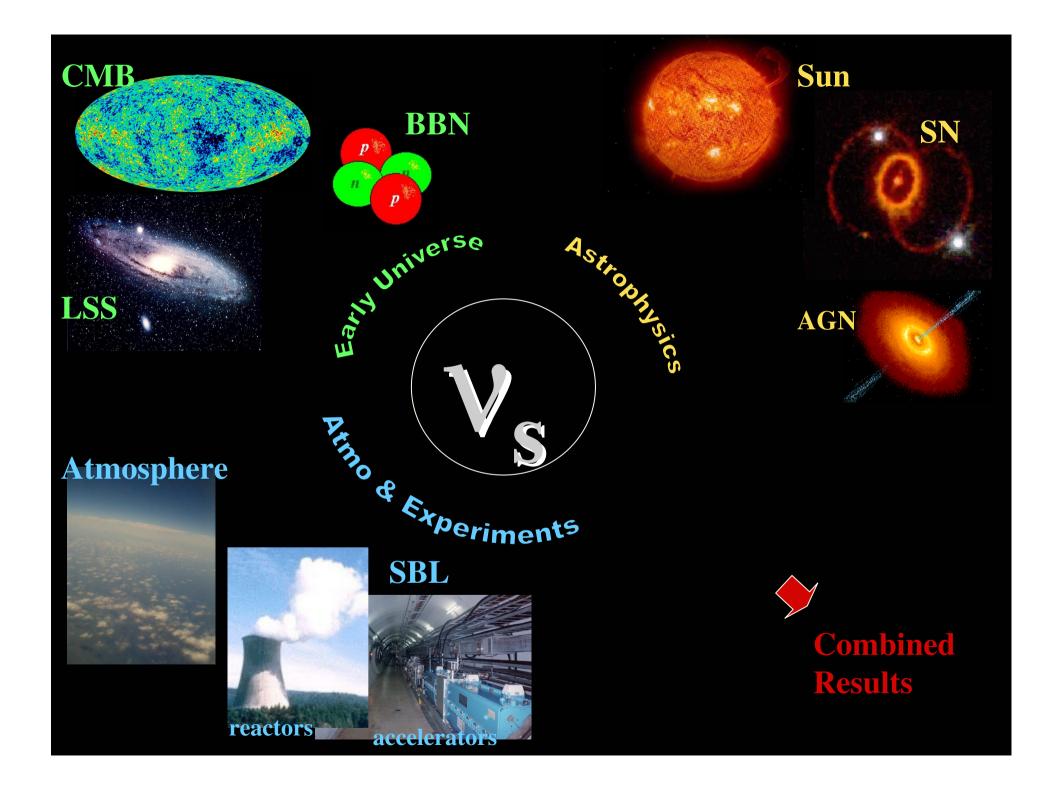
Results: percentual reduction of $\overline{\mathbf{v}_e}$ events (in a large Cerenkov detector) $(\overline{\mathbf{v}_e} p \rightarrow ne^+)$



The energy dependance of matter/vacuum conversions causes **spectral distortions**:



Possible very clear feature!



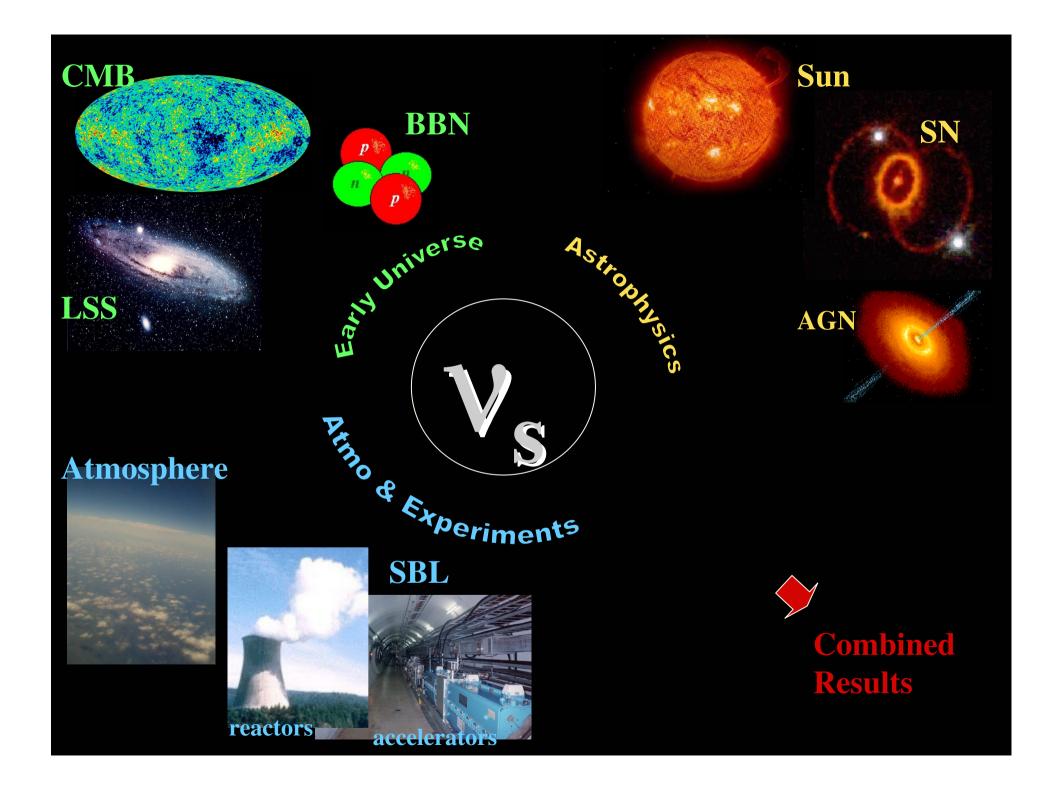
<u>Neutrinos from</u> 'extragalactic' sources

- produced in high-energy astrophysical processes
- expected flavor ratios $e: \mu: \tau = 1:2:0$ at production 1:1:1 after (active) oscillations
- if a v_s is introduced, a selective depletion can occur .

But:

- initial fluxes totally unknown
- we tag v_{μ} and v_{τ} which nevertheless equiparate (atmo oscillations)...

Not a very interesting probe.



Sterile effects in solar neutrinos

Neutrinos from the sun: (1) are a lot, and very well studied (2) undergo matter effects in the sun and in the Earth (3) come from far away (~150 Mkm)

An extra v_s can make a difference.

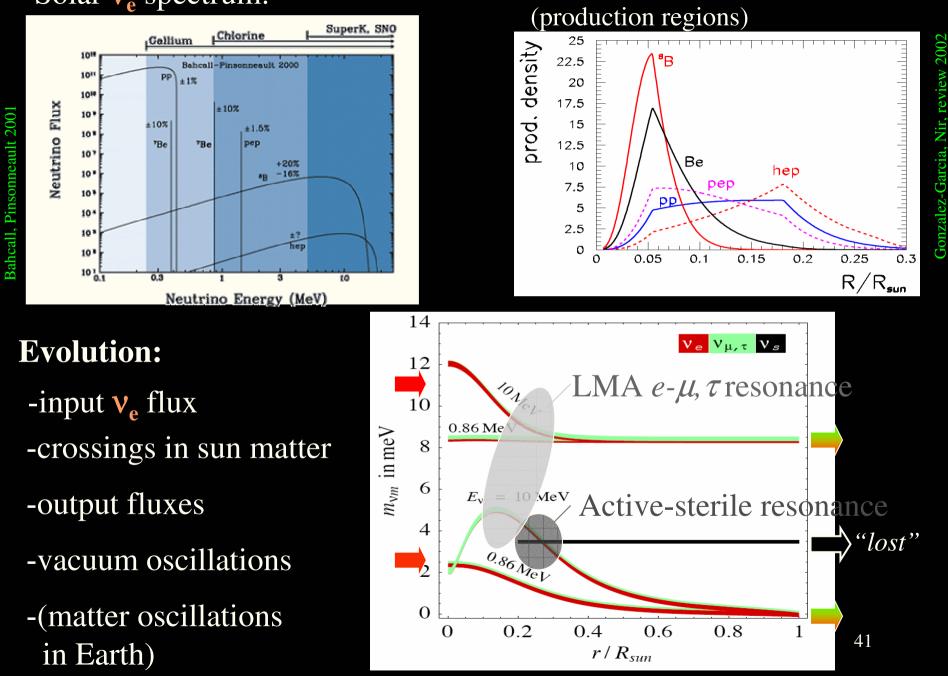


Look for evidence of v_s effects around the LMA solution. None <u>more details</u>

Set present bounds

Identify future probes

Solar v_e spectrum:



Neutrino density matrix formalism:

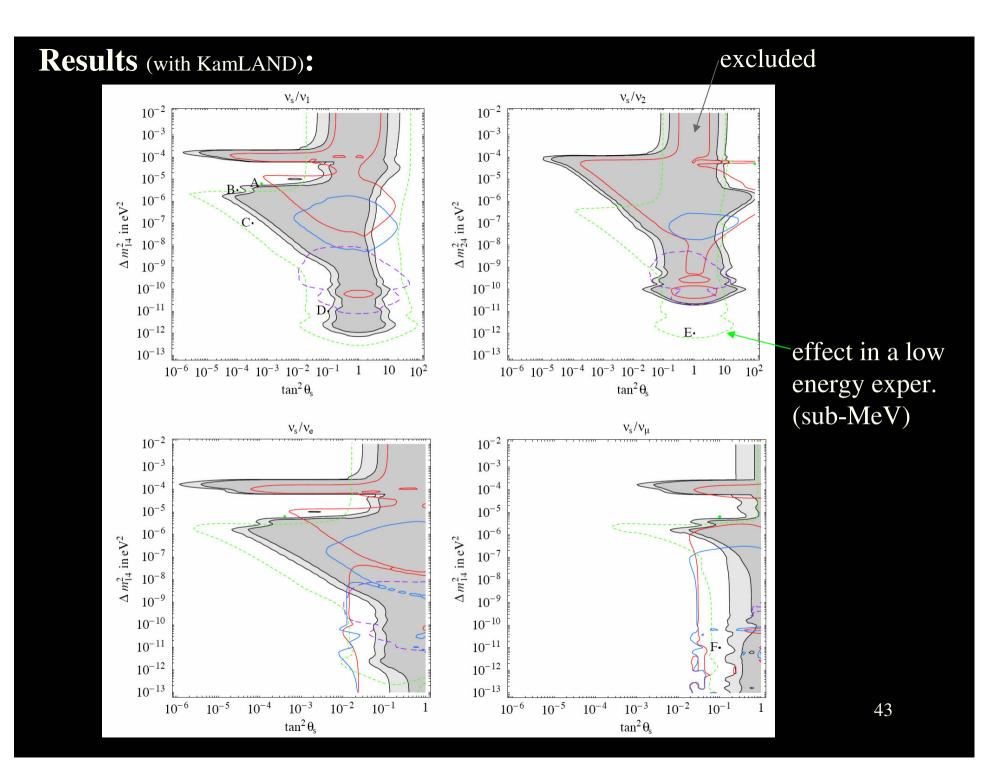
4x4 density matrix ρ

at production ($\mathbf{v}_{\mathbf{e}}$ in the sun) is $\rho_m = V_m^{\dagger} \cdot \operatorname{diag}(1, 0, 0, 0) \cdot V_m$ mixing matrices in matter (V_m) are computed diagonalizing the matter Hamiltonian

$$\mathscr{H} = \frac{mm^{\dagger}}{2E_{\nu}} + \sqrt{2}G_{\rm F} {\rm diag}\left(N_e - \frac{N_n}{2}, -\frac{N_n}{2}, -\frac{N_n}{2}, 0\right)$$

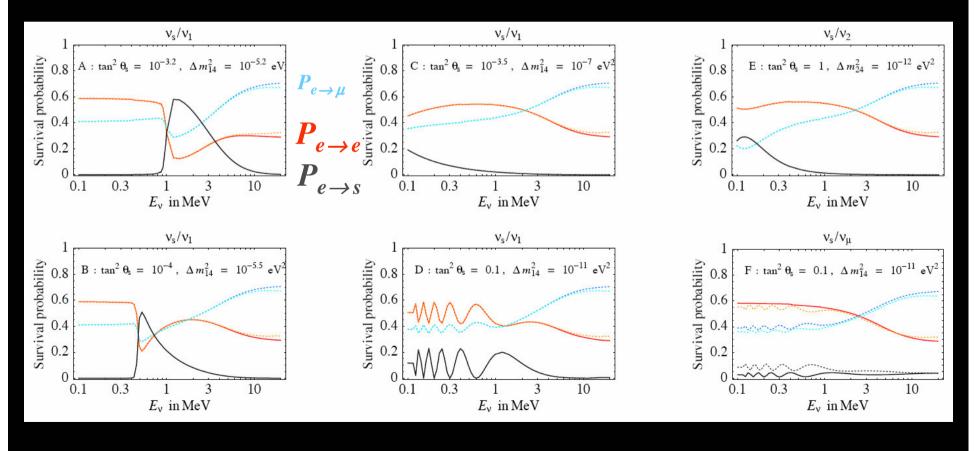
evolve ρ with evolution matrix $\mathscr{U} = \mathscr{U}_{earth} \cdot \mathscr{U}_{vacuum} \cdot \mathscr{U}_{sun}$ at each *ij* matter level crossing \mathscr{U}_{sun} rotates of $\tan^2 \alpha = P_C/(1 - P_C)$ with $P_C = \frac{e^{\tilde{\gamma} \cos^2 \theta_{as}^m} - 1}{e^{\tilde{\gamma}} - 1}$ $\gamma = \frac{4\mathscr{H}_{as}^2}{dH_a/dr} \equiv \tilde{\gamma} \cdot \frac{\sin^2 2\theta_{as}^m}{2\pi |\cos 2\theta_{as}^m|}$ $(\theta^m$ effective mixing angle in matter) at detection (back to flavor basis) $\rho = \langle V \cdot \mathscr{U} \cdot \rho_m(r, E_\nu) \cdot \mathscr{U}^{\dagger} \cdot V^{\dagger} \rangle$

E.g.
$$P(v_e \rightarrow v_e)$$
 corresponds to ρ_{ee} ...

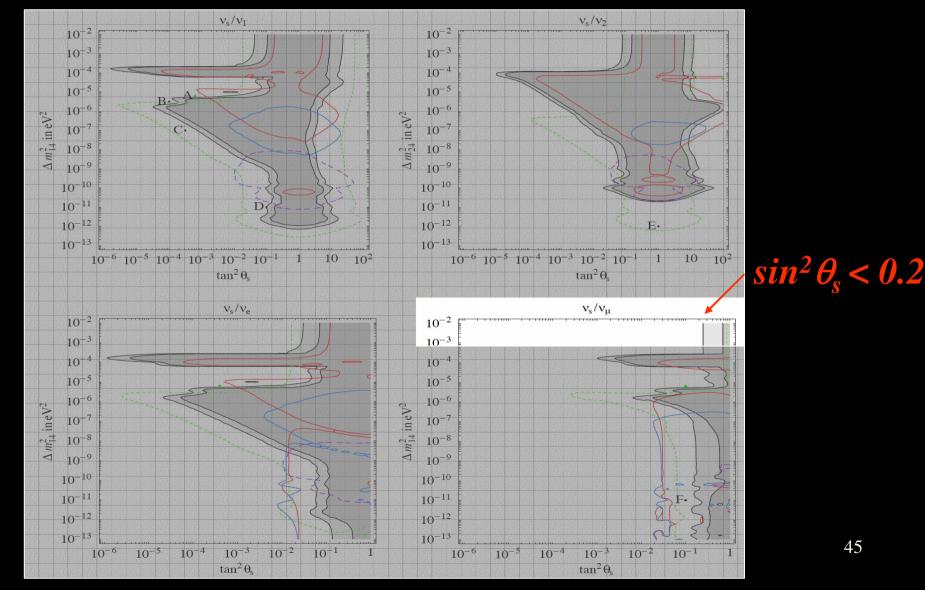


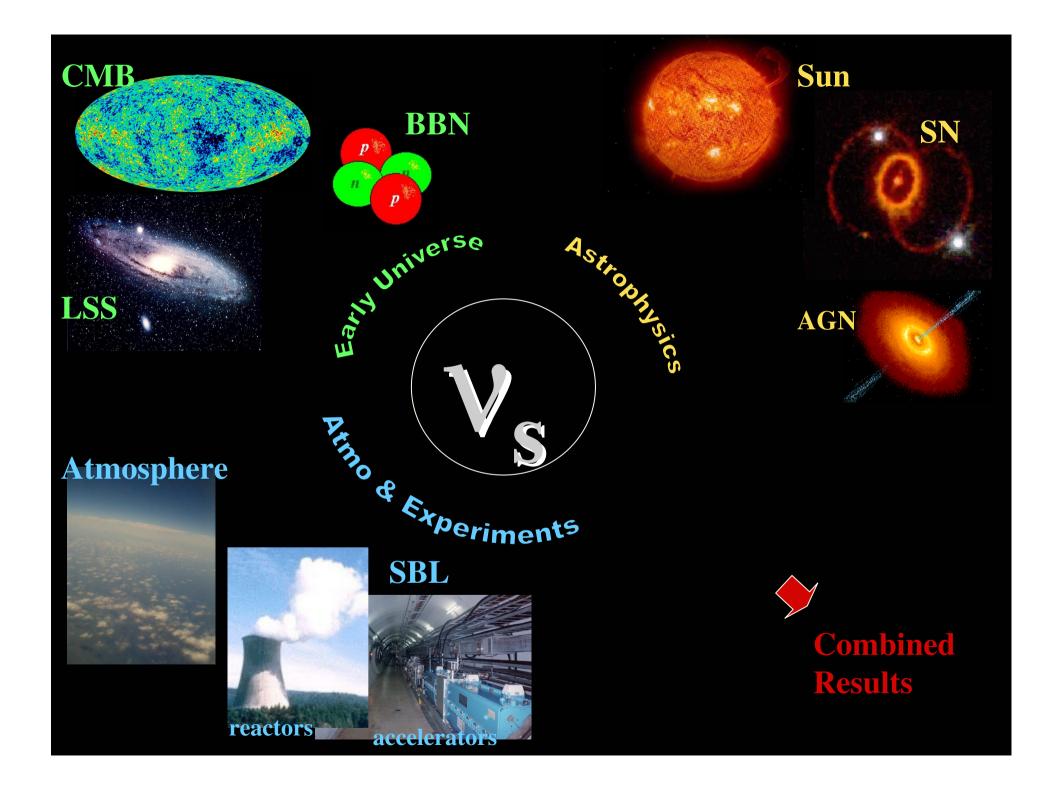
Spectral distortions:

- the energy dependance in the (matter and vacuum) oscillations distorts the original (well known) solar v_e spectrum
- a very distinctive feature!
- mainly at low energies

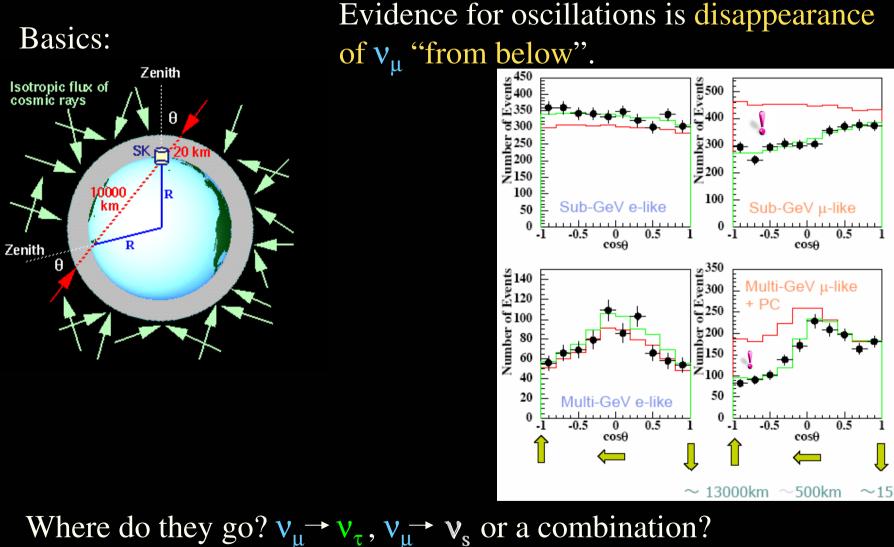


The "still allowed component" of v_s in solar neutrinos: means the naïve limit $v_e \rightarrow cos \theta_s v_{\mu,\tau} + sin \theta_s v_s$. In our framework:





Sterile effects in atmospheric neutrinos



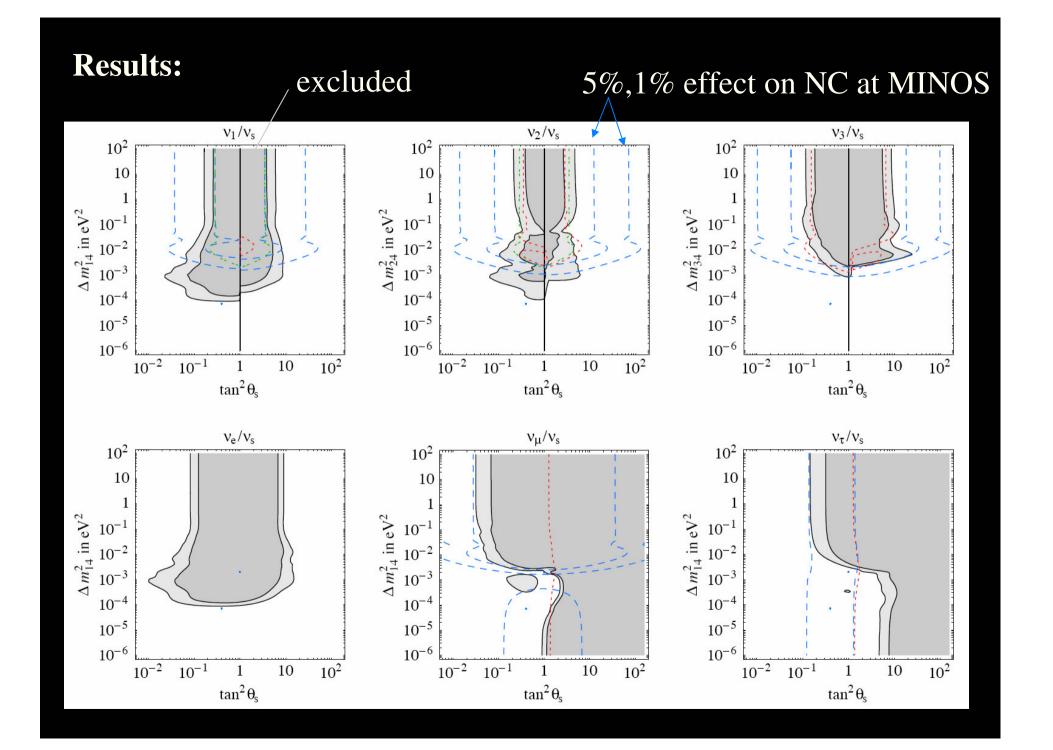
3 sensitive probes to discriminate and put bounds:

If
$$v_{\mu} \rightarrow v_{s}$$
:

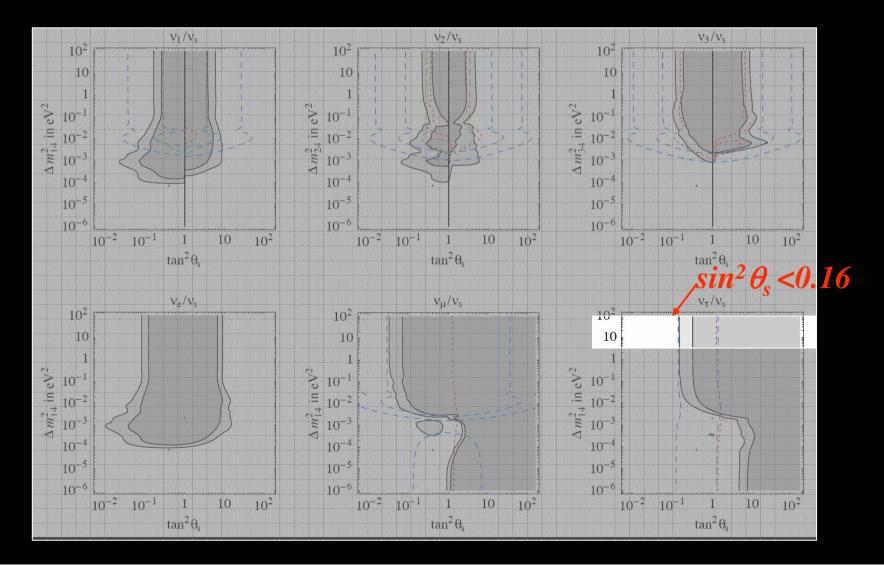
- (1) larger flux of thru-muons
- (1b) larger number of PC events
- (2) fewer NC-enriched events
- (3) tau appearance...

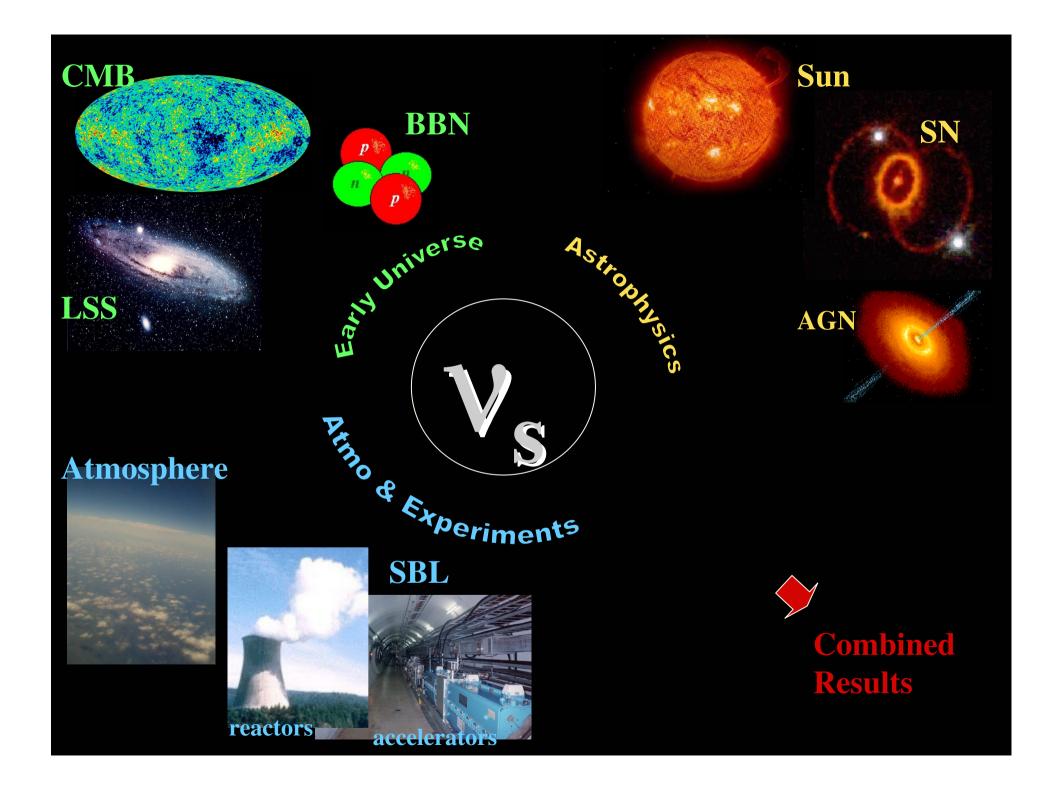
We perform a global χ^2 analysis of SK + Macro + K2K data.

"No improvements" w.r.t. pure $v_{\mu} \rightarrow v_{\tau}$ found: \Rightarrow no evidence for sterile neutrinos \Rightarrow excluded regions.



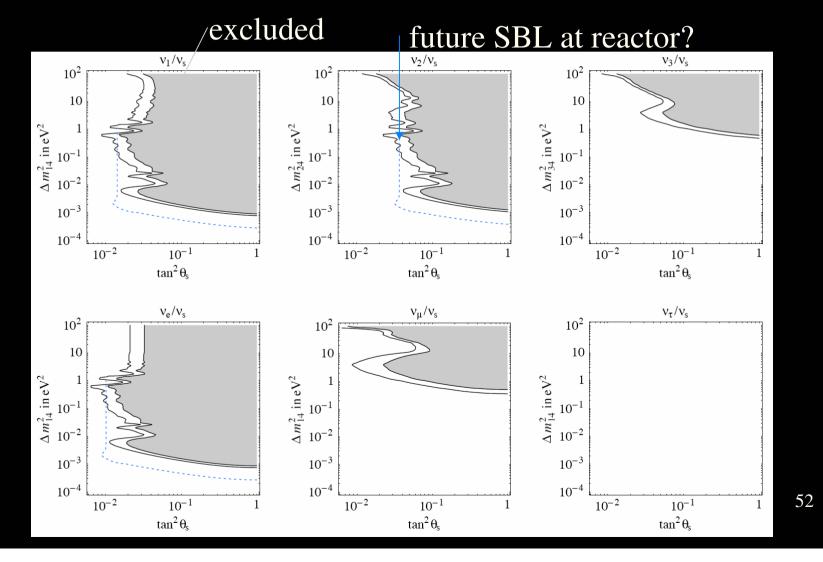
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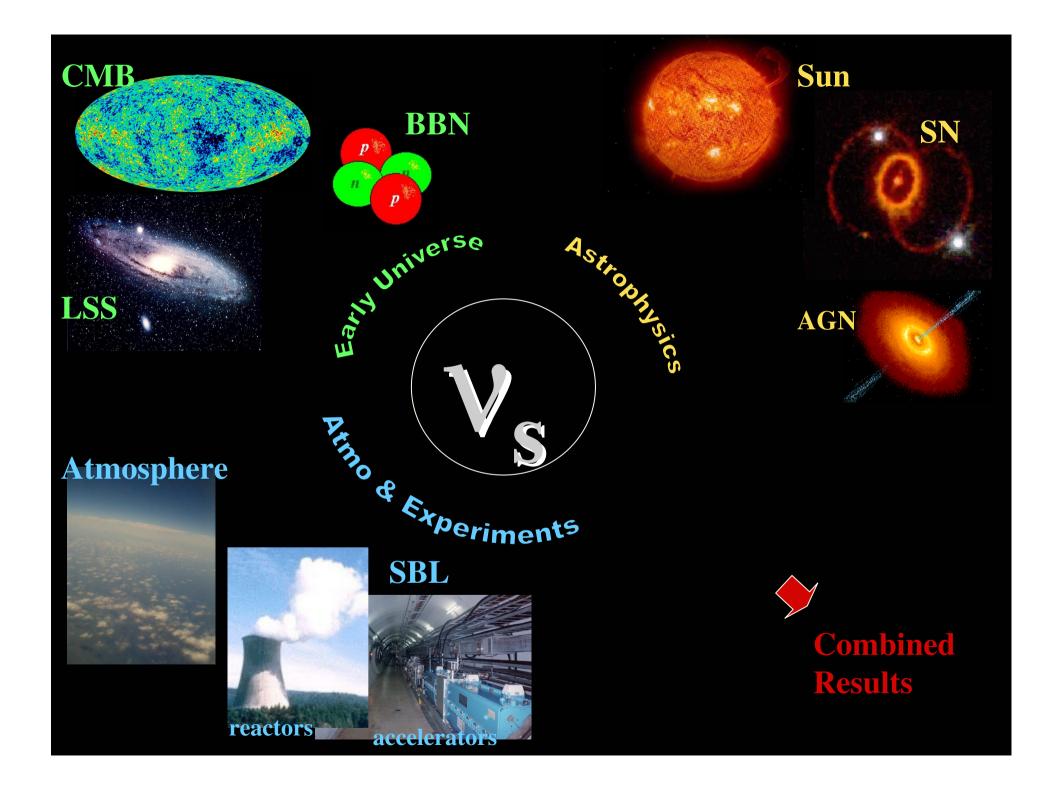




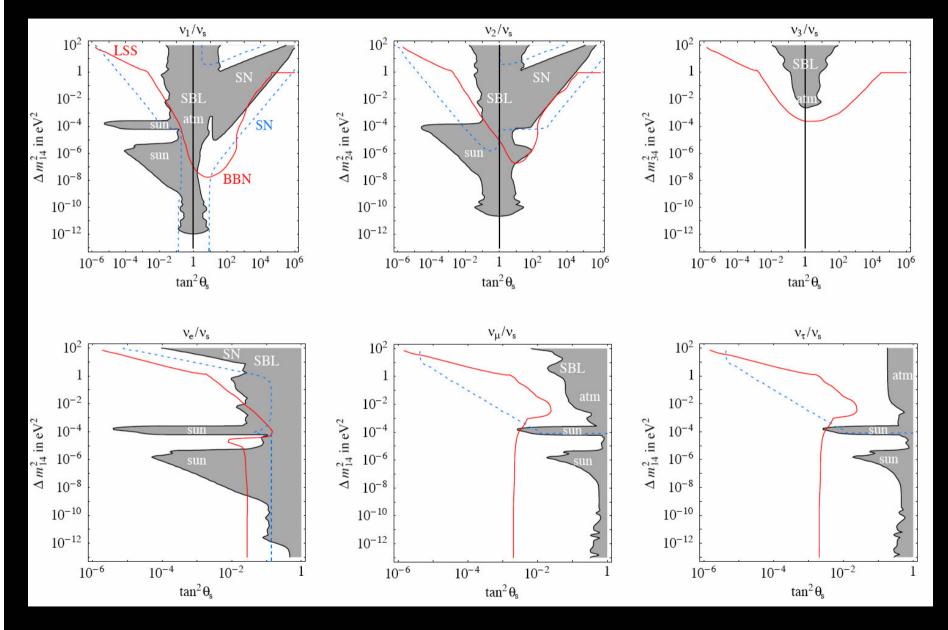
Sterile effects in SBL neutrinos

Chooz + Bugey + CDHS + CCFR + Karmen + Nomad + Chorus Main constraint comes from "no-disappearance".





Combined Results



Conclusions

- the "direct/easy way" for sterile neutrinos to enter our world (solar anomaly, atmospheric anomaly) is now ruled out
- performing a **general analysis**, we looked at more subtle and more interesting manifestations
- we find **no evidence** for sterile neutrinos so far
- we set the **present bounds**
- we identify several probes (more precise BBN, CMB, future SN explosions, sub-MeV solar neutrinos, ...)
- we show how LSND is really in trouble with cosmology (too)