



Penning trap measurement of the magnetic moment of the antiproton

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Villars Meeting, Sept. 25, 2004

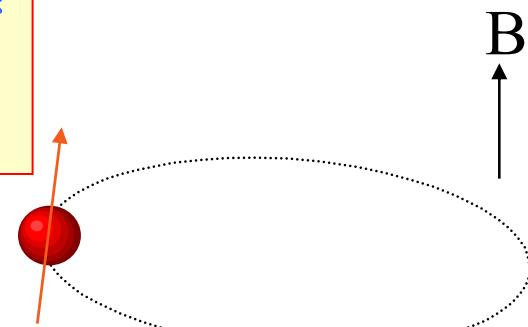
g-Factor of the antiproton

$$\frac{|\bar{\mu}_p|}{\mu_N} = g_p \cdot \frac{|\bar{s}|}{\hbar}$$

μ_p : magnetic moment
 g_p : g-factor
 s : spin
 μ_N : nuclear magneton

proton: $g_p = 2 \times 2.792847337(29)^*$
 accuracy: 10^{-8}

antiproton: $g_{p\bar{p}} = 2 \times 2.800(8)^*$
 accuracy: 10^{-3}



*Particle Data Group

g-Factor of the antiproton

Larmor precession frequency:

$$\omega_L = \frac{g_p}{2} \frac{e}{m_p} B$$



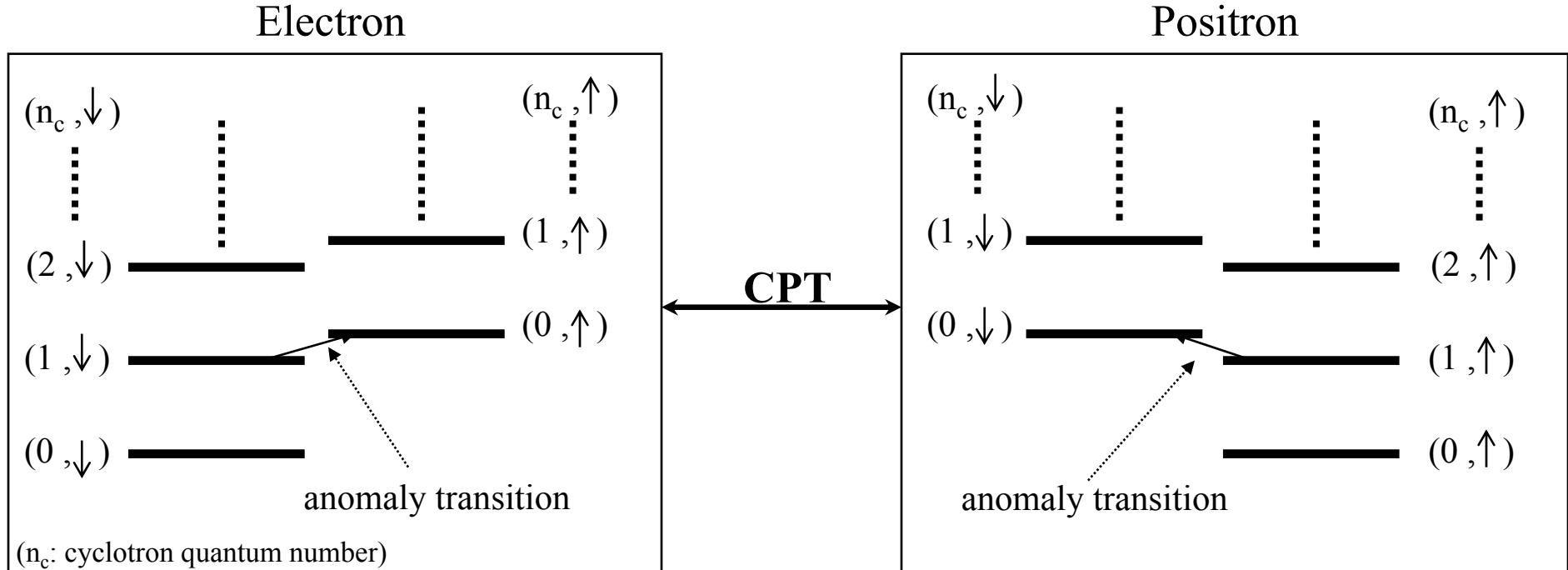
*B: magnetic field in
Penning trap*

cyclotron frequency:

$$\omega_c = \frac{e}{m_p} B$$

$$g_p = 2 \cdot \frac{\omega_L}{\omega_c}$$

Geonium: Single electron in a Penning trap

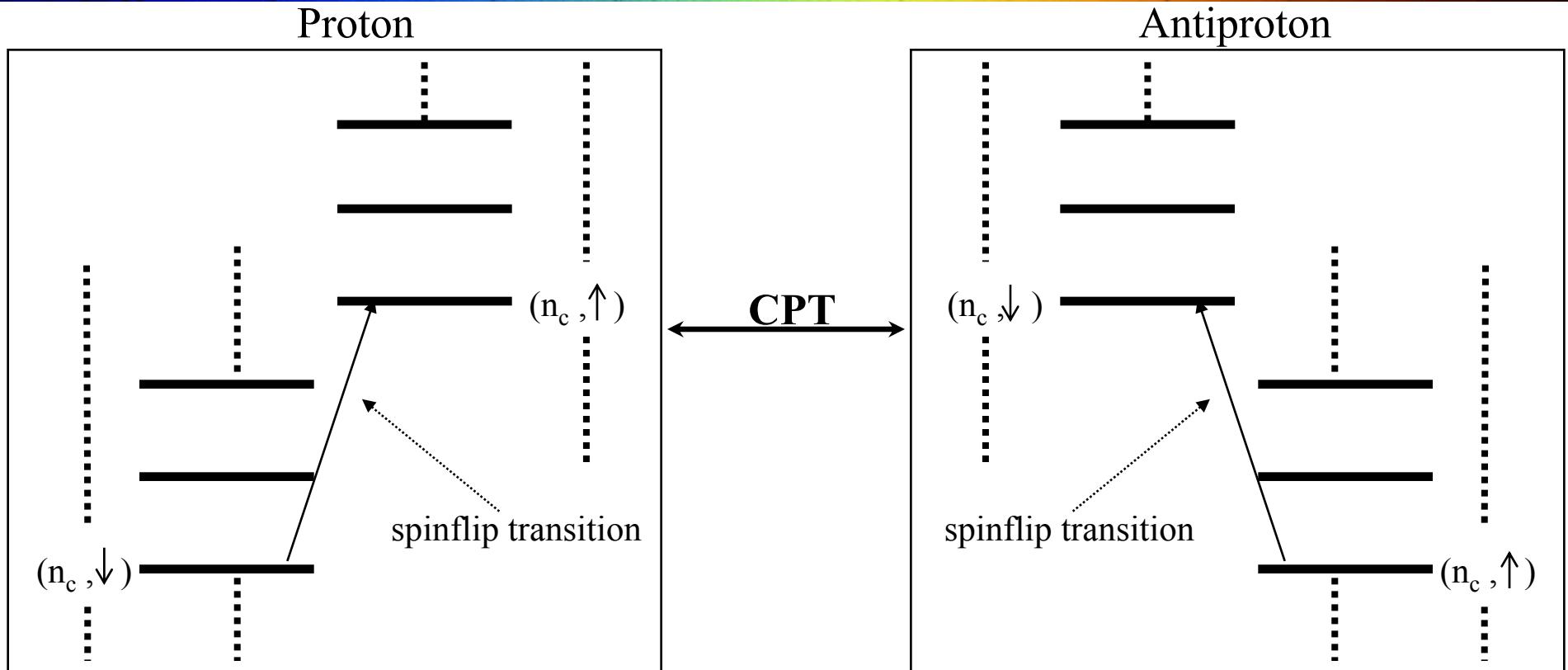


**Figure of merit for CPT violation
(Bluhm, Kostelecky, Russell):**

**(Dehmelt,
Van Dyck)**

$$\left| \hbar(\omega_a^+ - \omega_a^-) \right| / 2m_e c^2 \leq 1,2 \cdot 10^{-21}$$

Single antiproton in a Penning trap

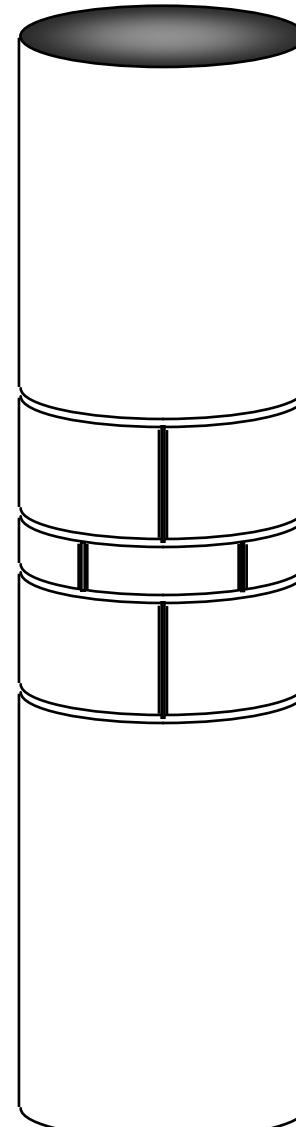
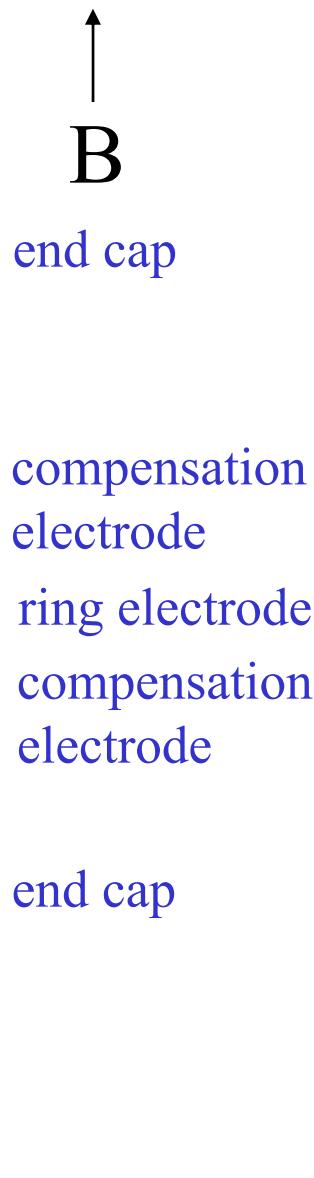


**Figure of merit for CPT violation
(Bluhm, Kostelecky, Russell):**

$$|\hbar(\omega_a^+ - \omega_a^-)| / 2m_p c^2 \leq 1 \cdot 10^{-25}$$

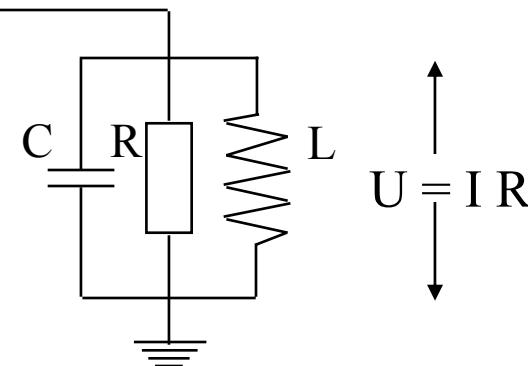
(expected accuracy)

Electronic detection of a single antiproton



$$v_c^2 = v_-^2 + v_z^2 + v_+^2$$

$$v_z = 1 \text{ MHz}$$



$$\frac{dE_p}{dt} = P_{\text{cool}} = -I^2 R$$

→ **cooling**

Cyclotron resonance of a single antiproton

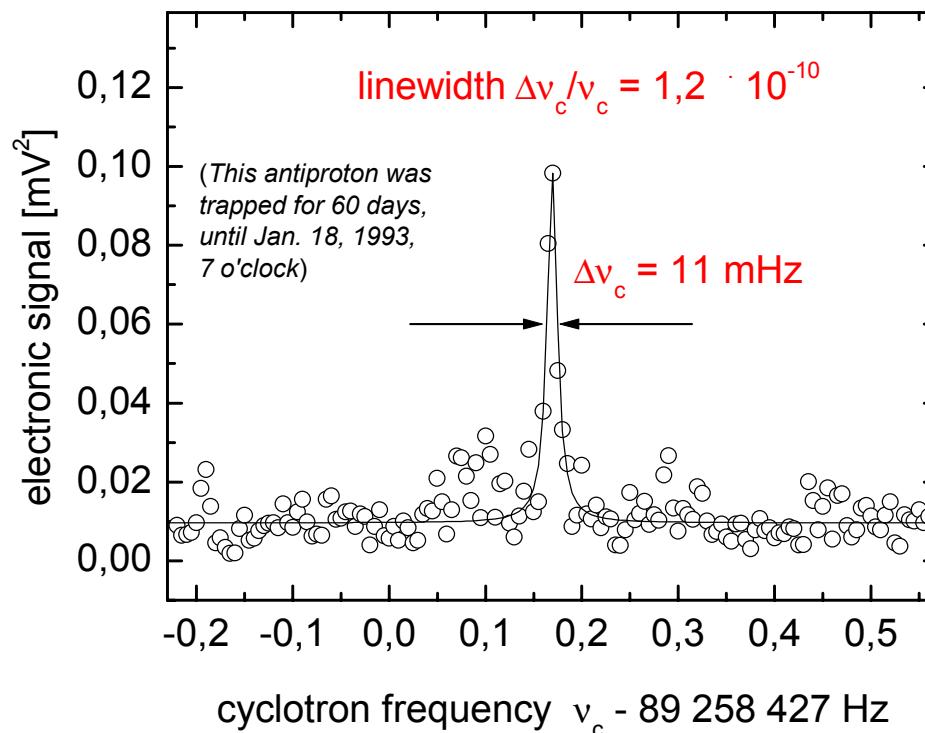
$$v_c = \frac{eB}{m\gamma}$$

$$\gamma = (1 - \beta^2)^{-1/2} = 1,000\,000\,005$$

relativistic frequency shift:

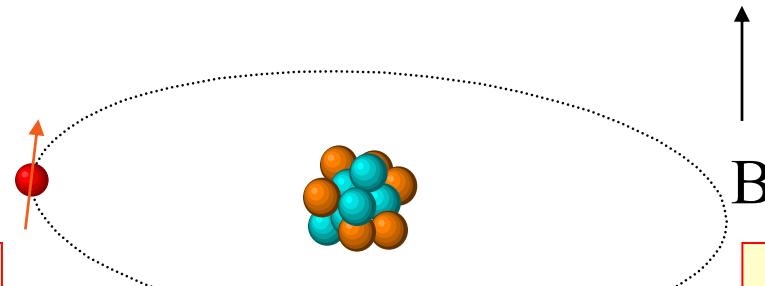
$$\Delta v_c / v_c = -E_c / mc^2, \quad E_c = 5 \text{ eV}$$

$$\Delta v_c = -0,5 \text{ Hz}$$



measured at LEAR,
1993
(G. Gabrielse,
D. Phillips,
W. Quint)

G-Factor of the bound electron in H-like ions



Larmor precession frequency of bound electron:

$$\omega_L = \frac{g_J}{2} \frac{e}{m_e} B$$

Ion cyclotron frequency:

$$\omega_c = \frac{q}{M_{ion}} B$$

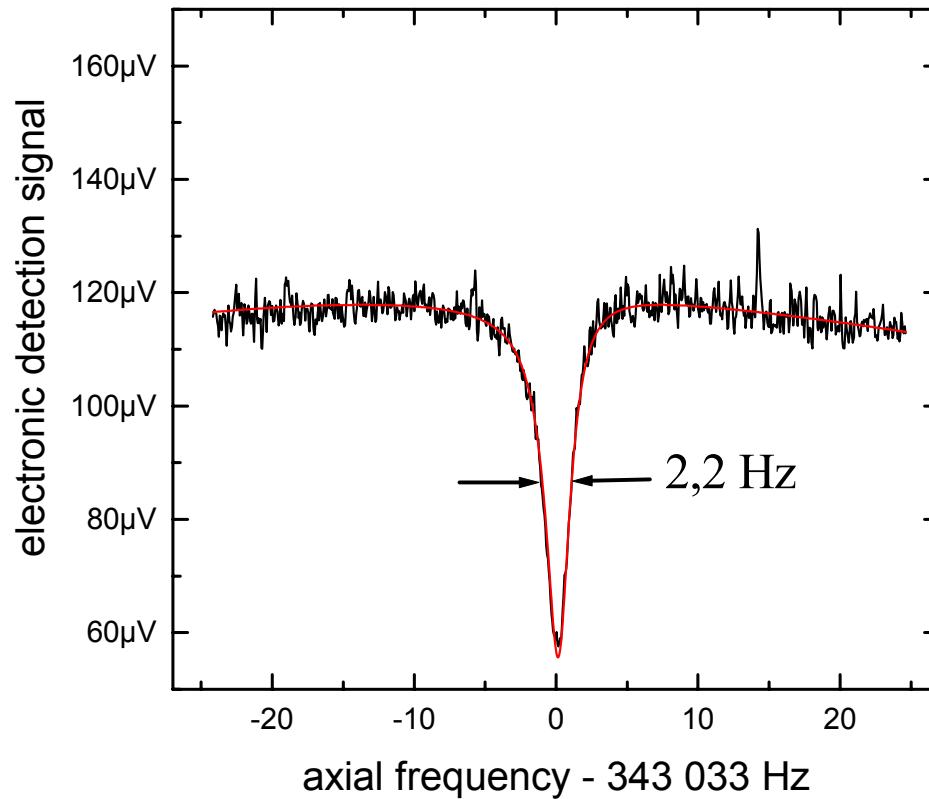
$$g_J = 2 \cdot \left(\frac{\nu_L}{\nu_c^{ion}} \right) \cdot \frac{\left(m/e \right)^e}{\left(M/q \right)^{ion}}$$



new value for the electron mass

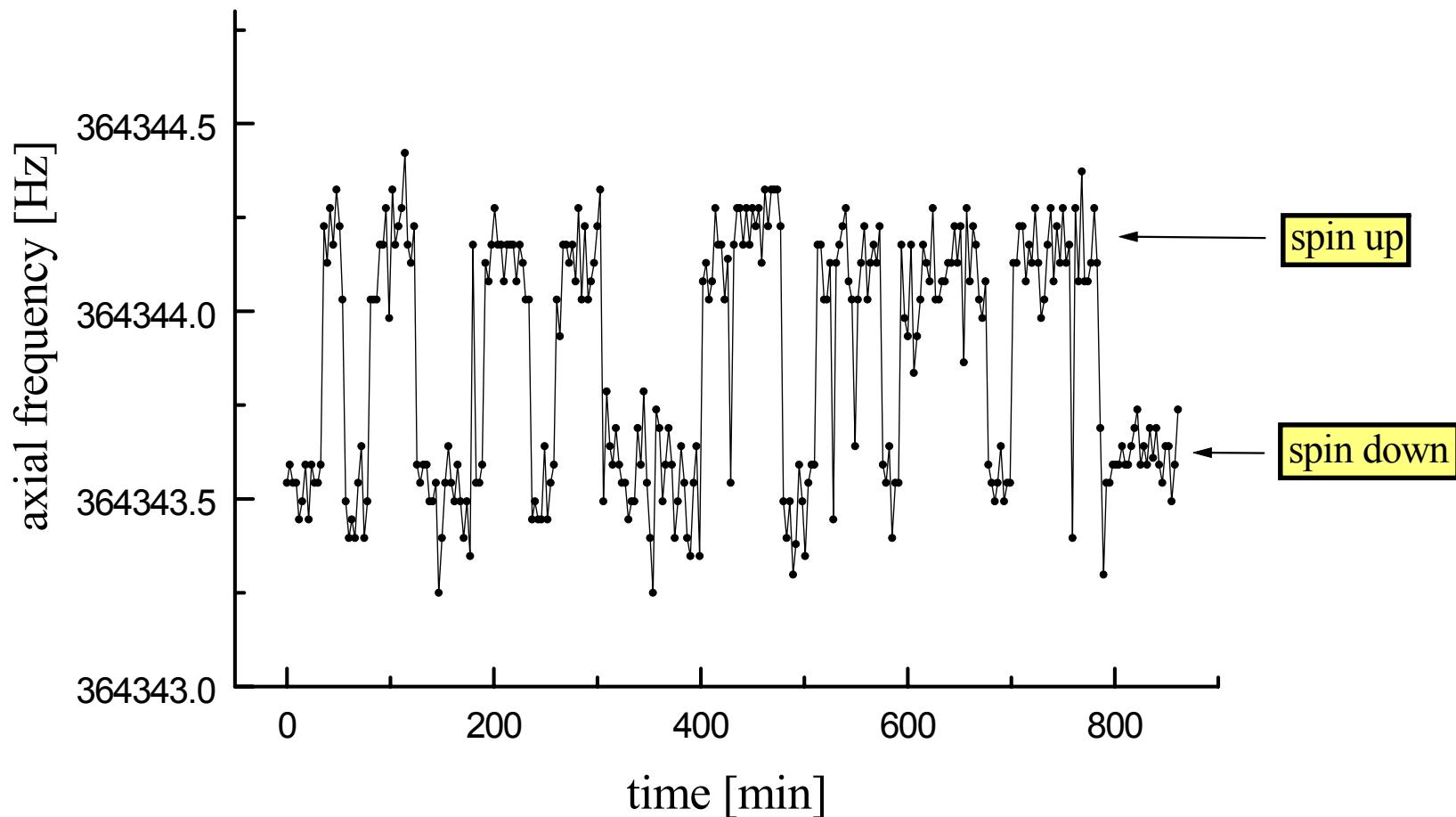
Measurement of the axial frequency
of a single C^{5+} -ion

◦ non-destructive detection at $T = 4$ Kelvin

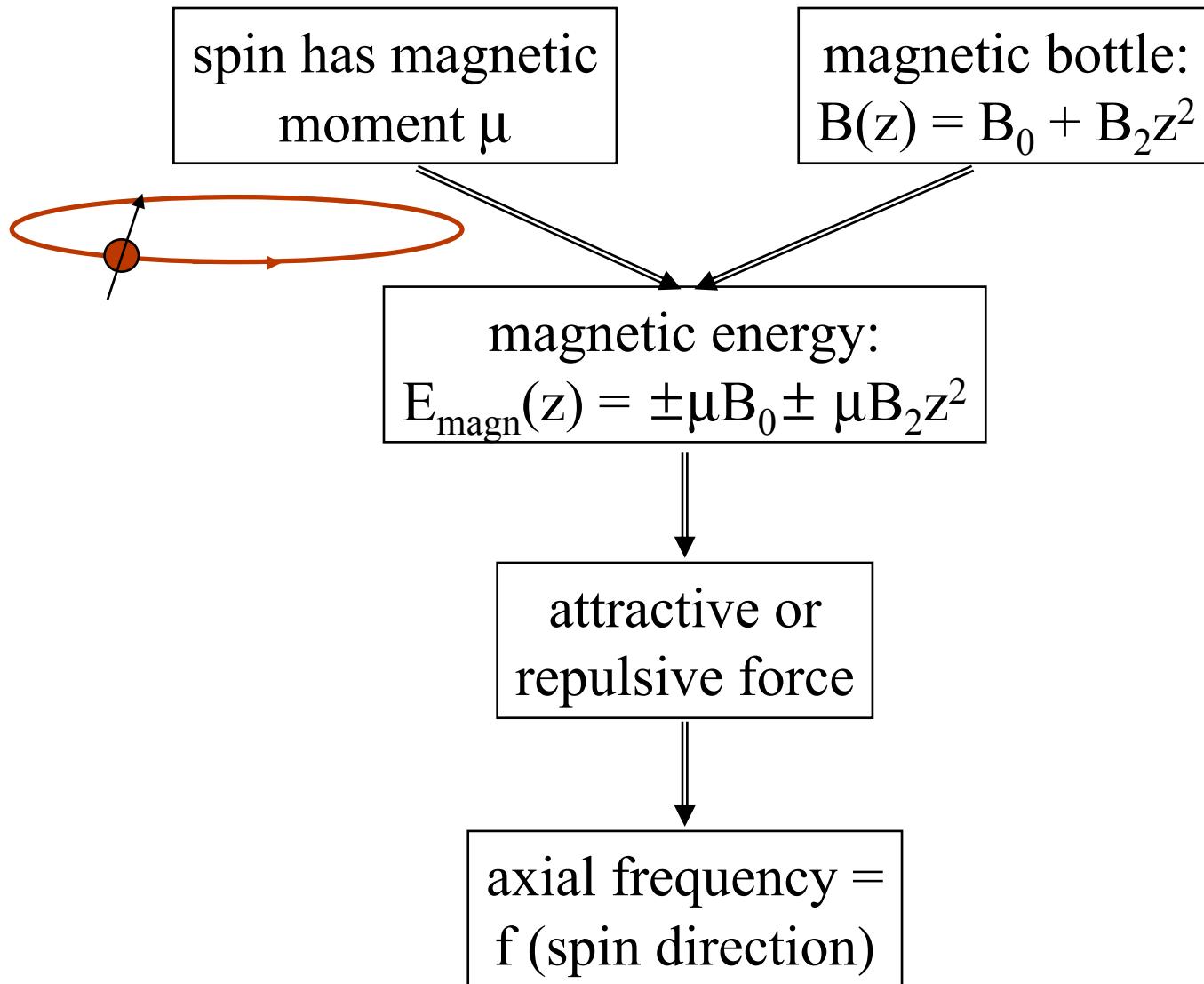




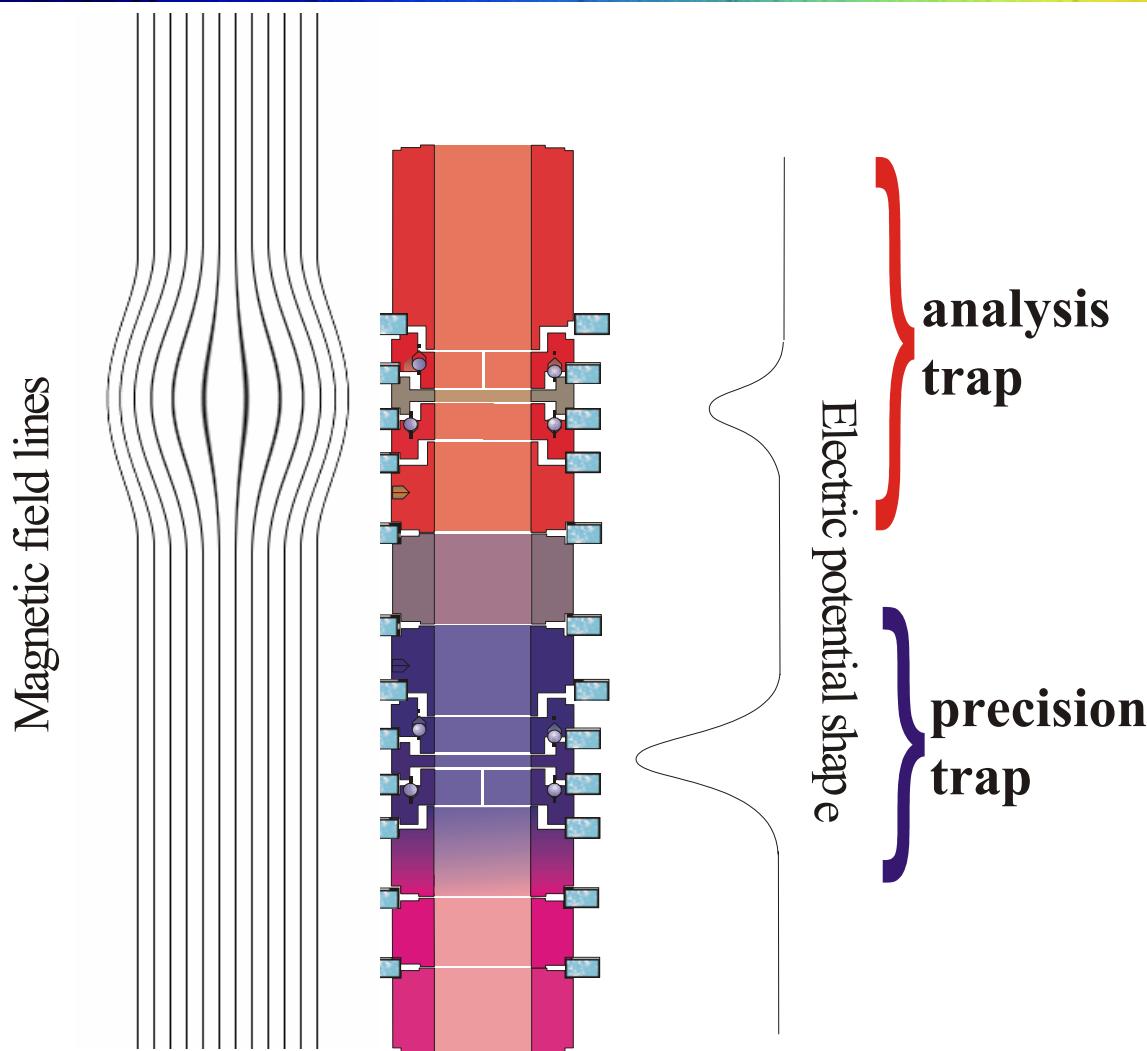
- Axial frequency depends on spin direction due to continuous Stern-Gerlach effect



Continuous Stern-Gerlach effect



Double-Trap Technique for g-Factor Measurements

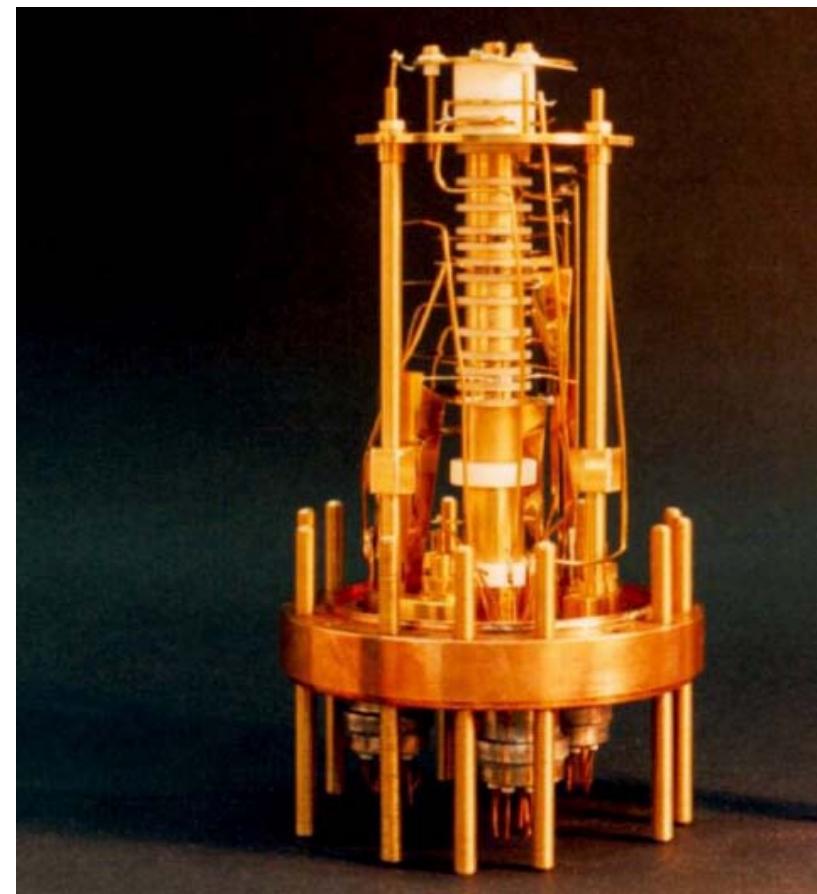
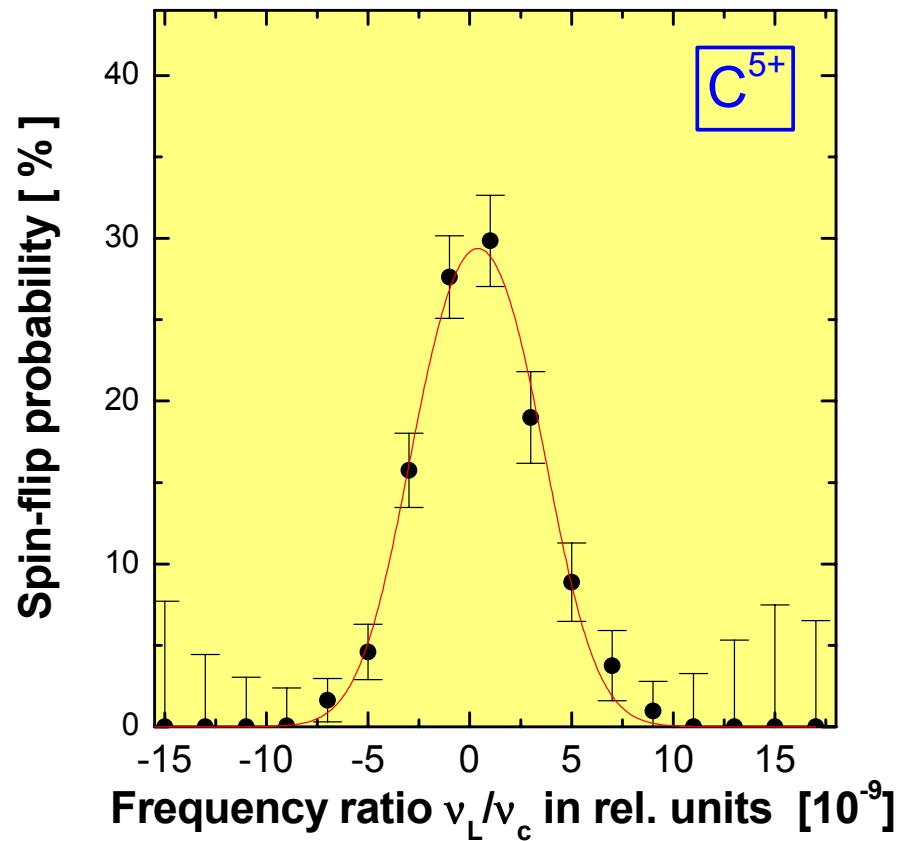


Principle:

- Excitation of spin-flip in precision trap (homogeneous magnetic field)
- Detection of spin-flip in analysis trap (inhomogeneous magnetic field for spin-flip detection)

G-Factor of bound electron in highly charged ions

- Measurement of the g-factor of the bound electron with an accuracy of 7×10^{-10}



Parameters of g-factor experiments

	Electron (Van Dyck/ Dehmelt)	C^{5+} (Mainz/ GSI)	O^{7+} (Mainz/ GSI)	Antiproton (proposed)
Magnetic moment	$g\mu_{\text{B}}/2$	$g\mu_{\text{B}}/2$	$g\mu_{\text{B}}/2$	$g\mu_{\text{N}}/2$
g-Factor	$g = 2.00\dots$	$g = 2.00\dots$	$g = 2.00\dots$	$g = 5.58\dots$
‘Magnetic bottle’	0.15 mT/mm^2	10 mT/mm^2	10 mT/mm^2	230 mT/mm^2
Δv_z due to spinflip	1.3 Hz	0.7 Hz	0.46 Hz	0.25 Hz

Conclusions

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- Measurement of the magnetic moment of the bound electron with an accuracy of 7×10^{-10} .
 - This experimental technique can be employed for the measurement of the magnetic moment of the antiproton.



Improvement of accuracy in $g_{p\bar{p}}$ by six orders of magnitude



Important test of CPT invariance for baryons