

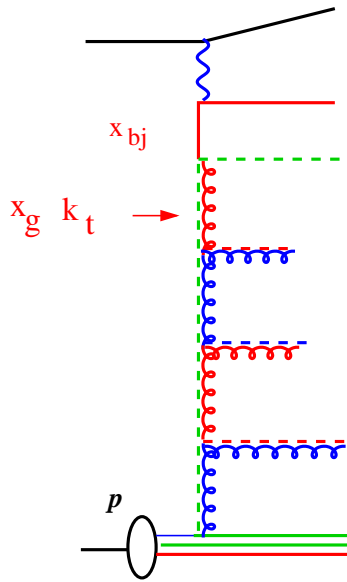
Constraining the Un-integrated PDFs status report ...

H. Jung, DESY

- check k_t and scale dependences of different processes
 - where to use inclusive measurements
 - where to use final state measurements
- restrict to gluon induced processes
 - heavy quark production at HERA and Tevatron
- aim to simultaneously describe measurements
- conclusion

Structure Function $F_2(x, Q^2)$

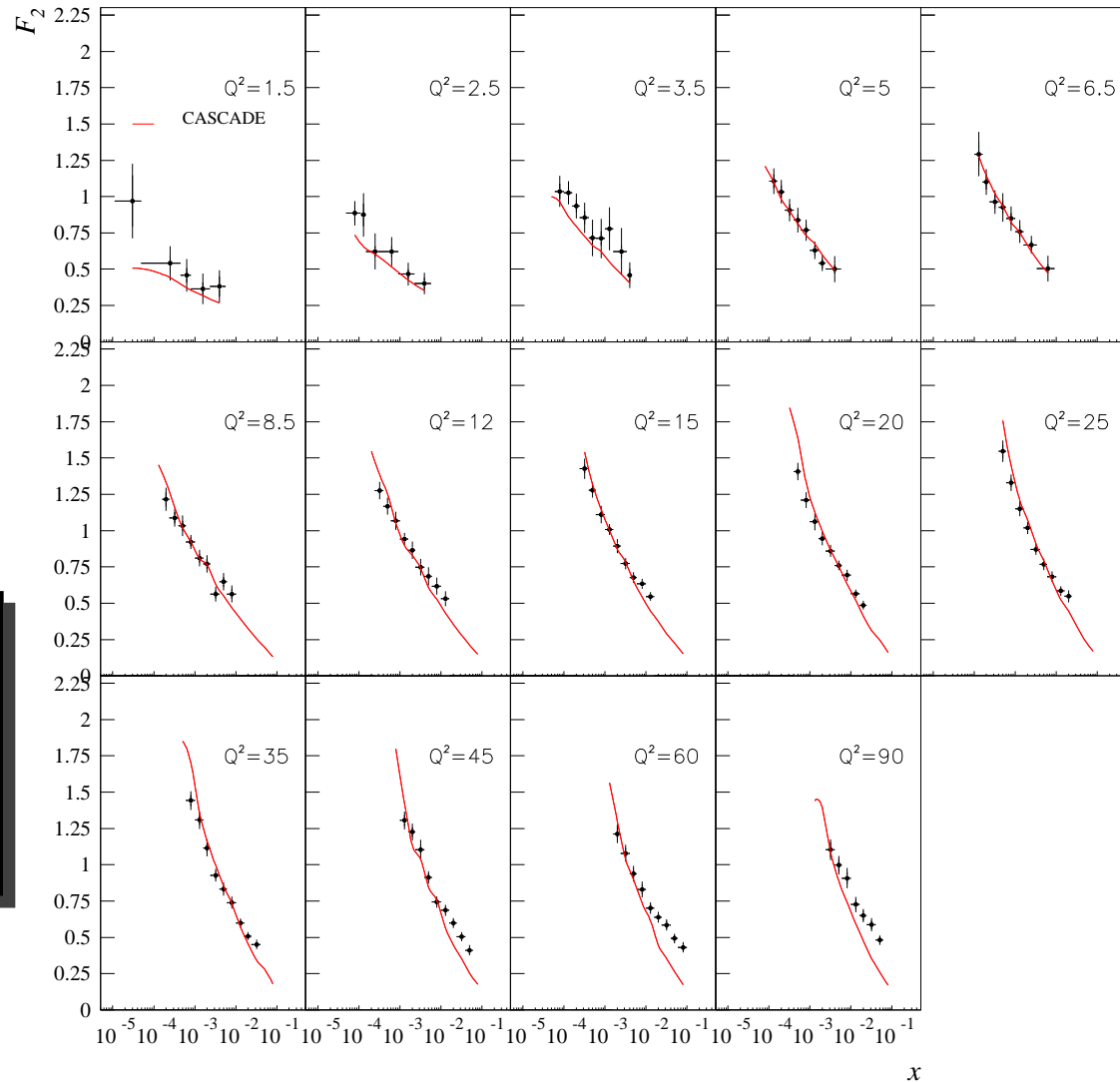
With $\sigma = \int dk_t^2 dx_g \mathcal{A}(x_g, k_t^2, \bar{q}) \sigma(\gamma^* g^* \rightarrow q\bar{q})$ fit $F_2(x, Q^2)$



un-integrated gluon density

$$x\mathcal{A}(x, k_t^2, \bar{q})$$

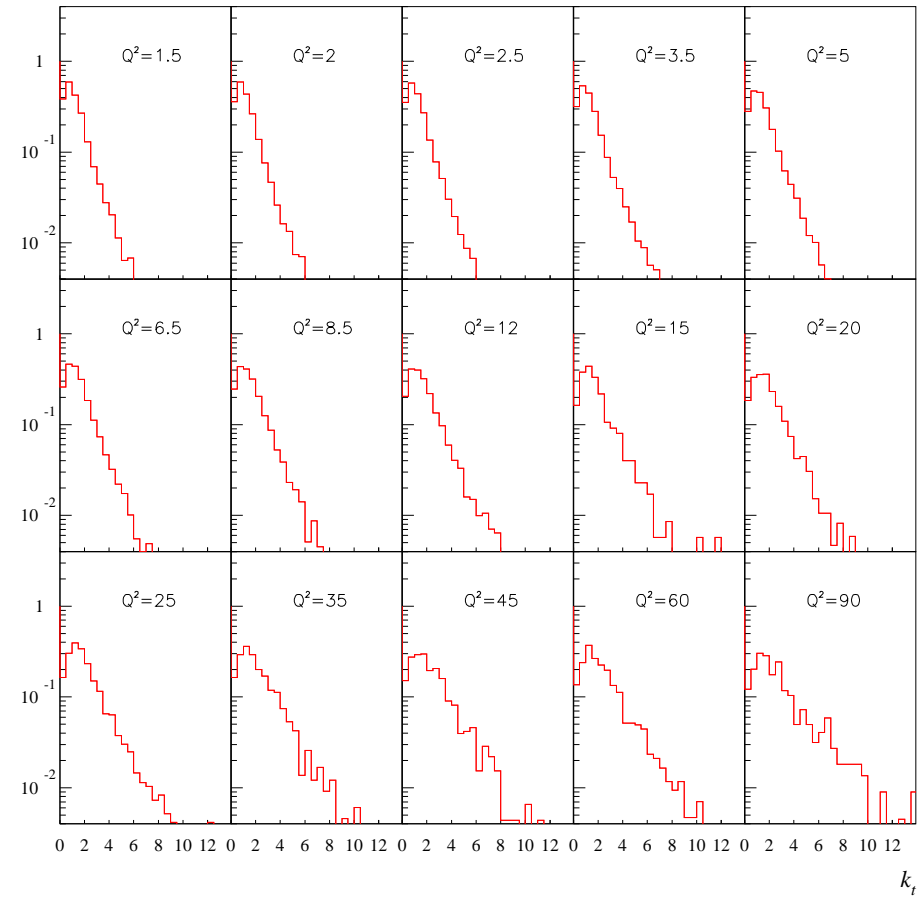
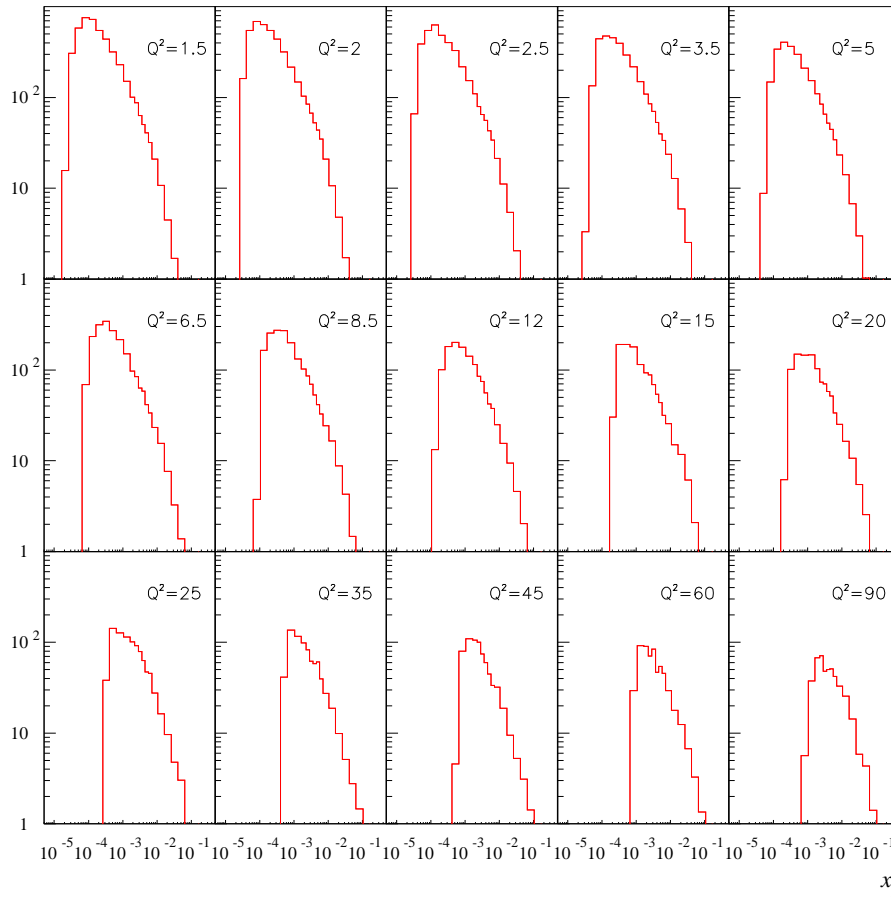
obtained from fit to F_2



$F_2(x, Q^2)$ kinematic plane for x_g and k_t

x_g

k_t



$F_2(x, Q^2)$ covers significant region in $x_g \gtrsim 10^{-4}$

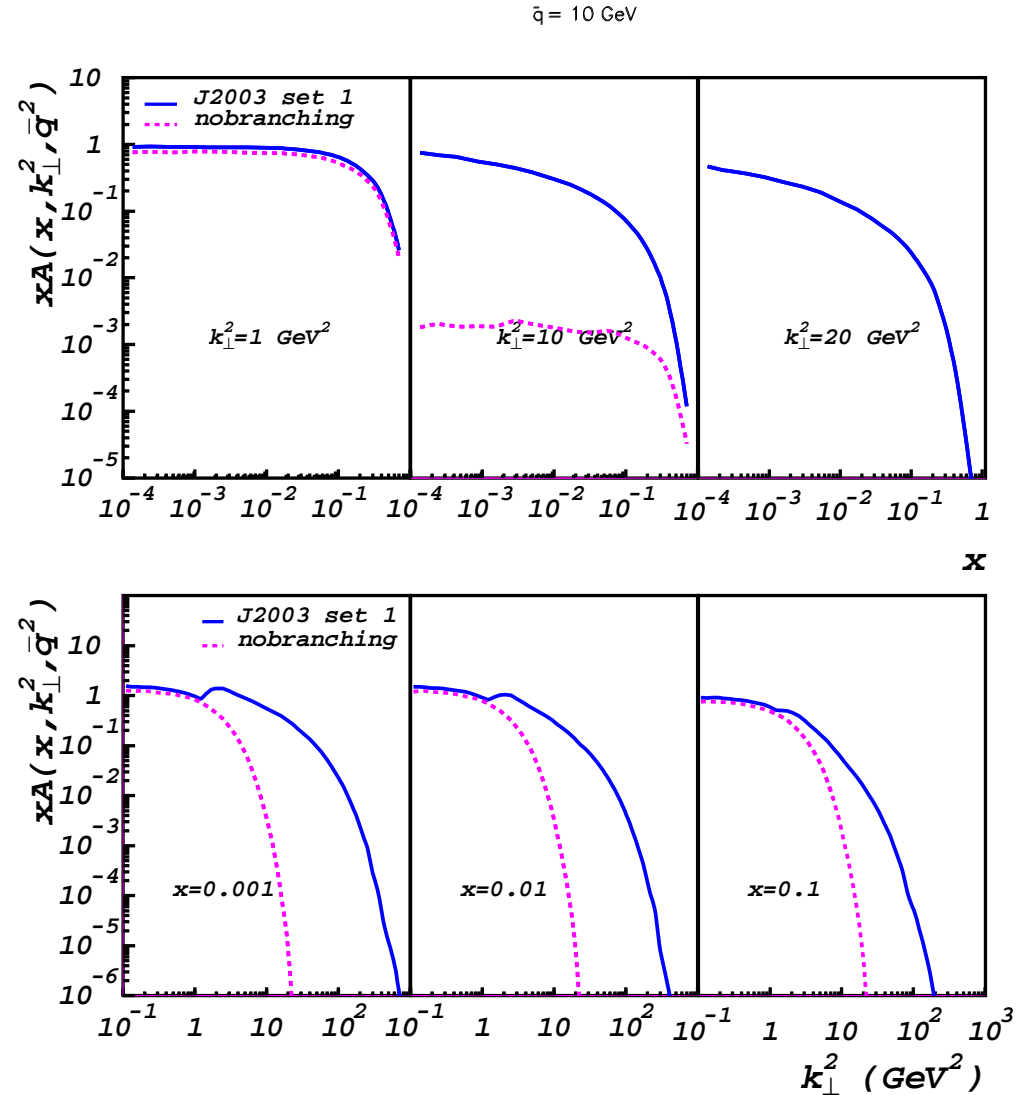
BUT mainly sensitive to small k_t region ... initial condition...

$F_2(x, Q^2)$ and unintegrated gluon !

- F_2 sensitive to small k_t
- F_2 measure of
 - ☞ initial k_t distribution
 - ☞ non-branching probability

$$\mathcal{A}(x, k_t, \bar{q}) = \mathcal{A}_0(x, k_t) \Delta_s(\bar{q}, Q_0) + \int \frac{dz}{z} \frac{d^2 q}{q^2} \Delta_s(\bar{q}, zq) \cdot \tilde{P}(z, \dots) \mathcal{A}\left(\frac{x}{z}, k'_t, q\right)$$

- what is contribution from $k_t \gtrsim 2 \text{ GeV}$?

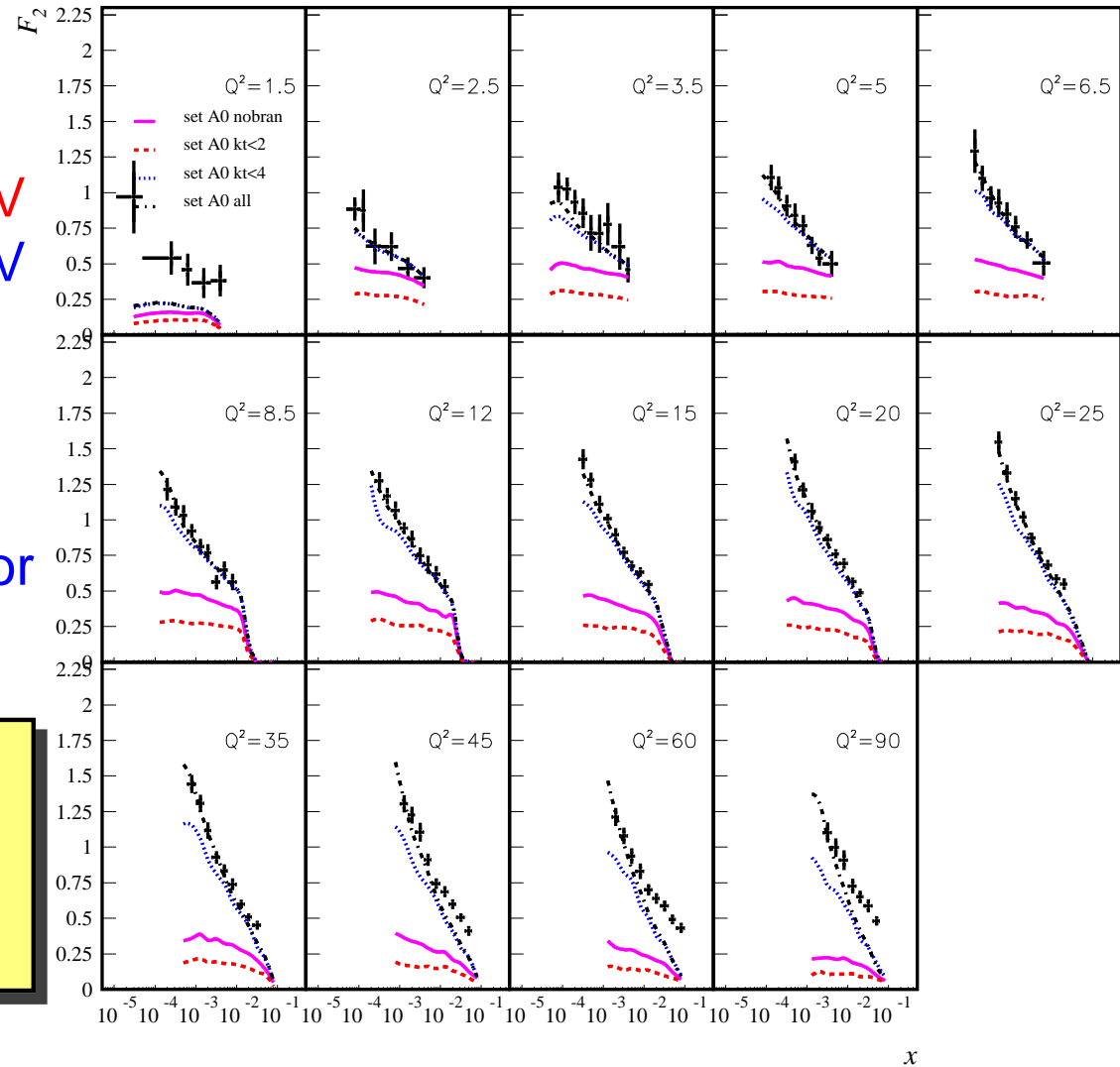


k_t dependence in $F_2(x, Q^2)$

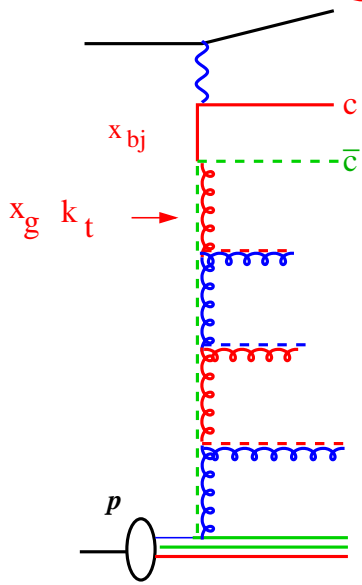
- check sensitivity on k_t
 - ☞ nobran contribution
 - ☞ contribution with $k_t < 2$ GeV
 - ☞ contribution with $k_t < 4$ GeV
 - ☞ all
- $k_t > 4$ GeV contributes very little to F_2 !!!
- $1 < k_t < 4$ GeV responsible for rise of F_2 !!!

● $F_2(x, Q^2)$ can constrain:

- ☞ small $k_t < 4$ GeV region
- ☞ range of $x_g \approx 10^{-4}$

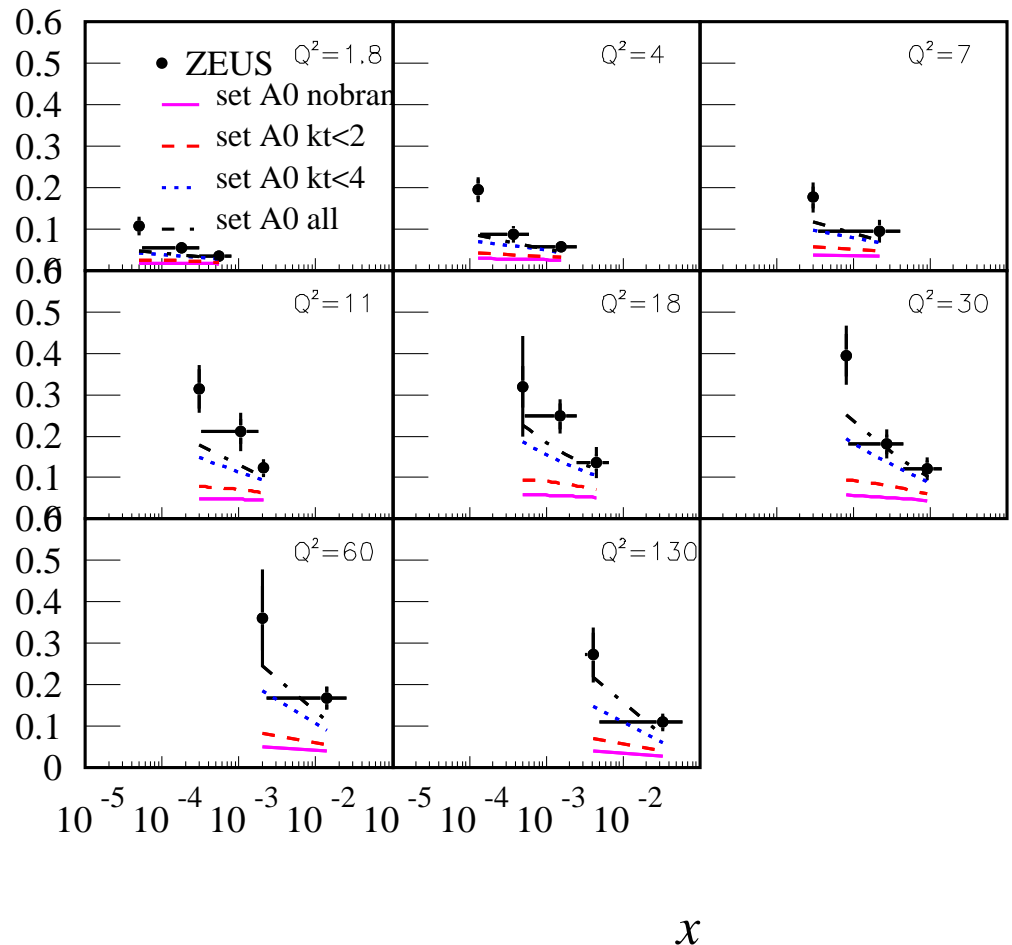


k_t dependence in $F_2^c(x, Q^2)$



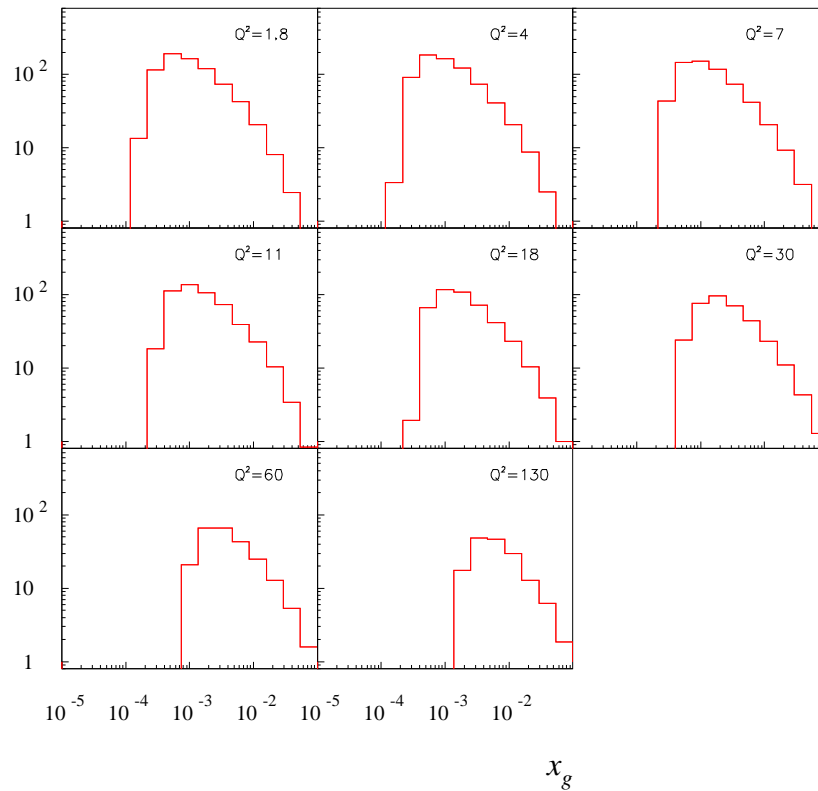
- check sensitivity on k_t
- ➡ nobran contribution
- ➡ contribution with $k_t < 2$ GeV
- ➡ contribution with $k_t < 4$ GeV
- ➡ all
- $k_t < 2$ GeV contributes very little to F_2^c !!!
- $2 < k_t$ GeV significant for F_2^c !!!

F_2^{charm}

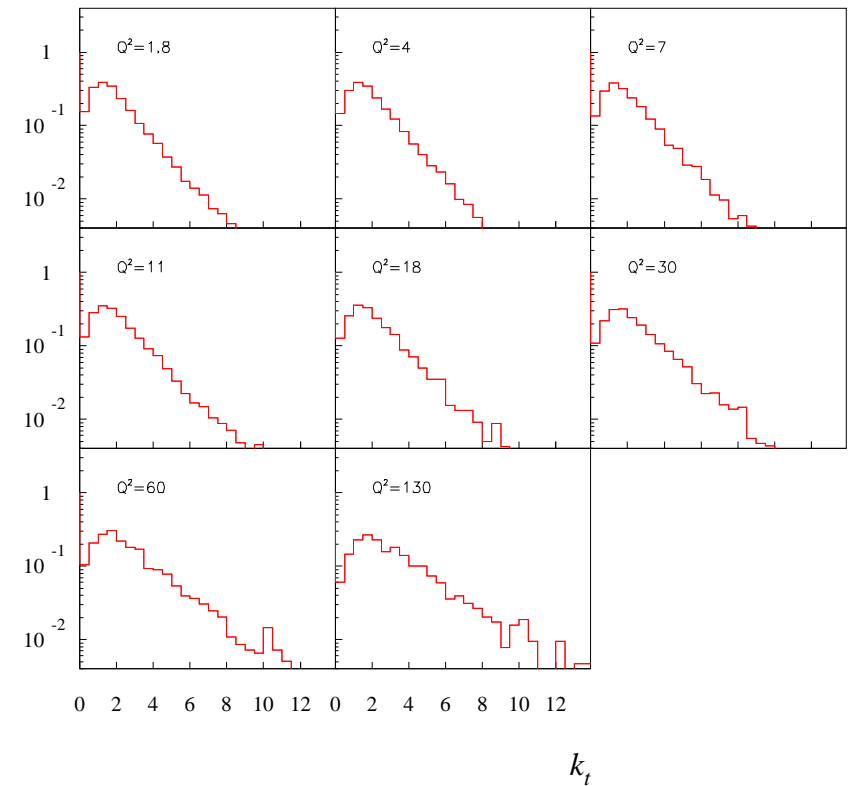


$F_2^c(x, Q^2)$ kinematic plane for x_g and k_t

x_g



k_t



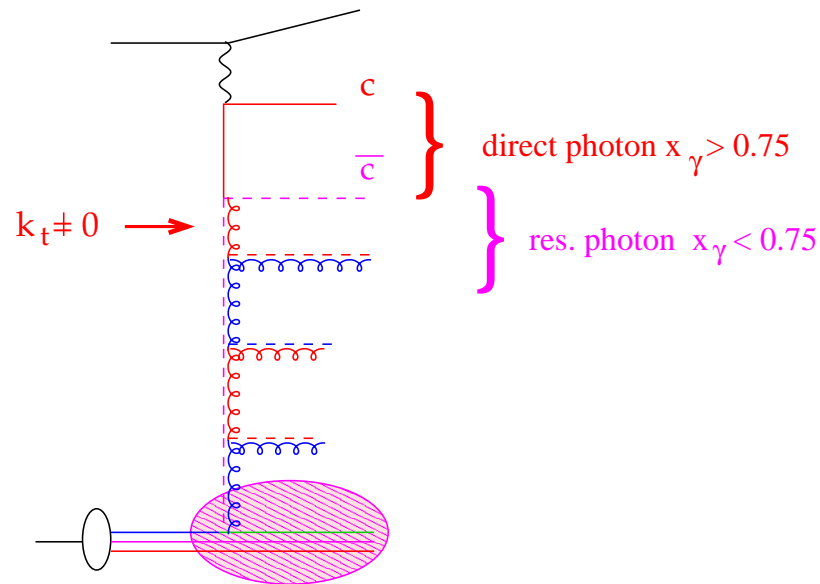
$F_2^c(x, Q^2)$ covers significant region in $x_g \gtrsim 10^{-3}$

AND sensitive to $k_t \gtrsim 2$ GeV region

Potential to better constrain un-integrated gluon !!!

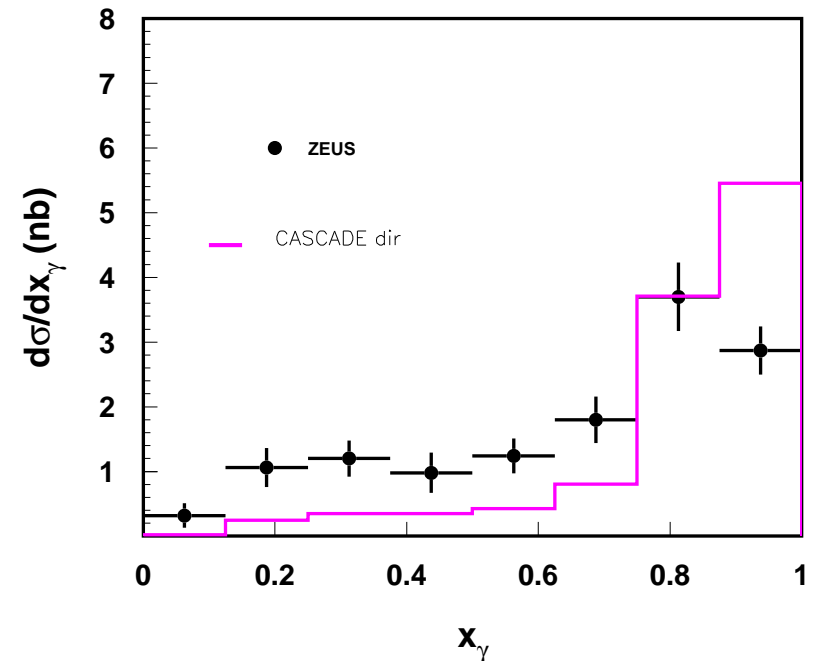
Unintegrated gluon density with heavy quarks

- identify one charm quark (D^*)
- reconstruct jets



- reconstruct x_γ
- x_γ related to k_t

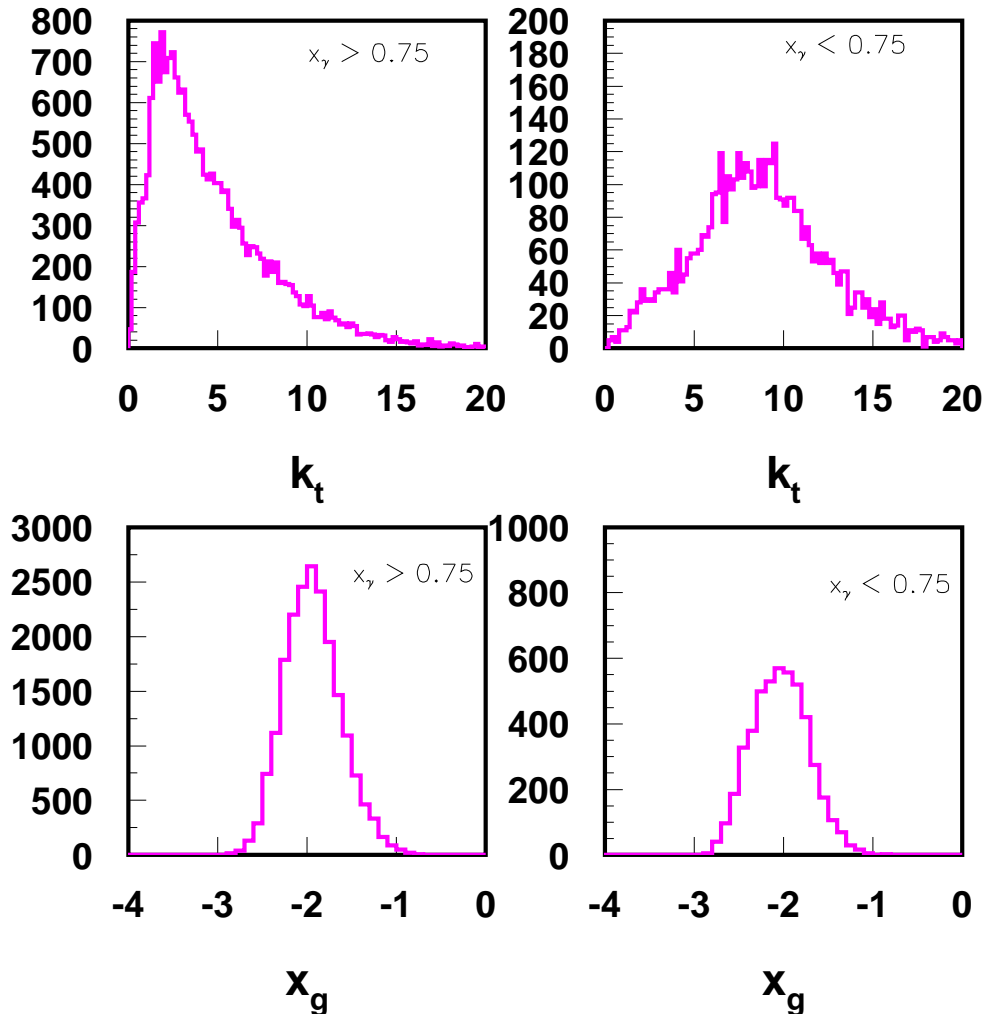
- $Q^2 < 1$, $0.2 < y < 0.9$,
 $p_t^D > 2 \text{ GeV}$, $|\eta^D| < 1.5$,
 $E_t > 7(6) \text{ GeV}$, $|\eta| < 2.4$



Charm in $\gamma p \rightarrow D^* + jet$ production

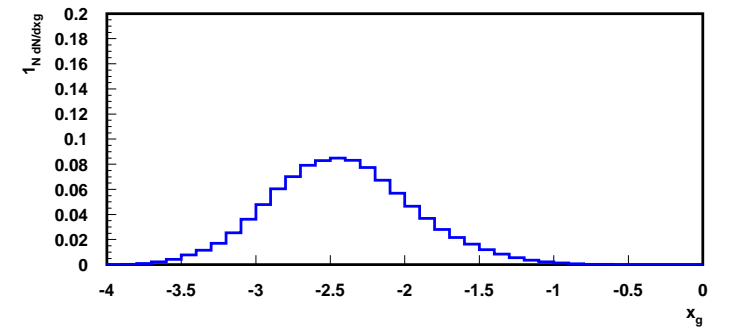
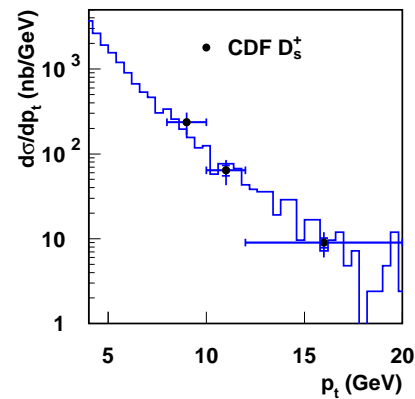
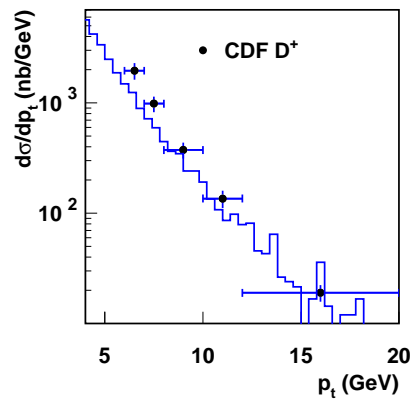
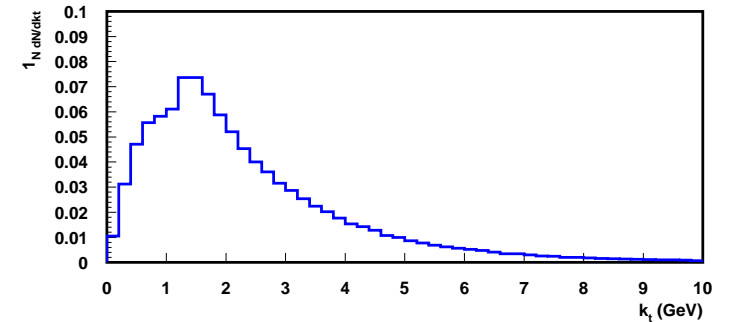
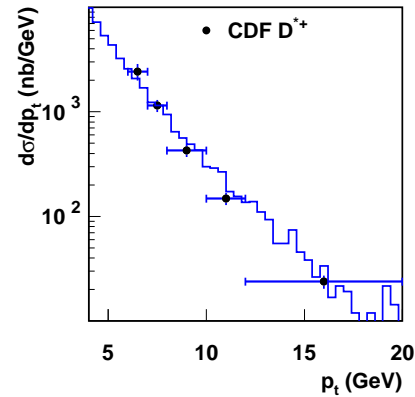
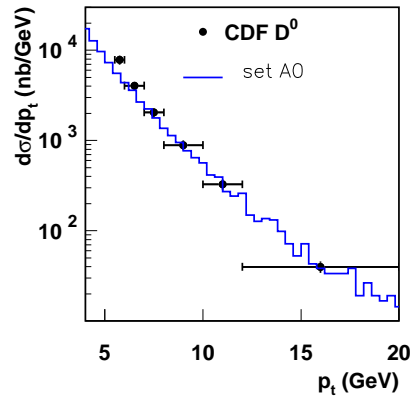
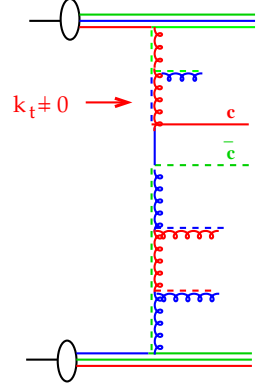
D^* photo - production (ZEUS Coll. EPJC 6 (1999) 67)

● $Q^2 < 1, 0.2 < y < 0.9, p_t^D > 2, |\eta^D| < 1.5, E_t > 7(6) \text{ GeV}, |\eta| < 2.4$



- truly perturbative region
- x_γ in D^* production
 - ➡ direct γ $k_t \sim 1 - 2 \text{ GeV}$
 - ➡ res. γ $k_t \sim 7 - 9 \text{ GeV}$
 - ➡ both at same x_g
- combine inclusive F_2^c with $D^* + Jet$
 - ➡ constrain un-integrated gluon

$c\bar{c}$ production at Tevatron



sensitive to $x_g \sim 0.005$ and $k_t \sim 2$ GeV

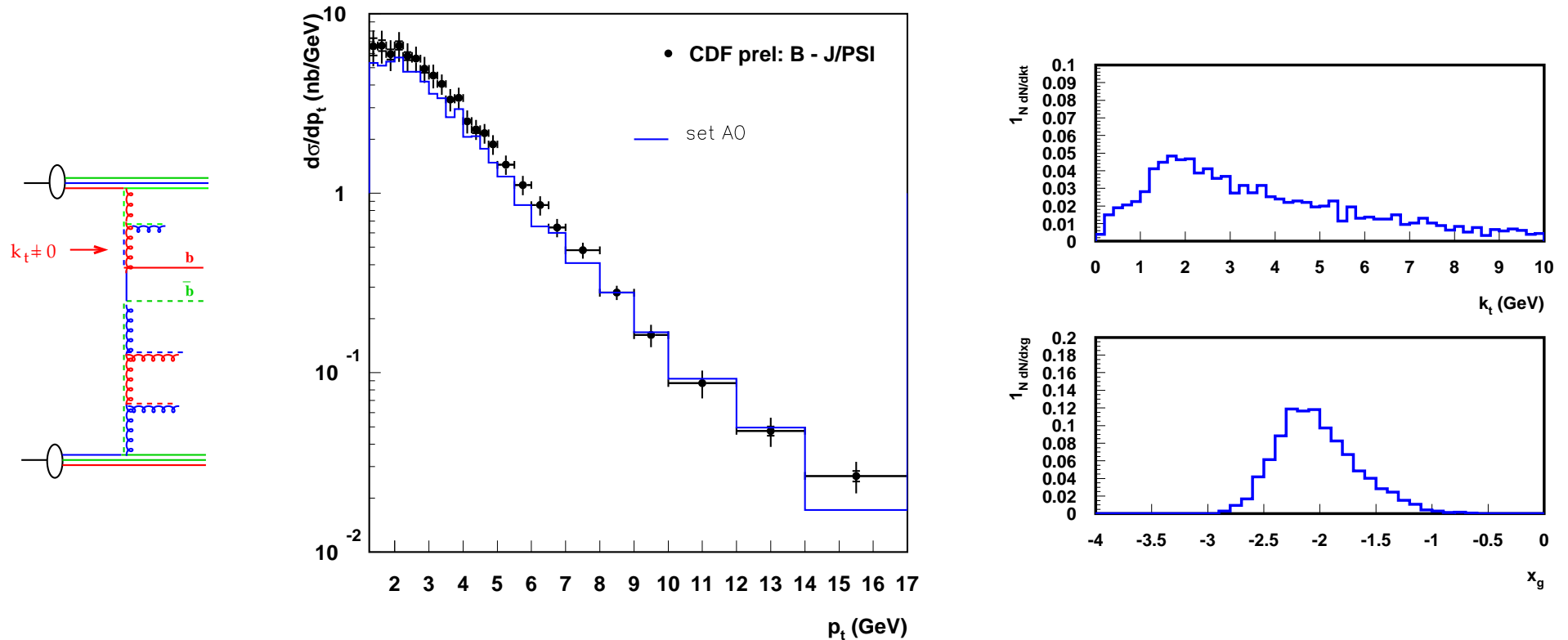


similar range in k_t as in charm photoproduction at HERA



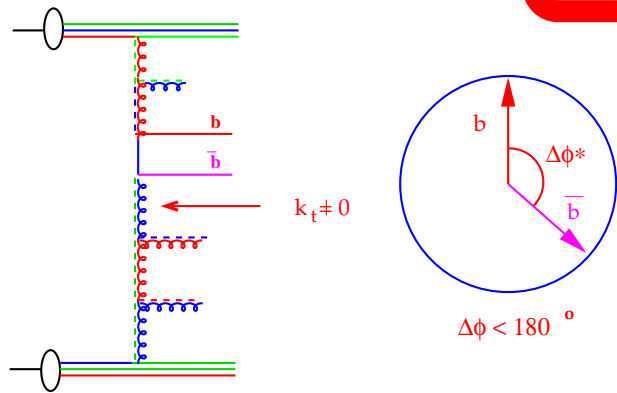
BUT different x_g range !!!

$b\bar{b}$ production at Tevatron $b \rightarrow J/\psi$

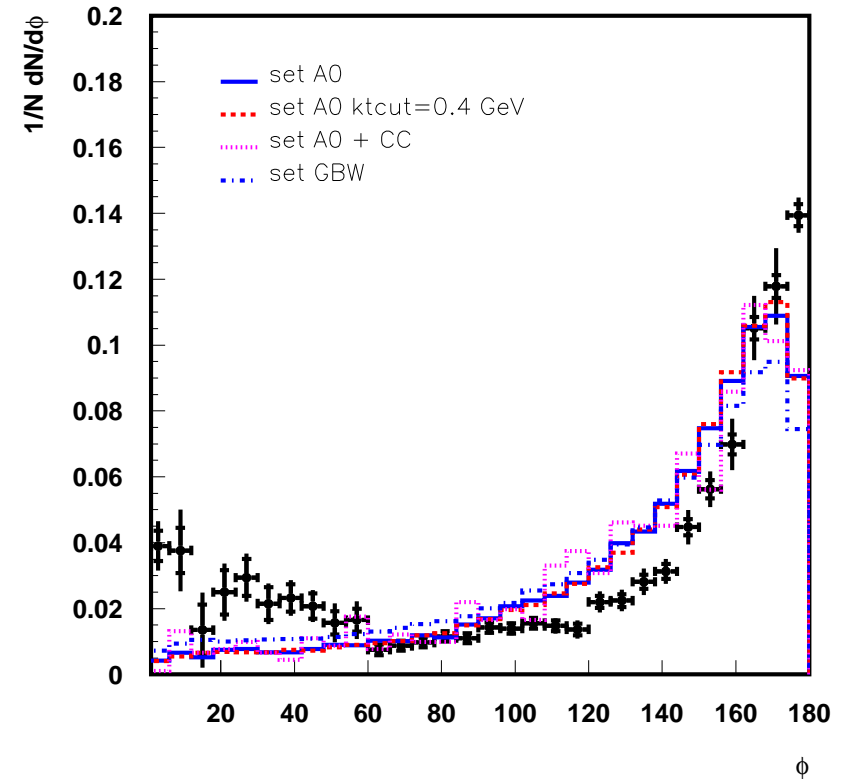


- sensitive to $x_g \sim 0.01$ and $k_t \sim 2$ GeV
- similar range as direct charm photoproduction at HERA
- **BUT** different factorisation scale !!!

$b\bar{b}$ $\Delta\phi$ distribution

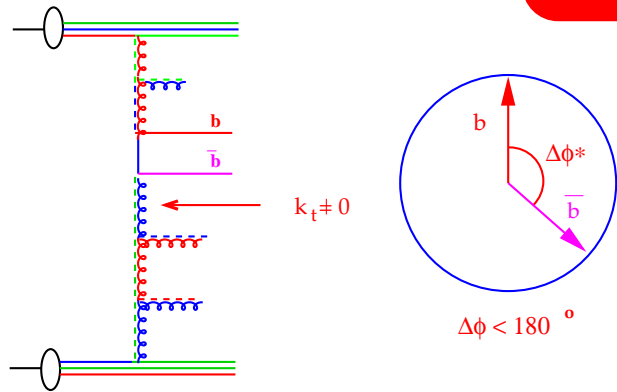


- no effect from changing:
 - splitting fct
 - initial condition
 - k_t -cutoff in cascade
 - applying consistency constraint

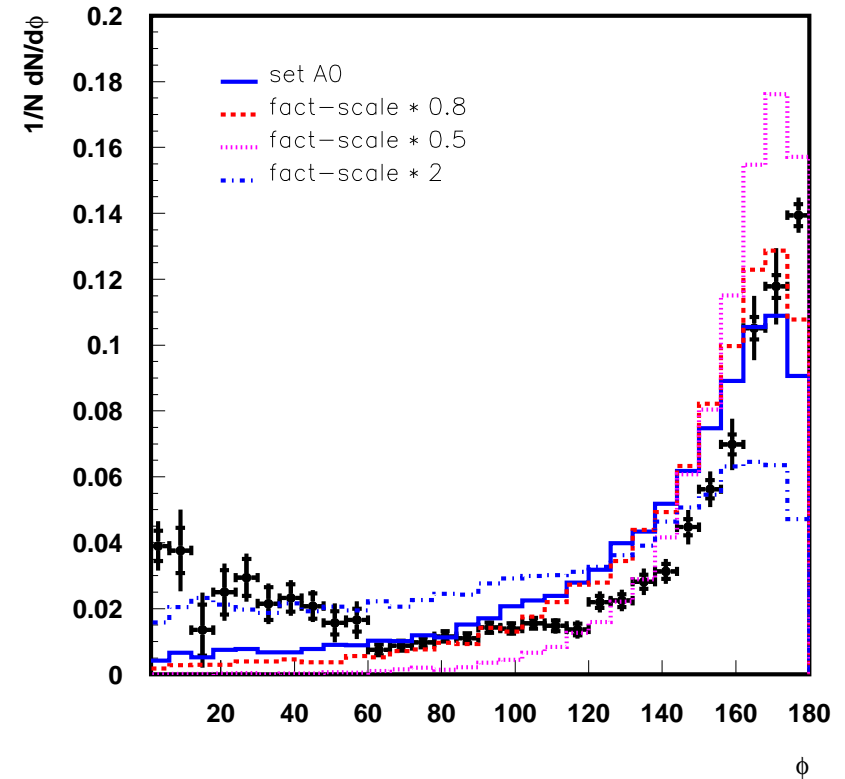


- $\Delta\phi$ is sensitive to shape of k_t distribution
- different initial conditions show similar behavior

$b\bar{b}$ $\Delta\phi$ distribution

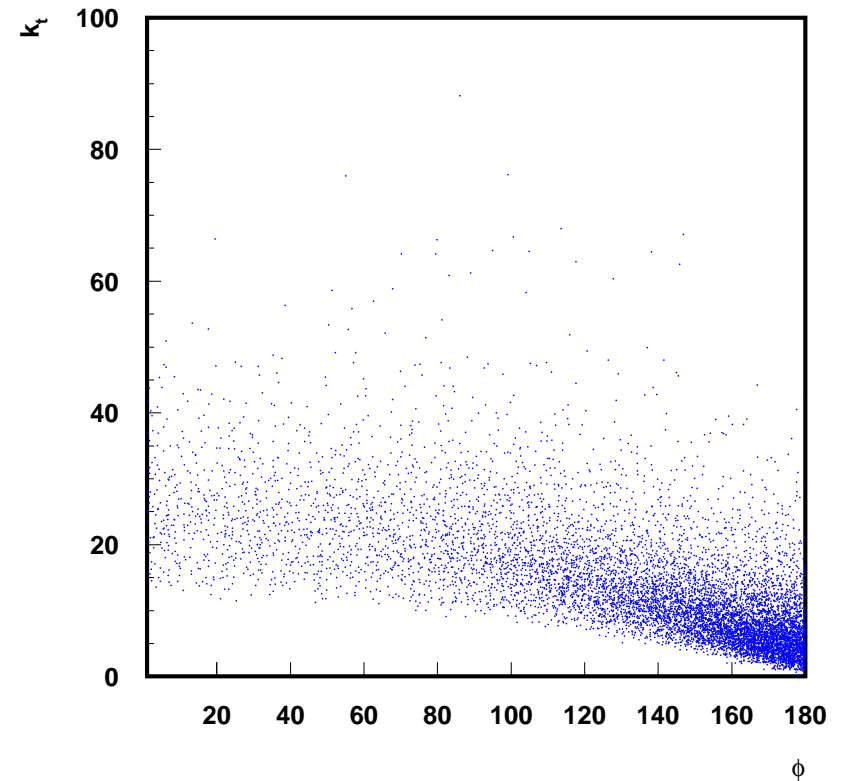
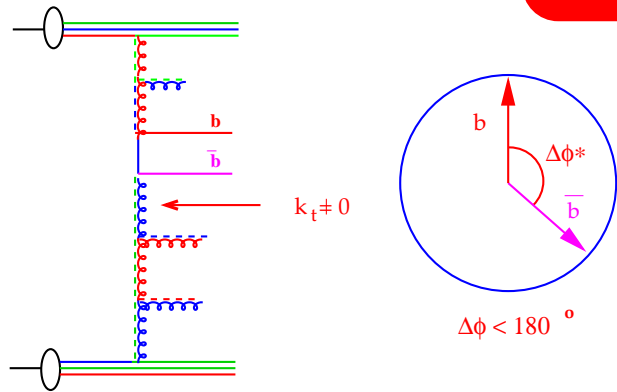


- no effect from changing:
 - splitting fct
 - initial condition
 - k_t -cutoff in cascade
 - applying consistency constraint
- effect from length of evolution
fact. scale



- $\Delta\phi$ is sensitive to shape of k_t distribution
- different initial conditions show similar behavior

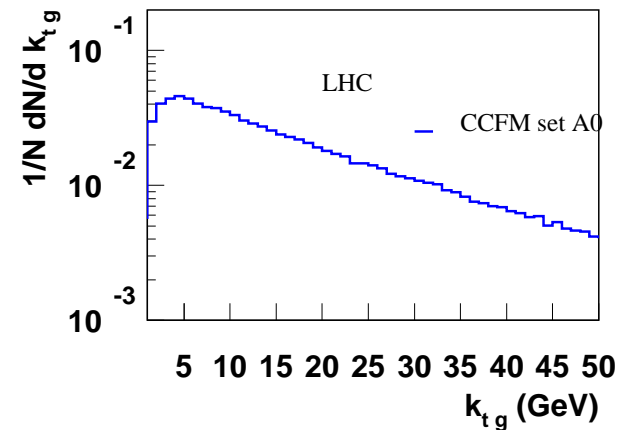
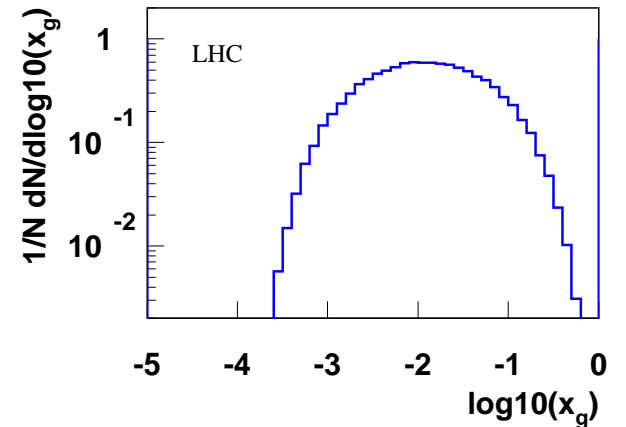
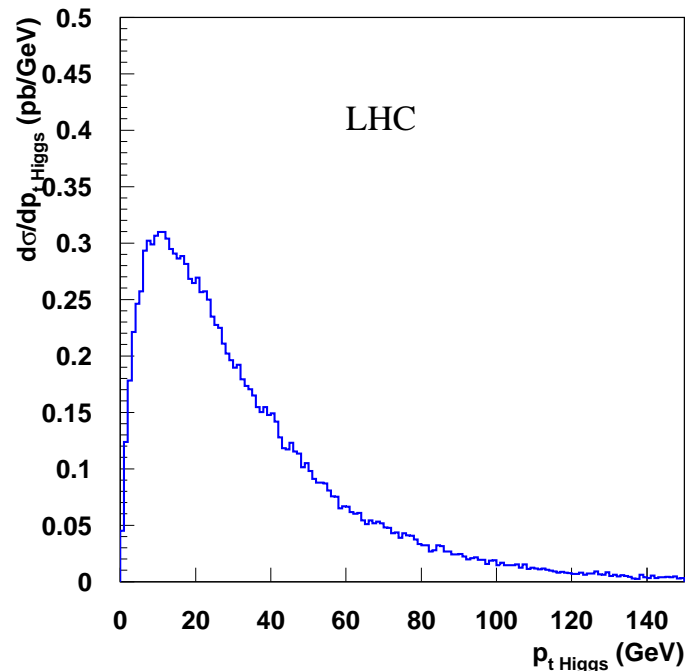
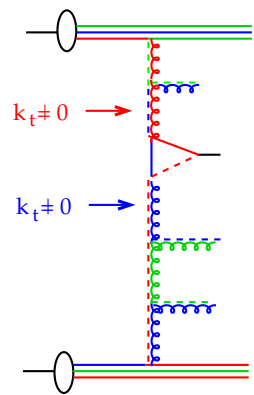
$b\bar{b}$ $\Delta\phi$ distribution



- no effect from changing:
 - splitting fct
 - initial condition
 - k_t -cutoff in cascade
 - applying consistency constraint
- effect from length of evolution fact. scale

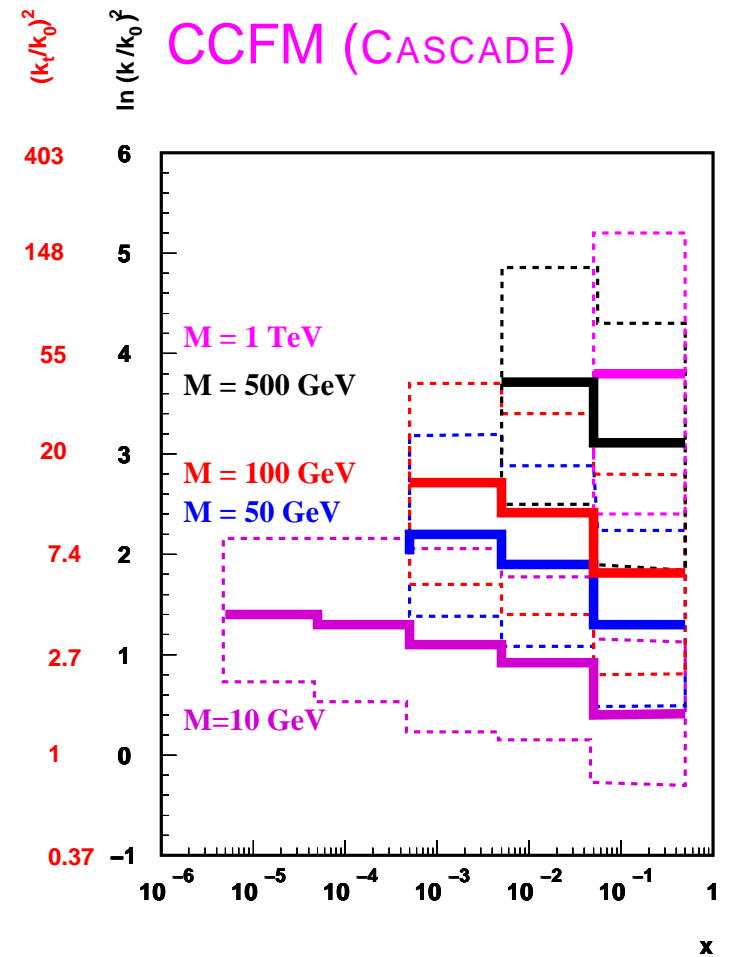
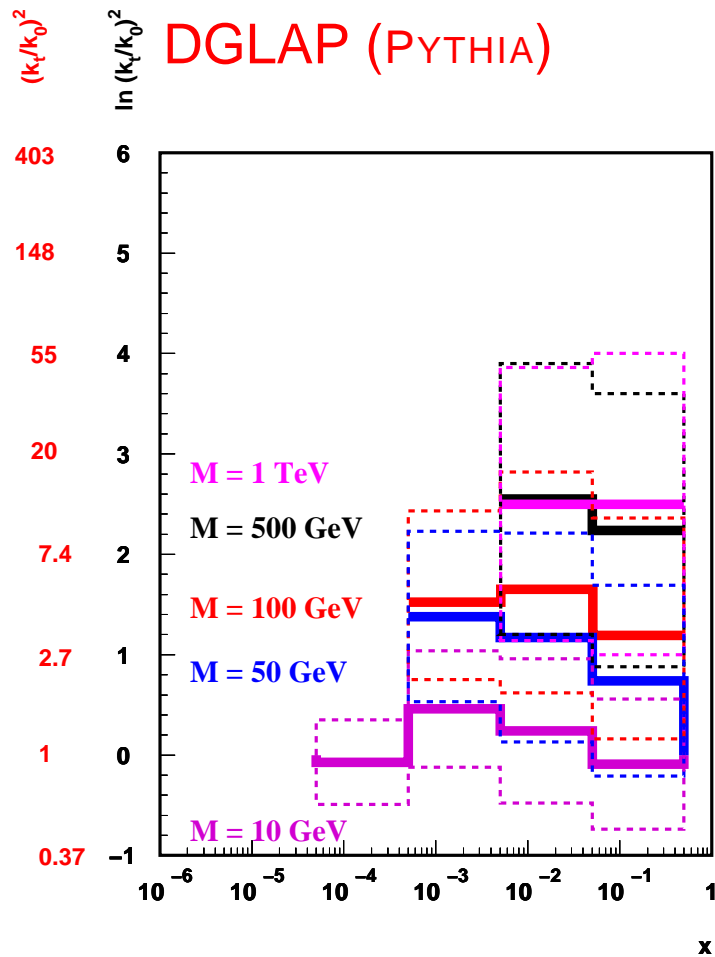
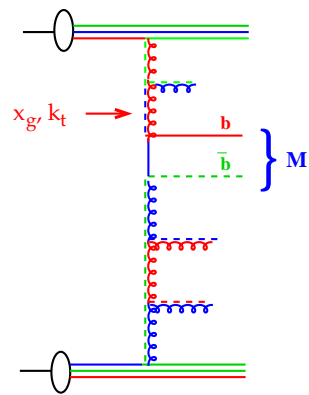
- $\Delta\phi$ is sensitive to shape of k_t distribution
- different initial conditions show similar behavior
- $\Delta\phi$ is sensitive to large k_t

Higgs production at LHC



- sensitive to $0.001 < x_g < 0.1$ and $k_t \sim 2 - 10$ GeV
- similar k_t range as in heavy quark prod at HERA and Tevatron
- **BUT** at very different factorisation scale $\mu_f \sim m_{higgs} !!!$

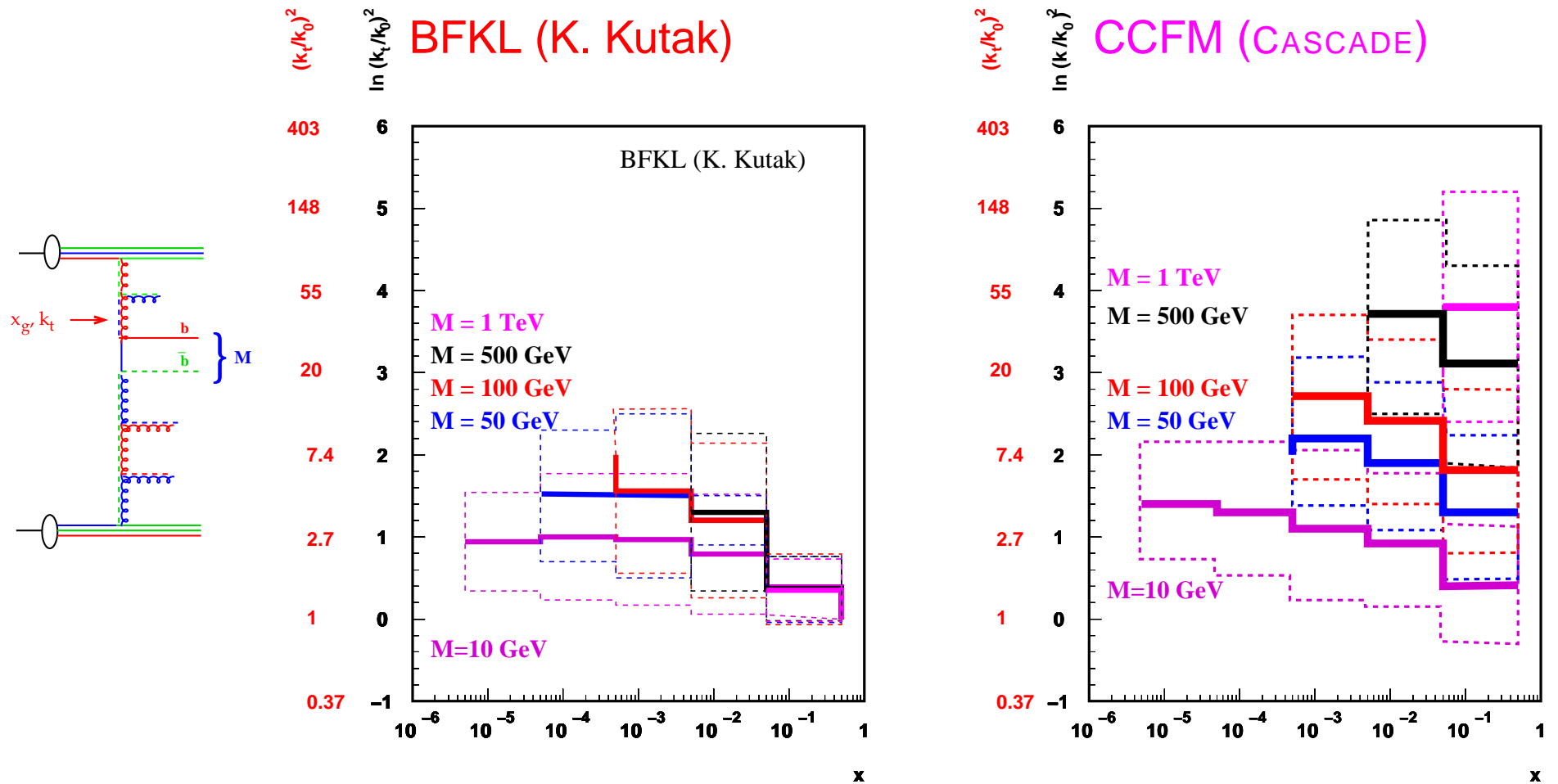
Dependence of $\langle k_t \rangle$: DGLAP vrs CCFM



DGLAP has smaller $\langle k_t \rangle$'s than CCFM !!!!

☞ still above 1 GeV even at small x ... saturation still relevant ?

Dependence of $\langle k_t \rangle$: BFKL vrs CCFM



BFKL with consistency constraint... !!!! \rightarrow at low x similar to CCFM
 BUT differences at larger M

Conclusions

- mapping of $k_t - x_g$ plane:
 - F_2 : concentrated at small $k_t < 4$ GeV $x_g \gtrsim 0.0001$
 - F_2^c : contribution from $k_t > 2$ GeV and $x_g \gtrsim 0.001$
 - charm photoprod at HERA: test $k_t \sim 1$ GeV and $k_t \sim 8$ GeV at same $x_g \sim 0.01$
 - charm at Tevatron: test $k_t \sim 1 - 3$ GeV at $0.001 < x_g < 0.01$
 - $\Delta\phi$ with bottom at Tevatron: test $k_t \sim 1 - 20$ GeV at $0.005 < x_g < 0.05$
- Need to understand better k_t spectrum of un-integrated gluon ...
- NEXT: combined fit to hadronic final state data from HERA & Tevatron

challenge to describe full range in x_g , k_t and μ_f