

# Challenges for MSSM Higgs Searches with CP Violation

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# CP Violation in the MSSM

- In low energy SUSY, there are **extra CP-violating phases beyond the CKM ones**, associated with complex SUSY breaking parameters
- One of the most important consequences of CP-violation is its possible impact on the **explanation of the matter-antimatter asymmetry**. (see C. Wagner's talk)

**Electroweak baryogenesis** may be realized even in the simplest SUSY extension of the SM, but demands **new sources of CP-violation associated with the third generation sector and/or the gaugino-Higgsino sector**.

- These **CP-violating phases** may induce effects on observables such as new contributions to the e.d.m. of the electron and the neutron.  
**However, effects on observables are small in large regions of parameter space**
- In the Higgs sector at tree-level, all CP-violating phases, if present, may be absorbed into a redefinition of the fields.
- **CP-violation in the Higgs sector appears at the loop-level**, associated with third generation scalars and/or the gaugino/Higgsino sector, **but can still have important consequences for Higgs physics**

# MSSM Higgs sector at Tree-Level

$H_1, H_2$  doublets  $\implies$  2 CP-even Higgs  $h, H$    1 CP-odd state  $A$    2 charged

Higgs masses and couplings given in terms of two parameters:

$$m_A \text{ and } \tan \beta \equiv v_2/v_1 \quad \text{mixing angle } \alpha \implies \cos^2(\beta - \alpha) = \frac{m_h^2 (m_Z^2 - m_h^2)}{m_A^2 (m_H^2 - m_h^2)}$$

Couplings to gauge bosons and fermions (norm. to SM)

$$hZZ, hWW, ZHA, WH^\pm H \quad \longrightarrow \sin(\beta - \alpha)$$

$$HZZ, HWW, ZhA, WH^\pm h \quad \longrightarrow \cos(\beta - \alpha)$$

$$(h, H, A) \quad u\bar{u} \quad \longrightarrow \cos \alpha / \sin \beta, \quad \sin \alpha / \sin \beta, \quad 1 / \tan \beta$$

$$(h, H, A) \quad d\bar{d}/l^+l^- \quad \longrightarrow -\sin \alpha / \cos \beta, \quad \cos \alpha / \cos \beta, \quad \tan \beta$$

If  $m_A \gg M_Z \rightarrow$  decoupling limit

- $\cos(\beta - \alpha) = 0$    up to correc.  $\mathcal{O}(m_Z^2/m_A^2)$

- lightest Higgs has SM-like couplings and mass  $m_h^2 \simeq m_Z^2 \cos^2 2\beta$

- other Higgs bosons: heavy and roughly degenerate

$$m_A \simeq m_H \simeq m_H^\pm \quad \text{up to correc. } \mathcal{O}(m_Z^2/m_A^2)$$

# CP violation in the Higgs Sector

- at tree level  $\implies$  MSSM Higgs potential invariant under CP
  - **After radiative corrections:** CP violation induced through loop effects via 3. generation sfermion and gaugino mass parameters
- Many possible relevant phases to Higgs sector
- $m_{\tilde{g}}$  (one phase if Univ. gaugino masses)      $A_f$     $\mu$    and    $m_{12}^2$

Due to U(1) symm. of the conformal inv. sector:

$\rightarrow$  one can redefine fields and absorb two phases

rephasing inv. combinations

if  $\text{Im}((m_{12}^2)^* A_f \mu) \neq 0$    and/or    $\text{Im}((m_{12}^2)^* m_{\tilde{g}} \mu) \neq 0$

$\implies$  CP violating effects will be present in the MSSM

in practice, take  $m_{12}^2$  and  $\mu$  real and leave phases in  $A_f$  and  $m_{\tilde{g}}$



# Higgs Potential → Quantum Corrections

Minimization should be performed with respect to real and imaginary parts of Higgs fluctuations

$$H_1^0 = \phi_1 + iA_1 \quad H_2^0 = \phi_2 + iA_2$$

Performing a rotation:  $A_1, A_2 \Rightarrow A, G^0$  (Goldstone)

Main effect of CP-Violation is the mixing of the three neutral Higgs bosons

$$\begin{pmatrix} A \\ \Phi_1 \\ \Phi_2 \end{pmatrix} = O \begin{pmatrix} H_1 \\ H_2 \\ H_3 \end{pmatrix}$$

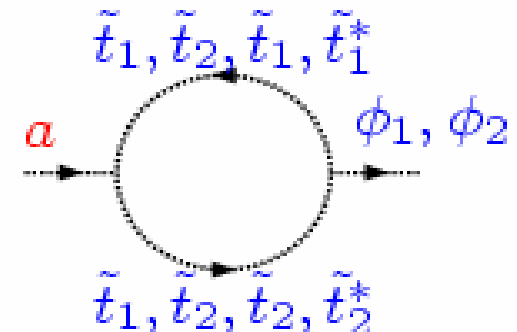
In the base  $(A, \Phi_1, \Phi_2)$

$$M_N^2 = \begin{bmatrix} \mathbf{m}_A^2 & (\mathbf{M}_{SP}^2)^T \\ \mathbf{M}_{SP}^2 & \mathbf{M}_{SS}^2 \end{bmatrix}$$

$M_{SS}^2$  is similar to the mass matrix in the CP conserving case, and  $M_A^2$  is the mass of the would-be CP-odd Higgs.

$M_{SP}^2$  gives the mixing between would-be CP-odd and CP-even states, predominantly governed by stop induced loop effects

$$\mathbf{M}_{SP}^2 \propto \frac{\mathbf{m}_t^4}{16\pi^2 v^2} \text{Im} \left( \frac{\mu \mathbf{A}_t}{\mathbf{M}_S^2} \right)$$



Glino phase relevant at two-loop level. Gluino effects may be enhanced for large tan beta

# Comments on Higgs Boson Mixing

- $m_A^2$  no longer a physical parameter, but the **charged Higgs mass  $M_{H^\pm}$**  can be used as a physical parameter, together with  **$M_S$ ,  $|\mu|$ ,  $|A_t|$ ,  $\arg(A_t)$  and  $\arg(M_{\tilde{g}})$**
- Elements of matrix  $O$  are similar to  **$\cos\alpha$  and  $\sin\alpha$**  in the CP-conserving case. But third row and column are zero in the non-diagonal elements in such a case.
- **Three neutral Higgs bosons can now couple to the vector bosons in a way similar to the SM Higgs.**
- Similar to the decoupling limit in the CP-conserving case, for large values of the charged Higgs mass, light Higgs boson with Standard Model properties.

# Interaction Lagrangian of W,Z bosons with mixtures of CP even and CP odd Higgs bosons



$$g_{H_i V V} = \cos \beta \mathcal{O}_{1i} + \sin \beta \mathcal{O}_{2i}$$

$$g_{H_i H_j Z} = \mathcal{O}_{3i} (\cos \beta \mathcal{O}_{2j} - \sin \beta \mathcal{O}_{1j}) - \mathcal{O}_{3j} (\cos \beta \mathcal{O}_{2i} - \sin \beta \mathcal{O}_{1i})$$

$$g_{H_i H - W^+} = \cos \beta \mathcal{O}_{2i} - \sin \beta \mathcal{O}_{1i} + i \mathcal{O}_{3i} \quad (V = W, Z)$$

$\mathcal{O}_{ij} \longrightarrow$  analogous to  $\sin(\beta - \alpha)$  &  $\cos(\beta - \alpha)$

$\rightarrow$  All couplings as a function of two:  $g_{H_k V V} = \mathcal{E}_{ijk} g_{H_i H_j Z}$

and sum rules:  $\sum_{i=1}^3 g_{H_i Z Z}^2 = 1 \quad \sum_{i=1}^3 g_{H_i Z Z}^2 m_{H_i}^2 = m_{H_1}^{2, \max} \lesssim 135 \text{ GeV}$

(equiv. to CP-conserv. case)

upper bound remains the same

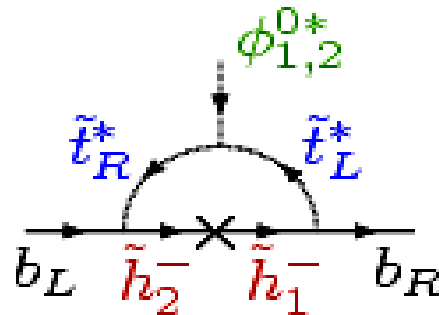
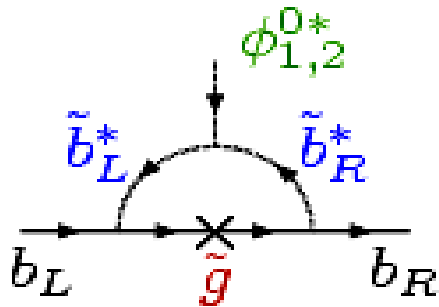
Decoupling limit:  $m_{H^+} \gg M_Z$

- Effective mixing between the lightest Higgs and the heavy ones is zero
- $\rightarrow H_1$  is SM-like
- Mixing in the heavy sector still relevant !

$$\rightarrow \begin{pmatrix} m_A^2 & \Delta \\ \Delta & \Delta' + m_A^2 \end{pmatrix} \quad \text{w/} \quad \Delta \sim \mathcal{O}(\Delta') \ll m_A^2$$

# Yukawa Couplings: CP violating vertex effects

$$-\mathcal{L}_{\phi^0 \bar{b} b}^{\text{eff}} = (h_b + \delta h_b) \phi_1^{0*} \bar{b}_R b_L + \Delta h_b \phi_2^{0*} \bar{b}_R b_L + \text{h.c.}$$



coupling  $\Delta h_b$  generated by SUSY breaking effects

$$\frac{\delta h_b}{h_b} \sim -\frac{2\alpha_s}{3\pi} \frac{m_{\tilde{g}}^* A_b}{\max(Q_b^2, |m_{\tilde{g}}|^2)} - \frac{|h_t|^2}{16\pi^2} \frac{|\mu|^2}{\max(Q_t^2, |\mu|^2)}$$

$$\frac{\Delta h_b}{h_b} \sim \frac{2\alpha_s}{3\pi} \frac{m_{\tilde{g}}^* \mu^*}{\max(Q_b^2, |m_{\tilde{g}}|^2)} + \frac{|h_t|^2}{16\pi^2} \frac{A_t^* \mu^*}{\max(Q_t^2, |\mu|^2)}$$

- The one loop effects to the Yukawa couplings introduce CP-violating effects which are independent of the Higgs mixing

the phase of the superfield  $b_R$  is real and positive:

$$h_b = \frac{g_w m_b}{\sqrt{2} M_W \cos \beta [1 + \delta h_b/h_b + (\Delta h_b/h_b) \tan \beta]}$$



# Higgs boson-quark Lagrangian

- taking into account both CP-violating self-energy and vertex effects (similar vertex effects in the up quark sector, but no  $\tan \beta$  enhancement)

$$L_{\text{Hff}} = -\sum_{i=1}^3 H_i \left[ (g_W m_d / 2M_W) \bar{d} (g_{H_i,dd}^S + g_{H_i,dd}^P \gamma_5) d \right. \\ \left. + (g_W m_u / 2M_W) \bar{u} (g_{H_i,uu}^S + g_{H_i,uu}^P \gamma_5) u \right]$$

with:

$$g_{H_i,dd}^S = \frac{1}{h_b + \delta h_b + \Delta h_b \tan \beta} \left\{ \text{Re}(h_b + \delta h_b) \frac{O_{1i}}{\cos \beta} + \text{Re}(\Delta h_b) \frac{O_{2i}}{\cos \beta} \right. \\ \left. - [\text{Im}(h_b + \delta h_b) \tan \beta - \text{Im}(\Delta h_b)] O_{i3} \right\}$$

$$g_{H_i,dd}^P = \frac{1}{h_b + \delta h_b + \Delta h_b \tan \beta} \left\{ [\text{Re}(\Delta h_b) - \text{Re}(h_b + \delta h_b) \tan \beta] O_{31} \right. \\ \left. - \text{Im}(h_b + \delta h_b) \frac{O_{1i}}{\cos \beta} - \text{Im}(\Delta h_b) \frac{O_{2i}}{\cos \beta} \right\}$$

- Decoupling limit:  $M_{H^\pm} \gg M_Z$

## CP violation effects in the Higgs-fermion couplings

$$O_{11} \rightarrow \cos \beta \quad O_{21} \rightarrow \sin \beta \quad O_{31} \rightarrow 0$$

hence:

- $H_1 bb$  and  $H_1 uu$  pseudoscalar couplings tend to zero while their scalar couplings tend to SM-like

with the bottom mass:

$$h_b = \frac{g_w m_b}{\sqrt{2} M_W \cos \beta [1 + \delta h_b / h_b + (\Delta h_b / h_b) \tan \beta]}$$

- Heaviest Higgs Scalar and Pseudoscalar couplings to up and down quarks do not vanish

→ non decoupling of CP-violating vertex effects as well as self energy ones

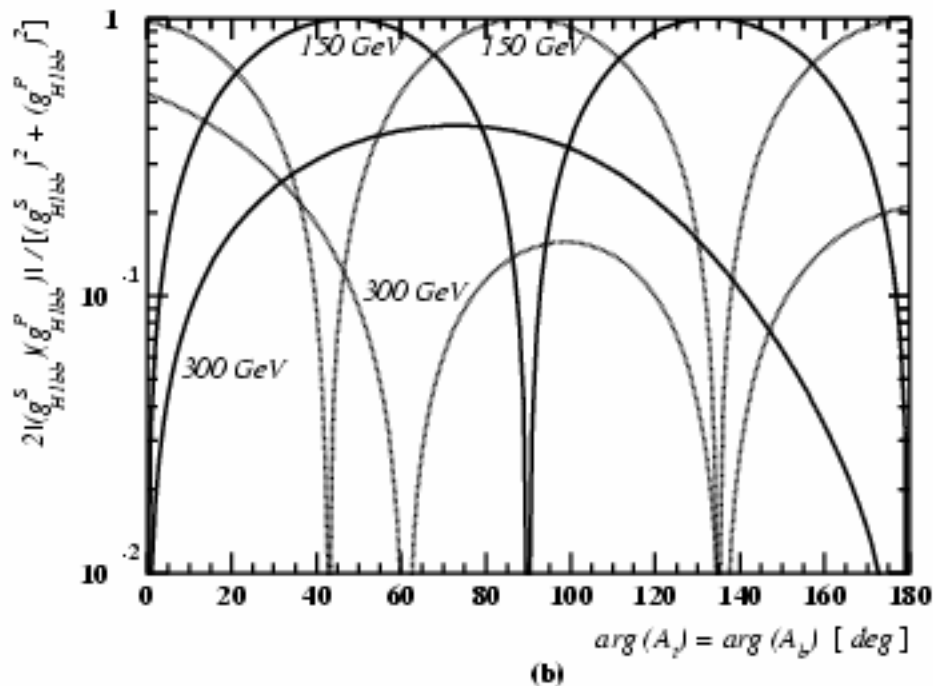
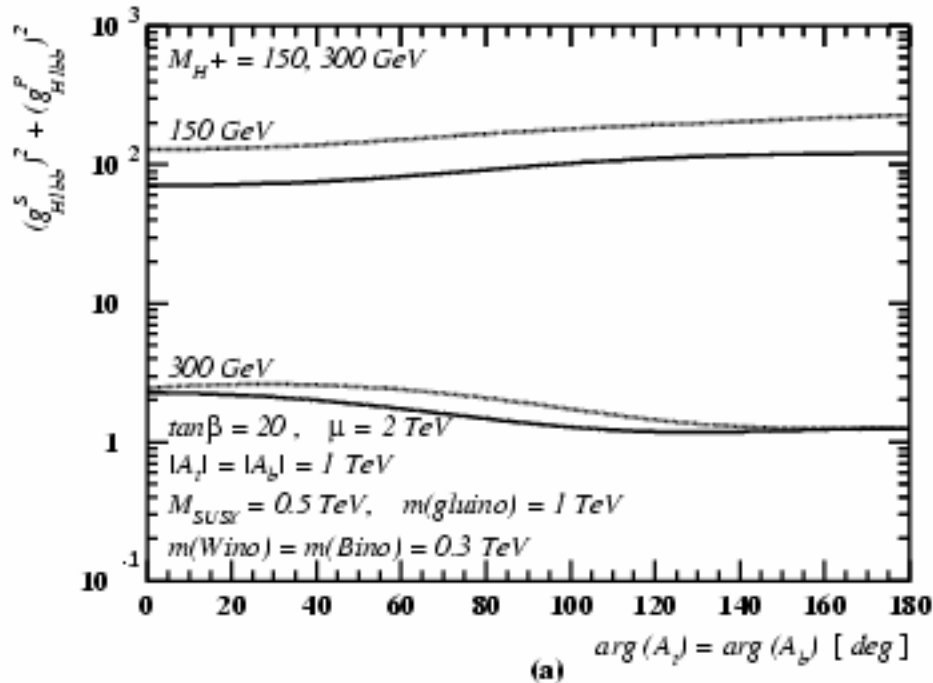
# H<sub>1</sub>bb Scalar and Pseudoscalar couplings as a function of phases

- Analyze behaviour in term of CP-even quantities: BR's and CP- odd quantities: Asymmetries

- Effects depend both on the dominant squark sector phases, as well as on the subdominant gaugino phases, affecting the vertex corrections.

- Cases with gluino mass phase zero (solid lines) and 90 degrees (dashed lines) shown in figures: stronger effects of gluino phase for larger tanβ

**CP-Violating phases affect both masses and couplings in relevant ways.**



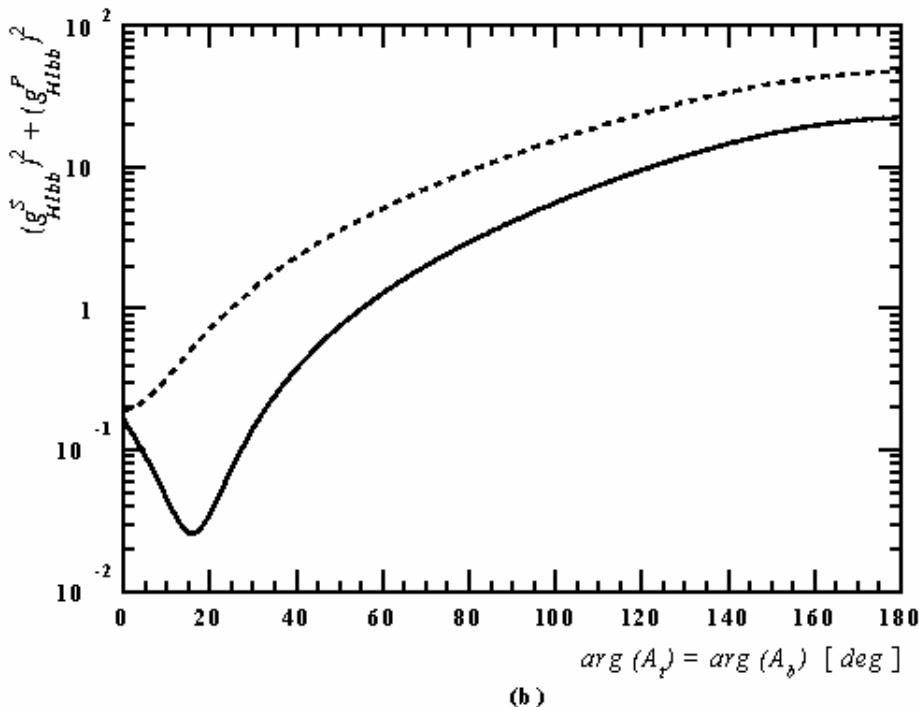
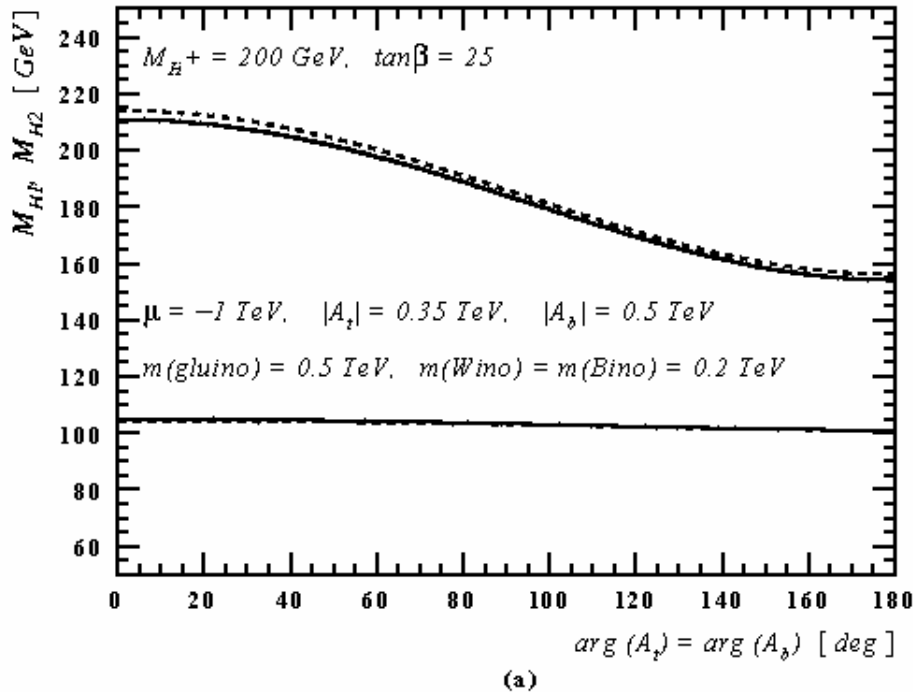
# Strong suppression of $H_1bb$ Coupling depending on the gluino phase

- Suppression of Higgs coupling to  $bb$  for a Higgs with SM-like couplings to vector bosons



Region of parameter space consistent with electroweak Baryogenesis

Searches at LEP excluded a mass up to about 112 GeV in the flavour independent analysis



# CP-Violating Higgs bosons at LEP: challenging scenarios

$$e^+e^- \rightarrow H_i Z \text{ and } e^+e^- \rightarrow H_i H_j$$

CPX Scenario:

$$M_{SUSY} = 0.5, 1 \text{ TeV}$$

$$\mu = 4 M_{SUSY}$$

$$m_{\bar{g}} = 1 \text{ TeV}$$

$$|A_t| = |A_b| = 2 M_{SUSY}$$

• interesting example:

$$\arg(A_{t,b}) = 90^\circ, \arg(m_{\bar{g}}) = 90^\circ$$

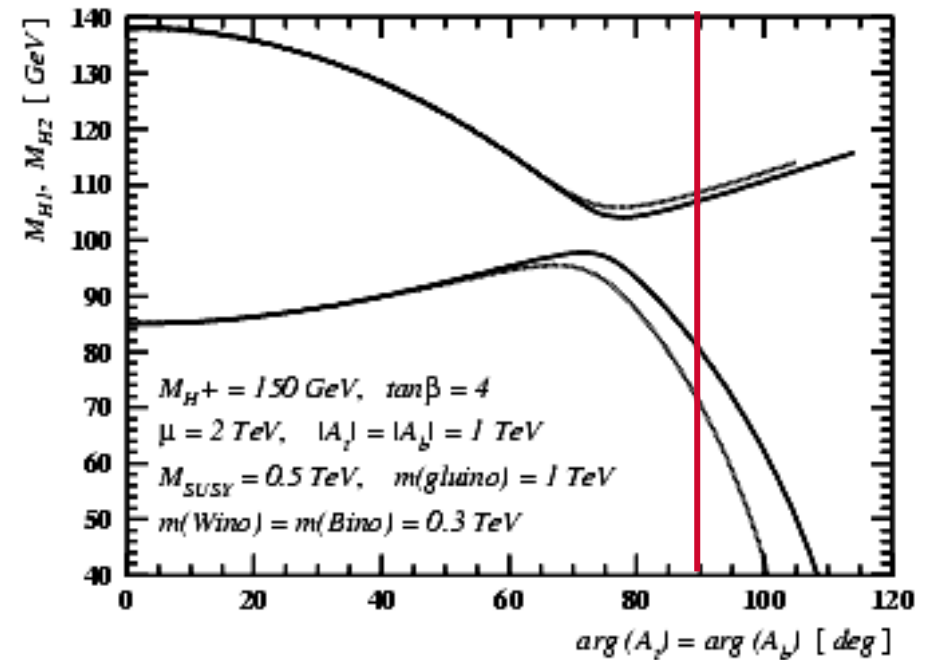
$$m_{H^\pm} \simeq 150 \text{ GeV}$$

$$\longrightarrow m_{H_1} \simeq 70 \text{ GeV}$$

$$m_{H_2} \simeq 105 \text{ GeV}$$

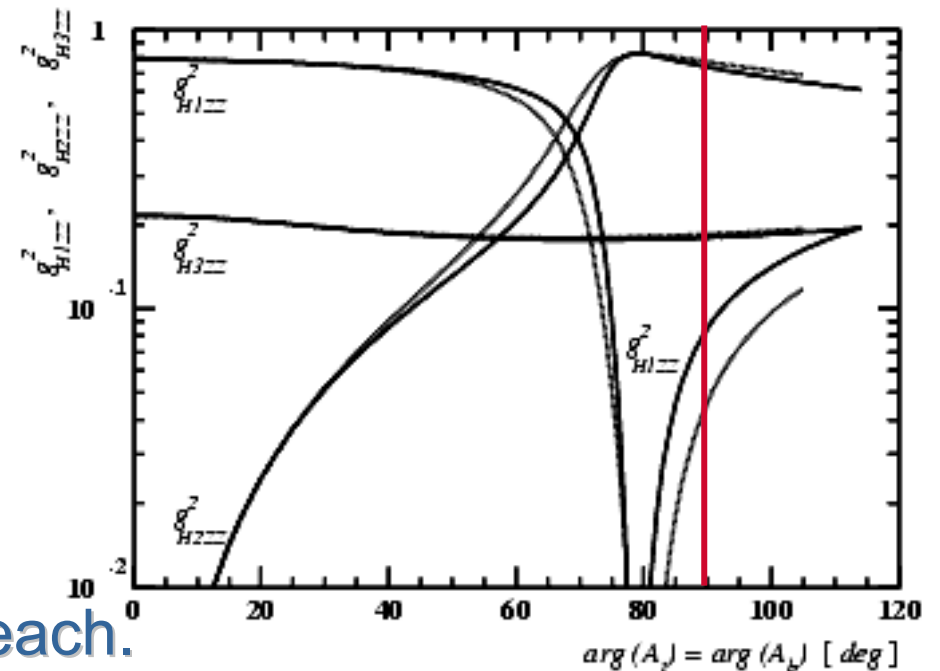
- $M_{H_1}$  very small but  $g_{H_1 Z Z} \rightarrow 0$ ,
- $M_{H_1} + M_{H_2}$  too heavy for the given value of the  $g_{H_1 H_2 Z}$  coupling
- $M_{H_2}$  just at the edge of LEP reach

$H_1$  decouples from the Z and  $H_2$  and  $H_3$  may be out of kinematic reach.



(a)

M.C., Ellis, Pilaftsis, Wagner



(b)

• Another interesting example within the CPX Scenario:

- (1)  $m_{H^\pm} = 160 \text{ GeV}$   $\tan\beta = 4$
- (2)  $m_{H^\pm} = 150 \text{ GeV}$   $\tan\beta = 5$
- (3)  $m_{H^\pm} = 140 \text{ GeV}$   $\tan\beta = 6$

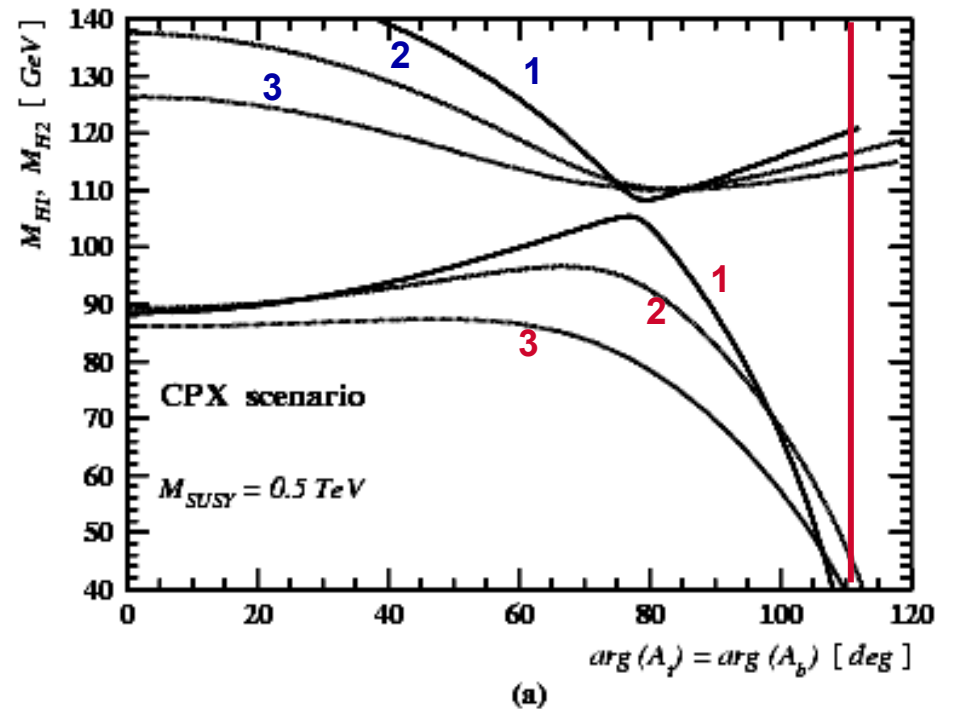
$\arg(A_{t,b}) = 110^\circ$  and case (3)

$\Rightarrow m_{H_2} = 112 \text{ GeV}$  and  $m_{H_1} = 40 \text{ GeV}$

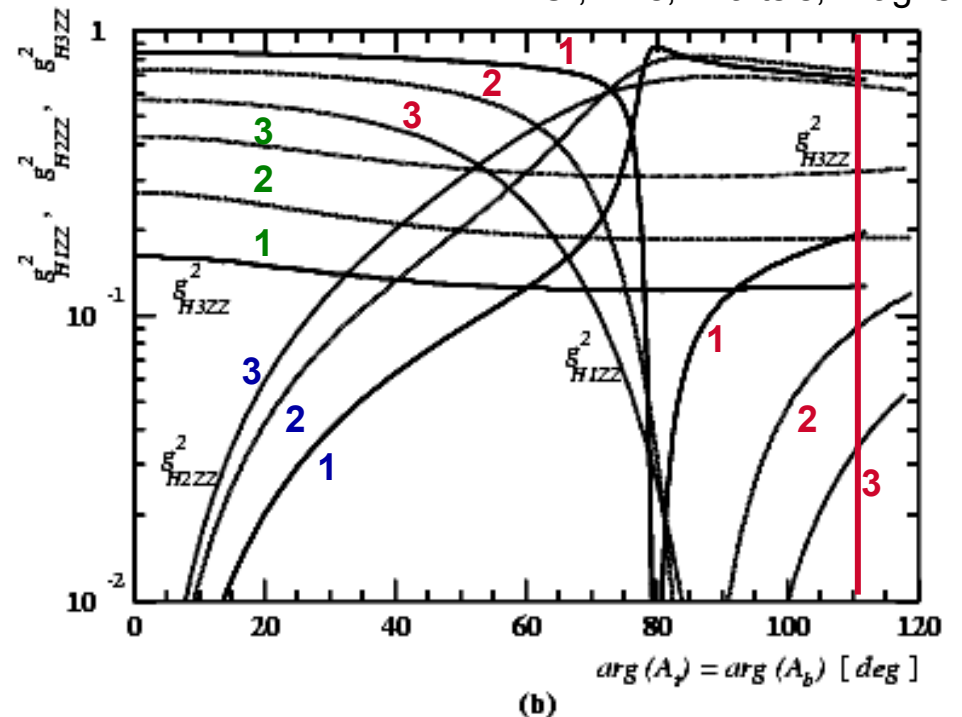
$g_{H_1ZZ}$  too small to detect  $H_1$

$H_2$  is produced via Higgs - strahlung but, it has sizeable decay rate into  $H_1H_1$

New search mode opens up:

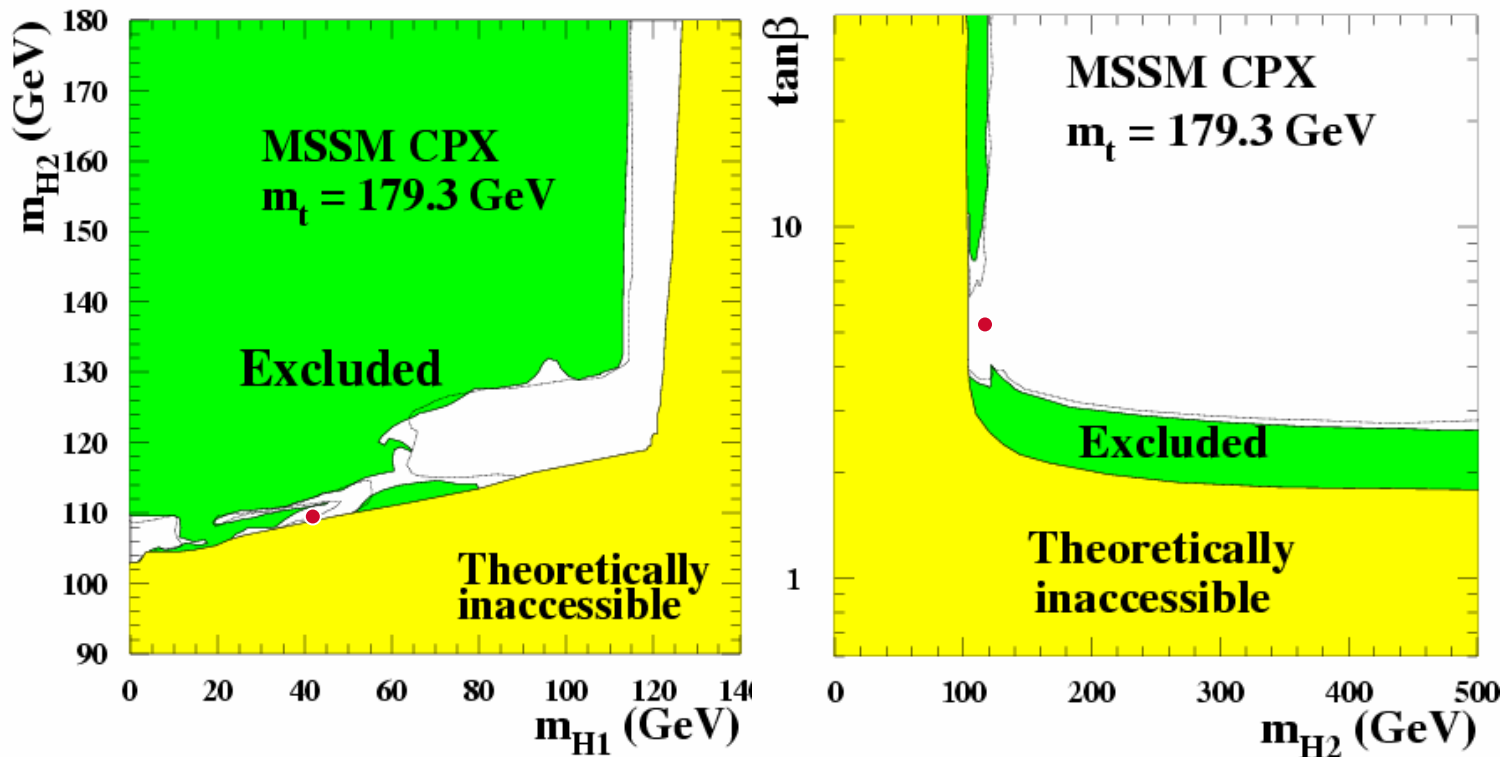


M.C., Ellis, Pilaftsis, Wagner



# CPX scenario: no lower bound on $M_{H_1}$ from LEP!

- $H_1$  decouples from the Z and  $H_2$  and  $H_3$  may be out of kinematic reach.
- or reduced couplings of  $H_1$  to Z and extended regions were  $H_2$  decays  $H_1H_1$  and the  $H_1$ 's decay into  $b$ 's



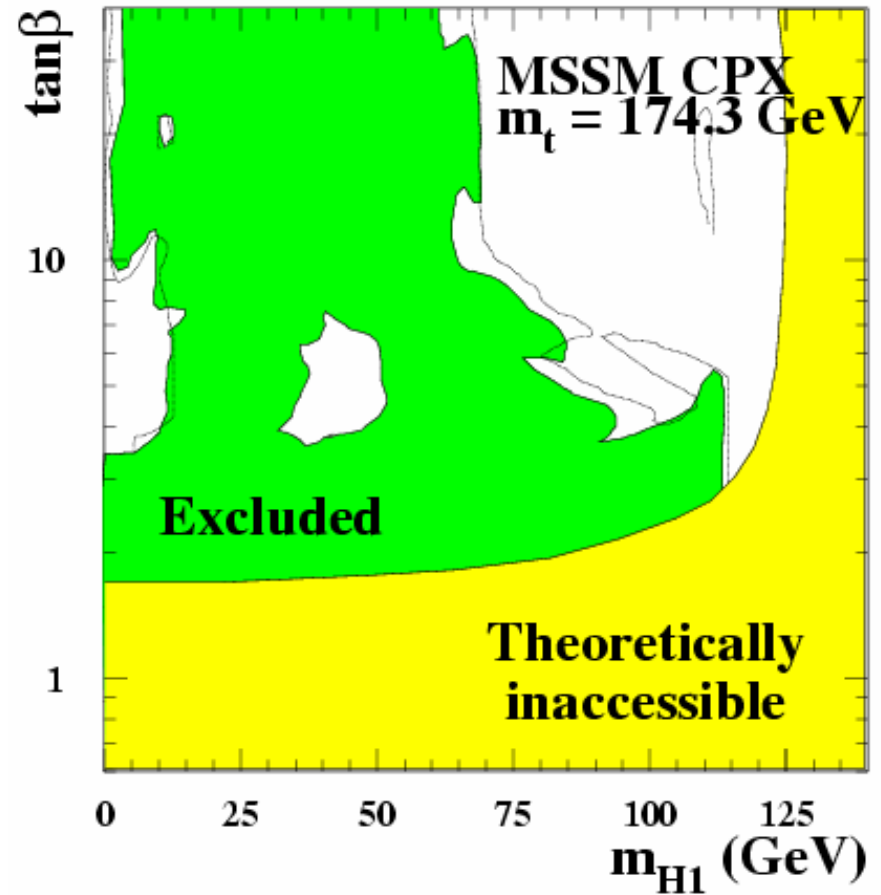
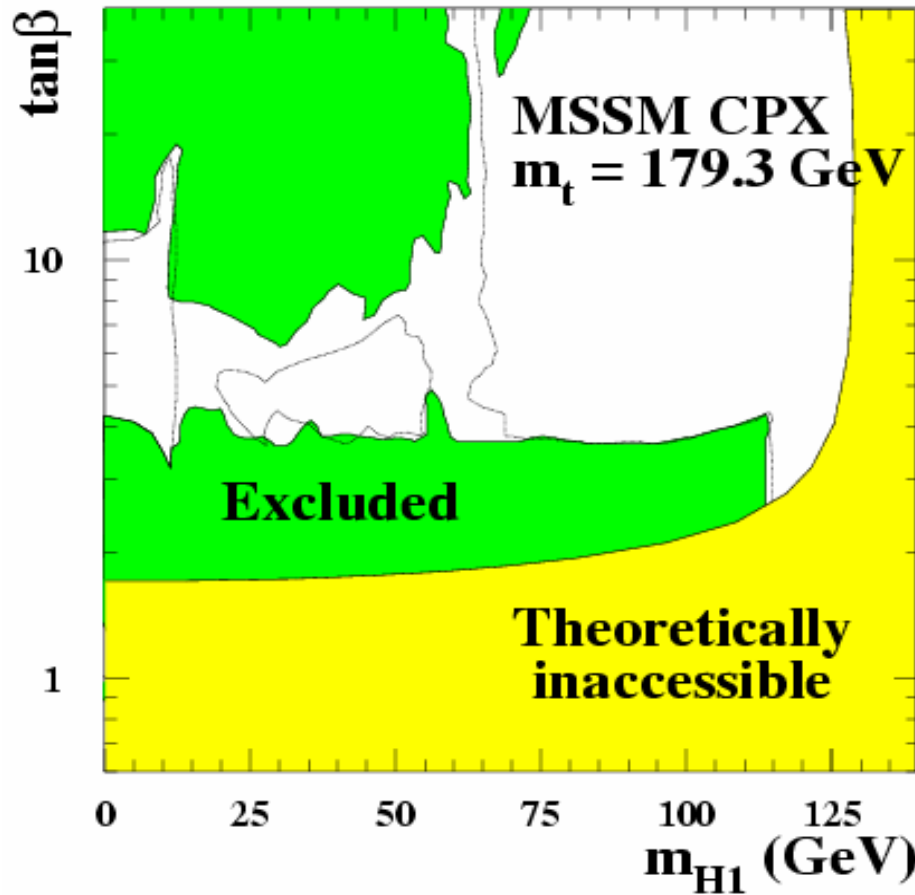
Including  
 $ZH_2$  and  $H_1H_2$   
 with  
 $H_2 \rightarrow H_1H_1 \rightarrow b\bar{b}b\bar{b}$   
 in the analyses

$m_{H_2} < 130$  GeV  $\rightarrow$  major role of CP-violating effects

Example:  $m_{H_1} = 40-45$  GeV,  $m_{H_2} = 110$  GeV,  $\tan\beta = 4-7$  Not excluded

No Universal lower limit on  $m_{H_1}$  but  $\tan\beta > 2.6-2.9$  (mt dep.)

# Impact of the top quark mass on the results



main effect for  $\tan\beta = 4-10$  is due to opening of  $H_1Z$ ,  $H_2Z$  channels as well as  $H_1H_2$



# CP-Violating Higgs bosons at the Tevatron

Example:

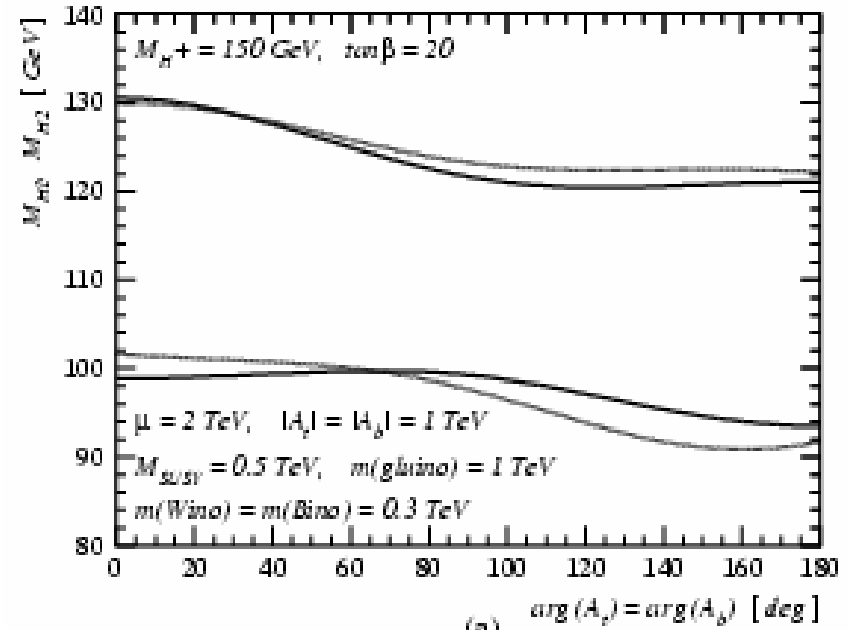
- $M_{H1}$  about 90 GeV but out of the reach of LEP.
- All other channels kinematically inaccessible

- $M_{H1}$  also hopeless at the Tevatron due to reduced  $W/Z$   $H1$  coupling

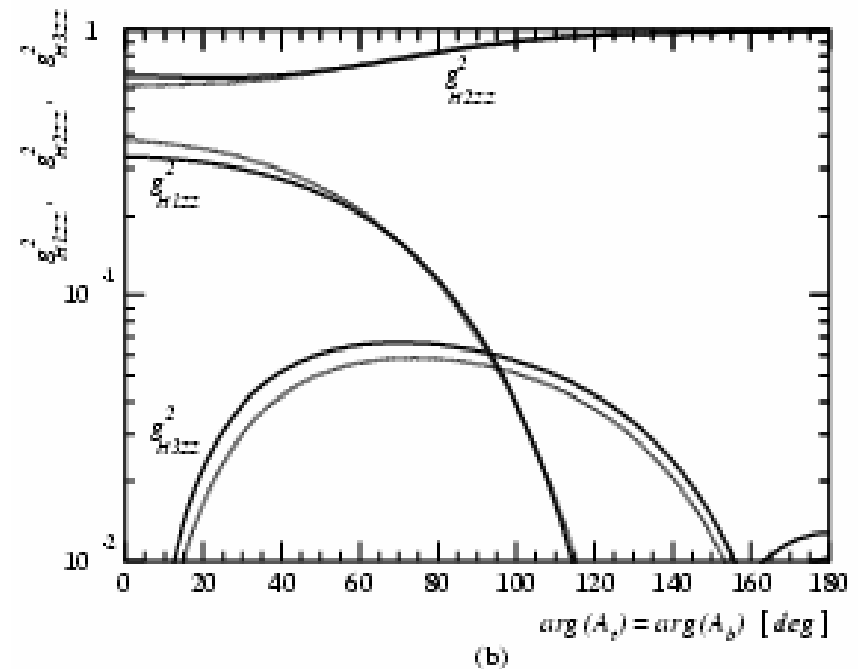
- $H1$  and  $H2$  masses have little variation with phase of  $A_t$ , but couplings to gauge bosons vary importantly

The Tevatron has a chance of having a first glance at  $H2$ .

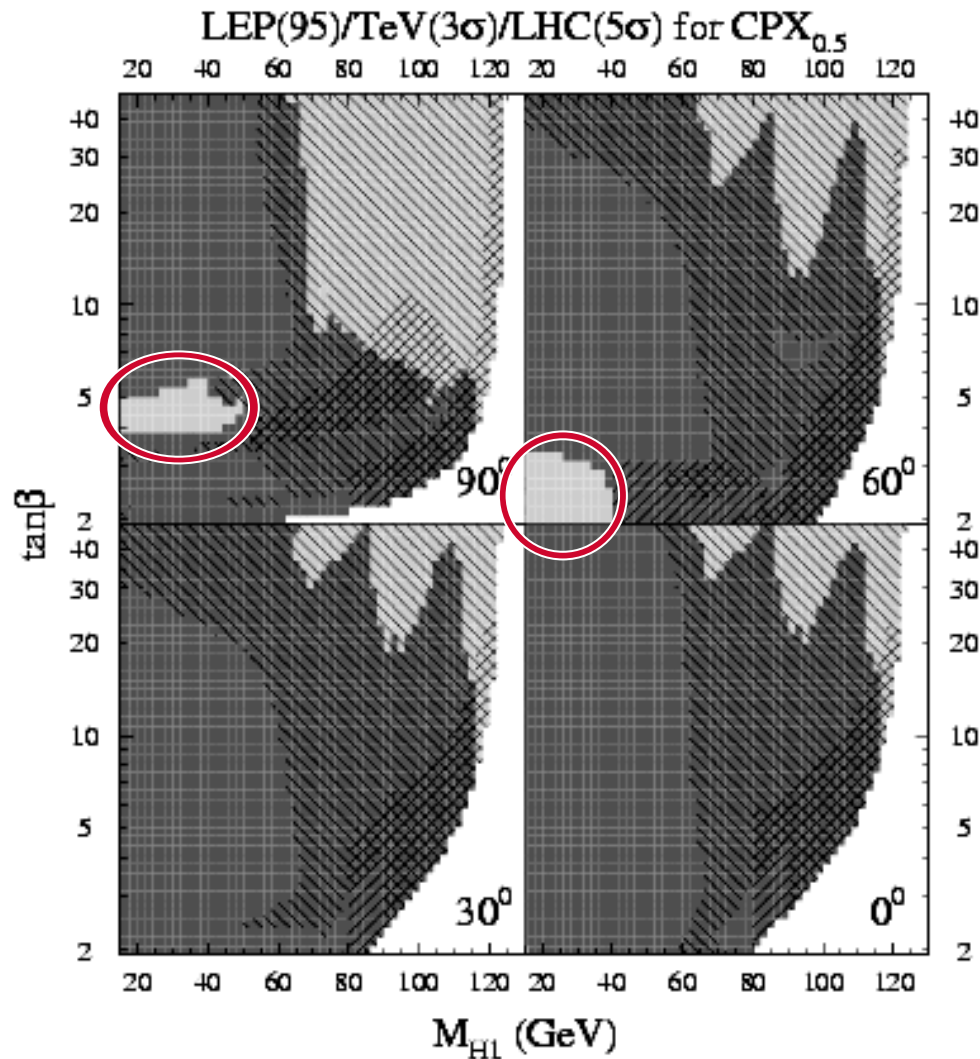
Most crucial however, explore similar regions but for  $M_{H_2} \geq 2M_{H_1}$



M.C., Ellis, Pilaftsis, Wagner



Approximate LEP exclusion and Tevatron ( $3\sigma / 5 \text{ fb}^{-1}$ ) and LHC ( $5\sigma$  discovery) limits in the  $m_{H_1} - \tan\beta$  plane for CPX scenarios with different phases ( $\arg M_{\bar{g}} = \arg(A_{t,b})$ )



$45^\circ$  lines  $\rightarrow$  Tevatron:  $W/Z H_i (\rightarrow b\bar{b})$

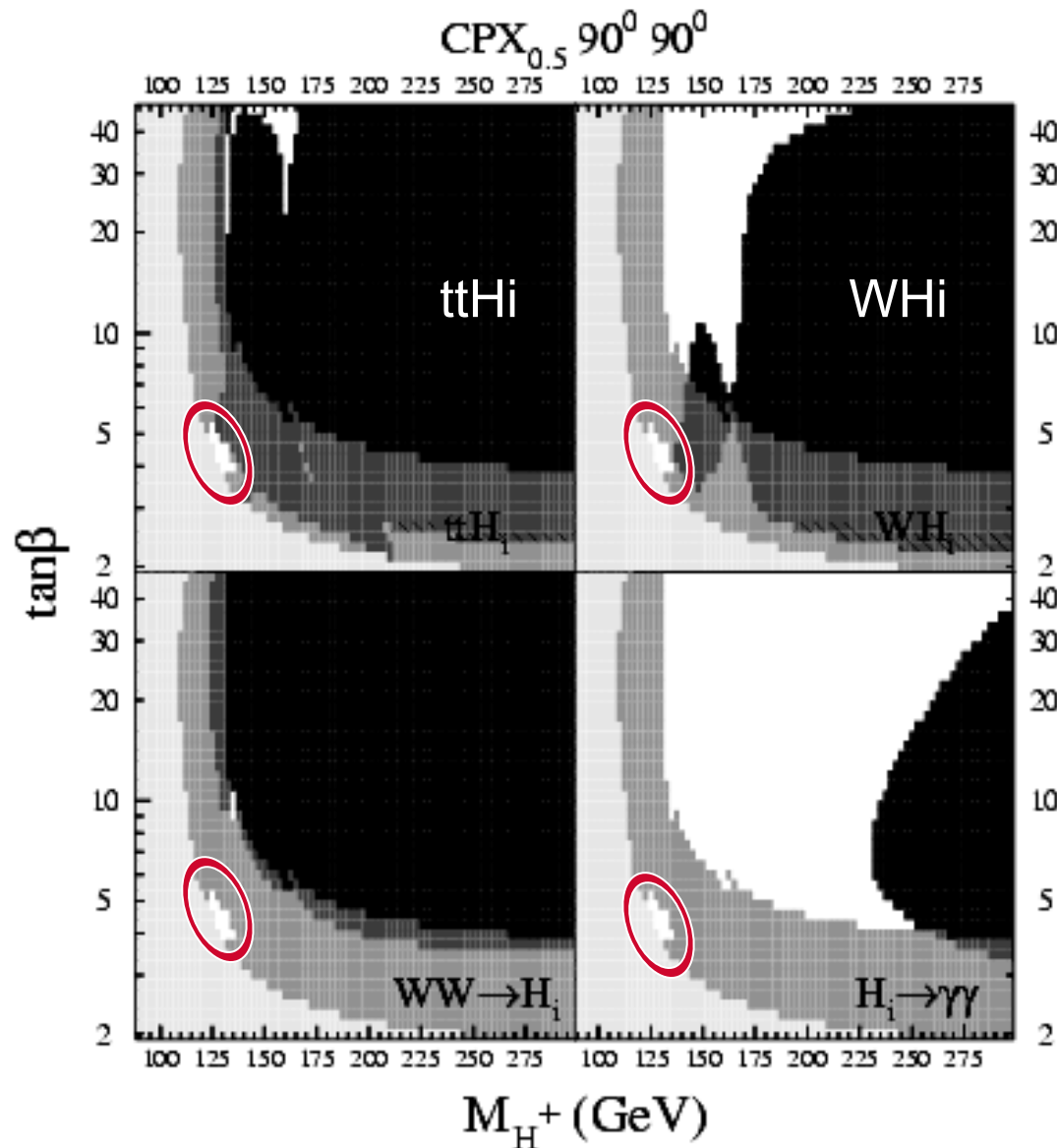
$135^\circ$  lines  $\rightarrow$  LHC:  $gg \rightarrow H_i \rightarrow \gamma\gamma$  ( $100 \text{ fb}^{-1}$ )  
 $t\bar{t} H_i (\rightarrow b\bar{b})$  ( $100 \text{ fb}^{-1}$ )

$WW/ZZ H_i (\rightarrow \tau^+\tau^-)$  ( $30 \text{ fb}^{-1}$ )

grey  $\rightarrow$  LEP exclusion. ( $m_t = 174.3 \text{ GeV}$ )

low  $\tan\beta$  and low  $m_{H_i}$  region  
 remains uncovered in the  
 absence of the  
 $H_2 \rightarrow H_1 H_1$  analysis

Similar plot as above but showing different channels separately  
and in the  $\tan\beta - m_{H^\pm}$  plane



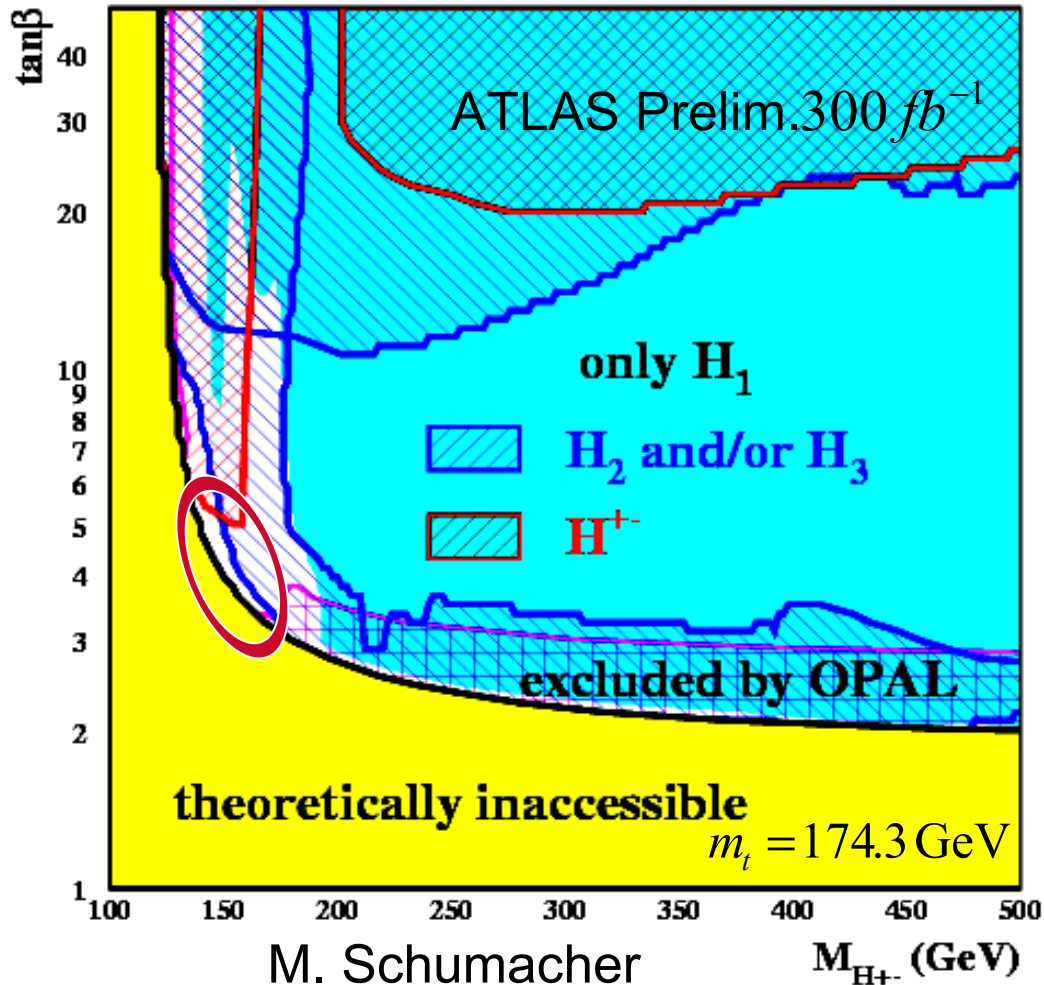
■ The Tevatron could see a  $3\sigma$  hint with  $5 \text{ fb}^{-1}$  in a sizeable area of parameter space

■ If  $\arg(M\tilde{g}) = 0$  instead, stronger suppression of  $BR(H_{1,2}) \rightarrow b\bar{b}$  and both upper channels less competitive

■ vector boson fusion Higgs production with subsequent decay into taus still crucial channel at first years of LHC!

# Can LHC discover the SM-like Higgs in the MSSM with explicit CP violation?

CPX scenario



$m_{H_1} < 70 \text{ GeV}$   
 $m_{H_2} : 105 \text{ to } 120 \text{ GeV}$   
 $m_{H_3} : 140 \text{ to } 180 \text{ GeV}$

- $H_2/H_3$  channels: VBF and  $t\bar{t}H_i$

Present limitations:

VBF only for mass  $> 110 \text{ GeV}$   
 No study for  $H_1$  below  $70 \text{ GeV}$

- Encourage the study of  $gg \rightarrow H_2$ ,  $t\bar{t}H_2$ ,  $W/Z H_2$  and  $WW/ZZ H_2$

with subsequent decay  $H_2 \rightarrow H_1 H_1$ , using the extra leptons from  $W/Z$ 's.

Also  $t\bar{t} \rightarrow WbH^\pm b$  with  $H^\pm \rightarrow WH_1 \rightarrow Wb\bar{b}$

# Looking for $H_2 \rightarrow H_1 H_1$

- Standard signatures not sufficient to probe the presence of a SM-like Higgs bosons decaying into lighter Higgs states.
- Lighter states have weak couplings to the weak gauge bosons, but large couplings to third generation down quarks and leptons.
- Possibility of looking for two taus and two bottoms (jets) signatures at LHC in the weak boson fusion production channel of two CP-odd like Higgs bosons. (J. Gunion et al. with 300 fb<sup>-1</sup> at the LHC, NMSSM)
- A detailed experimental simulation should be performed to test this possibility.

# CPsuperH

- Code to compute Higgs spectrum, couplings and decay modes in the presence of CP-violation

Lee, Pilaftsis, M.C., Choi, Drees, Ellis, Lee, Wagner.'03

- CP-conserving case: Set phases to zero. Similar to HDECAY, but with the advantage that charged and neutral sector treated with same rate of accuracy.
- Combines calculation of masses and mixings by M.C., Ellis, Pilaftsis, Wagner. with analysis of decays by Choi, Drees, Hagiwara, Lee and Song.
- Available at

<http://theory.ph.man.ac.uk/~jslee/CPsuperH.html>

# Conclusions

- Low energy supersymmetry has an important impact on Higgs physics.
- It leads to definite predictions to the Higgs boson couplings to fermions and gauge bosons.
- Such couplings, however, are affected by radiative corrections induced by supersymmetric particle loops.
- CP-violation in the Higgs sector is well motivated and should be studied in detail. It affects the searches for Higgs bosons at hadron and lepton colliders in an important way.
- At a minimum, it stresses the relevance of studying non-standard Higgs boson production and decay channels at lepton and hadron colliders.