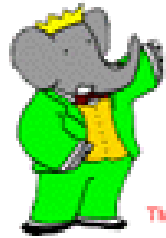


# Lepton Flavour Violation in $\tau$ decays: Status and Perspectives ...



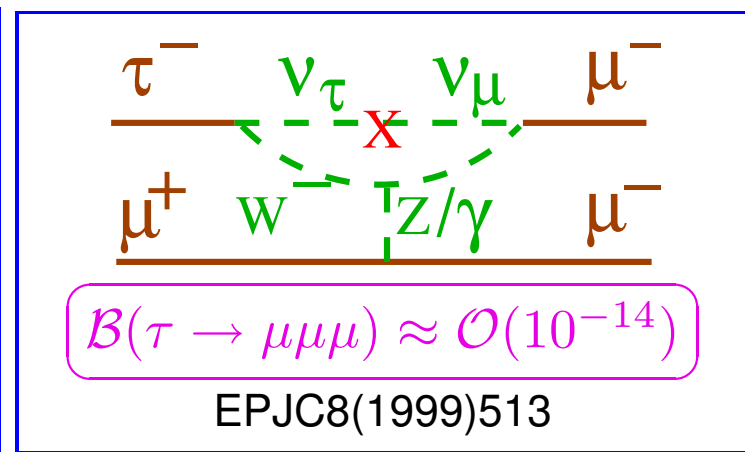
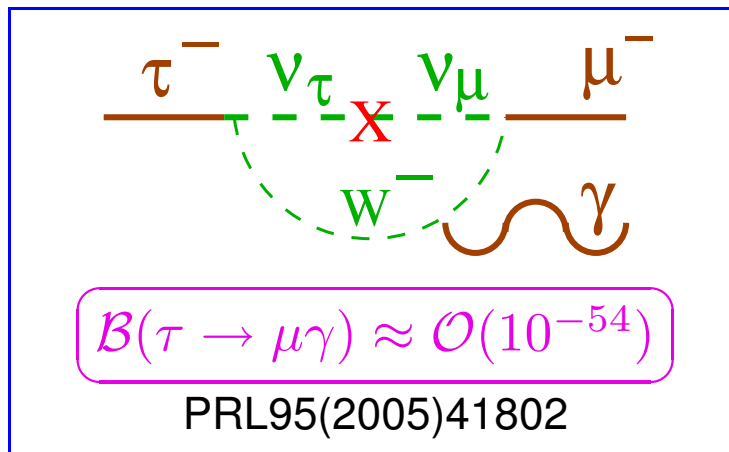
*Swagato Banerjee*



Flavour in the era of the LHC,  
Workshop at CERN (7<sup>th</sup> – 10<sup>th</sup> Nov 2005)

# Introduction

- Lepton flavor violation (LFV)
  - not forbidden by SM gauge symmetry
  - most new models explicitly include LFV vertex
- In SM, LF is conserved for zero degenerate  $\nu$  masses
  - SM extended to include finite  $\nu$  mass and mixing predicts LFV



... many orders below experimental sensitivity!

- Observation for LFV  $\Rightarrow$

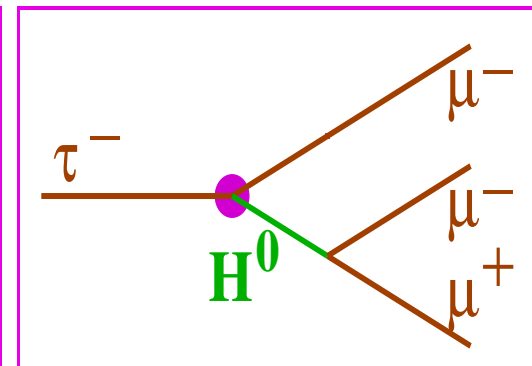
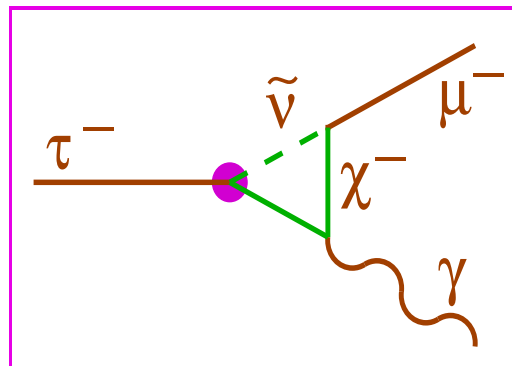
unambiguous signature of new physics

# LFV $\tau$ decays

- Mass dependent couplings enhance tau LFV w.r.t. lighter leptons
- Some models predict LFV upto existing experimental bounds
- Neutrinoless 2 and 3 body  $\tau$  decays have different sensitivity

	$\mathcal{B}(\tau \rightarrow l\gamma)$	$\mathcal{B}(\tau \rightarrow lll)$
mSUGRA+seesaw (EPJC14(2000)319, PRD66(2002)115013)	$10^{-7}$	$10^{-9}$
SUSY SO(10) (NPB649(2003)189, PRD68(2003)033012)	$10^{-8}$	$10^{-10}$
SUSY Higgs (PLB549(2002)159, PLB566(2003)217)	$10^{-10}$	$10^{-7}$
Non-Universal $Z'$ (PLB547(2002)252)	$10^{-9}$	$10^{-8}$
SM+Heavy Majorana $\nu_R$ (PRD66(2002)034008)	$10^{-9}$	$10^{-10}$

Illustrative scenarios ...



# $e^+e^- \rightarrow \tau^+\tau^-$ (clean environment)

Search for LFV  $\tau \rightarrow l\gamma$ ,  $\tau \rightarrow lll$ ,  $\tau \rightarrow lhh'$  decays ( $l = e, \mu$ ;  $h = \pi, K$ )

● Divide  $\tau$ -pair event  $\perp$  to thrust axis (CM frame) in 2 hemispheres

$\tau \rightarrow l\gamma$

**Signal-Side** **Tag-Side**

Backgrounds:

- $\tau \rightarrow e\gamma$  ( $\tau \rightarrow \mu\gamma$ ):
- Radiative Bhabha (di-muon)
- $\tau^+\tau^-\gamma$  ( $\tau \rightarrow l\nu\bar{\nu}$ )
- $q\bar{q}$  ( $\gamma$ )

$\tau \rightarrow lll$  ( $\tau \rightarrow lhh'$ )

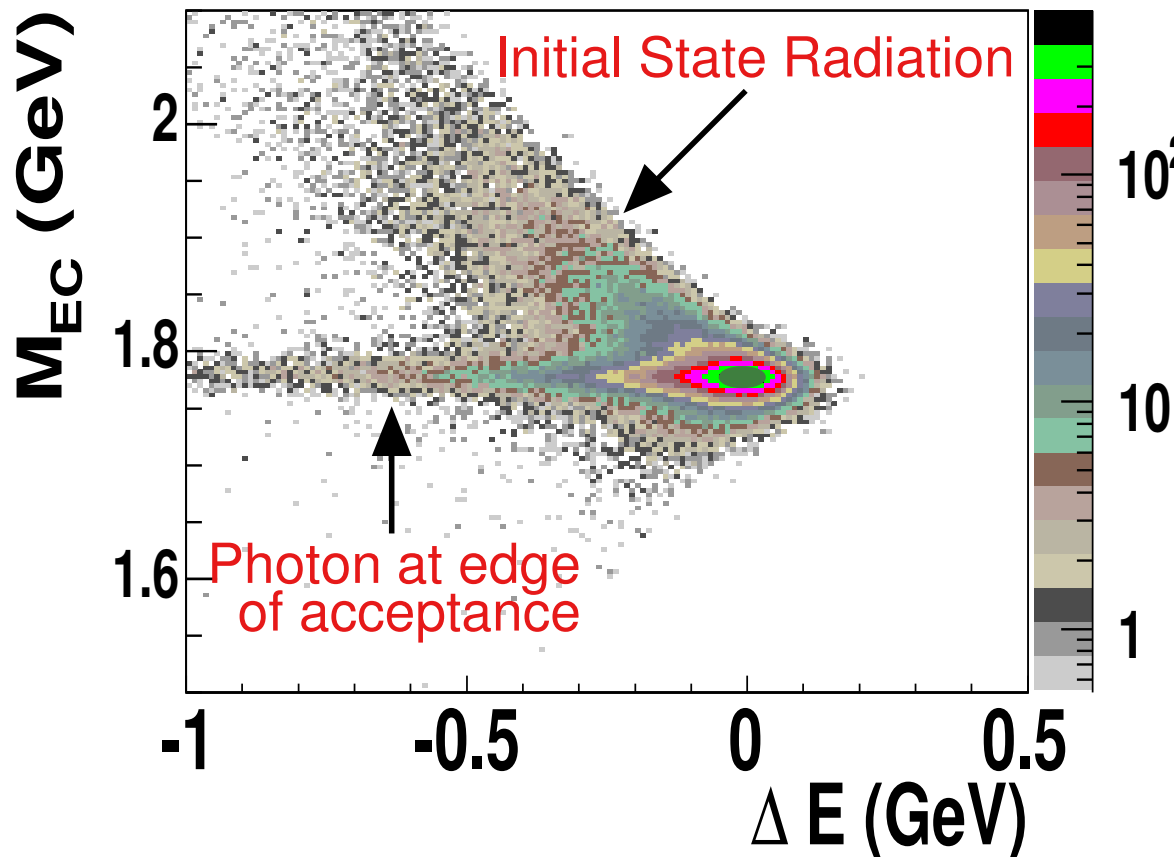
**Signal-Side** **Tag-Side**

Backgrounds:

- $\tau^- \rightarrow l'^-l^+l^-$ :
- Bhabha, di-muon
- $\tau^- \rightarrow l^+l'^-l'^-$ ,  $\tau \rightarrow lhh'$ :
- $\tau^+\tau^-$ ,  $q\bar{q}$

$$\tau \rightarrow \mu \gamma$$

- (Energy, Mass)<sub>daughters</sub>  $\sim (\frac{\sqrt{s}}{2}, m_\tau)$  (upto resolution & radiation)



$\tau \rightarrow \mu \gamma$  simulation

$$\Delta E = E_{\text{rec}} - \frac{\sqrt{s}}{2} \sim 0$$

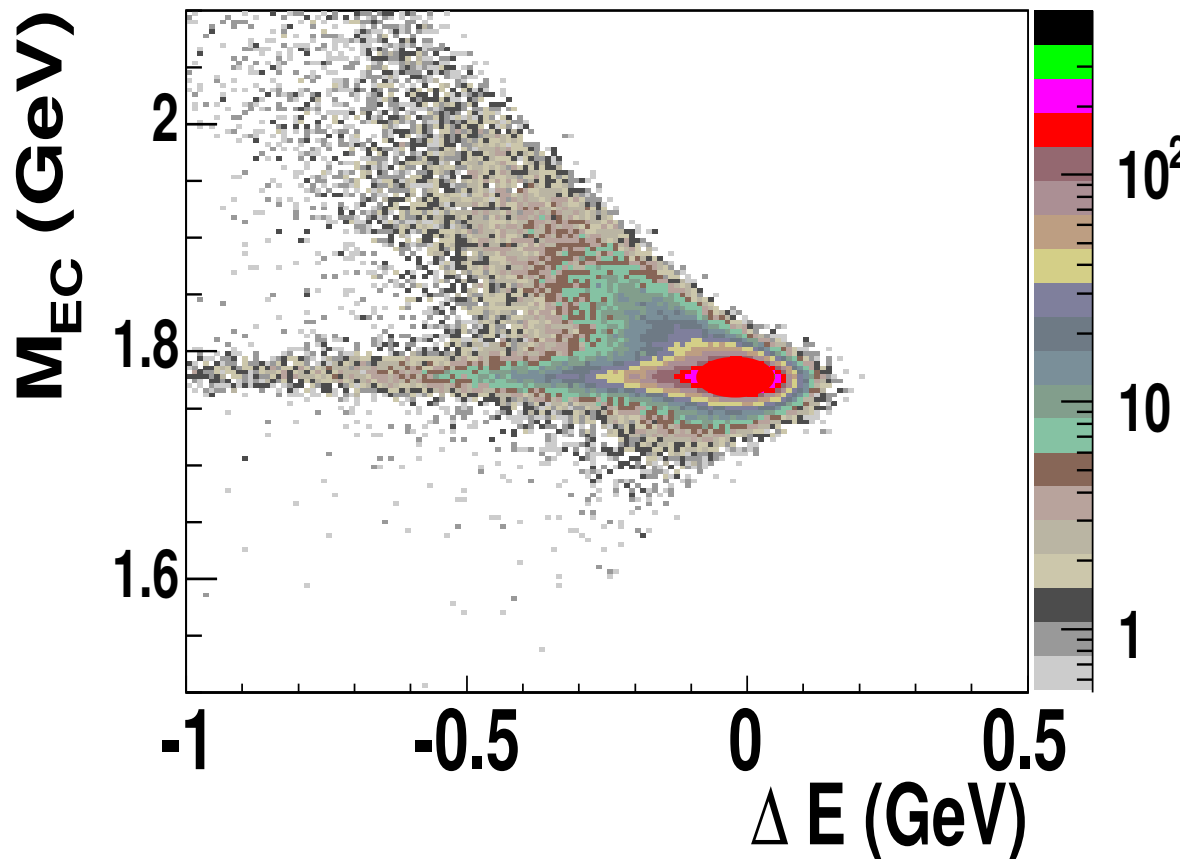
$$\sigma(\Delta E) \sim 50 \text{ MeV}$$

$M_{\text{EC}} (\sigma \sim 9 \text{ MeV})$   
 Beam energy  
 constrained mass  
 after vertexing  
 $\gamma$  at  $\mu$  POCA(XY)

👉 Signal Region:  $\pm 2 \sigma$  around  $(\langle \Delta E \rangle, \langle M_{\text{EC}} \rangle)$

$$\tau \rightarrow \mu \gamma$$

- (Energy, Mass)<sub>daughters</sub>  $\sim (\frac{\sqrt{s}}{2}, m_\tau)$  (upto resolution & radiation)



$\tau \rightarrow \mu \gamma$  simulation

$$\Delta E = E_{\text{rec}} - \frac{\sqrt{s}}{2} \sim 0$$

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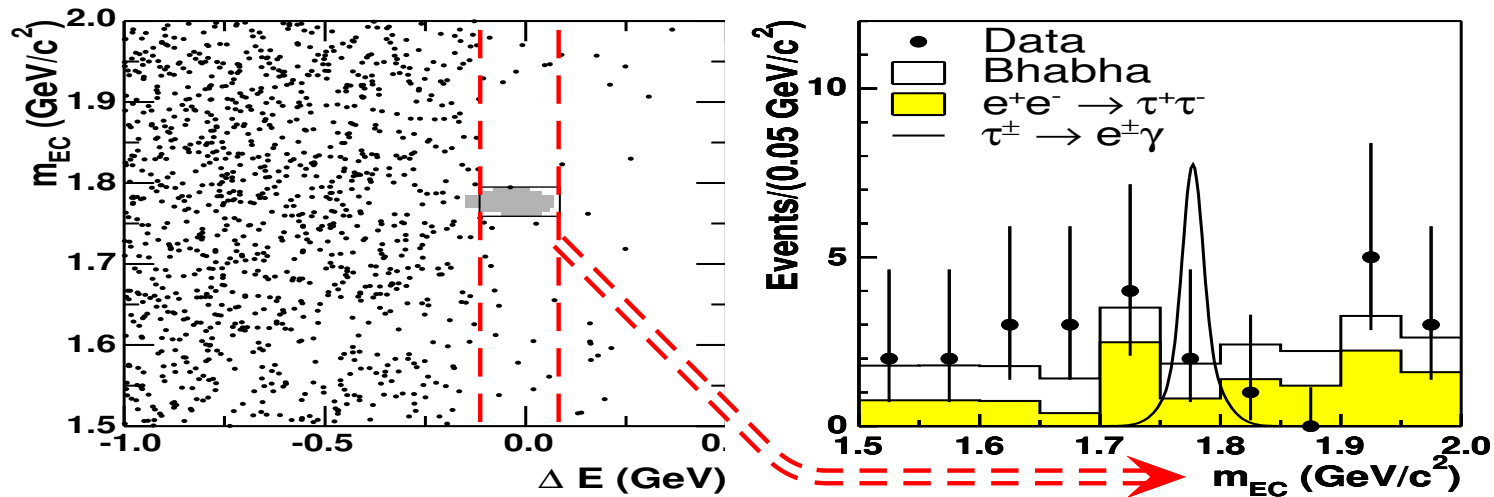
Beam energy  
constrained mass  
after vertexing

$\gamma$  at  $\mu$  POCA(XY)

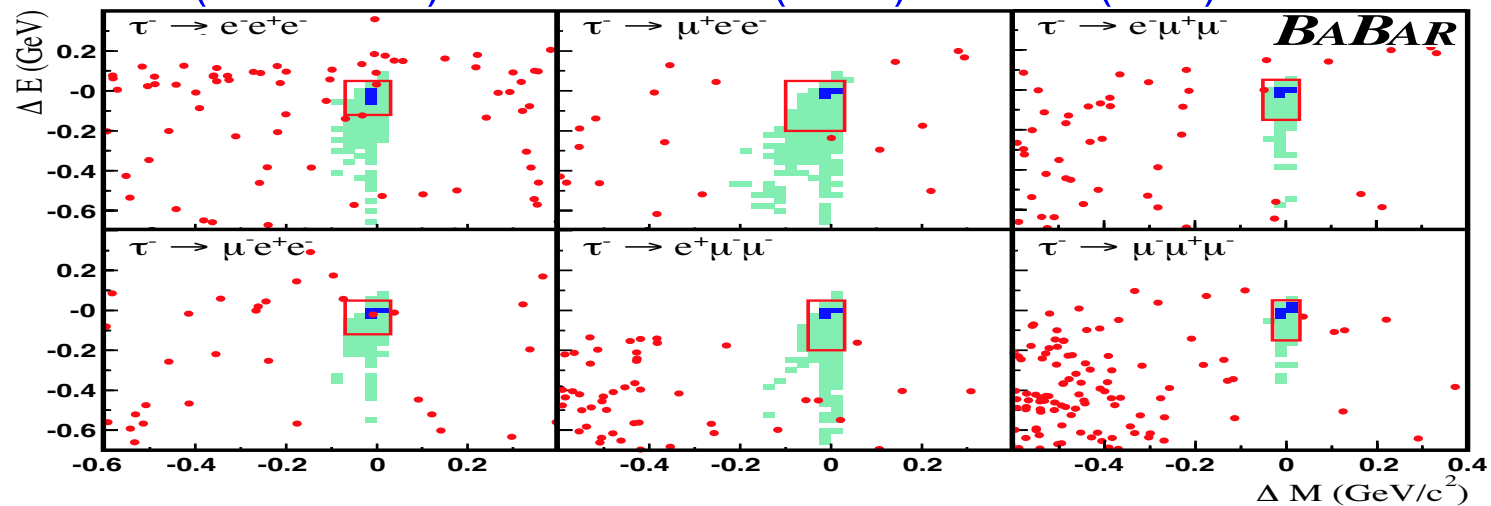
Blinded Region:  $\pm 3 \sigma$  around  $(\langle \Delta E \rangle, \langle M_{\text{EC}} \rangle)$

# Background estimation

- $\tau \rightarrow l\gamma$ : Background rate from PDF( $M_{EC}$ ) in  $\pm 2\sigma$  band in  $\Delta E$



- $\tau \rightarrow lll$  ( $\tau \rightarrow lhh'$ ): 2-D Fit PDF( $\Delta M$ )  $\times$  PDF( $\Delta E$ )



# Upper Limit

$$B_{UL}^{90} = N_{UL}^{90} / (N_{\tau} \times \varepsilon)$$

- $N_{UL}^{90}$ : 90% C.L. Upper Limit for  $(N_{obs}, N_{bkg})$  from Data
- $\varepsilon$ : high statistics signal MC simulated for different Data-taking periods

$\varepsilon =$  Trigger . Reco . Topology . PID . Cuts . Signal-Box

90%    70%    70%    50%    50%    50%

**Cumulative:**

90%    63%    44%    22%    11%    ~5%

- $N_{\tau} = 2 \times \mathcal{L} \times \sigma_{\tau+\tau-}$ 
    - $\sigma_{\tau+\tau-} (10.6 \text{ GeV}) \sim 0.89 \text{ nb}$
    - $L \sim 250 \text{ fb}^{-1}$  (BaBar Summer 2005)
- $\Rightarrow N_{\tau} \sim 4.5 \times 10^8$



# B-Factories: Status

Channel	BaBar		Belle	
	$B_{UL}^{90}$ ( $10^{-7}$ )	$\mathcal{L}$ ( $\text{fb}^{-1}$ )	$B_{UL}^{90}$ ( $10^{-7}$ )	$\mathcal{L}$ ( $\text{fb}^{-1}$ )
$\tau \rightarrow \mu\gamma$	0.7	232.2	3.1	86.3
	PRL95(2005)41802		PRL92(2004)171802	
$\tau \rightarrow e\gamma$	1.1	232.2	3.9	86.7
	hep-ex/0508012 (sub PRL)		PLB613(2005)20	
$\tau \rightarrow \mu\mu\mu$	1.9	91.5	2.0	87.1
	PRL92(2004)121801		PLB589(2004)103	
$\tau \rightarrow eee$	2.0	91.5	3.5	87.1
	PRL92(2004)121801		PLB589(2004)103	
$\tau \rightarrow lll$	(1-3)	91.5	(2-4)	87.1
	PRL92(2004)121801		PLB589(2004)103	
$\tau \rightarrow lhh'$	(1-5)	221.4	(2-16)	158.0
	PRL95(2005)191801		NPB(Proc)144(2005)173	
$\tau \rightarrow l\pi^0/\eta/\eta'$			(2-10)	153.8
			PLB622(2005)218	
$\tau \rightarrow lK_S^0$			(0.5-0.6)	281
			hep-ex/0509014	

# B-Factories: Projections

$$B_{UL}^{90} = N_{UL}^{90} / (N_{\tau} \times \epsilon)$$

●  $\tau \rightarrow \mu\gamma$  search: Optimize:  $N_{UL}^{90} / \epsilon$

● Sensitivity:  $B_{UL}^{90} \sim 1.2 \times 10^{-7}$  (BaBar, 232.2  $fb^{-1}$ )

	No Background	With Background
$N_{UL}^{90}$	$2.3 \times \sqrt{N_{obs}} \sim \mathcal{O}(1)$	$\sqrt{\mathcal{L}}$
$B_{UL}^{90}$	$\propto 1/\mathcal{L}$	$\propto 1/\sqrt{\mathcal{L}}$

● BaBar, Belle: 1  $ab^{-1}$  each (2008)

$\mathcal{L}$	( $ab^{-1}$ )	0.25 (Now)	1.0	50
$B_{UL}^{90}$	( $10^{-8}$ )	10	2.5 (5)	0.05 (0.7)

● Super B-Factory:

● 50  $ab^{-1} \Rightarrow B_{UL}^{90} < \mathcal{O}(10^{-10}) / \mathcal{O}(10^{-9})$  no/with Background

# $\tau \rightarrow \mu\gamma$ : LHC expectations

- Energy of  $\tau$  not known, Mass(daughters)  $\sim m_\tau$

## ● Signal

- $qq \rightarrow W \rightarrow \tau(\rightarrow \mu\gamma)\nu$   
 $\sigma \times \mathcal{B} = 14.8 \text{ nb}$   
 $\Rightarrow N_\tau \sim 1.5 \times 10^8$   
(for  $10 \text{ fb}^{-1}$  low  
luminosity 1yr data)

## ● Backgrounds

- FSR
  - $qq \rightarrow W \rightarrow \mu\nu\gamma$
  - $qq \rightarrow W \rightarrow \tau(\rightarrow \mu\nu\bar{\nu})\nu\gamma$
- Radiative production
  - $qq \rightarrow W\gamma \rightarrow \mu\nu\gamma$

- L. Serin and R. Stroynowski (ATL-PHYS-97-114):

- $\varepsilon = 5.4\%$ ,  $N_{bkg} = 17 \text{ events/yr}$  ( $10 \text{ fb}^{-1}$ )
- Sensitivity  $\mathcal{B}(\tau \rightarrow \mu\gamma) = (2.3 \times \sqrt{N_{bkg}}) / (N_\tau \times \varepsilon) \sim 10^{-6}$
- For  $30 \text{ fb}^{-1}$  data :  $\mathcal{B}(\tau \rightarrow \mu\gamma) < 0.6 \times 10^{-6}$

- E. Barberio (SMU, 2002):

- Signal:  $Z \rightarrow \tau\tau$  decays  $\Rightarrow N_\tau = 2 \times \mathcal{L} \times \sigma \times \mathcal{B}$
- For  $30 \text{ fb}^{-1}$  data :  $\mathcal{B}(\tau \rightarrow \mu\gamma) < 0.5 \times 10^{-7}$

# $\tau \rightarrow \mu\mu\mu$ : LHC expectations

## ● Event Signature:

- 3 prong vertex
- $\mu$  ID
- $m(\mu\mu\mu) \sim m_\tau$

$N_\tau / \text{yr (low lumi)}$

$$W \rightarrow \tau\nu \quad 1.5 \times 10^8$$

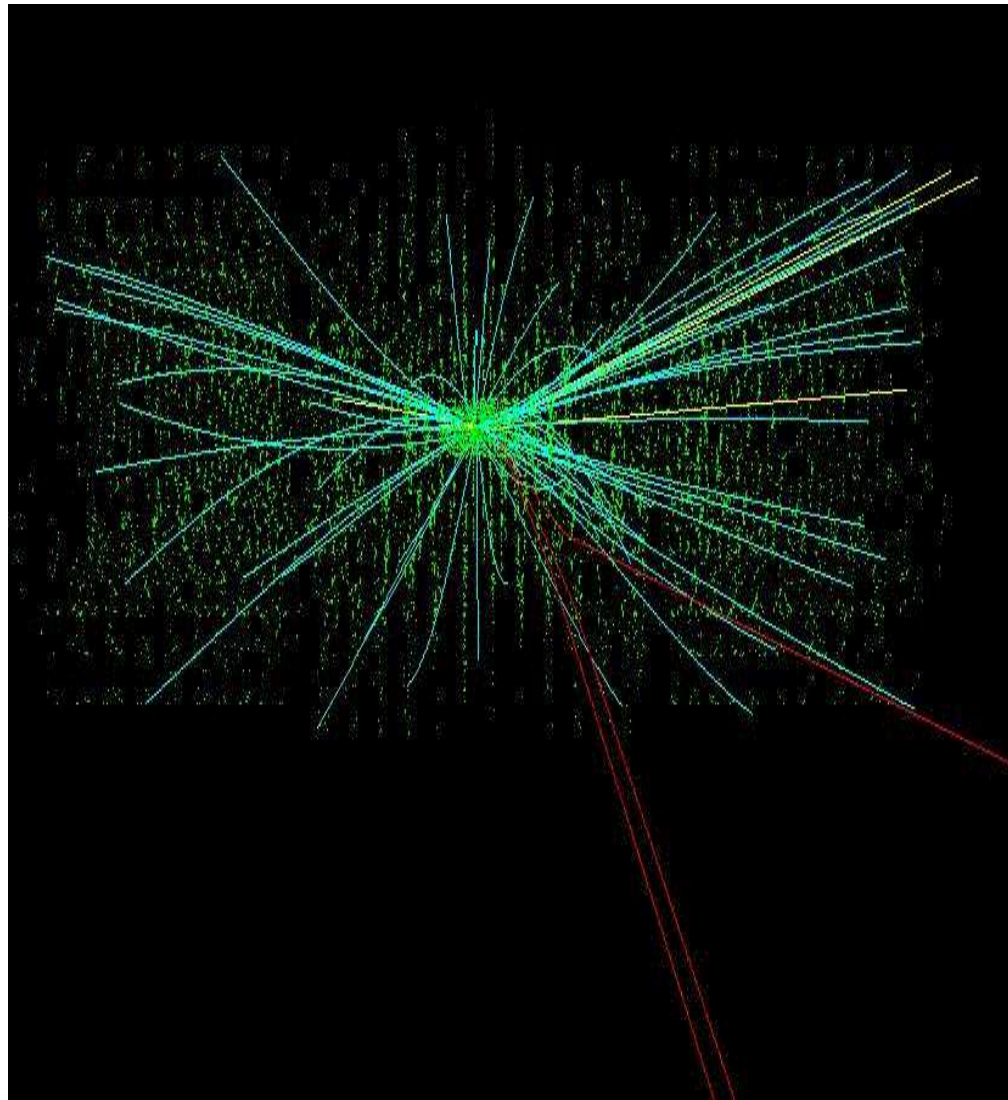
$$Z \rightarrow \tau\tau \quad 8.0 \times 10^8$$

$$D_S \rightarrow \tau X \quad 1.5 \times 10^{12}$$

$$B^0 \rightarrow \tau X \quad 4.0 \times 10^{11}$$

$$B^\pm \rightarrow \tau X \quad 3.8 \times 10^{11}$$

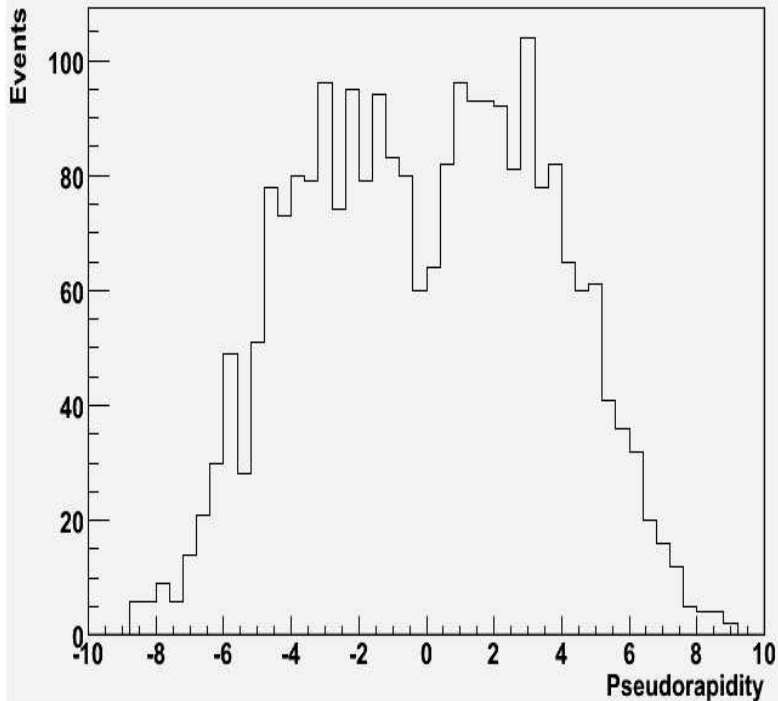
$$B_S \rightarrow \tau X \quad 7.9 \times 10^{10}$$



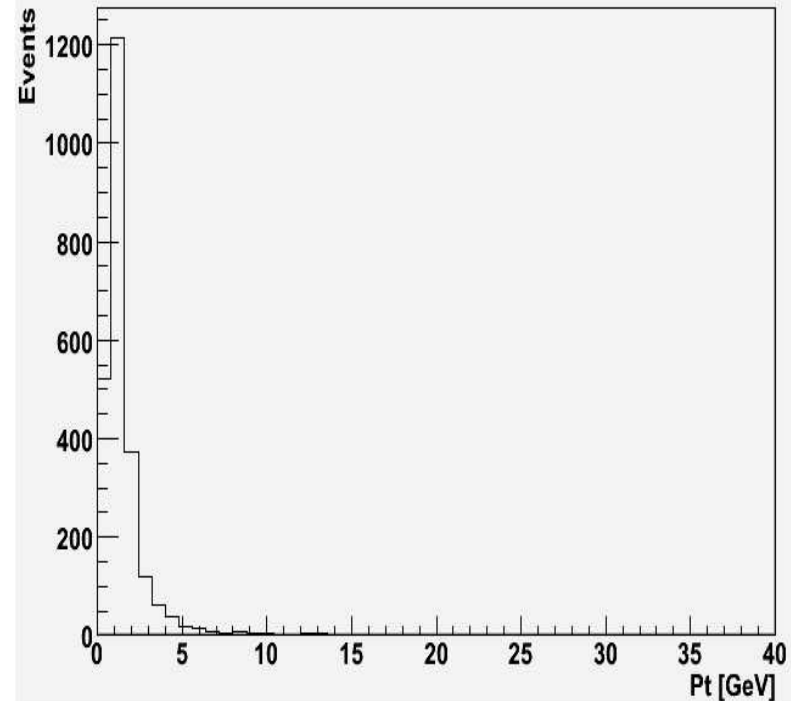
CMS Simulation

# $\tau \rightarrow \mu\mu\mu$ : LHC expectations

Pseudorapidity of the tau from Ds



Pt of leading muon from Ds Mesons

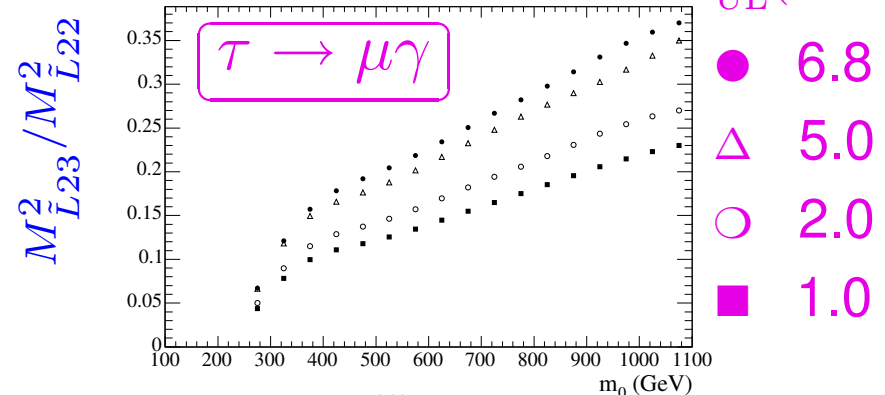


- Level 1 Trigger: single-muon  $p_T > 14$  GeV, di-muon  $p_T > 3$  GeV
- Backgrounds:  $D_S \rightarrow \mu\nu\phi$   
 $\phi \rightarrow \mu\mu, \phi \rightarrow \mu\mu\gamma$
- $\varepsilon \sim 1\%$  (?),  $\mathcal{B}(\tau \rightarrow \mu\mu\mu) < 10^{-10}$  (A.Stahl, Heraeus School 2005)

# B-Factories Reach (O.Igonkina, SUSY05)

- mSUGRA with off-diagonal elements  $\mathcal{L} = -M_{\tilde{L}}^2 \tilde{L}^* \tilde{L} - M_{\tilde{E}}^2 \tilde{E}^* \tilde{E}$   $B_{UL}^{90} (10^{-8})$

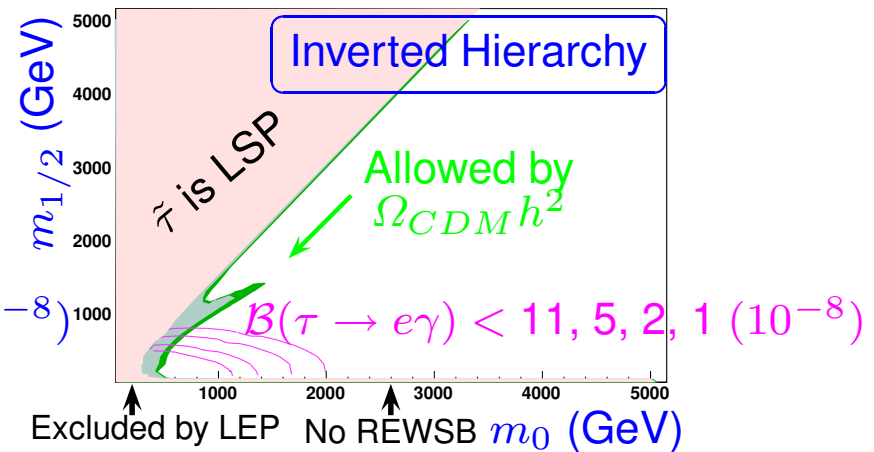
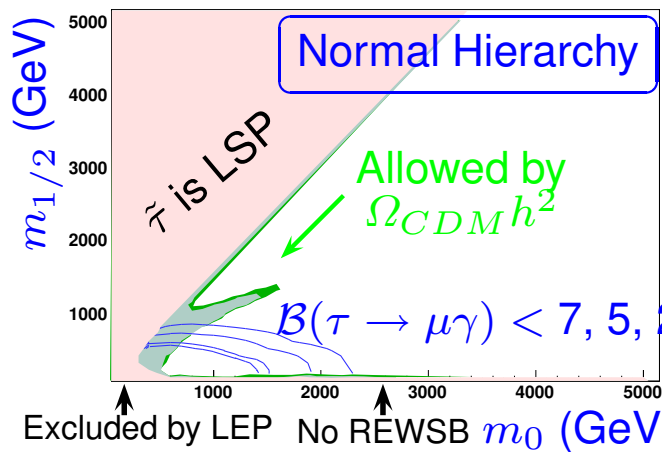
- Model-independent calculation (A.Brignole, A.Rossi, NPB701(2004)3)
- RGE using SPheno (W. Porod, CPC153(2003)275)
- Cold Dark Matter (WMAP) with micrOMEGAs (CPC149(2002)103)



$$m_{GUT} = 5 \cdot 10^{15} \text{ GeV}, \tan \beta = 55$$

$$\mu > 0, A_0 = 0, m_{1/2} = 100 + 0.8 \cdot m_0$$

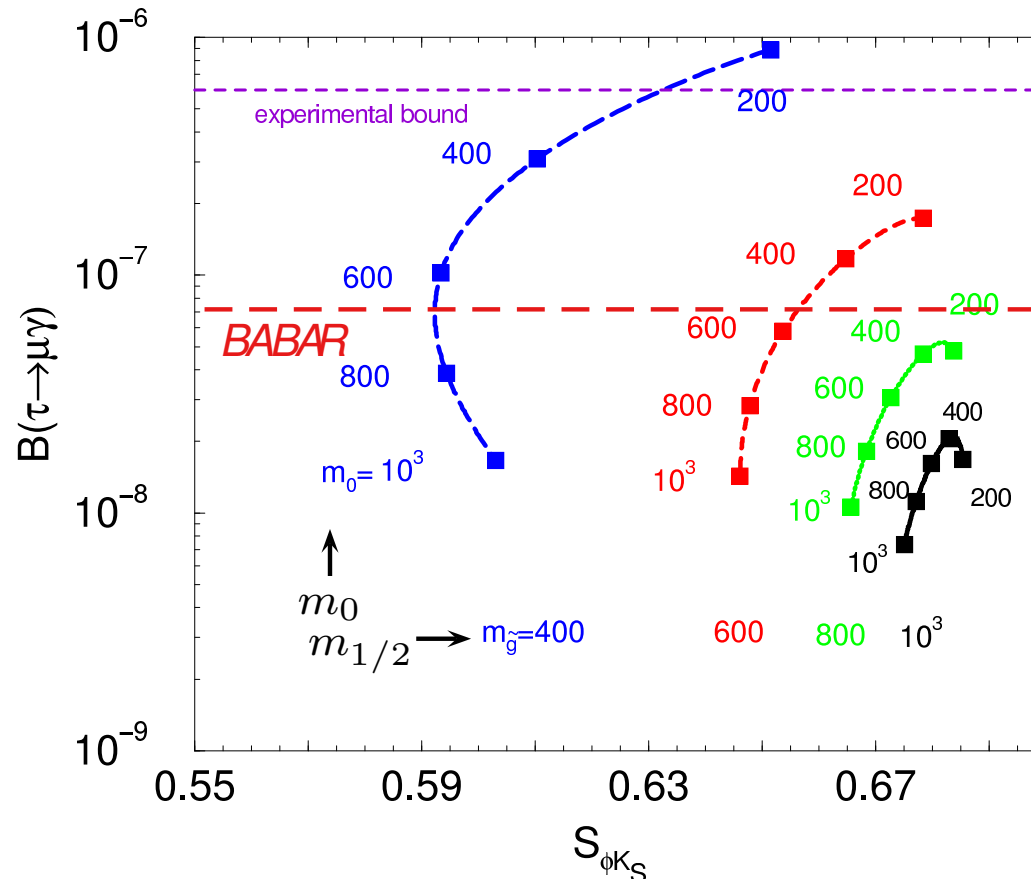
- mSUGRA + Seesaw:  $\mathcal{L} = Y_\nu L \tilde{H}_2 N_R$ ,  $Y_\nu \propto V_{MNS}$  mixing by RGE



- $m_{\nu_R} = 5 \times 10^{14} \text{ GeV}, \tan \beta = 55, \mu > 0, A_0 = 0, m_0, m_{1/2}, M_{\tilde{L}}^2, M_{\tilde{E}}^2$ : Diagonal

# $\tau \rightarrow \mu\gamma$ & $S_{\phi K_S}$

- SUSY SU(5) GUT: Flavour changing right-handed currents  $\Rightarrow$  Correlations between CP asymmetry in b-s penguins and  $\tau \rightarrow \mu\gamma$**



J. Hisano, Y. Shimizu  
(PLB565(2003)183)

$\tan \beta = 10, A_0 = 0,$   
 $m_{\nu_R} = 5 \times 10^{14} \text{ GeV},$   
 $m_{\nu_\tau} = 5 \times 10^{-2} \text{ eV}$

- Current measurement:  $S(B \rightarrow \phi K_S) = 0.47 \pm 0.19$  (HFAG, 2005). More sensitive  $\mathcal{B}(\tau \rightarrow \mu\gamma) < 6.8 \times 10^{-8}$  exclude some regions.**

# $\tau \rightarrow lll$ predictions

## SUSY + Higgs

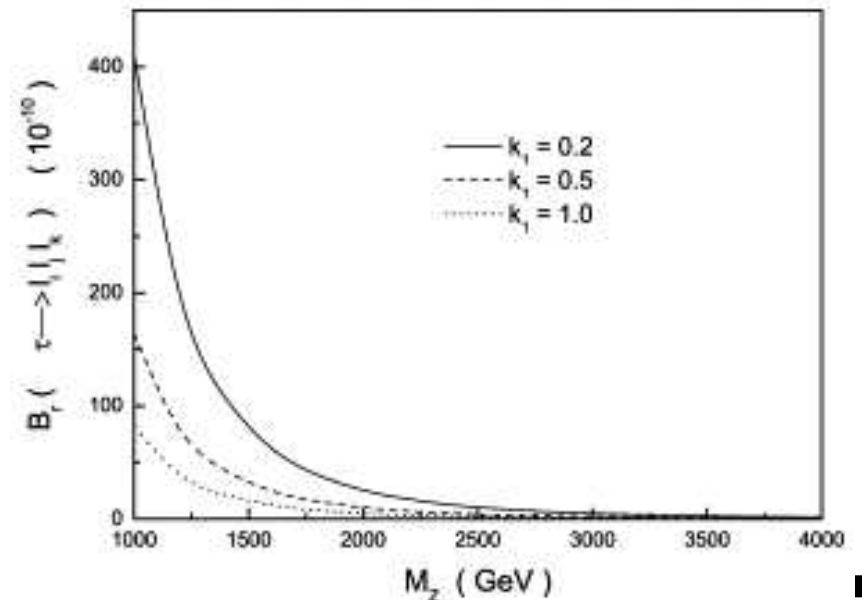
(A.Brignole, A.Rossi, PLB566(2003)217)

- $\mathcal{B}(\tau \rightarrow 3\mu) \simeq 10^{-7} \times \left(\frac{\tan\beta}{50}\right)^6 \times \left(\frac{100\text{GeV}}{m_A}\right)^4 \times \left(\frac{|50\Delta_L|^2 + |50\Delta_R|^2}{10^{-3}}\right)$
- If Higgs light, s-particles  $\sim \mathcal{O}(\text{TeV})$ ,  $\tan\beta \sim 50$
- No direct observation, but  $\tau \rightarrow \mu\mu\mu$  observable (?)
- Sensitivity  $\sim 10^{-8} - 10^{-10}$  at B-Factories, LHC

## Non Universal $Z'$ (Technicolor)

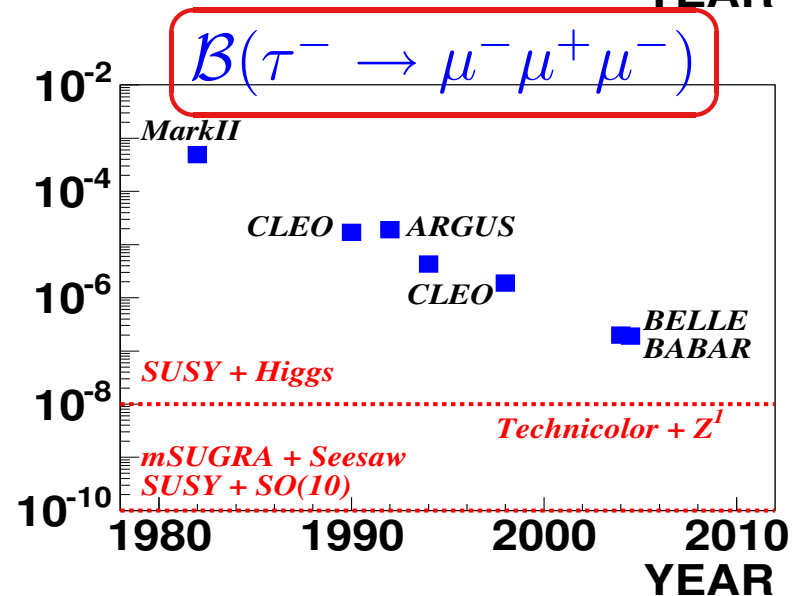
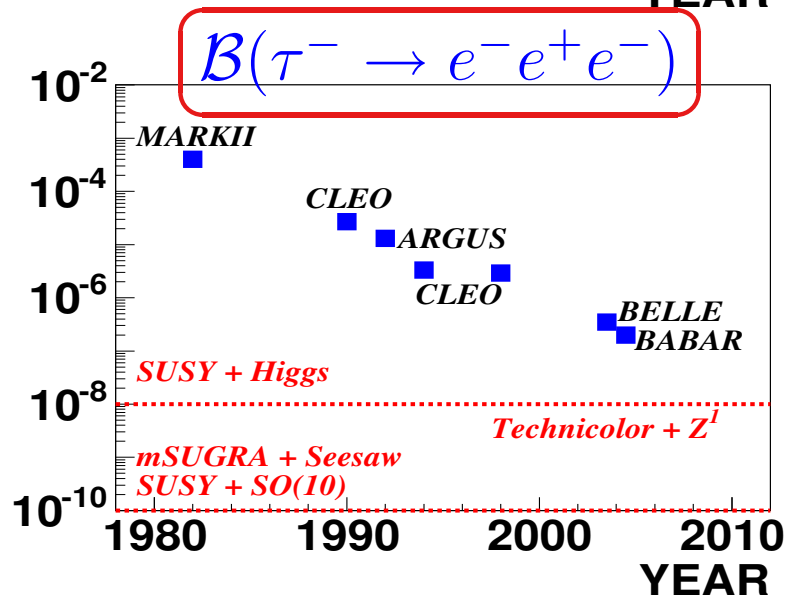
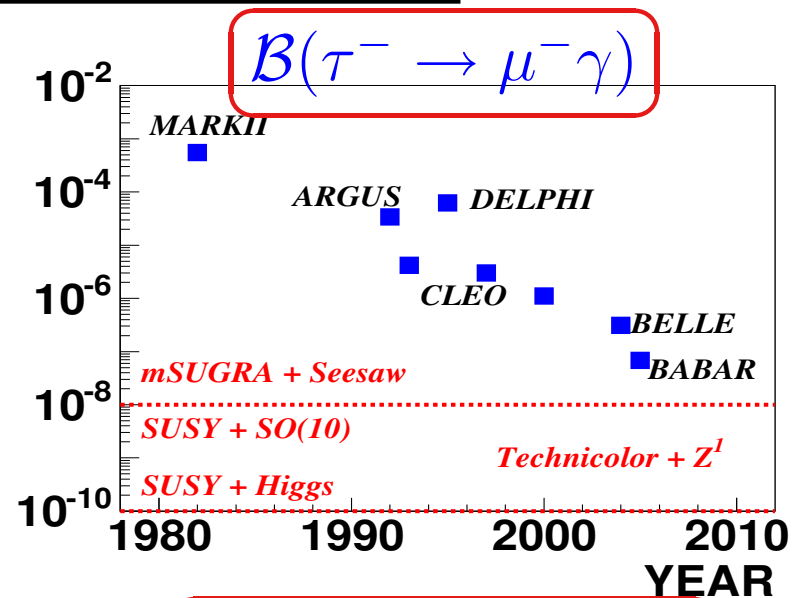
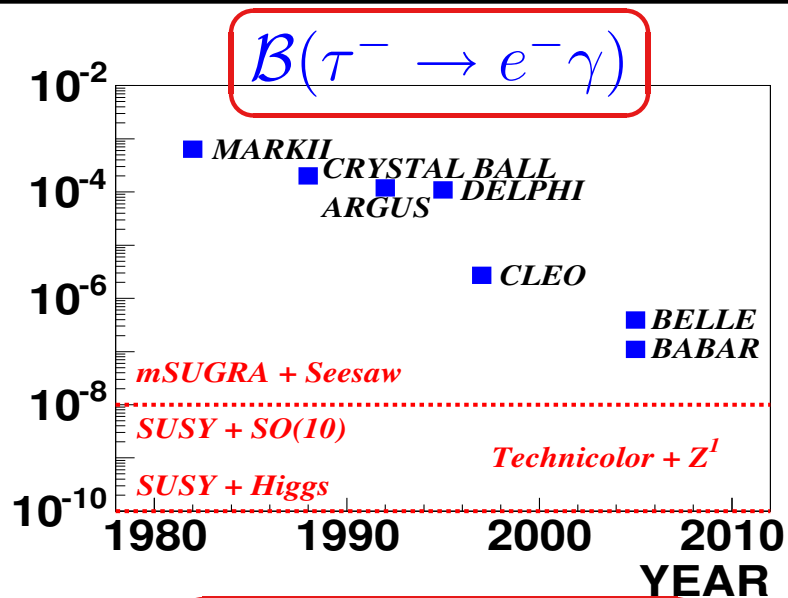
(C.Yue, Y.Zhang, L.Liu, PLB547(2002)252)

- $\tau \rightarrow lll$  most sensitive
- Flavour mixing ( $k_1$ ) = 0.2,  
 $\mathcal{B}(\tau \rightarrow lll) < 10^{-8}$   
 $\Rightarrow m_{Z'} < 1.2 \text{ TeV}$





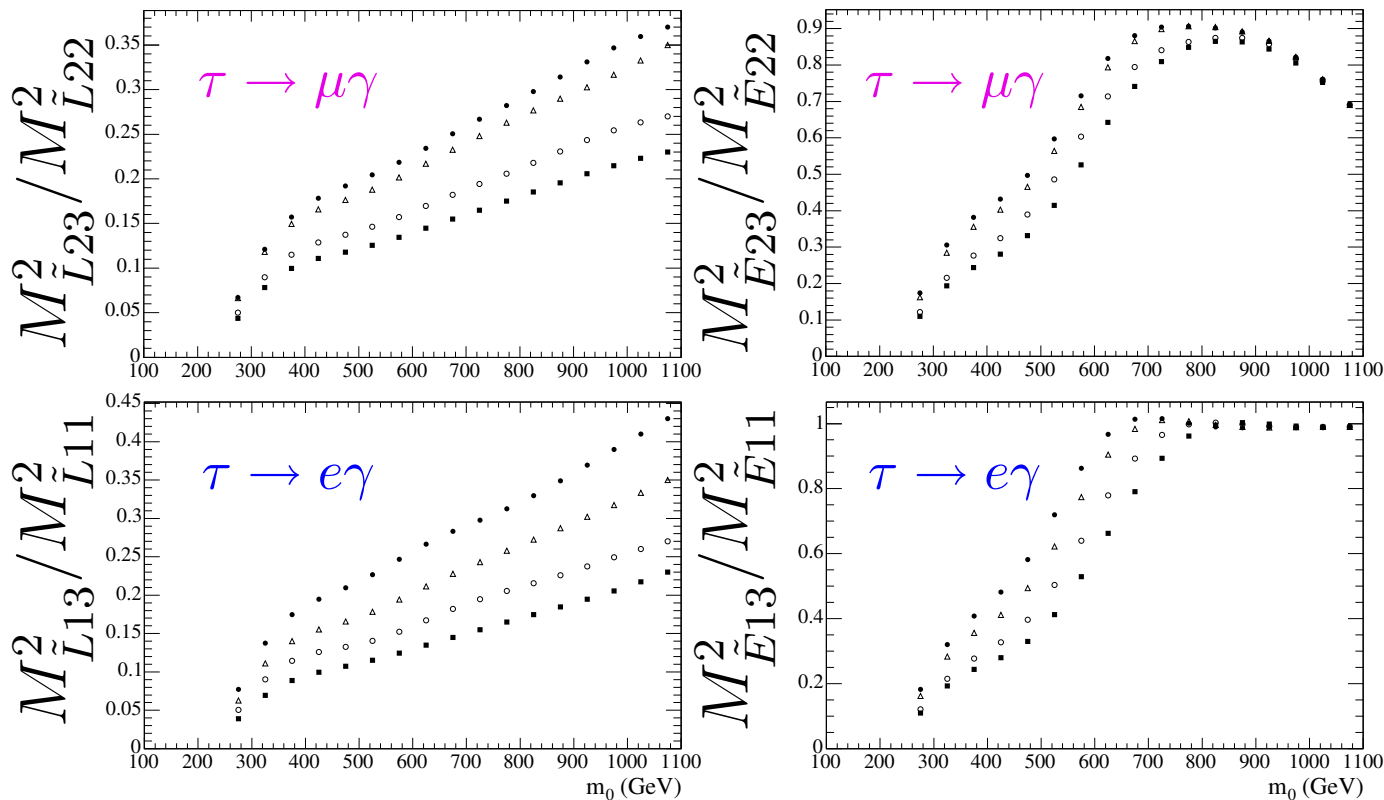
# Summary



# Backup Slides ...

# mSUGRA: mixing at GUT scale

●  $\mathcal{L} = -M_{\tilde{L}}^2 \tilde{L}^* \tilde{L} - M_{\tilde{E}}^2 \tilde{E}^* \tilde{E}$ , where  $\tilde{L} : (\tilde{\nu}_L, \tilde{\ell}_L)$ ,  $\tilde{E} : (\tilde{\ell}_R)$



$B_{UL}^{90} (10^{-8})$

● 6.8

△ 5.0

○ 2.0

■ 1.0

$B_{UL}^{90} (10^{-8})$

● 11

△ 5.0

○ 2.0

■ 1.0

$m_{GUT} = 5 \cdot 10^{15}$  GeV,  $\tan \beta = 55$ ,  $\mu > 0$ ,  $A_0 = 0$ ,  $m_{1/2} = 100 + 0.8 \cdot m_0$

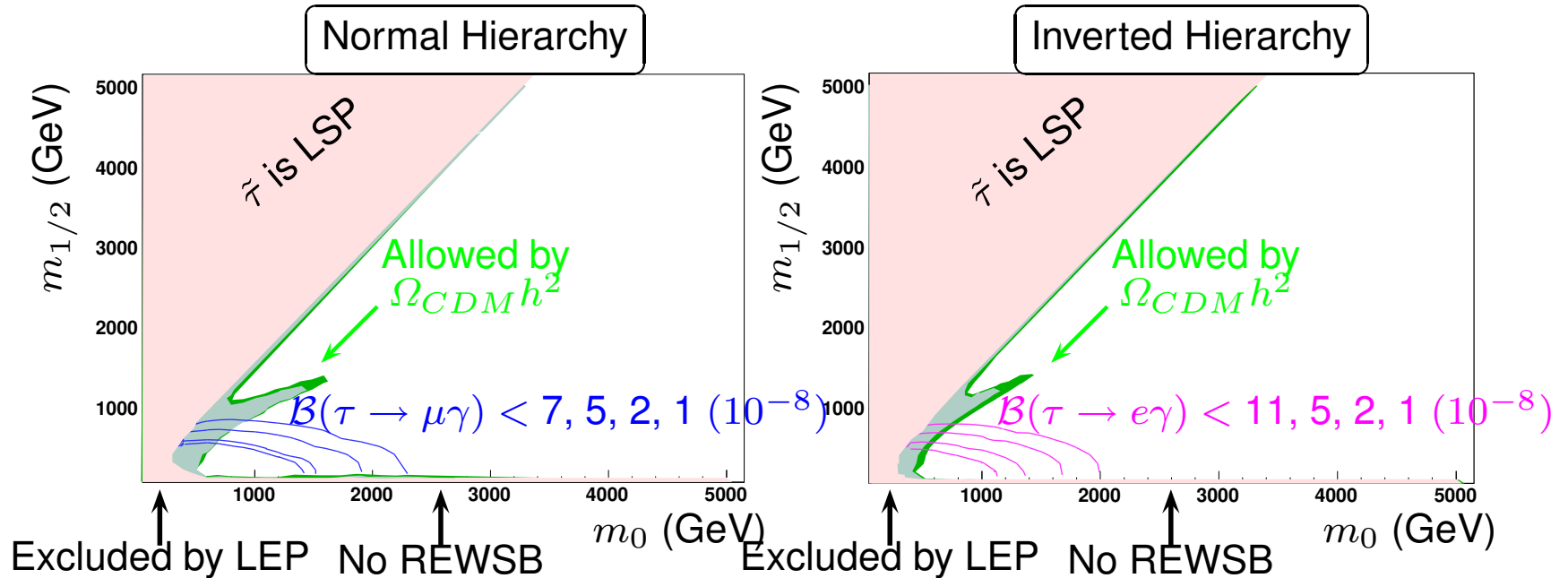
● BaBar Physics Reach Assessment 2005 (O.Igonkina, SUSY05)

● Model-independent calculation (A.Brignole, A.Rossi, NPB701(2004)3)

● RGE using SPheno (W. Porod, CPC153(2003)275)

# mSUGRA + Seesaw: mixing by RGE

- $\mathcal{L} = Y_\nu L \tilde{H}_2 N_R$ , where  $L : (\nu_L, \ell_L)$ ,  $N_R : (\nu_R)$   
 $Y_\nu = V_R V_{MNS}$ ,  $V_{R_{ii}}(m_{\nu_R}) = \sqrt{2m_{\nu_i} m_{\nu_R}} / v_2$   
 $V_{MNS}$ :  $\nu$ -mixing induces LFV at EW scale via RGE flow
- Global Analysis of  $\nu$  Data, M.C. Gonzalez-Garcia, hep-ph/0410030
- Cold Dark Matter (WMAP) with micrOMEGAs (CPC149(2002)103)



- $m_{\nu_R} = 5 \times 10^{14}$  GeV,  $\tan \beta = 55$ ,  $\mu > 0$ ,  $A_0 = 0$

- $m_0, m_{1/2}, M_{\tilde{L}}^2, M_{\tilde{E}}^2$ : Diagonal