

DYNAMICAL FERMION MASS GENERATION
BY STRONG YUKAWA INTERACTIONS

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Flavour in the Era of the LHC

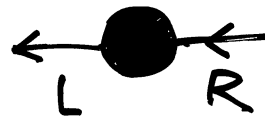
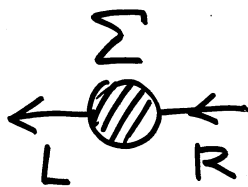
CERN, November 9, 2005

Use of the general principle of spontaneous breakdown of continuous symmetry for realistic $SU(2)_L \times U(1)_Y$ gauge and chirally invariant effective field theory description of electroweak phenomena is a necessity: hard fermion and gauge boson symmetry breaking mass terms ruin decent behavior of scattering amplitudes

SPONTANEOUS FERMION MASS GENERATION

- masslessness of the field protected by CHIRAL SYMMETRY
- fermion mass emerges as a pole in full propagator due to CHIRALLY INVARIANT INTERACTION

$$S(p) = \frac{1}{\not{p} - \Sigma(p)} = \frac{\not{p} + \Sigma(p)}{p^2 - \Sigma^2(p)}$$



$$m^2 = \Sigma^2(p^2 = m^2)$$

- by definition : non-perturbative

GENUINELY DISTINCT (KNOWN TO ME) REALIZATIONS

1. Complex scalars : $\mathcal{L}_{int} = y \bar{\Psi}_L \Psi_R \phi + H.c.$

arrange for condensation ($\phi_0 = (-m^2/\lambda)^{1/2}$)

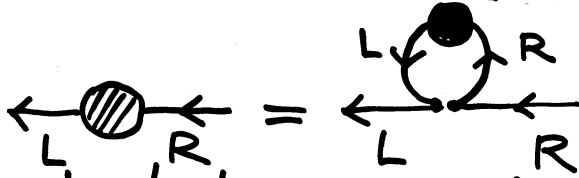
"non-pert." \uparrow

$$\mathcal{L}_{int} \rightarrow \bar{\Psi}_L \boxed{y \phi_0} \Psi_R + H.c.$$

this is what happens in S.M.

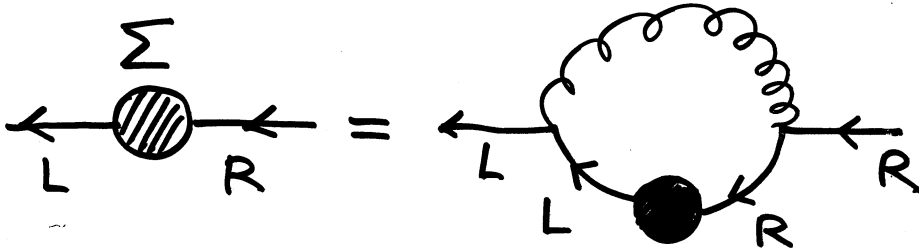
2. Fermions : $\mathcal{L}_{int} = G \bar{\Psi}_L \gamma_\mu \Psi_L \cdot \bar{\Psi}_R \gamma^\mu \Psi_R$

$$\mathcal{L}_{int} \rightarrow \bar{\Psi}_L \boxed{G \gamma_\mu \Psi_L \bar{\Psi}_R \gamma^\mu \Psi_R}$$



this is what happens in NJL & replicas

3. Vectors : $\mathcal{L}_{int} = [g_L \bar{\Psi}_L \gamma_\mu \Psi_L + g_R \bar{\Psi}_R \gamma_\mu \Psi_R] B^\mu$



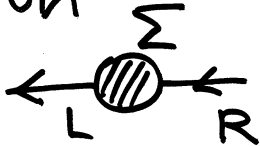
this is what happens in remaining models

OUR SUGGESTION

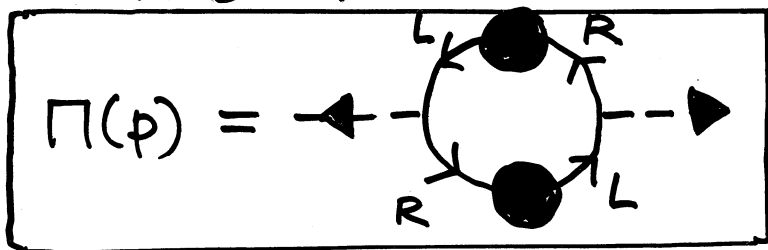
- employ complex scalars

$$\mathcal{L}_{int} = y \bar{\Psi}_L \Psi_R \phi + y \bar{\Psi}_R \Psi_L \phi^*$$

- consider $M^2 > 0$: ϕ is a heavy scalar
no condensation

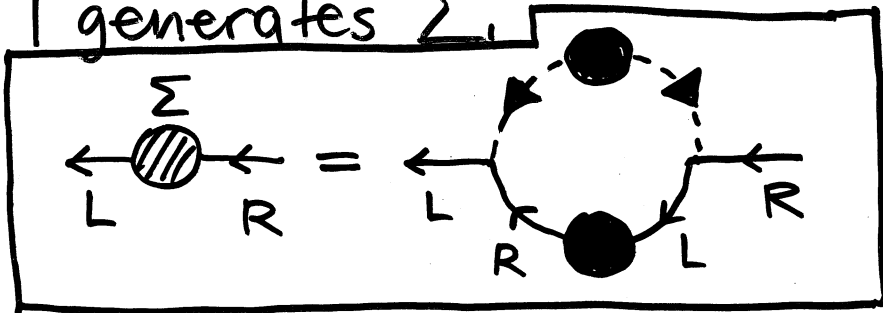
- assume $\Sigma(p)$ is generated : 


- Σ generates Π



$$\mathcal{L}_{eff}^{(0)}(\phi) = \partial_\mu \phi^* \partial^\mu \phi - M^2 \phi^* \phi - \frac{1}{2} \phi^* \Pi \phi^* - \frac{1}{2} \phi \Pi^* \phi$$

- Π generates Σ



 is the DIFFERENCE OF SCALAR PROP.

ϕ describes two spin-0 particles with different M_i

$$D^{-1}(p) = \begin{pmatrix} p^2 - M^2 & -\Pi(p) \\ -\Pi^*(p) & p^2 - M^2 \end{pmatrix}$$

$$D(p) = \frac{1}{(p^2 - M^2 - |\Pi|)(p^2 - M^2 + |\Pi|)} \begin{pmatrix} p^2 - M^2 & \Pi(p) \\ \Pi(p) & p^2 - M^2 \end{pmatrix}$$

symmetry breaking 

THE MODEL

Tomáš Brauner and Jiří Hošek,
Phys. Rev. D72, 045007 (2005)
(hep-ph/0505231)
(+ Petr Beneš, to be published)

- $\mathcal{L} = \bar{\Psi}_1 i \not{\partial} \Psi_1 + \bar{\Psi}_2 i \not{\partial} \Psi_2 +$
 $\partial_\mu \phi^* \partial^\mu \phi - M^2 \phi^* \phi - \frac{1}{2} \lambda (\phi^* \phi)^2$
 $+ y_1 [\bar{\Psi}_{1L} \Psi_{1R} \phi + \text{H.c.}] + y_2 [\bar{\Psi}_{2R} \Psi_{2L} \phi + \text{H.c.}]$

- symmetry : $U(1)_{V_1} \times U(1)_{V_2} \times U(1)_A$

$$\Psi_1 \rightarrow \exp[+i\theta \gamma_5] \Psi_1, \quad \Psi_2 \rightarrow \exp[-i\theta \gamma_5] \Psi_2$$

$$\phi \rightarrow \exp[-2i\theta] \phi$$

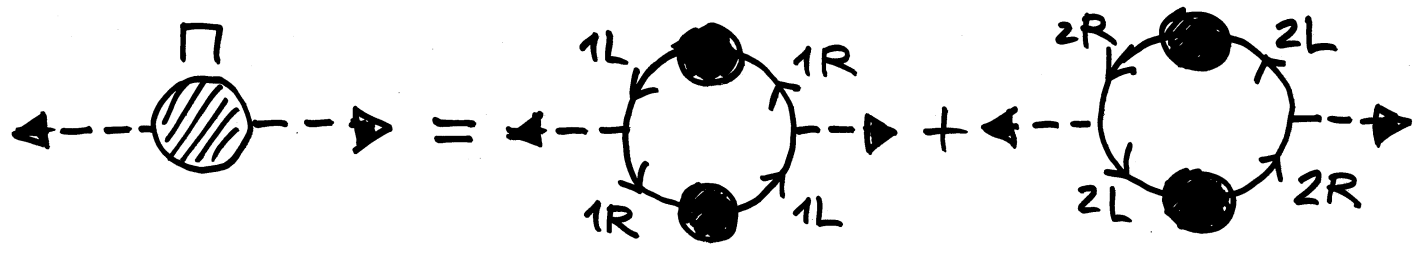
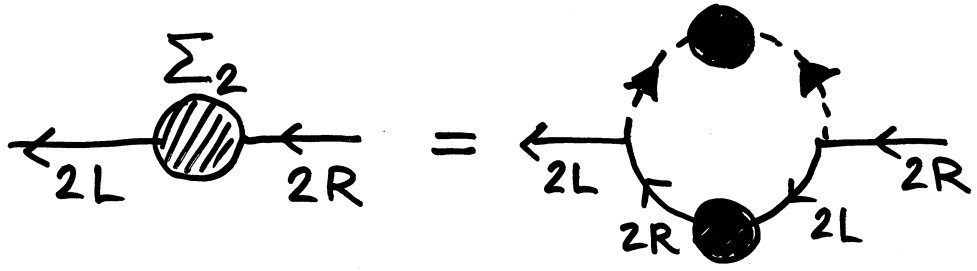
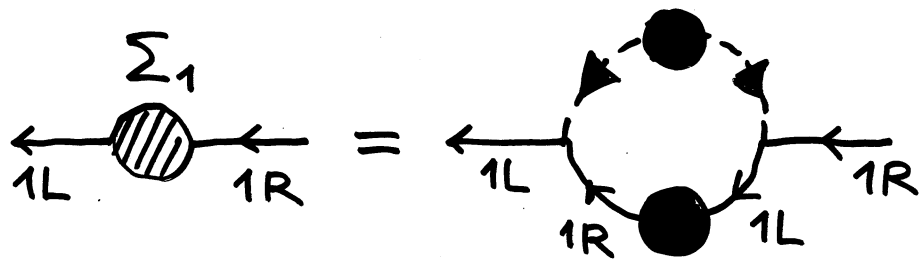
- why two fermion species ?

model amenable to gauging $U(1)_A$

axial anomaly has to be absent

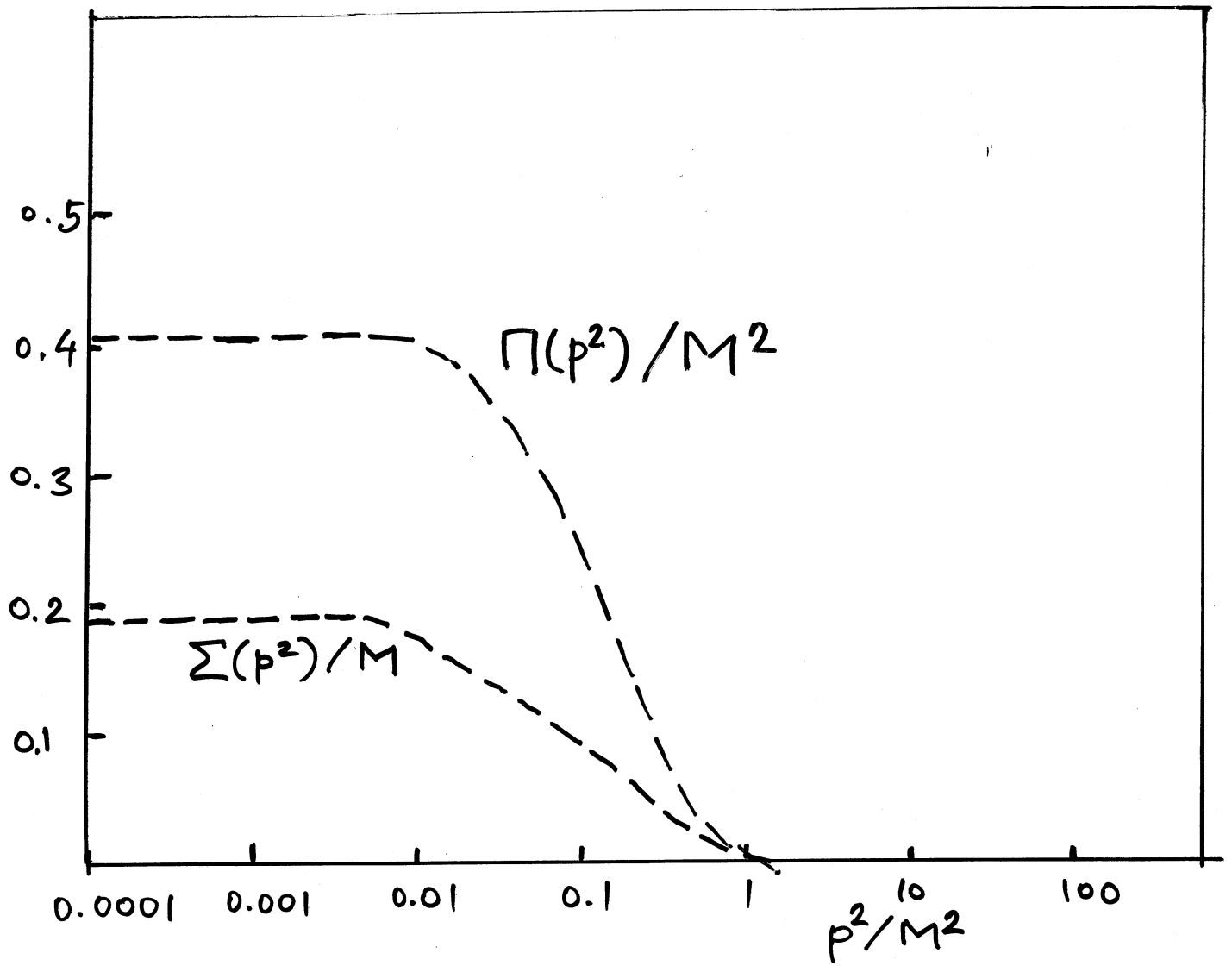
- $\lambda(\phi^* \phi)^2$ irrelevant for non-perturbative low-momentum driven mass generation

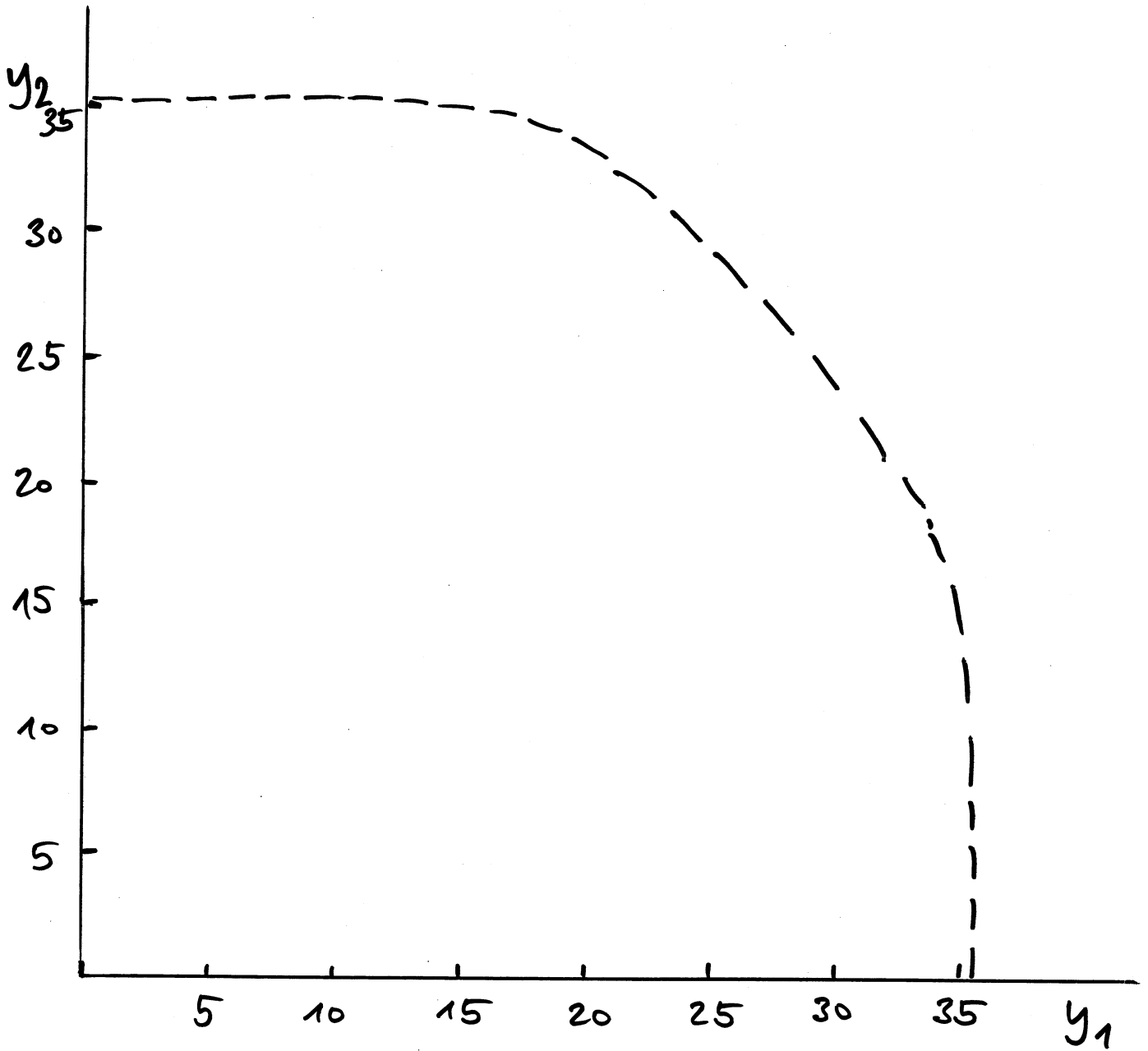
SCHWINGER-DYSON EQUATIONS FOR Σ AND Π



- If the solutions Σ_i , Π exist they should come out UV-finite :
corresponding counter-terms prohibited by symmetry
- robust, no tinkering

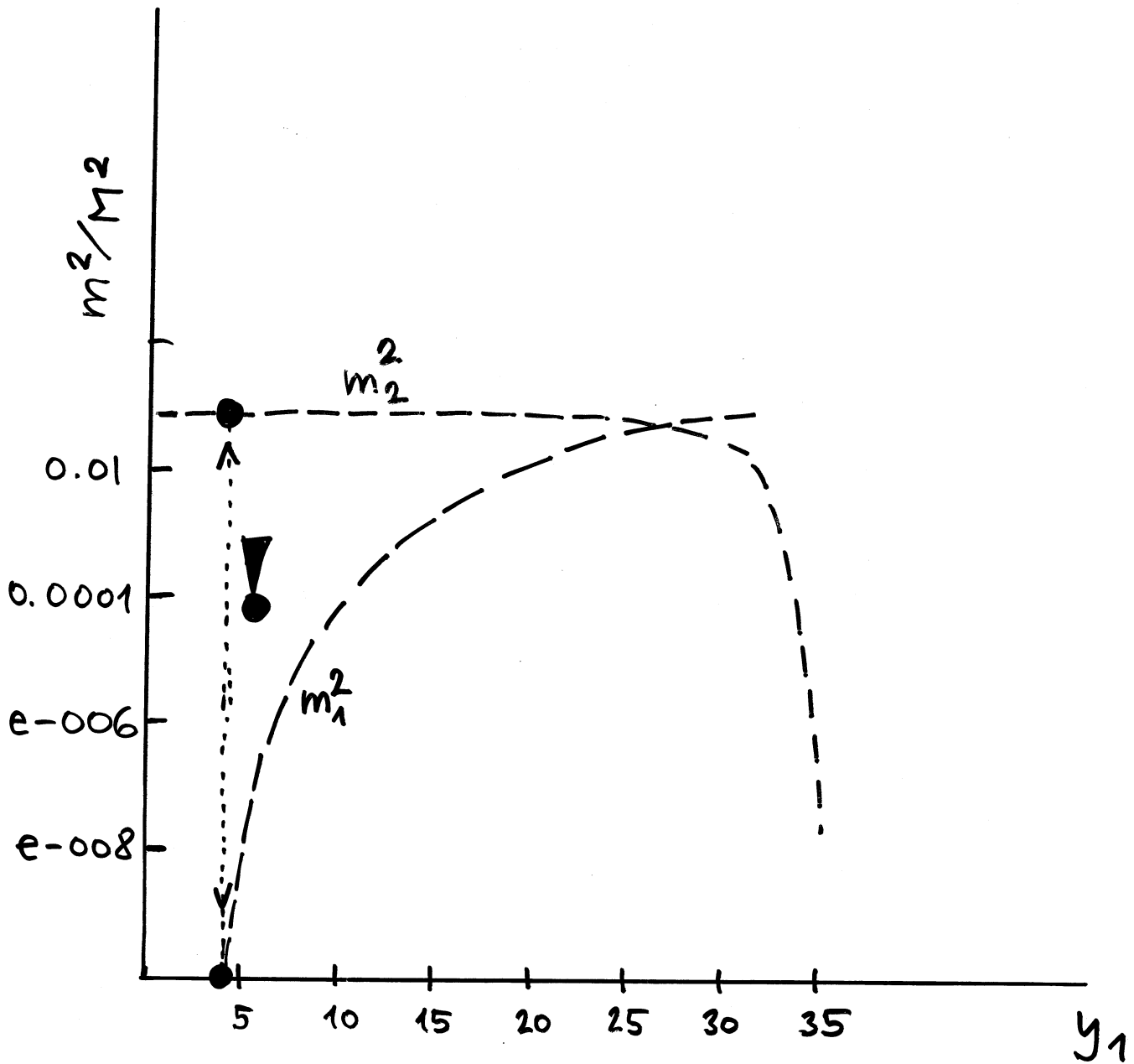
in paper





critical coupling constants

PRELIMINARY



Fermion masses

PRELIMINARY

- by dimensional argument $m_{1,2} = M f_{1,2}(y_1, y_2)$
- SM approach $m_{1,2} = (-M^2/\lambda)^{1/2} y_{1,2}$
- if verified this should NOT be called FINE TUNING

WHERE IS THE NAMBU - GOLDSTONE BOSON?

- $$j_A^\mu = \bar{\Psi}_1 \gamma^\mu \gamma_5 \Psi_1 - \bar{\Psi}_2 \gamma^\mu \gamma_5 \Psi_2 + 2i [(\partial^\mu \phi)^* \phi - \phi^* \partial^\mu \phi]$$

- fermion masses $m_i \sim \Sigma_i$
boson mass splitting M_1, M_2

naively:

- $$\partial_\mu j_A^\mu = 2im_1 \bar{\Psi}_1 \gamma_5 \Psi_1 - 2im_2 \bar{\Psi}_2 \gamma_5 \Psi_2 + 2i(M_1^2 - M_2^2) \phi_1 \phi_2$$

something is missing: NG excitation

axial-vector Ward identities:

$$q_\mu \Gamma_{A\Psi_1}^\mu(p+q, p) = S_1^{-1}(p+q) \gamma_5 + \gamma_5 S_1^{-1}(p)$$

$$q_\mu \Gamma_{A\Psi_2}^\mu(p+q, p) = -S_2^{-1}(p+q) \gamma_5 - \gamma_5 S_2^{-1}(p)$$

$$q_\mu \Gamma_{A\phi}^\mu(p+q, p) = -2D^{-1}(p+q) \Xi + 2\Xi D^{-1}(p)$$

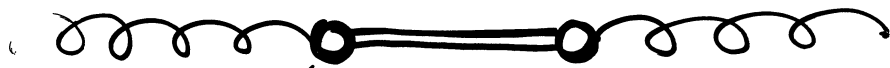
$$\Xi = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} : \text{operates in } \phi - \phi^* \text{ (analog of } \gamma_5)$$

massless pole in Γ_A^μ : NG boson

- its couplings to Ψ_1, Ψ_2 and ϕ are calculated
- it is a composite of Ψ_i and ϕ

GAUGE BOSON MASS²

is the residue at the massless pole of the gauge field polarization tensor; here the massless pole is due to the 'would-be' NG boson



UV finite loops containing Σ_i, Π

gauge boson mass is generated only if fermion masses are generated (in contrast with S.M.)

- gauging : $\partial \rightarrow D + (-\frac{1}{4}F^2)$
- obviously, for $y_1, y_2 = 0$ ($M^2 > 0$) the gauge boson stays massless

OUTLOOK

- "practical" : We know how to generalize the Abelian prototype to electroweak $SU(2)_L \times U(1)_Y$:
Tomáš Brauner and Jiří Hošek, hep-ph/0407339
- "theoretical" : We believe that finding non-perturbatively the full propagators in the strongly coupled Yukawa model should allow the reconstruction of beta functions at large values of the couplings