

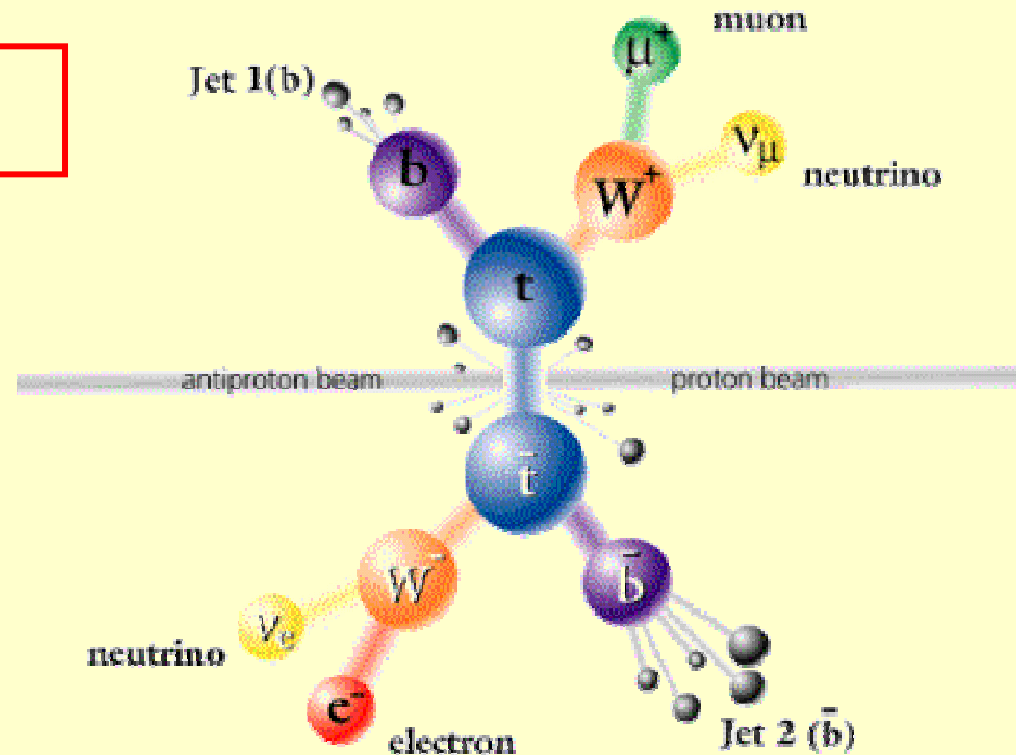
Measuring $t\bar{t}$ events at the LHC

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- ❖ Physics : the top quark knowledge within few (!?) years
- ❖ Method : overview of measurements in the $pp \rightarrow t\bar{t}$ channels
 - several methods with their individual features
- ❖ New ideas : LHC compared to the Tevatron
 - from statistical improvement to detailed systematics
 - could open new possibilities...
 - new measurements become possible...

Differentiate our analyses !!!



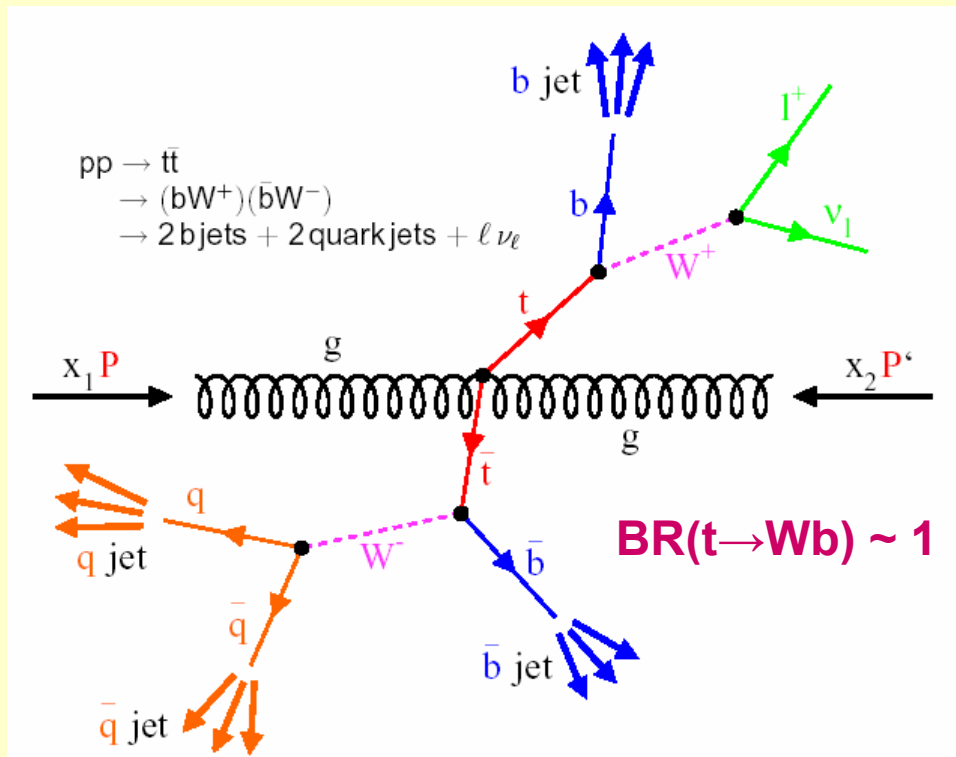
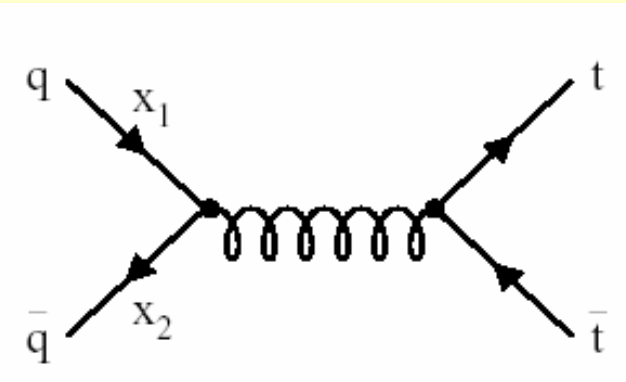
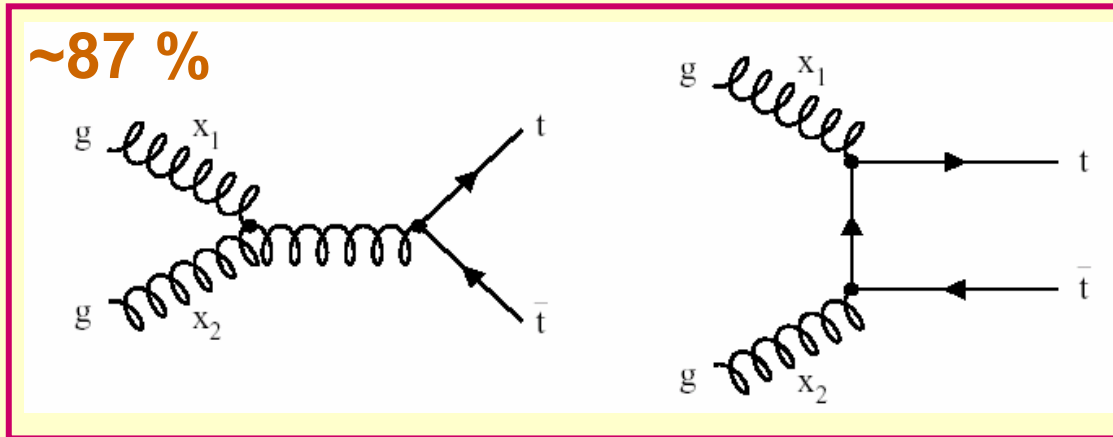
Do not concentrate on few particular analysis tools...

- ❖ study many different tools (for example jet clustering algorithms)
- ❖ identify their positive and negative features in the LHC environment

Optimize the analyses for both statistical and systematical uncertainties !!

The $pp \rightarrow t\bar{t}$ process at the LHC

~87 %



- ❖ Many **physics** parameters to be measured with these events (hence reconstruct the **complete** event !)
- ❖ Also it is the main **background** for searches beyond the Standard Model at the LHC
- ❖ NLO cross-section for $t\bar{t}$ production $\sigma^{\text{NLO}} = 833 \text{ pb} \Rightarrow \sim 8\text{M}$ events for 10fb^{-1}
($10 \text{ fb}^{-1} = 1$ year of LHC running at low luminosity, hence by summer 2008)

The $pp \rightarrow t\bar{T}$ process at the LHC : event selection

Main background processes for $pp \rightarrow t\bar{T} \rightarrow WbWb$:

❖ Fully hadronic channel : $3.7 \text{ Mevnt}/10\text{fb}^{-1}$

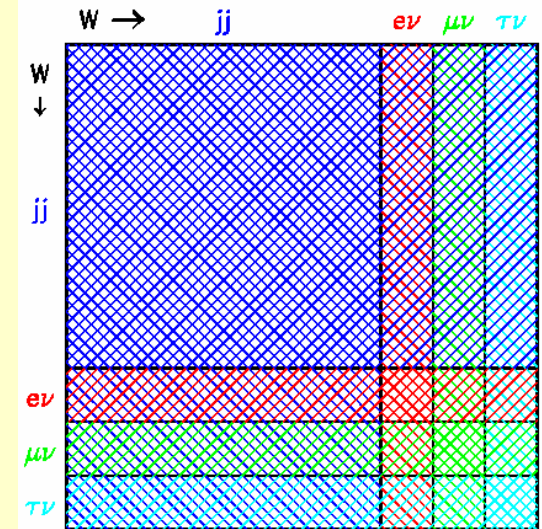
- QCD multijet ($2 \rightarrow 2$ parton processes)
- 6-jets $p_T > 40 \text{ GeV}$, $b\text{-tags} \geq 2$: $S/B \sim 1/19$, $\epsilon \sim 2.7\%$

❖ Lepton + jets channel (lepton = e/μ) : $2.5 \text{ Mevnt}/10\text{fb}^{-1}$

- $bb \rightarrow lv + \text{jets}$, $W + \text{jets} \rightarrow lv + \text{jets}$, $Z + \text{jets} \rightarrow ll + \text{jets}$,
- $WW \rightarrow lv + \text{jets}$, $WZ \rightarrow lv + \text{jets}$, $ZZ \rightarrow ll + \text{jets}$
- before selection we have $S/B \sim 10^{-5}$
- $p_T^{\text{lepton}} > 20 \text{ GeV}$, $E_T^{\text{miss}} > 20 \text{ GeV}$, $p_T^{\text{jet}} > 40 \text{ GeV}$, $b\text{-tags} \geq 2$: $S/B \sim 78$, $\epsilon \sim 3.5\%$
- $p_T^{\text{lepton}} > 20 \text{ GeV}$, $E_T^{\text{miss}} > 20 \text{ GeV}$, $p_T^{\text{jet}} > 40 \text{ GeV}$, $b\text{-tags} \geq 1$: $S/B \sim 28$, $\epsilon \sim 14\%$

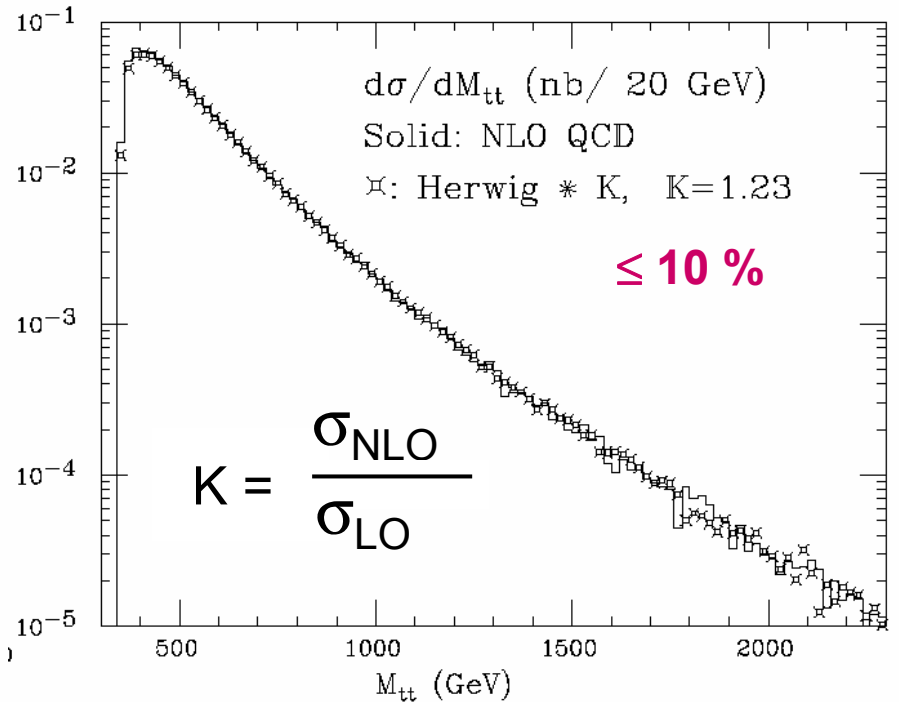
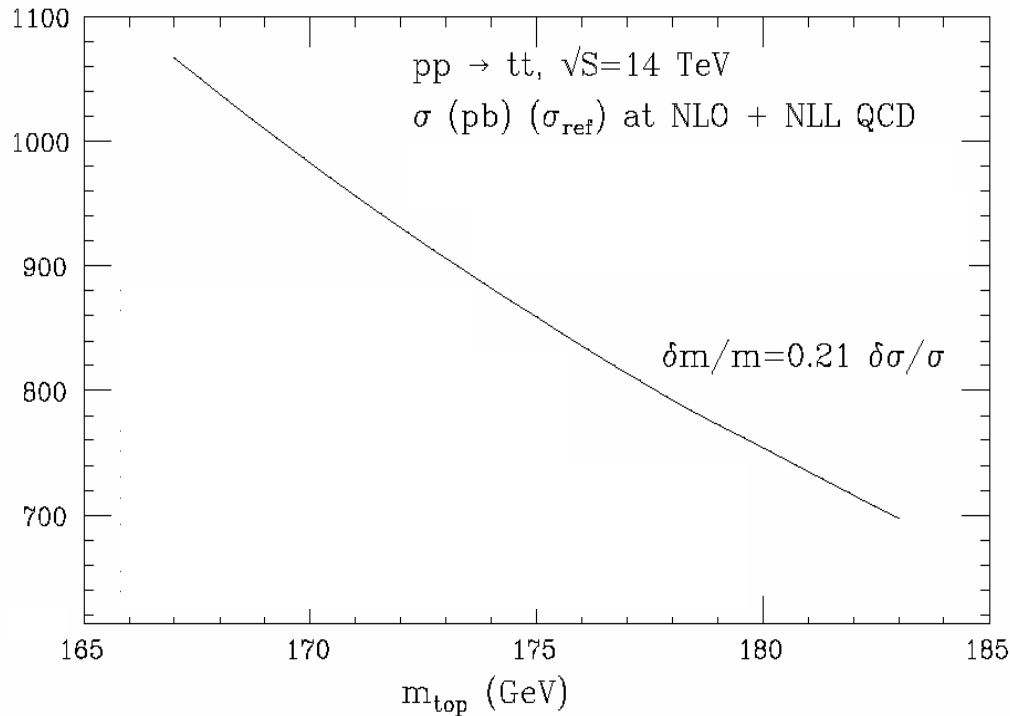
❖ Di-lepton channel : $0.4 \text{ Mevnt}/10\text{fb}^{-1}$

- Drell-Yan processes, $Z + \text{jets} \rightarrow ll + \text{jets}$, $WW + \text{jets}$, bb
- $p_T^{l^+} > 35 \text{ GeV}$, $p_T^{l^-} > 25 \text{ GeV}$, $E_T^{\text{miss}} > 40 \text{ GeV}$, $p_T^{\text{jets}} > 25 \text{ GeV}$: $S/B \sim 10$, $\epsilon \sim 20\%$



The $pp \rightarrow t\bar{t}$ process at the LHC : cross section

❖ **Sensitive to top mass** : $\Delta\sigma/\sigma \sim 5 \Delta m_t/m_t \rightarrow$ 5% on σ gives **2 GeV on m_t**



systematics dominated by the uncertainty on the luminosity

ATLAS preliminary

Time	Number of events at 10^{33}	$\Delta\sigma/\sigma$ (stat)
1 "week"	2×10^3	2.5%
1 "month"	7×10^4	0.4%
1 "year"	3×10^5	0.2%

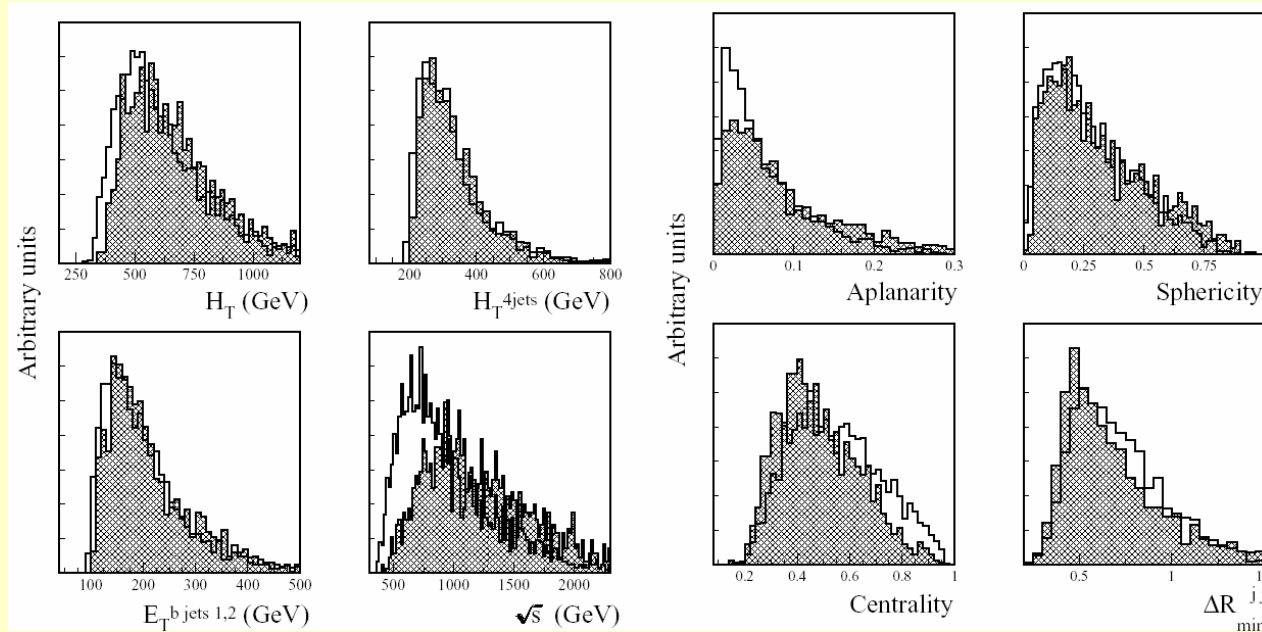
Cross-section sensitive to renormalisation and factorisation **scale**, and to the choice of **PDF** (Parton Density Function)

... influence known ??

The $pp \rightarrow t\bar{t}$ process at the LHC : fully hadronic

❖ Fully hadronic channel : $3.7 \text{ Mevnt}/10\text{fb}^{-1}$

- 6-jets $p_T > 40 \text{ GeV}$, $b\text{-tags} \geq 2$: $S/B \sim 1/19$, $\epsilon \sim 2.7\%$
- discriminant variables (energy flow, additional radiation, event shape)



some based on the D0
Neural Network procedure

not as powerful as in D0

ATLAS paper
hep-ex/0403021

- *hatched* : $t\bar{t}$ signal
- *open* : QCD background

- kinematic fit (χ^2 on the jet energies) + mass window 130-200 GeV :

$S/B \sim 6$, $\epsilon \sim 0.18\%$ (uncertainty on remaining background B is $\sim 40\%$)

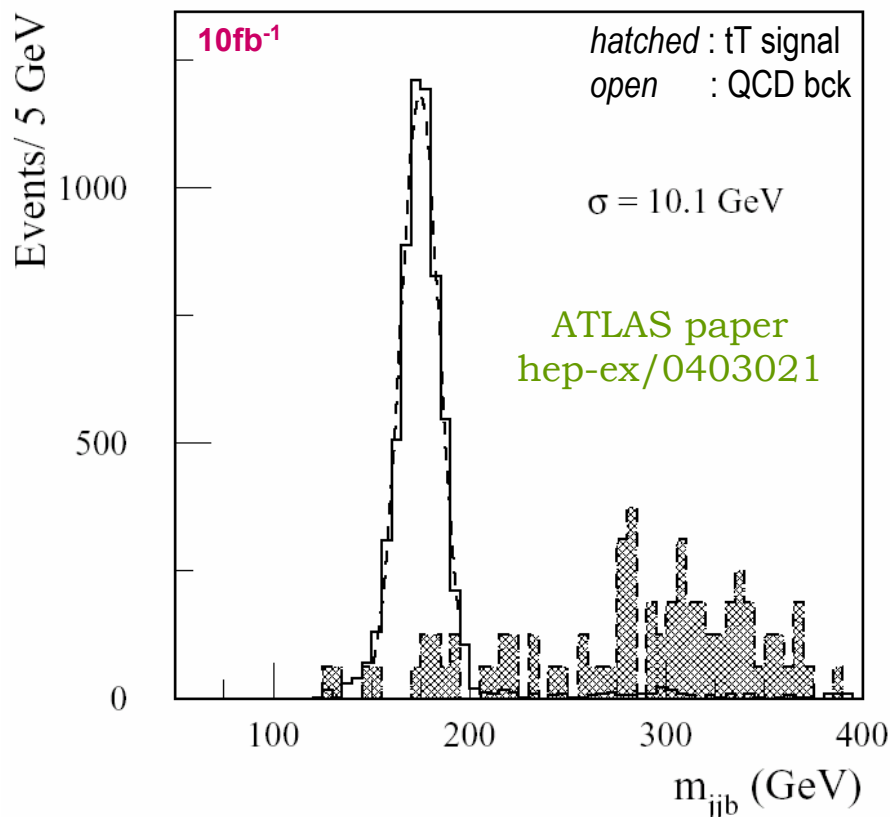
- can be further improved by asking $p_T^{\text{top}} > 200 \text{ GeV}$: $S/B \sim 18$, $\epsilon \sim 0.09\%$

A clean sample of signal events with $\sim 3.3 \text{ kevnt}/10\text{fb}^{-1} \Rightarrow$ for top mass estimation

The $pp \rightarrow t\bar{t}$ process at the LHC : fully hadronic

❖ Fully hadronic channel : $3.7 \text{ Mevnt}/10\text{fb}^{-1}$

- $p_T^{\text{top}} > 200 \text{ GeV}$: $S/B \sim 18$, $\epsilon \sim 0.09\%$ $\Rightarrow \sim 3.3 \text{ kevnt/year}$
- using the kinematic fit and the jet combination with the lowest χ^2



Gaussian fit in the window 130-200 GeV results in a peak width of 10.1 GeV

for $10\text{fb}^{-1} \Rightarrow \delta m_t(\text{stat}) = 180 \text{ MeV}$

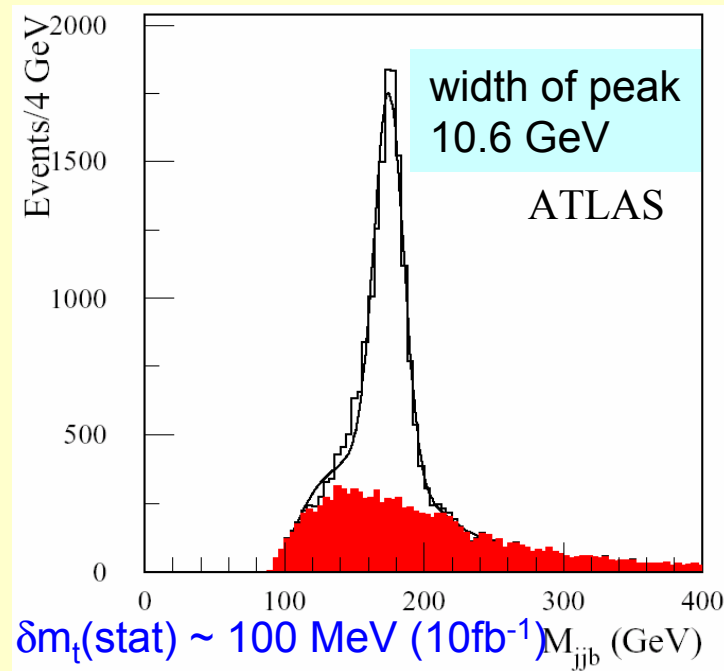
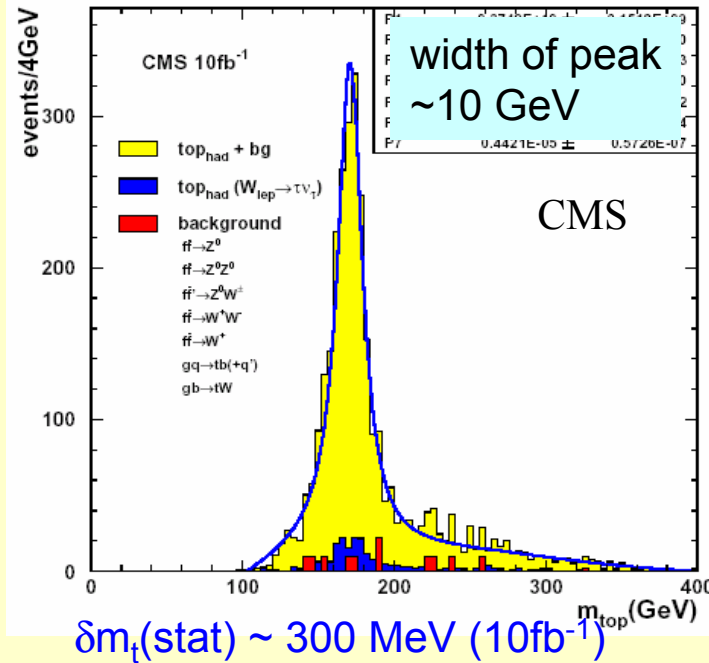
Systematics	$\delta m_t \text{ (GeV)}$
Light jet energy scale	0.8
b-jet energy scale	0.7
b-quark fragmentation	0.3
Initial state radiation	0.4
Final state radiation	2.8

Total systematic uncertainty $\sim 3.0 \text{ GeV}$

\Rightarrow This clean sample will also be exploited for differential distributions.

The $pp \rightarrow t\bar{t}$ process at the LHC : lepton+jet channel

Preliminary plots of ATLAS/CMS are similar :



Systematics	ATLAS	δm_t (GeV)
Light jet energy scale		0.2
b jet energy scale		$0.7 \times x\%$
Initial State Radiation		0.1
Final State Radiation		1
b-quark fragmentation		0.1
Combinatorial background		0.1
Statistical error		0.1

kinematic fit

Internal Systematics	ATLAS	δm_t (GeV)
light jet energy scale		0.2
Initial State Radiation		0.1
Final State Radiation		≤ 0.5
b-quark fragmentation		0.1
Combinatorial background		0.1
Total		≤ 0.6
Statistical error		0.1
b jet energy scale		$0.7 \times x\%$

❖ **Single lepton plus jets : High p_T sample with $p_T(jjb) > 200$ GeV (Jet-Analysis)**

Yellow Report LHC

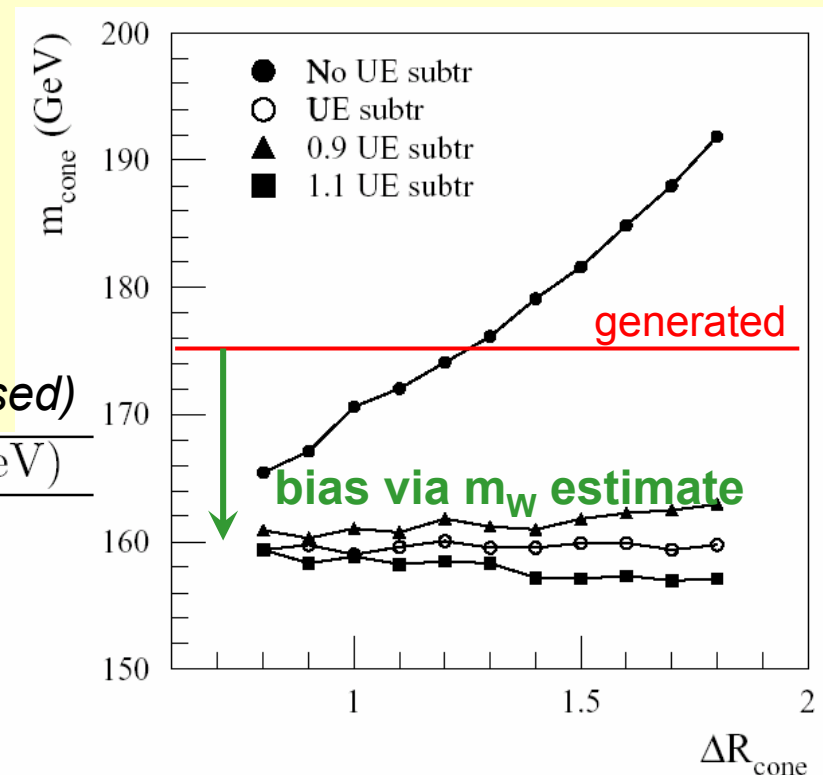
- ✓ back-to-back top pair production (lab-frame) : hence different hemi-spheres
- ✓ less combinatorial background or other background
- ✓ smaller systematics from energy calibration and gluon radiation
- ✓ statistical uncertainty $\Delta m_t \sim 250$ MeV/c²
- 🔥 jet overlapping probability increases \Rightarrow affects jet calibration

❖ **Single lepton plus jets : High p_T sample with $p_T(jjb) > 200$ GeV (Cluster-Analysis)**

ATLAS-COM-PHYS-99-050

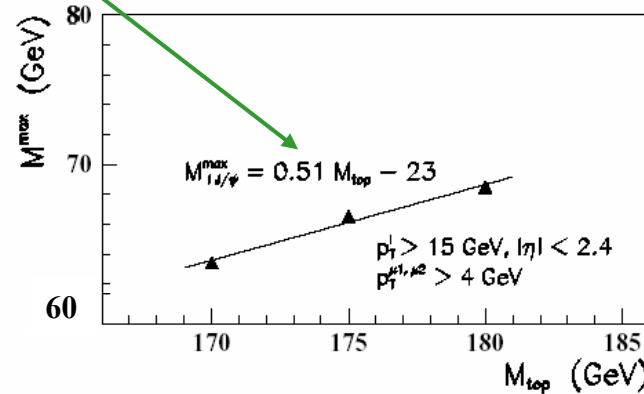
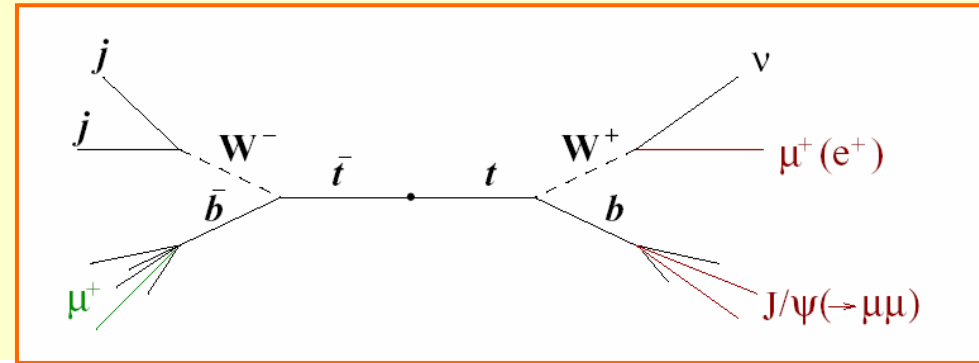
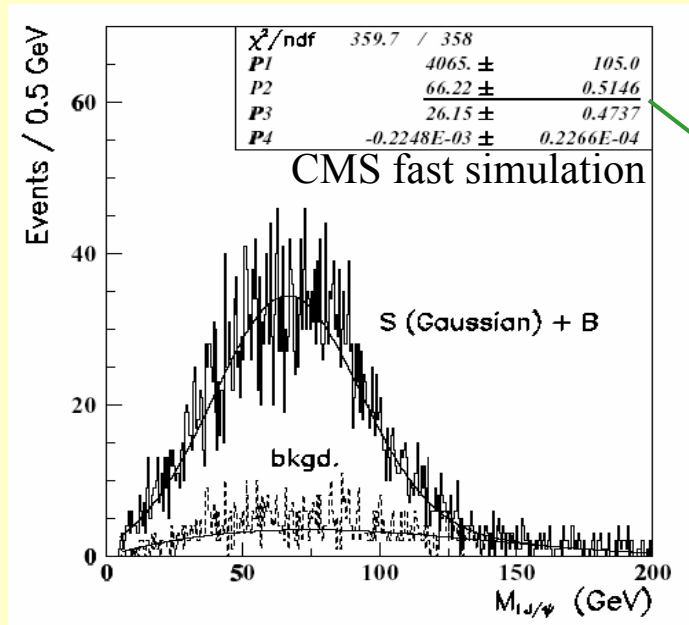
- ✓ collect all energy in a cone around the top direction
- ✓ less sensitive to jet calibration and the jet topology of the event
- 🔥 large dependence on cone size
- 🔥 should subtract underlying event energy
- 🔥 m_W estimate in $t\bar{t} \rightarrow \text{lepton} + \text{jets}$ (data based)

	$ \Delta m_t $ (GeV)	δm_t (GeV)
Initial state radiation	0.7	0.1
Final state radiation	0.3	0.1
b-quark fragmentation	0.3	0.3
UE estimate ($\pm 10\%$)	1.3	1.3
mass scale calibration	0.9	0.9



❖ From $t \rightarrow l + J/\psi + X$ decays :

[hep-ph/9912320](https://arxiv.org/abs/hep-ph/9912320)



- ⇒ 100 fb^{-1} gives after selection $\sim 1,000$ signal events ($S/B > 100$)
- ✓ the large mass of the J/ψ induces a strong correlation with the top mass
- ✓ easier to identify (extremely clean sample)
- 🔴 $BR(\text{overall in } tT) \sim 5.3 \times 10^{-5}$
- ✓ no jet related systematics !!

New method : [hep-ex/0501043](https://arxiv.org/abs/hep-ex/0501043)
 correlate the b transverse decay length with m_t

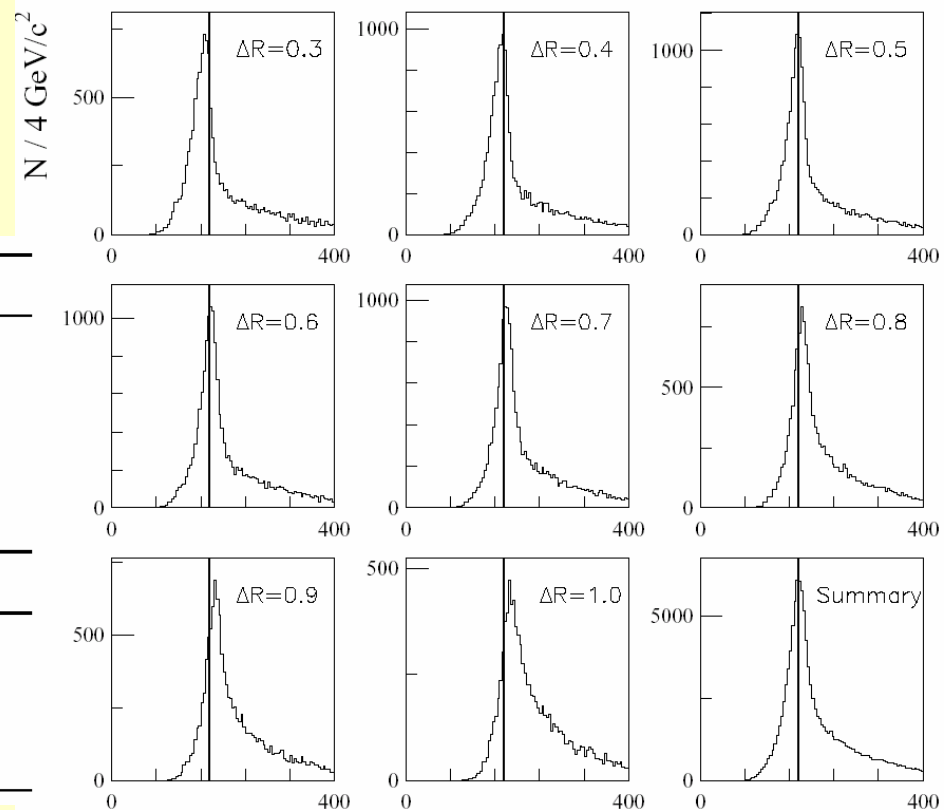
Systematic uncertainties	$\delta M_{t-J/\psi}^{\text{peak}} (\text{GeV}/c^2)$
Final State Radiation	0.15
PDF	0.1
b-quark fragmentation	0.3
Background	0.1
Statistical error	0.5

❖ Continuous jet algorithms :

ATLAS paper hep-ex/0403021

- ⇒ use the same event selection as for the nominal analysis
- ✓ use the cone-based jet clustering algorithm, but scan the hole ΔR range
- ✓ for each event several m_t are determined depending on ΔR
- ✓ let the event itself choose its jet broadness... less sensitive to radiation
- ✓ statistical unc. (10fb^{-1}) $\sim 100 \text{ MeV}/c^2$
- 🔥 systematics : b-jet energy scale

Source	δm_t (GeV)
Range of jet cone sizes	0.25
χ^2 dependence	0.2
Signal and background shape	0.1
ISR and FSR	0.2
External b-jet calibration 1%	0.7
Internal b-jet calibration	
Physics effects	0.13
W signal shape	0.1



3-Jet invariant mass

The $pp \rightarrow t\bar{t}$ process at the LHC : di-lepton channel

❖ Di-lepton channel : $0.4 \text{ Mevt}/10\text{fb}^{-1}$

(Jet-Analysis with m_{lb} , Jet-Energies, Tri-lepton events and Full-reconstruction)

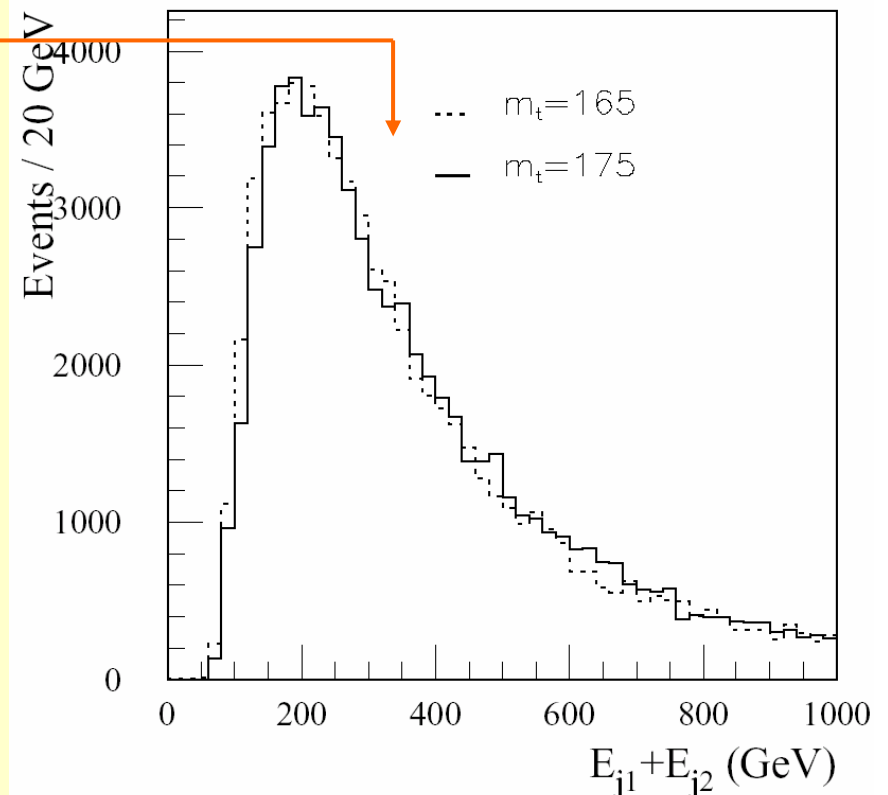
⇒ 10 fb^{-1} gives after selection $\sim 80,000$ signal events ($S/B \sim 10$)

- i. ✓ $m_t^2 = M_W^2 + 2 \langle m_{lb}^2 \rangle / (1 - \langle \cos\theta_{lb} \rangle)$ (high p_T b-tagged jets → 15,000 events)
- ✓ statistical uncertainty $\sim 900 \text{ MeV}/c^2$

🔴 b-quark fragmentation could give large systematics

- ii. ✓ energy distribution of two leading jets
- ✓ match with correct MC distribution
- ✓ statistical uncertainty $\sim 400 \text{ MeV}/c^2$
- 🔴 jet energy calibration $\sim 1.5 \text{ GeV}/c^2$

- iii. ✓ $t \rightarrow l\nu b$ followed by $b \rightarrow l\nu c$
- ✓ invariant mass distribution of the two leptons from the same top decay
- ✓ only about 7250 events
- ✓ statistical uncertainty $\sim 1000 \text{ MeV}/c^2$
- 🔴 systematics from b-quark and ISR and FSR up to $1.5 \text{ GeV}/c^2$

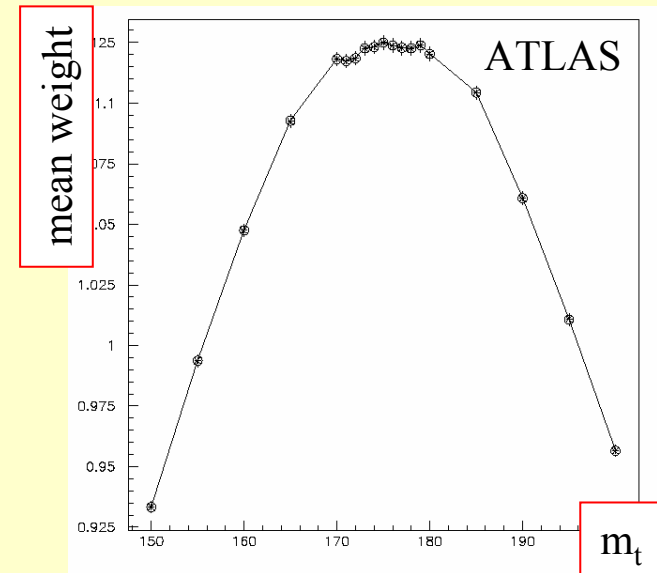


The $pp \rightarrow t\bar{t}$ process at the LHC : di-lepton channel

- iv. ✓ full event reconstruction by assuming a fixed value for the top mass
- ✓ a χ^2 can be determined as a function of this value $m_t \rightarrow \chi^2(m_t)$
- ✓ based on solving a set of equations (kinematic constraints)

- ✓ solution is found in 98% of the selected events
- ⇒ $\delta m_t(\text{stat}) \sim 300 \text{ MeV} (10\text{fb}^{-1})$

- ✓ small systematics due to radiation
(switching on/off ISR/FSR)



source of uncertainty	$ \Delta m_t $ (GeV)	δm_t (GeV)
Statistics and reconstruction method		0.3
b-jet energy scale	0.6	0.6
b-quark fragmentation	0.7	0.7
Initial state radiation	0.4	0.6
Final state radiation	2.7	
Parton distribution function	1.2	1.2

} → 20%

Overview of precision expected for each analysis

CMS notes [1]

ATLAS paper hep-ex/0403021 [2]

LHC Yellow Report on Standard Model Physics [3]

		<u>Stat.Unc.</u> MeV	<u>Syst.Unc.</u> MeV
<ul style="list-style-type: none"> ▪ Single-lepton channel (Full-Analysis) ▪ High p_T single-lepton sample (Jet-Analysis) ▪ High p_T single-lepton sample (Cluster-Analysis) ▪ Single-lepton channel (Continuous jet algorithm) 	[1,2]	100	~1000
	[3]	250	~1000 (?)
	[3]	150	~1500
	[2]	100	~1000
<ul style="list-style-type: none"> ▪ Di-lepton channel (Jet-Analysis with m_{lb}) ▪ Di-lepton channel (Energy-Analysis) ▪ Di-lepton channel (Tri-lepton events) ▪ Di-lepton channel (Full-reconstruction) 	[3]	900	~1300
	[3]	400	~2000
	[3]	1000	~1500
	[2]	300	~1300
<ul style="list-style-type: none"> ▪ From $t \rightarrow l + J/\psi + X$ decays (4 years high lumi) 	[1,2,3]	1000	<1000
<ul style="list-style-type: none"> ▪ High p_T fully-hadronic channel 	[2]	180	>3500

- ❖ combining all those results could lead to a more precise measurement
(correlations to be estimated !!)
- ❖ systematic effects do not necessary overlap between analyses

Expectation : top mass determination better than 1 GeV after understanding the detector

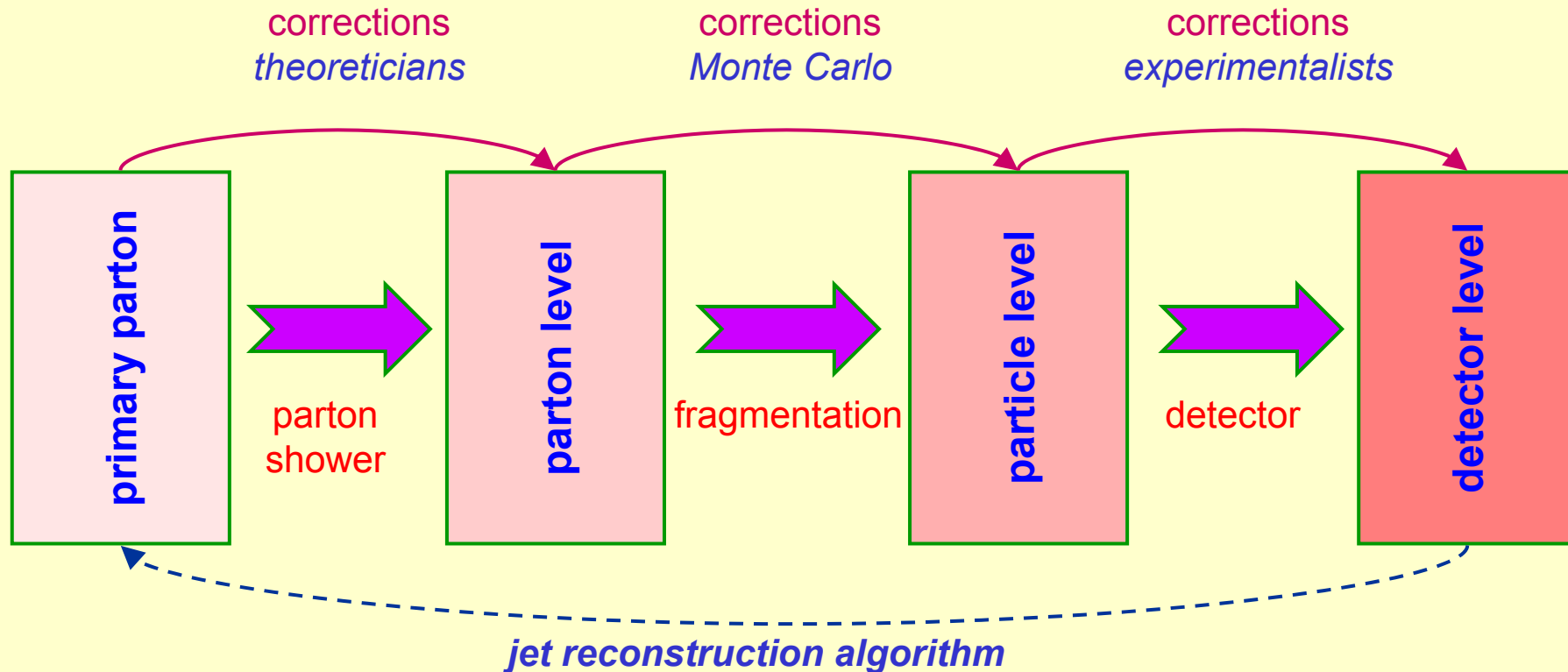
Definition of the systematic uncertainties

- Jet energy scale : *(underlying event, pile-up, jet definition ?)*
 - different mis-calibration coefficients were applied to the jets
 - it was assumed that the jet energy scale is known to the 1% level
 - a difference is made between light and heavy quark jets
- Radiation in the initial and final state (ISR/FSR) : *(procedure ?)*
 - it assumed that our knowledge of ISR/FSR is 10%
 - conservatively 20% of the shift between with-ISR/FSR and no-ISR/FSR was taken (linear rescaling)
- b-quark fragmentation : *(MC tuning issue ?)*
 - described in the fragmentation by the Peterson function (parameter ϵ_b)
 - PYTHIA default $\epsilon_b = -0.006$ with an uncertainty of 0.0025
 - the shift between $\epsilon_b(\text{default})$ and $\epsilon_b(0.0019)$ was taken
- Background :
 - dominated by combinatorial background (S/B is high)
 - estimated by changing the assumed shape in the fit

💣 *list to be updated, refined, unified between experiments, ... discussion !!*

Tevatron paper hep-ex/0005012

- ❖ A jet of particles is a very complex object !!
 - ◆ *and we will see many of these particles*
 - ◆ *jet algorithms can have both theoretical and experimental difficulties*



- ❖ Aim : optimize the resolution on the reconstructed primary parton kinematics
 - ◆ *use several jet clustering algorithms and study their features (cut on differences !!)*
 - ◆ *understand the influence of each step in the production of the detected jet*
 - ◆ *important steps : input object → clustering algorithm → calibration*

❖ Spin correlations

⇒ the top quark does not lose its spin information before it is decaying into W and b

$$\Rightarrow \mathcal{A} = \frac{N(t_L \bar{t}_L + t_R \bar{t}_R) - N(t_L \bar{t}_R + t_R \bar{t}_L)}{N(t_L \bar{t}_L + t_R \bar{t}_R) + N(t_L \bar{t}_R + t_R \bar{t}_L)} \quad \text{with } \mathcal{A} = 0.431 \text{ (gg) and } \mathcal{A} = -0.469 \text{ (qQ)}$$

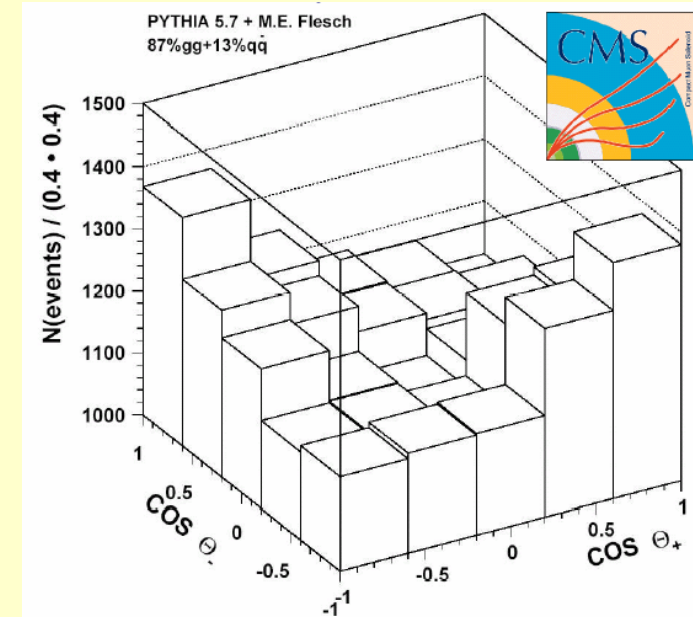
⇒ two observables $\theta^+(\theta^-)$: angle between t(T) direction in the tT c.m. frame and the $\ell^+(\ell^-)$ direction of flight in the t(T) rest frame

⇒ fit to double differential distribution

$$\frac{1}{N} \frac{d^2 N}{d \cos \theta_{\ell^+}^* d \cos \theta_{\ell^-}^*} = \frac{1}{4} (1 - \mathcal{A} \cos \theta_{\ell^+}^* \cos \theta_{\ell^-}^*)$$

⇒ result (30fb^{-1}): \mathcal{A} (stat) = 0.035 and \mathcal{A} (syst) = 0.028

ATL-PHYS-2003-012 : similar results from ATLAS



❖ Measuring the difference between m_t and m_T

⇒ almost all systematics cancel when taking the difference between both

⇒ after several years the precision could be around 50 MeV

⇒ get theorist to work what we could learn from that ?

⇒ differences between t and T can learn us something about the PDF's (rapidity distributions)

⇒ other differences between t and T (CP violation ?) *identify them !!!*

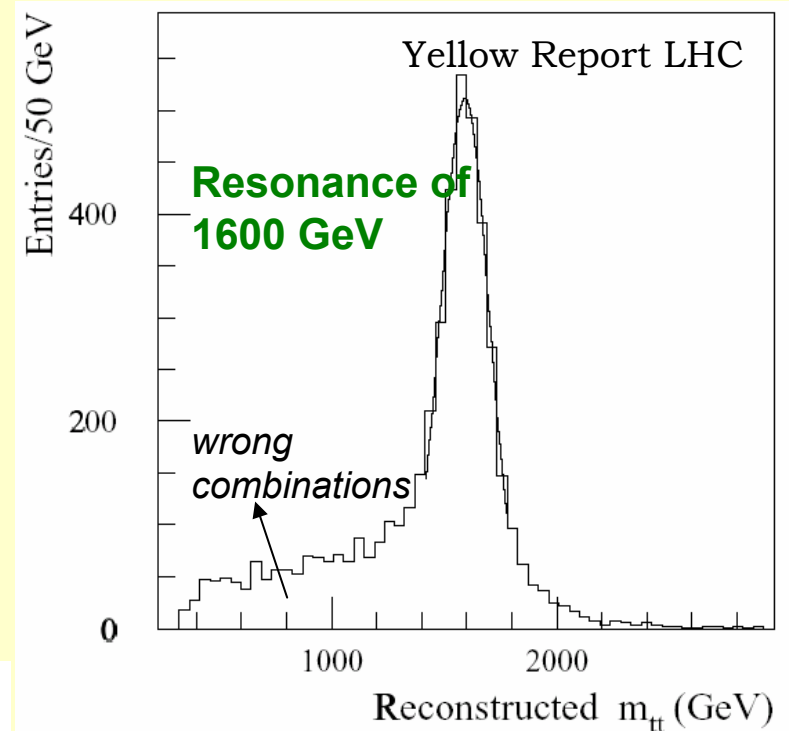
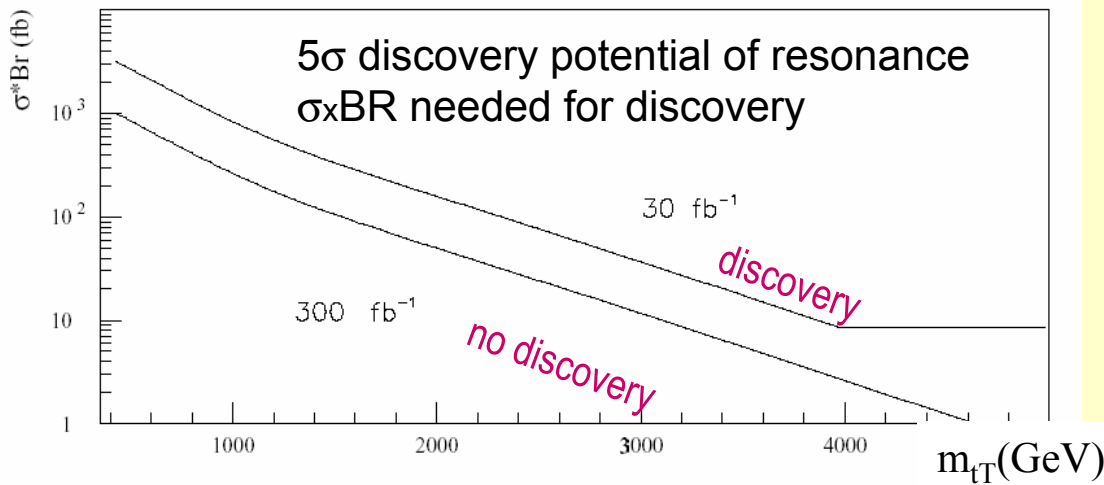
❖ A lot more when we differentiate the selected events in phase-space !!

⇒ search for resonances in the $d\sigma_{tT}/dM_{tT}$ spectrum

- **SM** : BR(H → tT) too small to be visible above continuum tT production (Γ_H too large)
- **MSSM** : if $M_{H,A} > 2m_t$ then BR(H/A → tT) ≈ 100 % for $\tan\beta \approx 1$
- **Technicolor models** : in some models heavy particles decaying to tT

- selection of lepton plus jets channel
- precise kinematic reconstruction : $\delta m_{tT}/m_{tT} \sim 6.6\%$

For a random resonance :
(choose jet combination which match best the tT event kinematics)



❖ **If extra-dimensions exist and TeV-scale gravity models are correct**

- top quarks will be produced from the decay of black holes via Hawking Radiation hep-ph/0205199
- $\Delta m_t = 0.28 \text{ (stat)} \oplus 0.5 \text{ (syst)} = 0.57 \text{ GeV}$ (LHC using 10 fb^{-1})
- Yukawa coupling via single top production
$$\text{BR}(t \rightarrow tH) = 0.046 y_t^2 / |V_{tb}|^2$$
improvement (30 fb^{-1}) from 16.2% till 2.7%
- ... but mixing up a lot of unknowns

❖ **Get jet calibration from W mass constraint**

- the selected event sample can be very clean
- the jets assigned to the W can be associated in a clean way
- a kinematic fit of the full event can be exploited
- enough jets left to estimate $E^{\text{rec}}/E^{\text{gen}}$ as a function of observables

- use half of the events for calibration and the other half for measurements

⇒ *first results by ATLAS, soon expected by CMS*

❖ **Get b-tag efficiency out of data rather than MC**

- extremely interesting for $H \rightarrow b\bar{b}$ searches
- a clean b enriched jet sample can be extracted from data (purity > 95%)
- apply the b-tag method and count how much jets remain...

⇒ *first analysis by CMS, preliminary results soon*

- ❖ **standard and alternative methods have been exploited for mass measurement**
 - dominated by systematic uncertainties → definition of systematic uncertainties
 - optimize the analysis results by reducing systematic uncertainties
 - design procedures to combine and compare results between CMS/ATLAS

- ❖ **other standard physics parameters to be measured**
 - cross-section and differential cross-sections: MC@NLO
 - spin correlations : which generators are applicable
 - top quark width... any interest ? can we use MC@NLO for this ?

- ❖ **new ideas**
 - differences between top and anti-top quark $t \leftrightarrow \bar{t}$ (reduced systematics)
 - more alternative methods... ?
 - signals of models beyond the Standard Model and rare decays

- ❖ **providing information for general reconstruction tools**
 - b-tagging efficiency and jet energy calibration (light quark jets)

- ❖ **key issues to be successful** (almost clean samples)
 - definition of the jet, radiation effects, jet combinations, ...

- ❖ **possibly much more...**