

- MathLib work package from ROOT SEAL merge
- new proposed structure for Math:
 - *MathCore* and *MathMore* libraries
- new Vector package for 3D and LorentzVector
- Random, Linear Algebra and Fitting
- Conclusions



ROOT MathLib Work Package

- Work package from ROOT-SEAL merge
 - people: Andras Zsenei, Anna Kreshuk, Lorenzo Moneta, Eddy Offermann
 - contribution also from Fermilab: Mark Fischler and Walter Brown
- Main responsibilities for this work package:
 - Basic Mathematical functions
 - Functions and Fitting
 - Random Numbers
 - Linear Algebra
 - Physics and geometry Vectors (3D and 4D)
- Not considered now, but still relevant :
 - Histograms
 - Statistics (confidence level)
 - Neural Net, multivariate analysis, etc..

Current Math Libraries



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New Math Libraries





MathCore

- CVS repository *mathcore* with basic functionality
- build-able as a standalone library (*libMathCore.so*)
 - no dependency on others ROOT packages or external libraries
- in ROOT is inside *libCore* for convenience
- content of MathCore:
 - Basic and common used mathematical functions
 - Random numbers
 - Basic numerical algorithms
 - 3D and LorentzVectors
- will not use algorithms from GSL
 - for ROOT we need to be distributed with free license
 - and the GSL is based on the GPL (restricted) license

MathMore

- will include more mathematical functions
 - less used special functions (i.e. Bessel)
- additional and more sophisticated algorithms
 - will use interface defined in MathCore
 - we will start putting there the C++ wrapper to GSL, which are now in SEAL
 - See http://seal.web.cern.ch/seal/MathLibs/MathCore/html/index.html
 - use GSL and build library together
 - will include tar file with the needed GSL functions in CVS
 - use similar procedure to existing one in ROOT (freetype, libAfterImage)
 - GSL interfaces are not exposed to the users
- repository for needed and useful extra Math functionality
 - could include other useful math libraries

Lorenzo Moneta,

Proposed new structure

- Core Mathematical Library: MathCore
- An extended library: *MathMore*



Special Functions

- most common and basic functions in MathCore
 - gamma functions
 - tgamma with log (Igamma) and incomplete Gamma
 - Error functions (erf and erfc)
- other less used functions will be in MathMore
 - use same namespace, it will be transparent for the user
- Implement the functions using proposed interface to the C++ standard
 - as it is currently done in SEAL

```
namespace ROOT {
  namespace Math {
    double cyl_bessel_i (double nu, double x);
    .....
  }
  use GSL for the functions present in MathMore
```

Statistical Functions

- Probability functions used in statistics
 - Many of these functions are computed using the gamma and error functions
 - those can be in *MathCore*
- We will have a consistent set of:
 - Probability distributions (pdf)
 - Gaussian, BreitWigner, Gamma, Chi2, Landau,...
 - Cumulative distributions (cdf)
 - Iower and upper integrals of each pdf we provide
 - Inverse of each cdf
- Provide also functionality to generate randoms according to these pdf's
- Have also pdf C++ classes to be used for fitting

Numerical Algorithms

some basic numerical algorithms for

- adaptive integration, differentiation, interpolation, root finders, simple minimization (1D)
- define interface for these algorithms and have implementations in *MathCore* or/and *MathMore*
 - start defining interfaces and API for the algorithms
 - import SEAL implementations based on GSL in *MathMore*
 - move what is in ROOT (from TF1) in *MathCore*
 - adapt TF1 to use new classes
- have more sophisticated and less used algorithms in *MathMore*
 - MonteCarlo integration, Differential Equations, FFT

Physics and Geometry Vectors

- Classes for 3D Vectors and LorentzVectors with their operations and transformations (rotations and boosts)
 - specialized vector for geometry and kinematics and not generic Linear Algebra Vectors
- Merge functionality from ROOT Physics classes and CLHEP Vector and Geometry packages
- A new prototype with API available since one month
 - work in collaboration with Fermilab computing group (Mark Fischler and Walter Brown)
 - contribute in reviewing the code, provide some of the implementations and the tests
- Developments done in contact with the LHC experiments
 - re-use some ideas from CMS Common Vector package
 - had useful discussions with some representative from the 4 LHC experiments

New Vector Classes

- Have minimal interfaces (and possibly stable)
 - minimal number of methods and try to avoid duplications
 - no x() and getX() like in CLHEP
 - no single setter methods (setX() or setPhi())
 - Separate extra functionality in global functions in a namespace
 - deltaR(v1,v2), invariantMass(q1,q2)
 - template functions which can work with any Vector type with the pre-requisite:
 - implements a well defined set of coordinate accessors:
 - x(), y(), z(), r(), phi(), theta(), eta(), etc....
 - with the current interface works with CLHEP vectors

New Vector classes properties

- New classes template on the scalar type
 - Vector based on single precision (float) to decrease memory usage and for persistency
- Generic Coordinate type
 - describe the Coordinates concept as a type
 - have Vectors based on the coordinate system type:
 - can have Vectors represented by cartesian (x,y,z), polar (r, theta,phi) or cylindrical coordinates (rho, eta, phi)
 - express this as a template parameter on the Vector
 - *PositionVector3D<double, Cartesian3D>*
 - PositionVector3D<double, Polar3D>
 - allow conversions and operations between mixed vectors
 - can improve performances in some use cases
 - some representation can be optimal for persistency

New Vector classes properties (2)

Points and Vector distinction

- have in the geometry case (3D) different classes for Points and Vectors:
 - PositionVector
 - rotate and translate
 - cannot be added and their difference results in a DisplacementVector
 - DisplacementVector
 - only rotate
 - have cross and dot multiplications
- This distinction is present in the CLHEP Geometry
 - but using a common base class
- No need to have this separation for LorentzVectors
 - used in kinematics (DisplacementVectors in 4D)

Rotations and Transformations

• 3D Rotations

- describe them according to different representations:
 - 3x3 orthogonal matrix representation (9 numbers)
 - 3 Euler angles
 - Direction Axis (Vector) + angle
 - could add also quaternion (4 numbers)
- generic rotation is template on the representation type
- LorentzRotations (Boost + 3D Rotations)
 - described by a 4x4 matrix
 - symmetric 4x4 in the case of pure Boosts
- 3D Transformations (3D Rotations + Translation)
 - described as a 3D Rotation + 3D Vector
 - have interface to look like a 4x4 matrix (as CLHEP)

Examples of usage: LorentzVector

- we have Lorentz Vectors based on
 - Cartesian4D (x,y,z,t) or (px,py,pz,E)
 - CylindricalEta4D (pt, eta, phi, E)
 - EEtaPhiMSystem (E, eta, phi, M)
 - and we could have more type of system (flexible to extend)
 - one based on px,py,pz, M to avoid some numerical problems (electrons at LHC)
- template class on scalar type and Coordinate type
- use typedef's to hide template complexity to the users
 - typedef BasicLorentzVector<double, Cartesian4D> LorentzVector;
 - typedef BasicLorentzVector<double, CylindricalEta4D> LorentzVectorPtEtaPhiE;

LorentzVector Example

Constructors

LorentzVector v0; // create an empty vector (x=y=z=t=0) LorentzVector v1(1,2,3,4); // create a vector (x=1, y=2, z=3, t=4) LorentzVectorPtEtaPhiE v2(1,2, M PI,5); // create a vector (pt=1,eta=2,phi=PI,E=5)

LorentzVectorPtEtaPhiE v3(v1); // create from a Cartesian4D LV CLHEP::HepLorentzVector q(1,2,3,4); LorentzVector v3(q) // create from a CLHEP LV

Accessors

double x = v1.x() = v1.px(); double t = v1.t() = v1.e(); double eta = v1.eta(); XYZVector w = v1.vec(); //have both x() and px()
// have both t() and e()

//return vector with spatial components

Operations

v1 += v2; v1 -= v2; v3 = v1 + v2; v3 = v1 - v2; double a; v1 *= a; v1 /= a; double p = v1.dot(v2); // additions and subtructions

//multipl. and divisions with a scalar
//prefer dot (less ambiguous)

Connection to Linear Algebra

- Some experiments require easy connection/conversion
 - between 3D/4D Vectors and Linear Algebra Vectors
 - between 3D/4D Rotations and Linear Algebra matrices
- Avoid direct dependency on any LA package
- Proposed solution:
 - construct and assignment using template member functions for LA objects implementing the operator[]
 - store vector and rotation data in a C array :
 - construct/assign from C array pointers (double *)
 - return a C array pointer
 - able to use Vector/Rotation content in a LA package
 - ROOT Linear Algebra allows to create matrices by copying the data or by using the data

Linear Algebra Example

From a Linear Algebra Vector TVectorD a(3); // ROOT Linear Algebra Vector XYZVector v1(a,0); // construct vector from x=a[0], y=a[1], z=a[2]
<pre>double *dd = a.GetMatrixArray(); XYZPoint pl(dd); // construct point from x=a[0], y=a[1], z=a[2]</pre>
TVectorD b(N); //ROOT Linear Algebra Vector containing many vectors
XYZVector v2(b, INDEX); // construct vector from x=b[INDEX], y=b[INDEX+1],
HepVector c(4); //CLHEP Linear algebra vector
LorentzVector q(c,0); // construct using px=c[0], py=c[1], pz=c[2], E=c[4] To a Linear Algebra Vector
XYZVector v(x,y,z); double *pp = v.coordinates().data();

TVectorD t(3,pp); //create a new Linear Algebra vector copying the data

TVectorDw;w.Use(3,p);// fill an existing Vector using the data (no copying)

Note that ROOT Linear Algebra Object can use external data storage

Lorenzo Moneta,

Vector Performance Tests

- comparison between CLHEP, ROOT and new classes for LorentzVector's
 - better results than ROOT because a 4D Vector is not now based on a 3D object
 - factor of 2 improvements in additions of LorentzVectors
 - performance improvements if used optimal coordinate system when needed
 - Example: DeltaR for a large set of Vectors
 - some order of magnitude in speed improvements

I/O tests

- some performance obtained with TLorentzVector if TObject stream is ignored for TLorentzVector
 - otherwise performance improvement ~ 20%

Current Status

Current proposed version available for feedback:

http://seal.web.cern.ch/seal/MathLibs/GenVector/0-1-0/html/index.html

Main Page | Namespace List | Class List | Directories | File List | Namespace Members | Class Members | File Members | Related Pages

Proposal for a new Vector Package

0_1_0

Generic Vectors for 2, 3 and 4 dimensions

This is a proposal for a new vector package, **GenVector**, describing vectors and their operations in 2, 3, and 4 dimensions. The 4 dimensional space is used for describing relativistic particles. These vectors are different from generic vectors of the Linear Algebra package which describe N-dimensional vectors. The functionality of this package is currently provided by the CLHEP <u>Vector</u> And <u>Geometry</u> packages and the ROOT <u>Physics Vector</u> classes (Tvector2, TVector3 and TLorentzVector). It is also re-uses concepts and ideas from the CMS <u>Common Vector package</u>. The main characteristics of this package are :

Minimal interface

We define a minimal interface trying to avoid duplications in contrast to what is currently provided by the Vector package of CLHEP.

Lorenzo Moneta,

LCG Application Area meeting, 8 June 2005 21

Vector Feedback

- asked for feedback to LHC experiments and also ROOT users
- Received very useful comments
 - requested connection to Linear Algebra
 - representation based on px,py,pz, m instead of E to avoid negative masses when E >> m
 - have well defined set of accessors like x(),y(),z()
 - like that to have generic helper functions which can then be used by the experiment classes
 - want some compatibility (inter-operability) with CLHEP for a smooth migration
 - have also concept of coordinate errors for providing error propagation in the operations
 - use quaternion to represent rotations

Some Open questions

- Error handling (related to all Math libraries)
 - what to do with Nan and infinities
 - Proposed solution:
 - throw exception
 - In the Vectors have a a simple exception class deriving from std::runtime_error
 - Returning a Nan to the user could be OK for a simple user application but NOT for a reconstruction job
- Naming convention for member functions
 - need to decide on names like x() or X() ?
 - advantage of having same signature as CLHEP will provide some inter-operability
 - for ROOT users the TLorentzVector and TVector3 classes will not disappear
 - will be implemented as proxy to new classes

Future Work for Vectors

- Solve open issues and finalize implementations
 - take into account the feedback received
- Move in the ROOT CVS directory
 - Module.mk for building already exist
 - need to integrate also the tests
 - Preferable to have them in same location as the code in a tests sub-directory
 - solve some remaining problems in generating CINT dictionary for some template member functions
- Should be ready for first ROOT 5 release at the end of the month

Random Numbers

- Merge CLHEP and ROOT Random number classes
- CLHEP and ROOT have a different design
 - ROOT has a common base class for all the engines and defining also the distributions
 - easier to use (no need to create separate classes)
 - CLHEP separates distribution classes from engine classes
 - easier to extend if user wants to add new distributions
 - distributions classes can have a state
- New design has been proposed to the C++ standard
 - Fermilab people are implementing a first version of this new library
 - need to evaluate it and try to re-implement the TRandom classes using the new library

New C++ Random Numbers

 design based on generic engine classes and distributions

• define engine using template parameters:

typedef mersenne_twister<double,32,624,....> mt19937

```
typedef subtruct_with_carry_01<double,48,10,24>
ranlux64_base_01
```

Distribution classes template on value type:

```
uniform_real<T>, exponential_distribution<T>,
normal_distribution<T>
```

• class variate_generator<Engine,Distribution> to generate the random numbers:

```
mt19937 engine(seed);
uniform_real<double> dist(xMin,xMax);
variate_generator<mt19937, uniform_real<double> > r(engine, dist);
// generate random number xMin < x < xMax
double x = r();
```

rather complex for end-users (should not be exposed)

Linear Algebra

- Proposal is to base on ROOT Linear Algebra
- Functionality in ROOT Linear Algebra
 - decompositions for solving LA systems
 - support for sparse matrices
 - support for external data storage
 - pre-allocation on the stack up to 6x6 matrix and optimized inversion
- Consider to move in the long term to template classes for double/float matrices
- Continue detailed evaluation with new LA packages
 - decide if need later a standalone library optimized for small matrices
 - follow evolution of new GLAS (Boost) project

Fitting and Minimization

- Import new C++ Minuit from SEAL in ROOT
 - contains all minimizer (Migrad, Simplex) and in addition the Fumili algorithm
 - have already a class which implements TVirtualFitter
 - complete with support for Fumili
 - it could be migrated soon
 - evaluate/merge with minimizer package from Fermilab
- Improve ROOT fitting and minimization interfaces
 - current interfaces are too much adapted to old Fortran Minuit API
 - have a more generic interface to satisfy requirements from different minimizers and fitting algorithms
 - new linear and robust fitters
- work is on-going on importing the RooFit package

Conclusions

- Have first version of MathCore and MathMore libraries
 - Vectors, math functions and basic algorithms for the first ROOT 5 release (end of June)
 - first proposal for Vector package already exists
 - fruitful collaboration with CLHEP editors (M.F.)
 - received feedback from experiments and ROOT users
 - any other comment or feedback is still highly desirable
- Later activities:
 - Evaluate new C++ standard Random number
 - decide if to use for re-implementing ROOT Random
 - detailed evaluation of the Linear Algebra
 - improve ROOT Fitting and import RooFit and new C++ Minuit

References

- Special functions C++ proposal
 - link to C++ extension draft (includes Random proposal)
 - http://www.open-std.org/jtc1/sc22/wg21/docs/papers/2004/n1687.pdf
- Statistical functions proposal (for Boost)
 - http://www.open-std.org/jtc1/sc22/wg14/www/docs/n1069.pdf
- SEAL Math inventory
 - http://seal.web.cern.ch/seal/snapshot/workpackages/mathlibs/mathTable.html
- SEAL MathCore reference doc (GSL C++ wrappers)
 - <u>http://seal.web.cern.ch/seal/MathLibs/MathCore/html</u>
- Proposal for new Physics Vectors
 - http://seal.web.cern.ch/seal/MathLibs/GenVector/0-0-2/html/index.html