

# Quark Gluon Plasma Physics

---

Johanna Stachel

Physikalisches Institut, Universität Heidelberg  
CERN Summer Student Program - July 25 and 26, 2005

---

- Lecture I: Dense Matter and the Quark-Gluon Plasma
- Lecture II: Statistical Hadron Production
- Lecture III: Heavy Quarks and Jets as Probes of the QGP

Lectures assembled in collaboration with Peter Braun-Munzinger

# Lecture I: Dense Matter and the Quark Gluon Plasma

---

Johanna Stachel, Universität Heidelberg, Germany

## Outline:

- Introduction, historical remarks
- Early universe
- Critical temperature and density
- The phases of strongly interacting matter
- Results from lattice QCD
- Making strongly interacting matter in nuclear collisions
- Survey of experiments

# Historical Remarks

---

- Pomeranchuk 1951: finite hadron size  $\rightarrow$  **critical density**  $n_c$ .  
Dokl. Akad. Nauk. SSSR 78 (1951) 889.
- Hagedorn 1965: mass spectrum of hadronic states  $\rho(m) \propto m^\alpha \exp(m/B)$   
 $\rightarrow$  **critical temperature**  $T_c = B$ .      Nuovo Cim. Suppl. 3 (1965) 147.
- QCD 1973: **asymptotic freedom**      **Nobelprize 2004**  
D.J. Gross, F. Wilczek, Phys. Rev. Lett. 30 (1973)1343  
H.D. Politzer, Phys. Rev. Lett. 30 (1973) 1346.
- asymptotic QCD and **deconfined quarks and gluons**:  
N. Cabibbo, G. Parisi, Phys. Lett. B59 (1975) 67.  
J.C. Collins, M.J. Perry, Phys. Rev. Lett. 34 (1975) 1353.
- first perturbative corrections to ideal gas: Baym, Chin 1976, Shuryak 1978
- since 1980 new phase was called **Quark-Gluon Plasma (QGP)**: excitations are quark/gluon quasiparticles plus collective plasmon modes (similar to QED plasma)

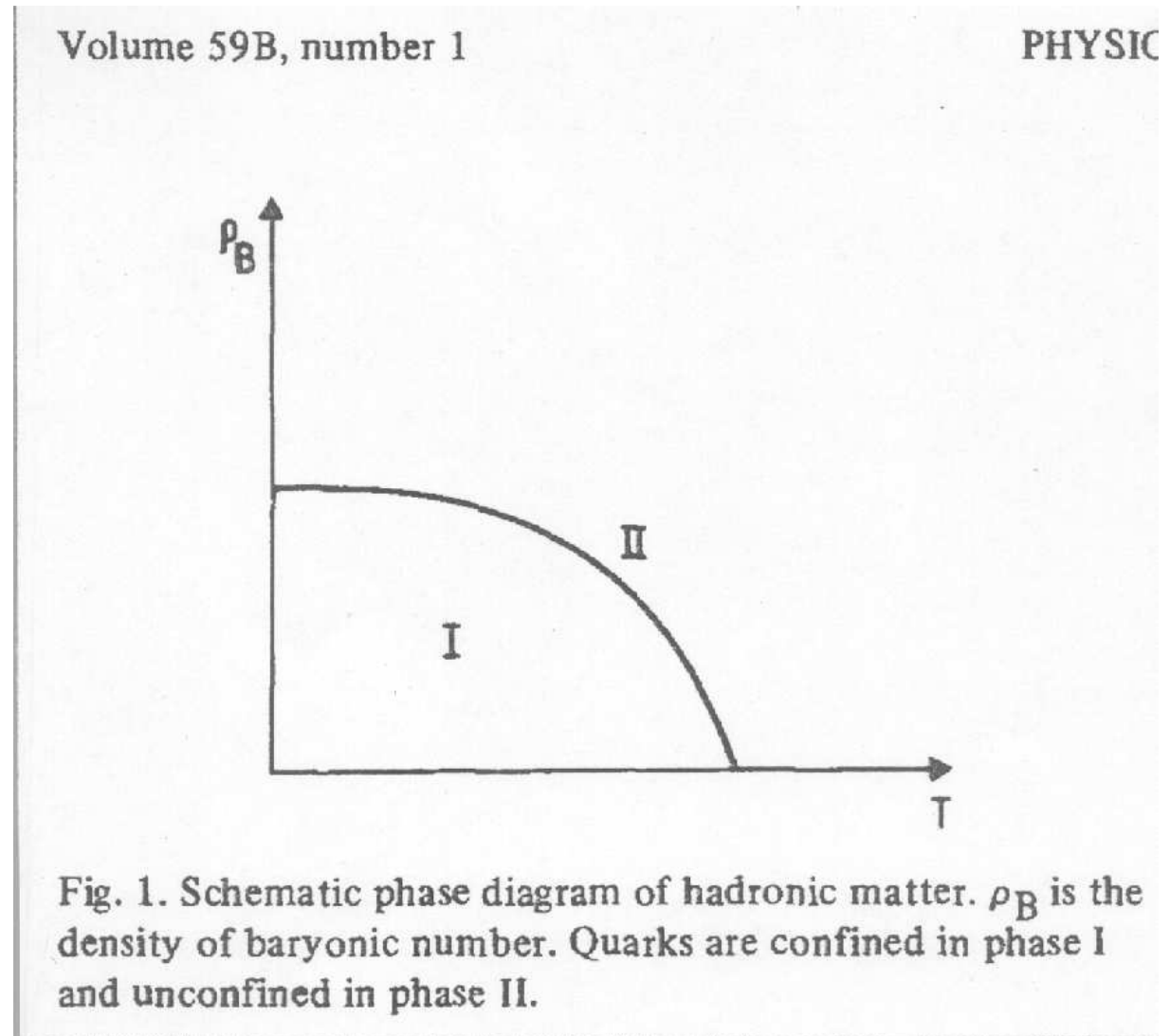
# First Phase Diagram

Cabibbo/Parisi PL(1975)

more refined:

G. Baym 1983, see also

Nucl.Phys. A698 (2002)xxiii

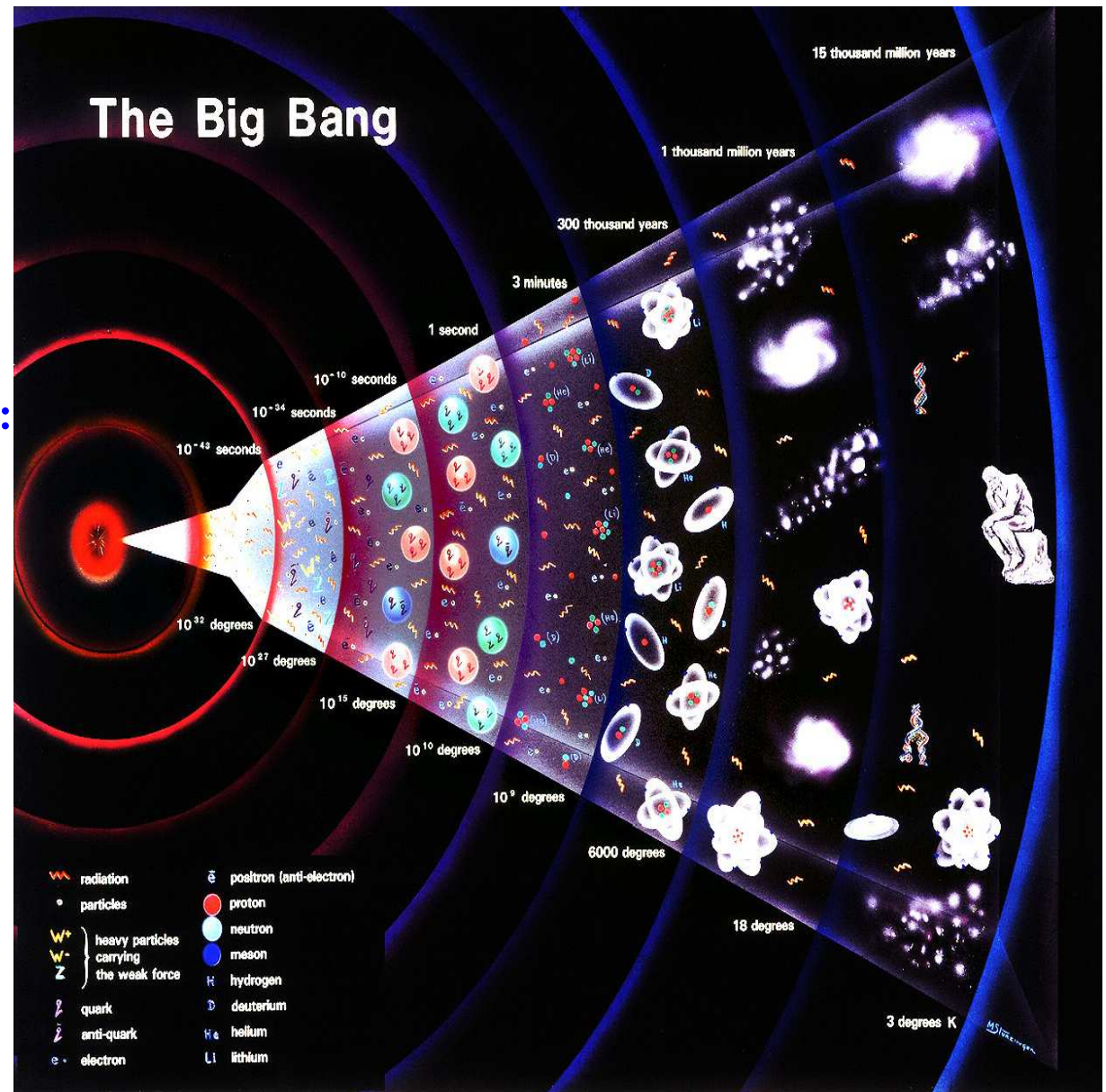


# Evolution of the Universe

from the big bang to galaxies

$10^{-5}$  s after big bang:  
phase transition from quarks  
and gluons to hadronic matter

temperature at phase transition:  
 $T \approx 2 \cdot 10^{12} \text{K} = 200 \text{ MeV}$



# Simple Estimates of critical conditions

---

1. deconfinement at high temperature (a la Polyakov 1978):

$$T = 0$$

energy of color string  $E_{q\bar{q}}(\mathbf{r}) = \sigma r$

with string tension  $\sigma \approx 1 \text{ GeV/fm}$

$$T > 0$$

$$\begin{aligned} \text{free energy of string } F_{q\bar{q}}(L) &= E_{q\bar{q}}(L) - T S(L) \\ &= \sigma L - T \ln N(L) \\ &= (\sigma - T/a \ln 5)L \\ &= \sigma_{eff}(T) L \end{aligned}$$

with number of string configurations:  $N(L) = 5^{L/a}$

and typical stepsize  $a =$  string thickness  $\approx 0.3 \text{ fm}$

critical temperature when  $\sigma_{eff}(T)=0$

$$\rightarrow T_c = \frac{1\text{GeV} \cdot 0.3\text{fm}}{\text{fm} \ln 5} = 185 \text{ MeV}$$

## 2. at high baryon density:

- normal nuclear matter:

$$\text{baryon density } \rho_0 = \frac{A}{4\pi/3R^3} = \frac{1}{4\pi/3r_0^3} \approx 0.16 \text{ /fm}^3$$

with  $r_0 = 1.15 \text{ fm}$

- if nuclei are compressed, eventually nucleons start to overlap

nucleon charge radius  $r_n = 0.8 \text{ fm}$

$$\rightarrow \rho_c = \frac{1}{4\pi/3r_n^3} \approx 0.47/\text{fm}^3 = 3 \rho_0$$

- more stringent:

pressure of quark-gluon bubble has to sustain  
vacuum pressure

at  $T=0$  with bag constant  $B = 0.2 \text{ GeV}/\text{fm}^3$

$$\rightarrow \mu \geq 0.42 \text{ GeV}$$

critical net quark density  $n_q - n_{\bar{q}} \geq 1.9/\text{fm}^3$

$$\rightarrow \rho_c = 1/3(n_q - n_{\bar{q}}) \geq 0.64 = 4\rho_0$$

# Hagedorn's Limiting Temperature

---

all thermodynamical quantities diverge at  $T_{limit}$

(R. Hagedorn, Suppl. Nuovo Cim. 3 (1965) 147)

assume  $\rho_m \propto (m_0^2 + m^2)^{-5/4} \exp(m/b)$

take energy density of hadron gas,  $\epsilon(T)$

$$\epsilon(T) = \sum_{m_\pi}^M \epsilon(m_i, T) + \int_M^\infty \epsilon(m, T) \rho(m),$$

but for large masses  $m > M$ ,  $\epsilon(m, T) \propto \exp(-m/T)$

→ integral diverges if  $T > b$



# Hagedorn's Limiting Temperature

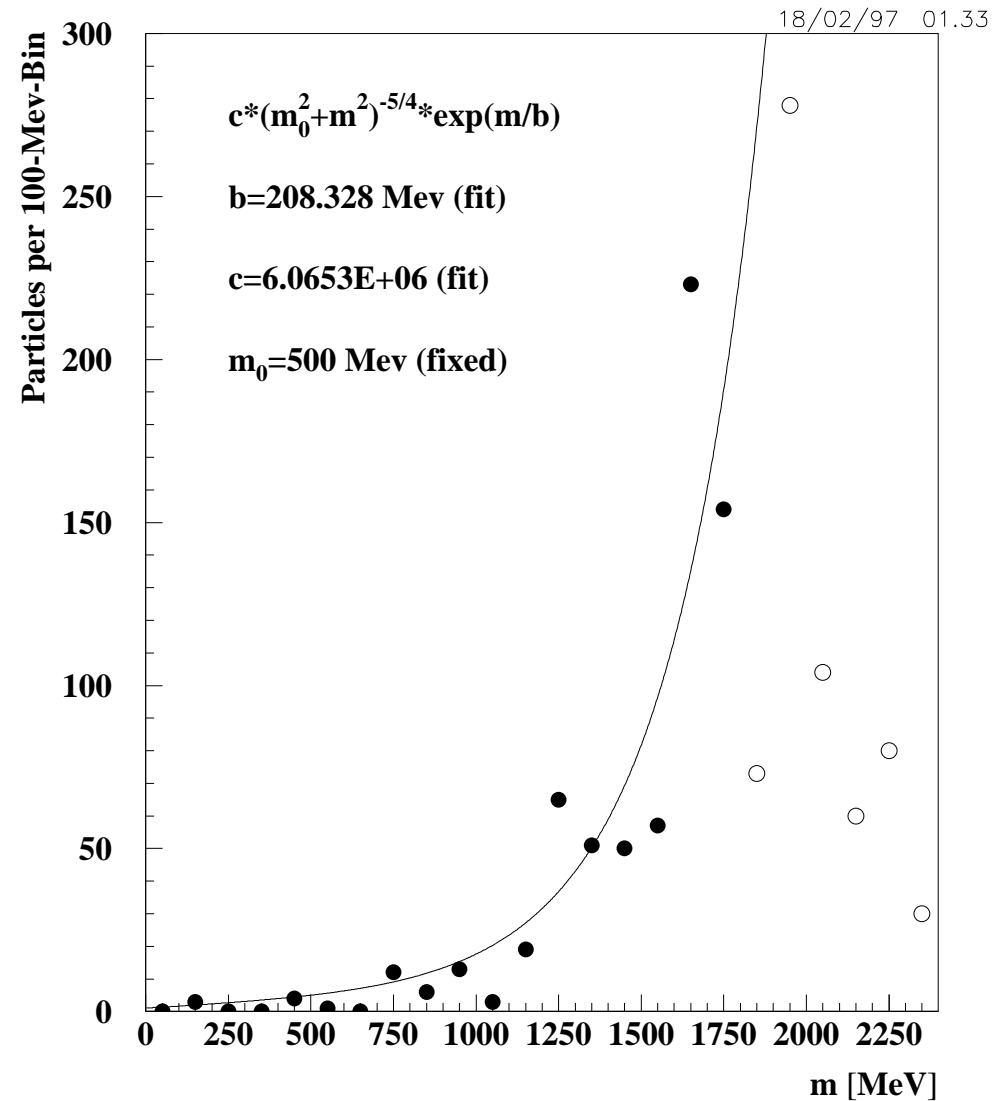
hadronic mass spectrum as of 1997

fit with

Hagedorn mass formula

$$\rho_m \propto (m_0^2 + m^2)^{-5/4} \exp(m/b)$$

$$b = T_{limit} = 200 \pm 30 \text{ MeV}$$



# Simple Construction of Phase Transition

---

**Basis: MIT bag model with bag constant  $B$**

$B$  is energy density of QCD vacuum (see above)

energy density of quark-gluon matter:  $\epsilon = \epsilon_{thermal} + B$

pressure:  $P = 1/3 (\epsilon - 4 B)$

with  $\epsilon_{thermal} \propto n_{thermal}^{4/3}$  and  $P = n^2 \partial(\epsilon/n) / \partial n$

note: at  $T = 0$ ,  $P = -B!$

energy density (pressure) of hadron gas:

sum up energy density (pressure) due to each particle

**Gibbs criterion for phase transition:**

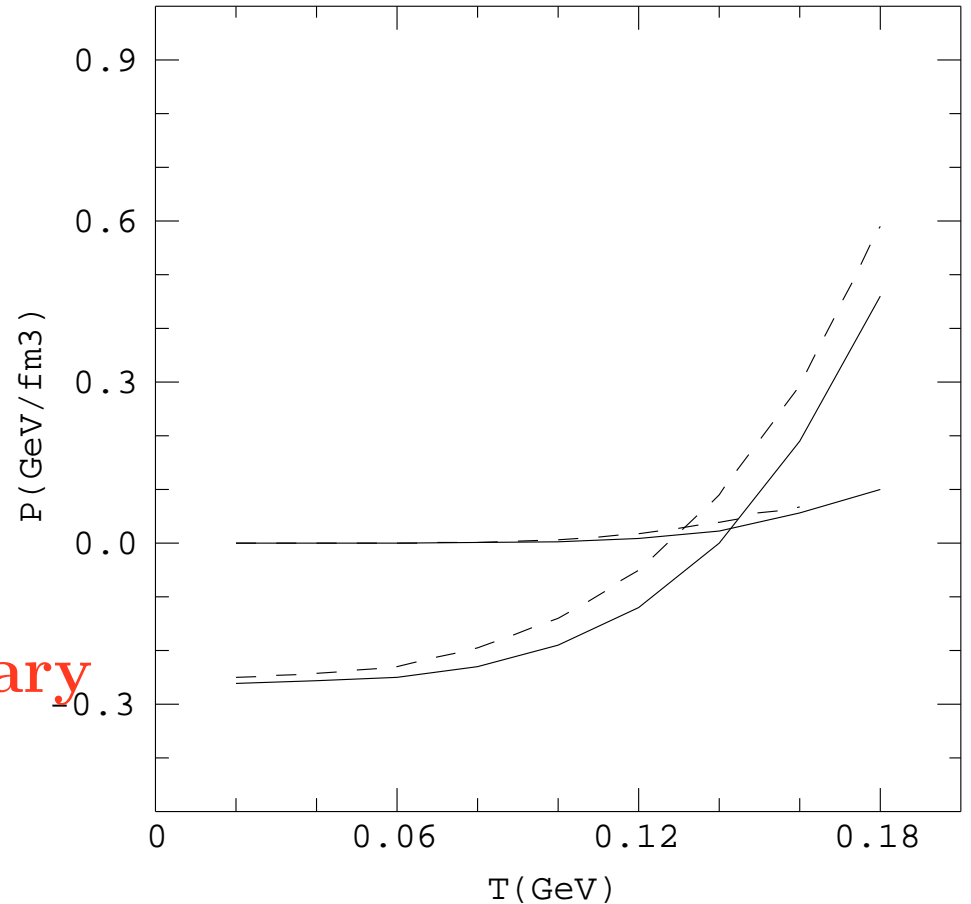
$$P_{had} = P_{QGP} \text{ and } \mu_{had} = \mu_{QGP}$$

# Constructing the Phase Boundary

compute  $P$  as above and  
look for the crossing points  
first order phase transition  
by construction  
 $B = 250 \text{ MeV}/\text{fm}^3$   
from lattice QCD  
determination of the phase boundary  
in the  $T - \mu$  plane

solid lines:  $\mu = 170 \text{ MeV}$

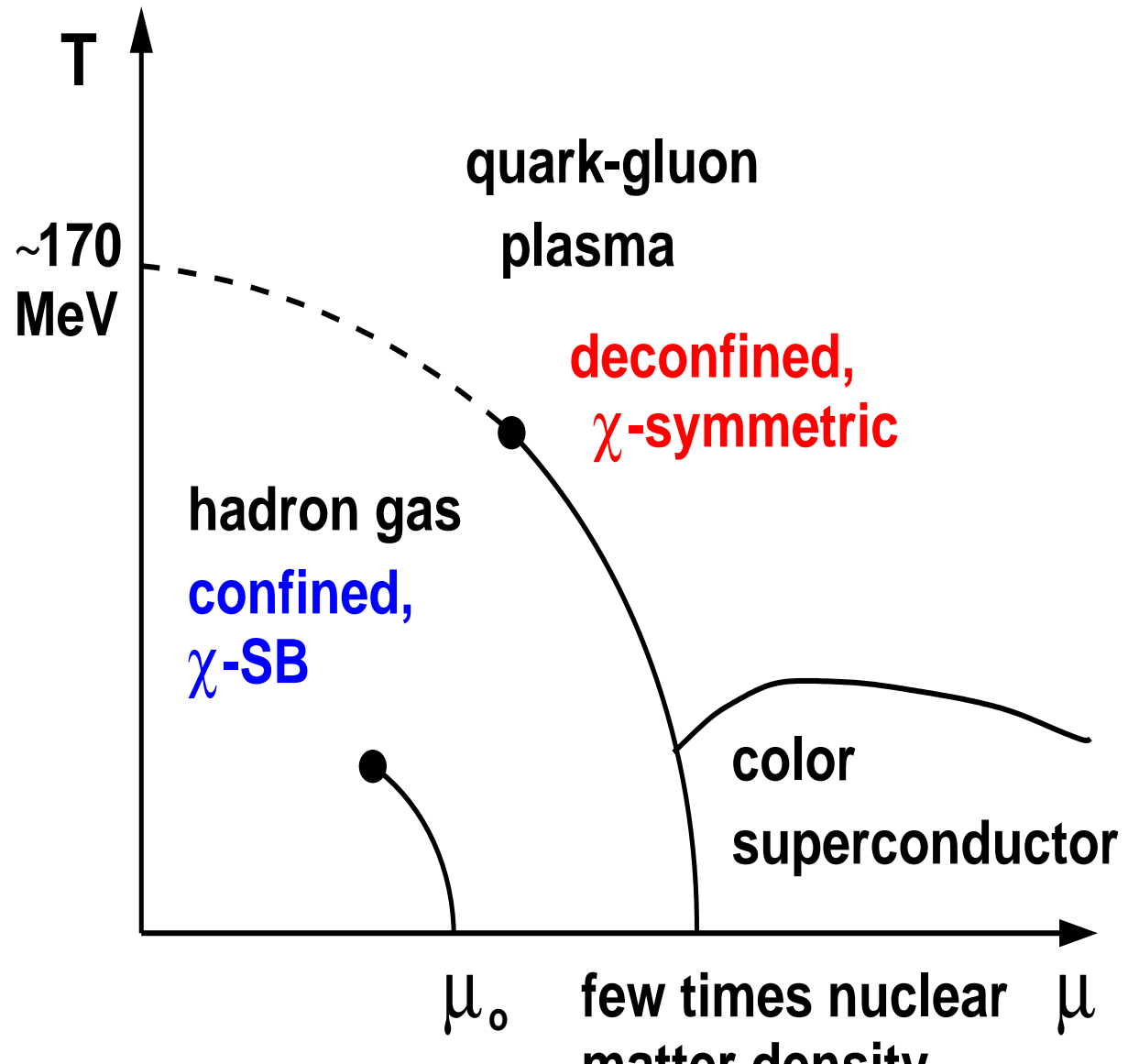
dashed lines:  $\mu = 540 \text{ MeV}$



# Phase Diagram (modern)

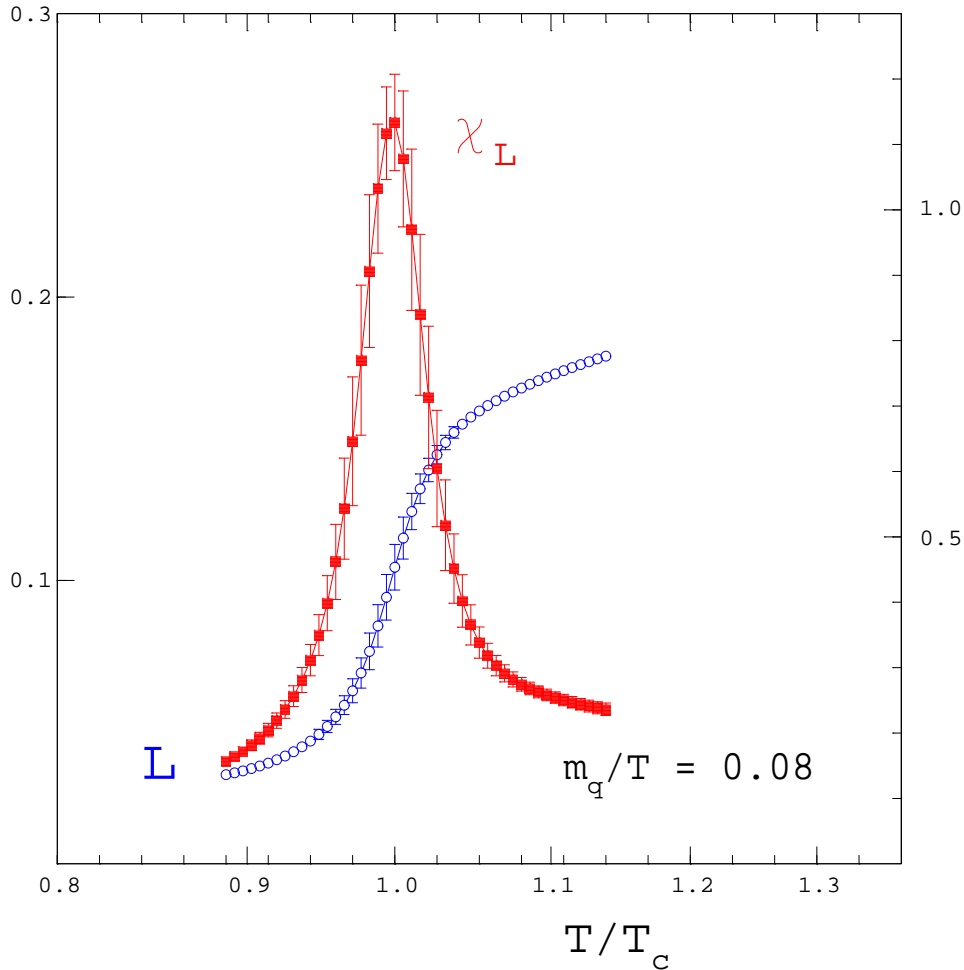
from nuclear to quark matter

at low temperatures:  
color is confined  
and  
chiral symmetry is broken  
temperature at  
phase transition:  
 $T \approx 170 \text{ MeV}$  for  $\mu = 0$

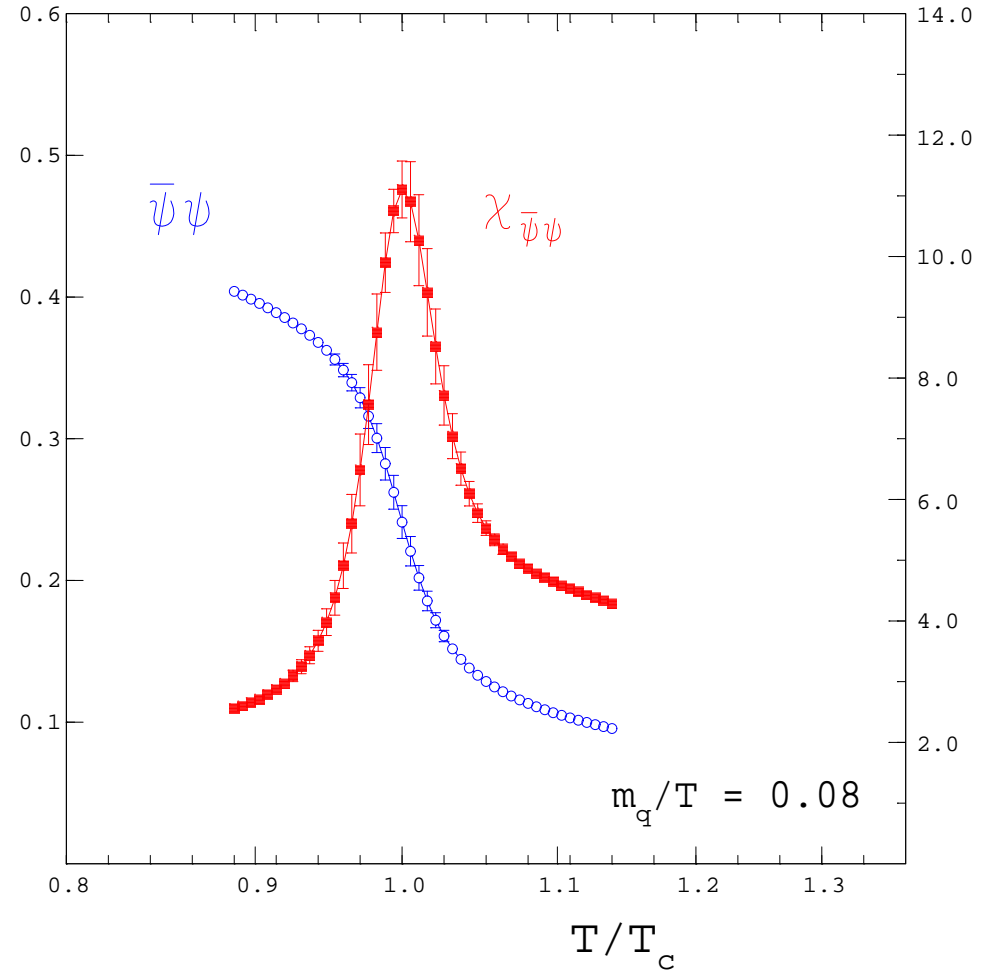


# Results from “Lattice QCD”

Polyakov loop - deconfinement



quark condensate - chiral sym. restoration

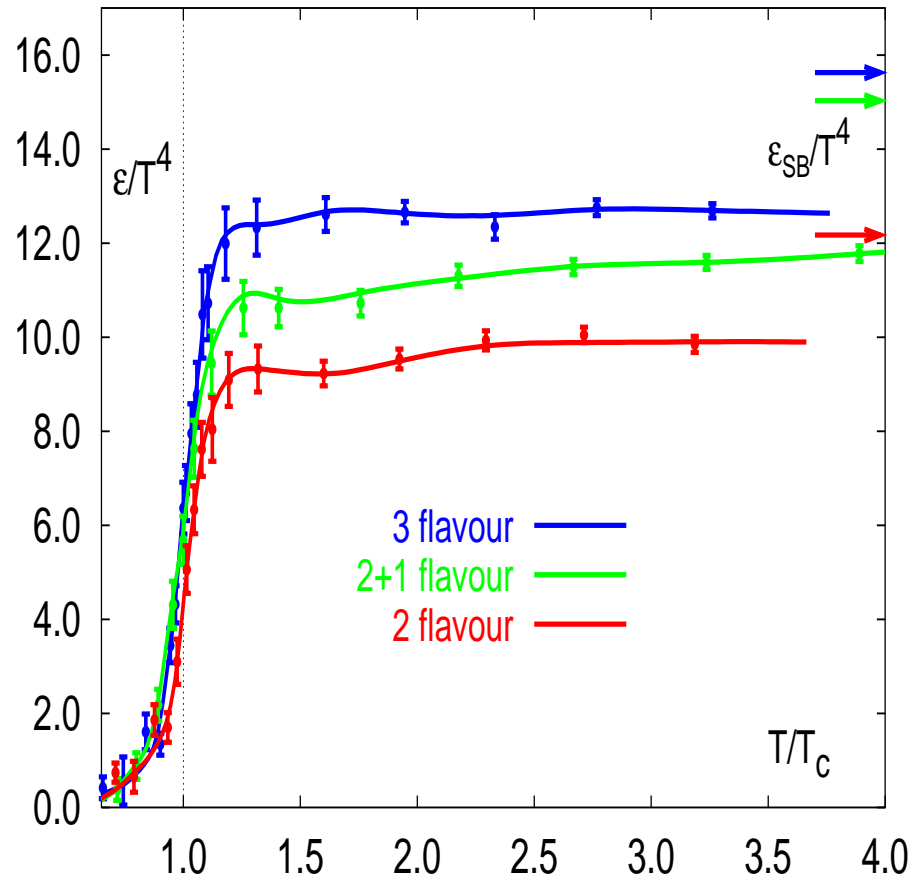


Suceptibilities  $\chi$ : measure of fluctuations

F. Karsch, E. Laermann, hep-lat/0305025

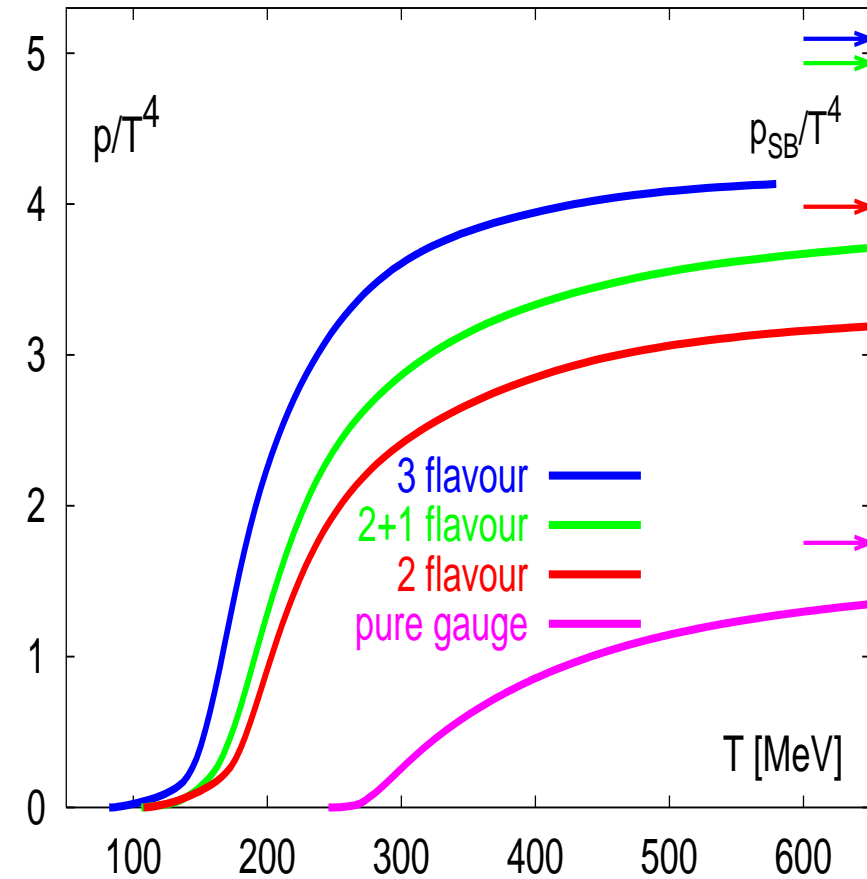
# Results from “Lattice QCD”

energy density



$$\epsilon_c = 0.7 \text{ GeV}/\text{fm}^3$$

pressure

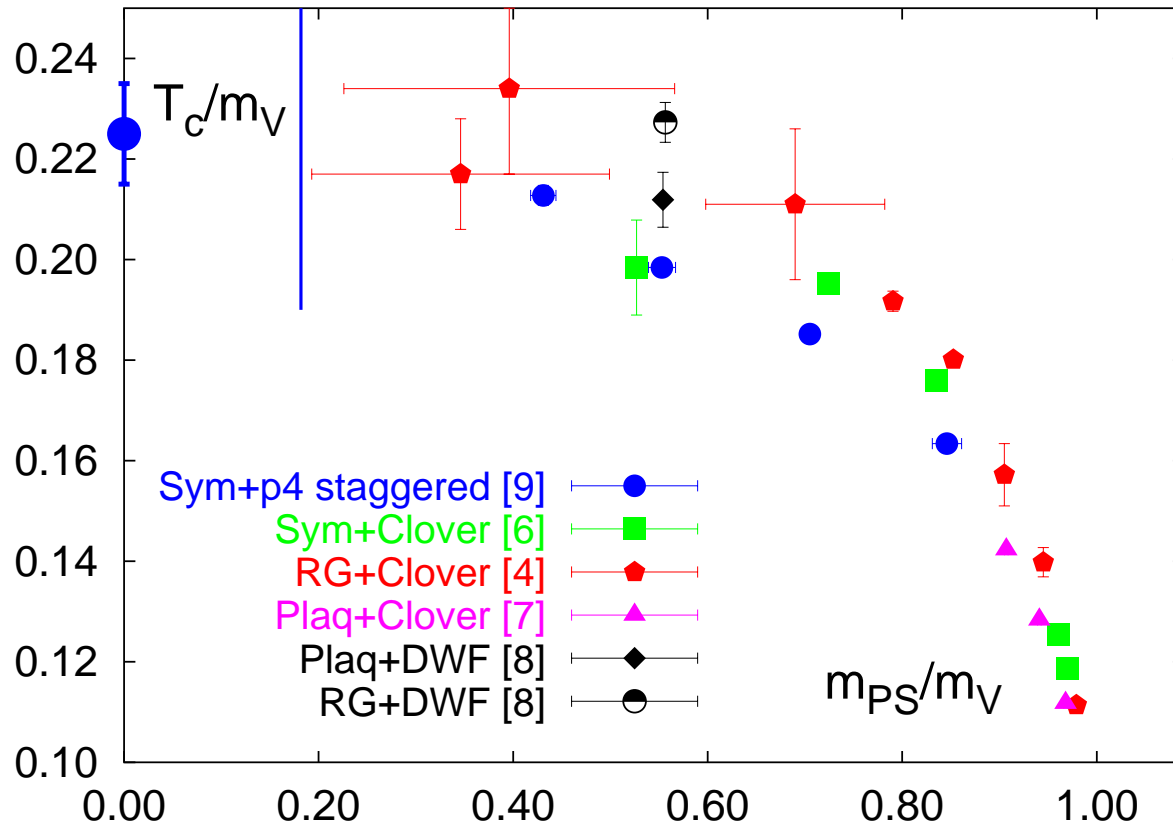


F. Karsch et al. Bielefeld group, Phys. Lett. B478(2000)447 and Nucl. Phys. A698(2002)199c

$16^3 \times 4$  lattice,  $m_{ql}/T=0.4$ ,  $m_{qh}/T=1$

# Critical Temperature from “Lattice QCD”

F. Karsch, Nucl. Phys. A698(2002)199c and E. Laermann, Proc. Hirschegg 2002



fix temperature scale with  $m_\rho$

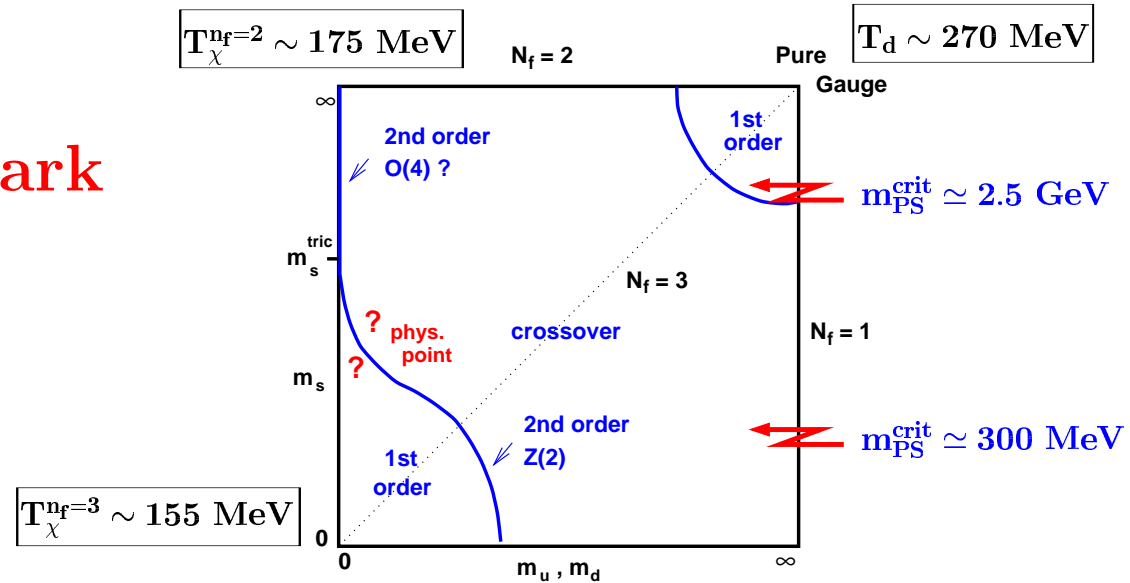
→

$$T_c = 173 \pm 8 \text{ MeV}$$

# Order of the Phase Transition

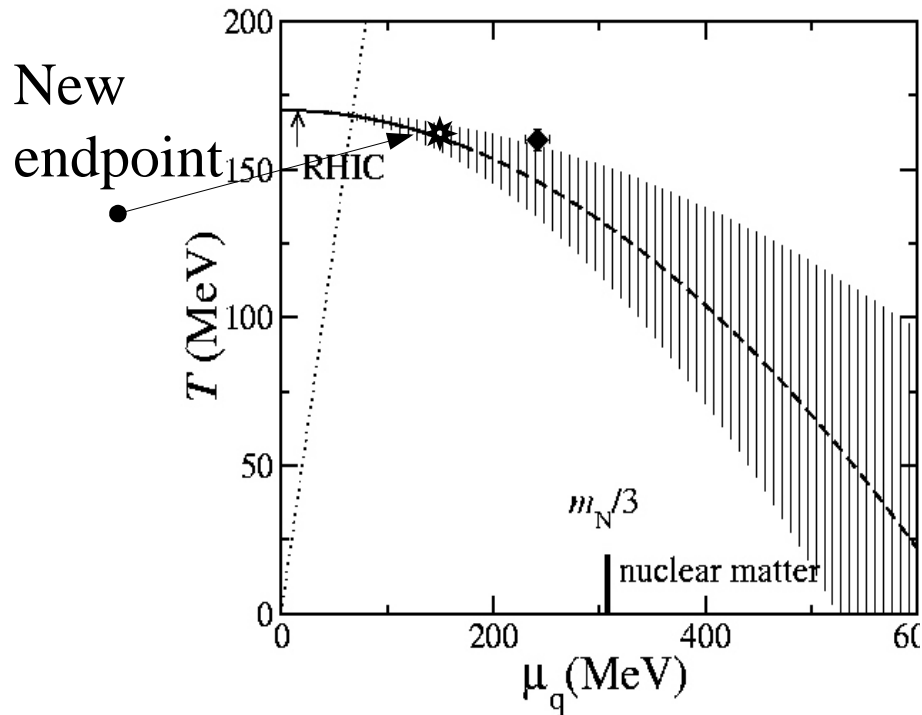
key role of strange quark

### 3-flavour phase diagram

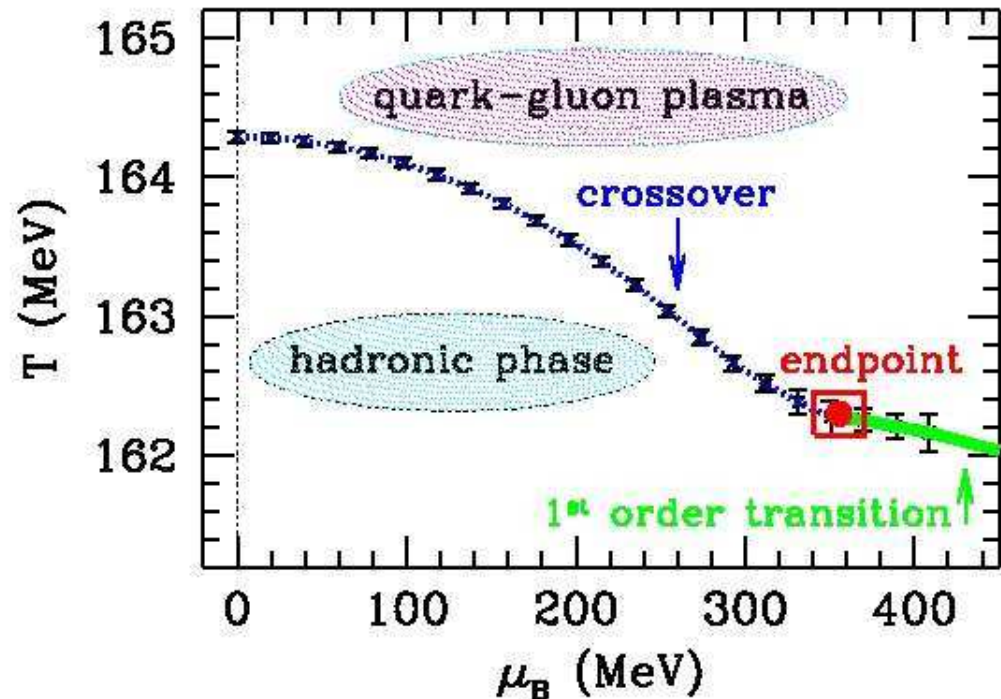




# Phase boundary from lattice QCD at finite baryon density



S. Ejiri et al, hep-lat/0312006



Z. Fodor, S. Katz, JHEP0404, (2004) 050

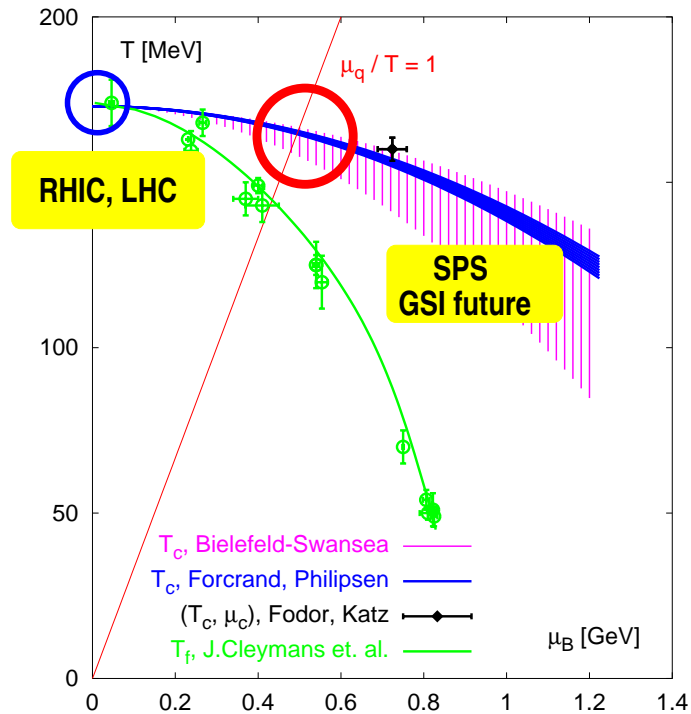
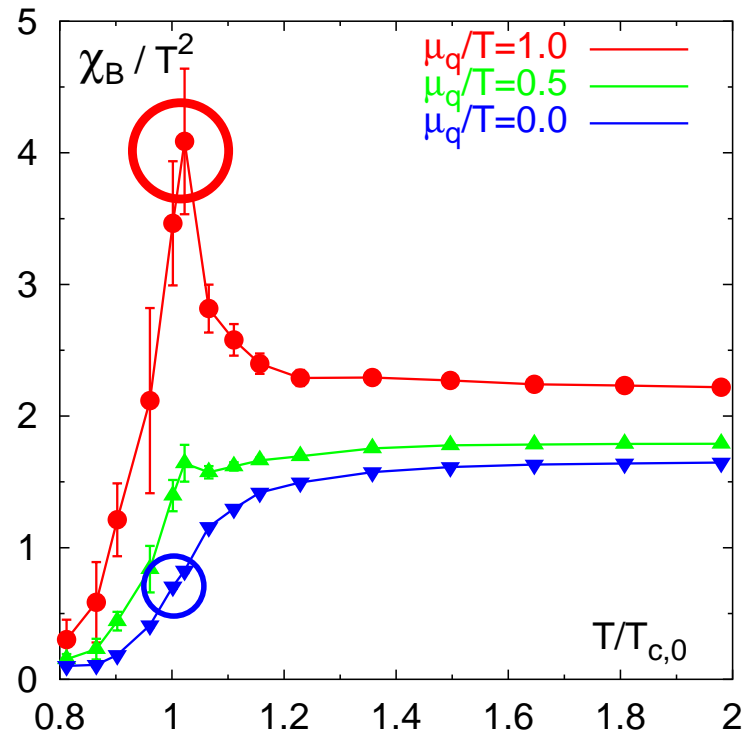
Note:  $3 \mu_q = \mu_B$

critical end point not (yet) well determined theoretically

# Fluctuations of the baryon number density ( $\mu > 0$ )

baryon number density fluctuations:  
(Bielefeld-Swansea, in preparation)

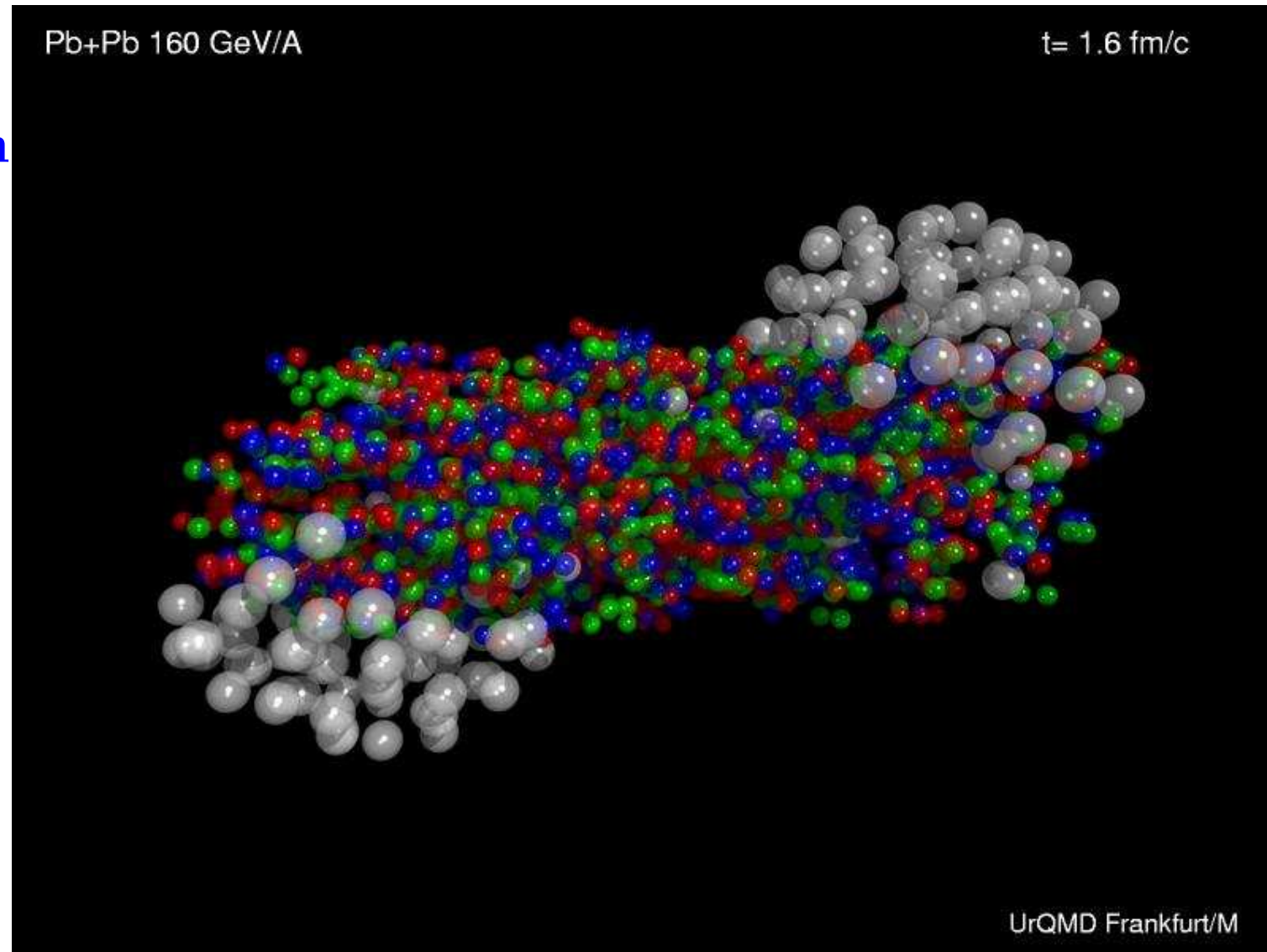
$$\frac{\chi_B}{T^2} = \left( \frac{d^2}{d(\mu/T)^2} \frac{p}{T^4} \right)_{T \text{ fixed}}$$



.- p.12/12

# Snapshot of a Pb – Pb Collision

SPS Energy  
semi-central collision



white: hadrons      colored: quarks and gluons

# Space Time Development

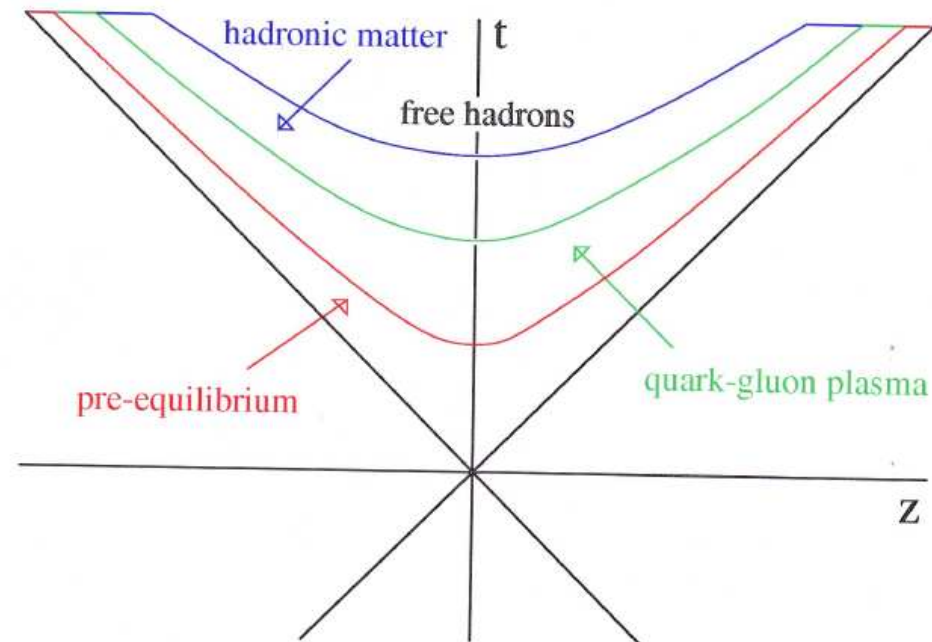
---

1st stage: liberation of quarks and gluons

2nd stage: equilibration of quarks and gluons  
→ formation of QGP

3rd stage: hadronization

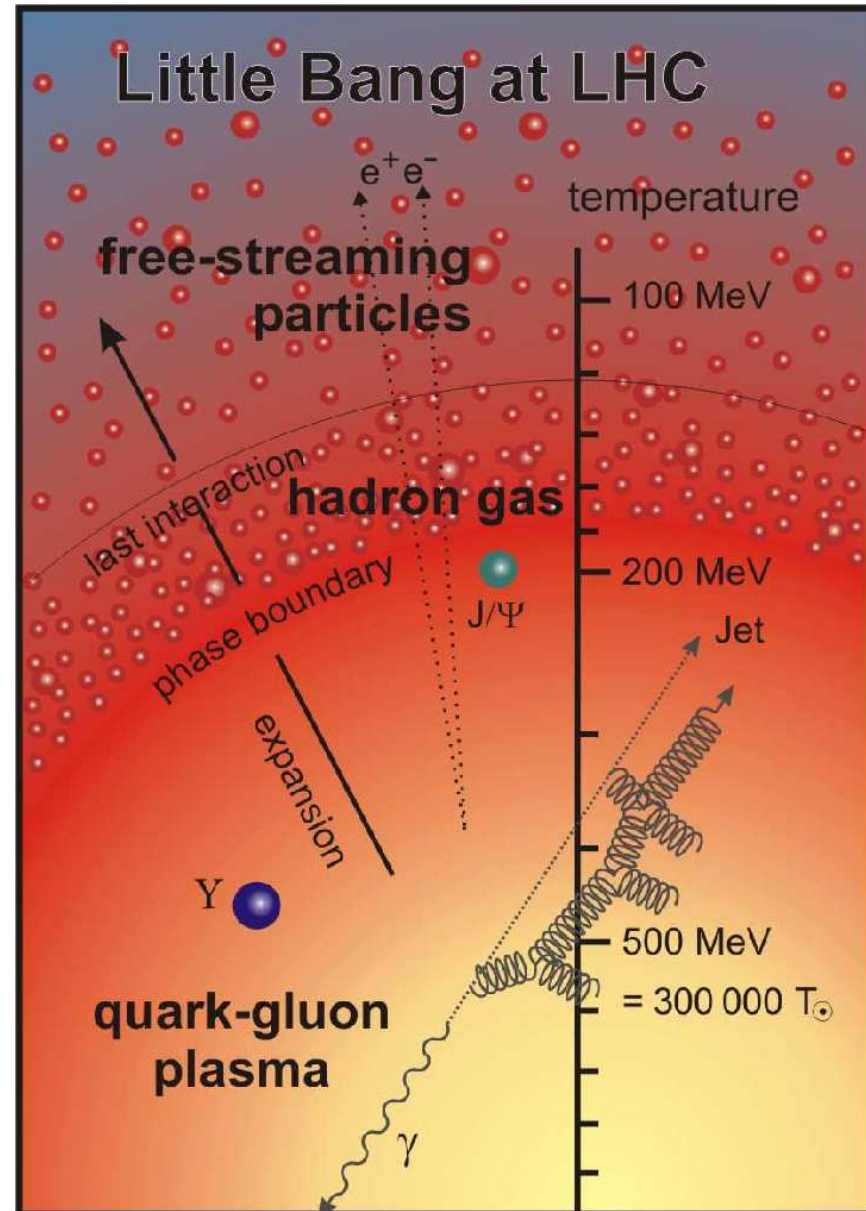
4th stage: freeze-out



# Evolution of the Fireball

signals of hot phase:  
penetrating probes  
jets,  $\gamma$ , lepton pairs

information on  
phase boundary:  
yields of produced hadrons



# Accelerators where ultra-relativistic nuclei collide

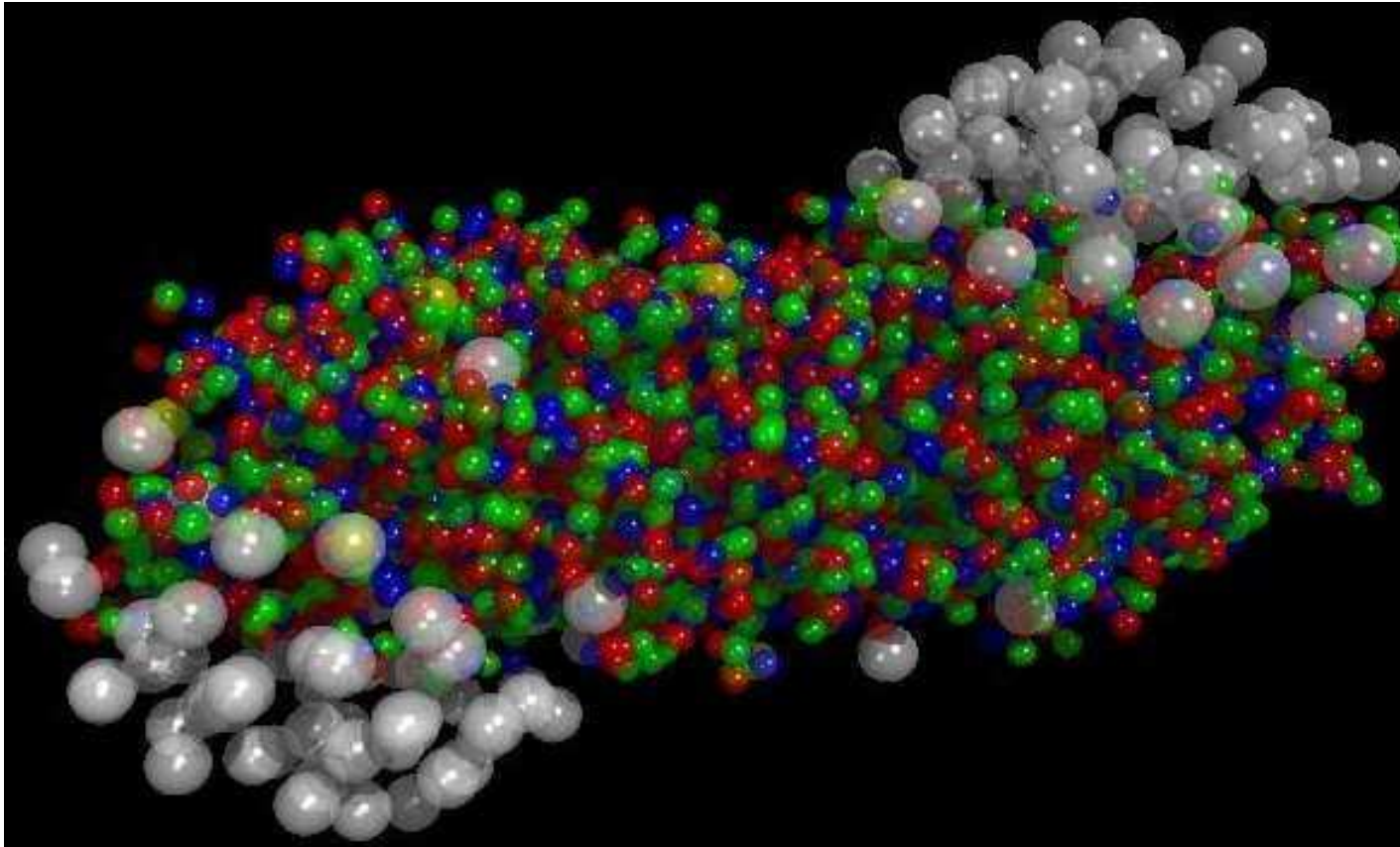
	fixed target		collider	
	AGS	SPS	RHIC	LHC
	1987-2000		since 2000	from 2007
beam momentum	$29 \cdot Z \text{ GeV}/c$	$450 \cdot Z \text{ GeV}/c$	$ea250 \cdot Z \text{ GeV}/c$	$ea7000 \cdot Z \text{ GeV}/c$
projectile	p...Au	p...Pb	p...Au	p...Pb
energy available in c.m. system	Au+Au 600 GeV	Pb+Pb 3200 GeV	Au+Au 40 TeV	Pb+Pb 1150 TeV
hadrons produced per collision	900	2400	7500	40000?

# Accelerators and Experiments for Nuclear Collisions

---

- **BNL-AGS (1986 - 2002):**  $\sqrt{s} = 5.5 \text{ GeV}$ , Au + Au collisions  
5 large experiments: E802/866/917, E810, E814/877, E864, E895.
- **CERN-SPS (1986 - 2004):**  $\sqrt{s} = 17 \text{ GeV}$ , Pb + Pb collisions  
7 large experiments: WA80/98, NA35/49, NA38/50/60, NA44  
NA45/CERES, WA97/NA57, NA52.
- **BNL-RHIC (from 2000):**  $\sqrt{s} = 200 \text{ GeV}$ , Au + Au collisions  
4 large experiments: BRAHMS, PHENIX, PHOBOS, STAR.
- **CERN-LHC (from 2007):**  $\sqrt{s} = 5.5 \text{ TeV}$ , Pb + Pb collisions  
3 large experiments: ATLAS, ALICE, CMS

## Press Release Feb. 2000: **New State of Matter** created at CERN



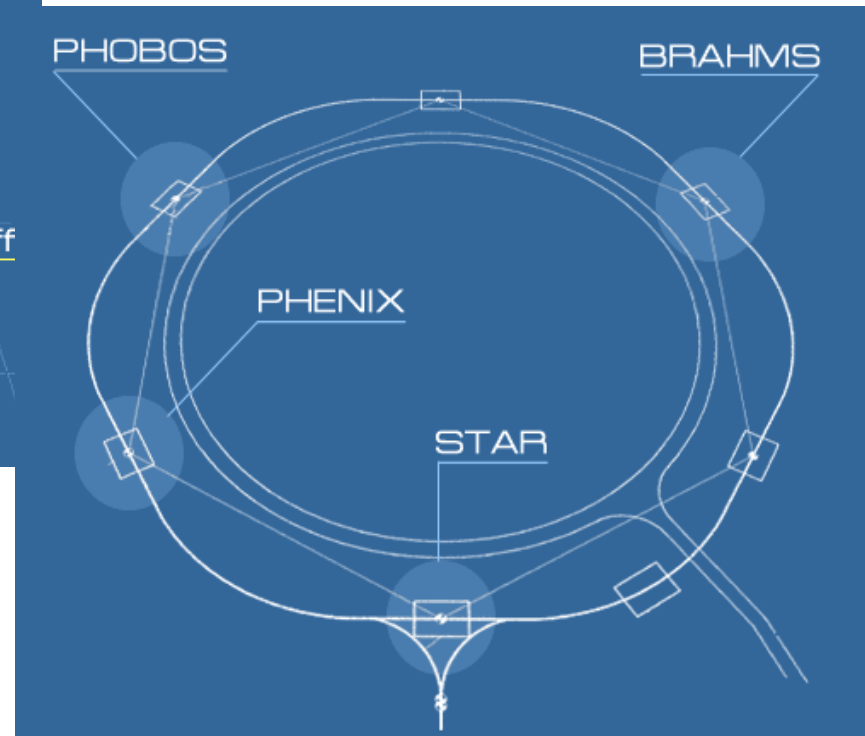
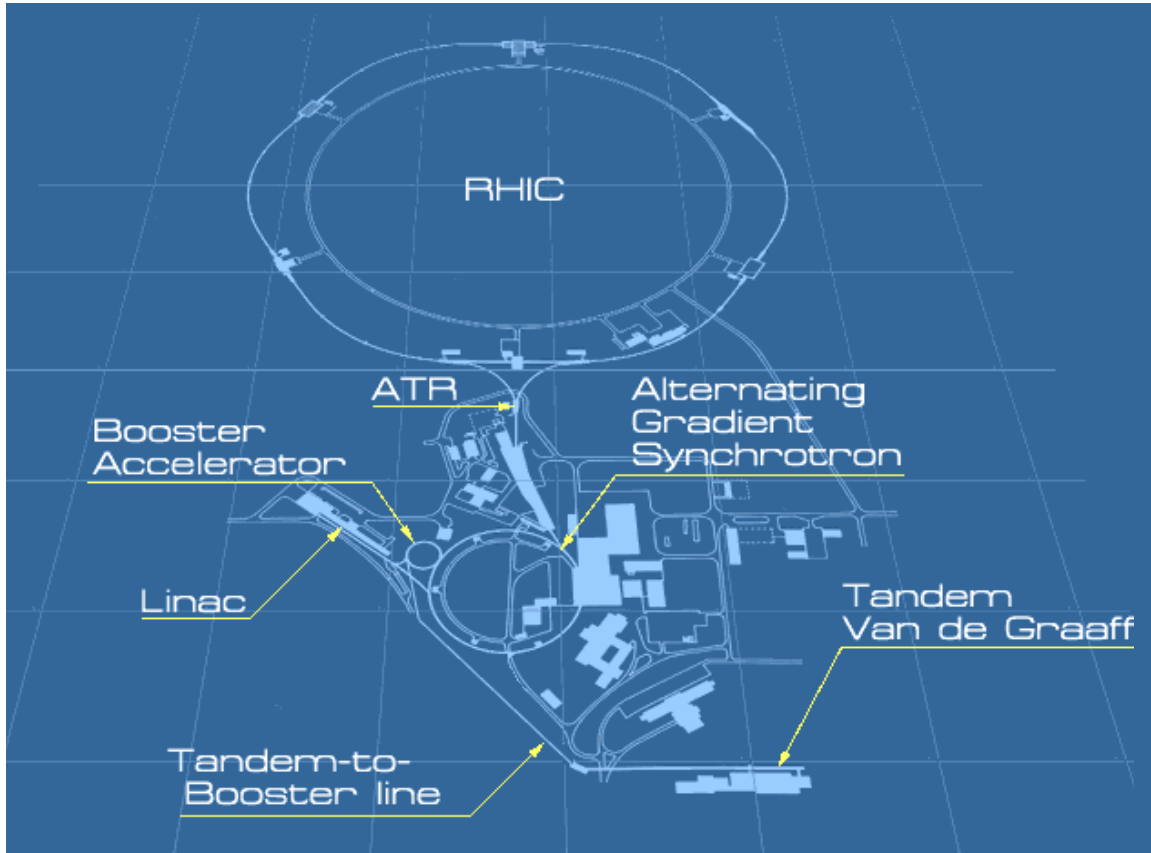
At a special seminar on 10 February, spokespersons from the experiments on **CERN\*** 's Heavy Ion programme presented compelling evidence for the existence of a new state of matter in which quarks, instead of being bound up into more complex particles such as protons and neutrons, are liberated to roam freely.

nothing know yet about properties of new state

**RHIC** starts from here



# heavy ion collider RHIC – dedicated machine



# RHIC press release after analysis of first 3 years



Contact: Karen McNulty Walsh, (631) 344-8350 or Mona S. Rowe, (631) 344-5056

## RHIC Scientists Serve Up “Perfect” Liquid

**New state of matter more remarkable than predicted -- raising many new questions**

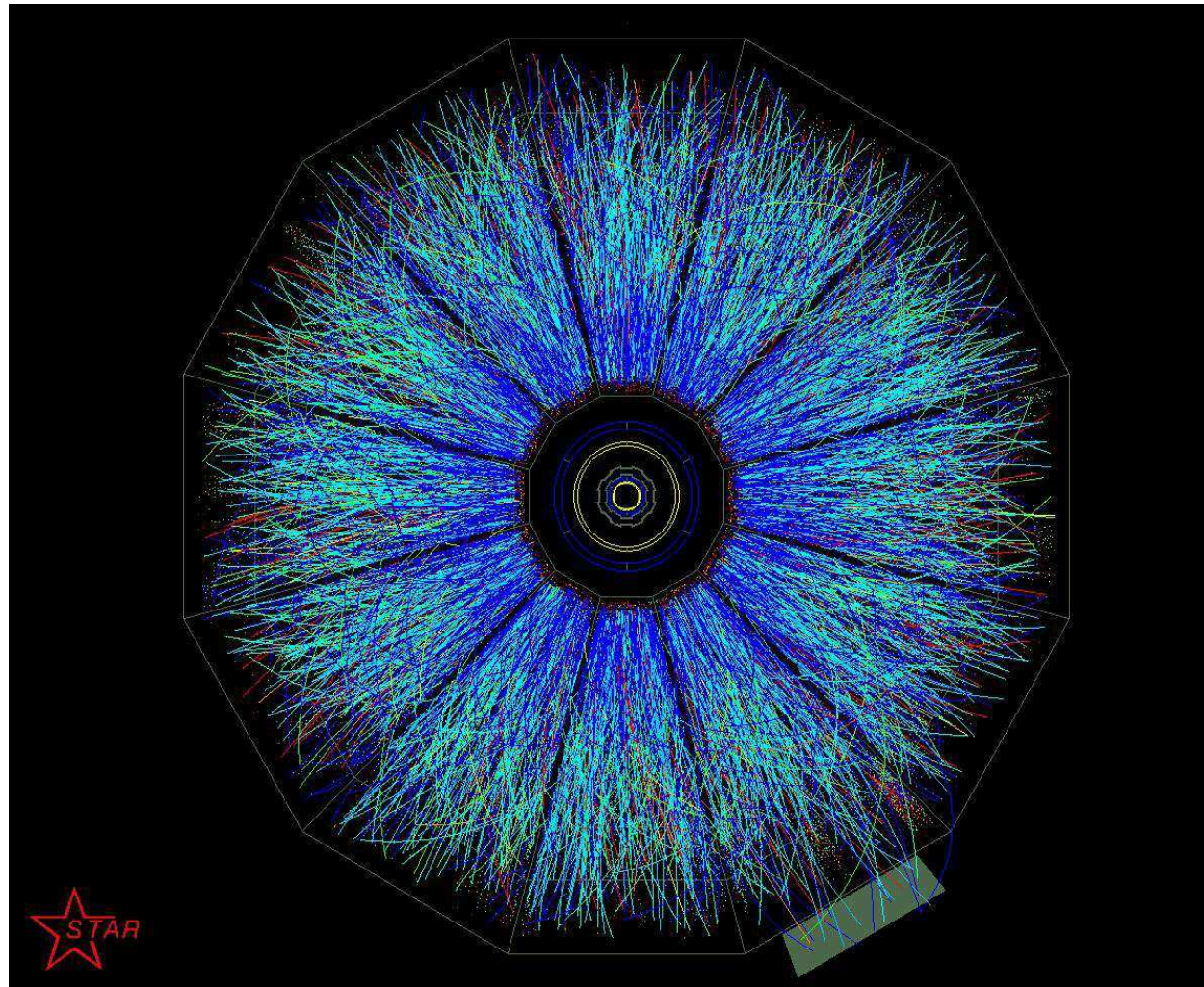
April 18, 2005

TAMPA, FL -- The four detector groups conducting research at the [Relativistic Heavy Ion Collider \(RHIC\)](#) -- a giant atom “smasher” located at the U.S. Department of Energy’s Brookhaven National Laboratory -- say they’ve created a new state of hot, dense matter out of the quarks and gluons that are the basic particles of atomic nuclei, but it is a state quite different and even more remarkable than had been predicted. In [peer-reviewed papers](#) summarizing the first three years of RHIC findings, the scientists say that instead of behaving like a gas of free quarks and gluons, as was expected, the matter created in RHIC’s heavy ion collisions appears to be more like a liquid.

# STAR event display

in central AuAu collisions  
at RHIC  $\sqrt{s} = 200$  GeV  
about 7500 hadrons  
produced

about three times as  
much as at CERN SPS



# Experimental Challenge of High Energy Heavy Ion Experiments

---

- Very high multiplicities demanded new developments

1. Time Projection Chambers (TPC)

developed to unprecedented performance

2. Silicon Pixel (and Drift) Detectors

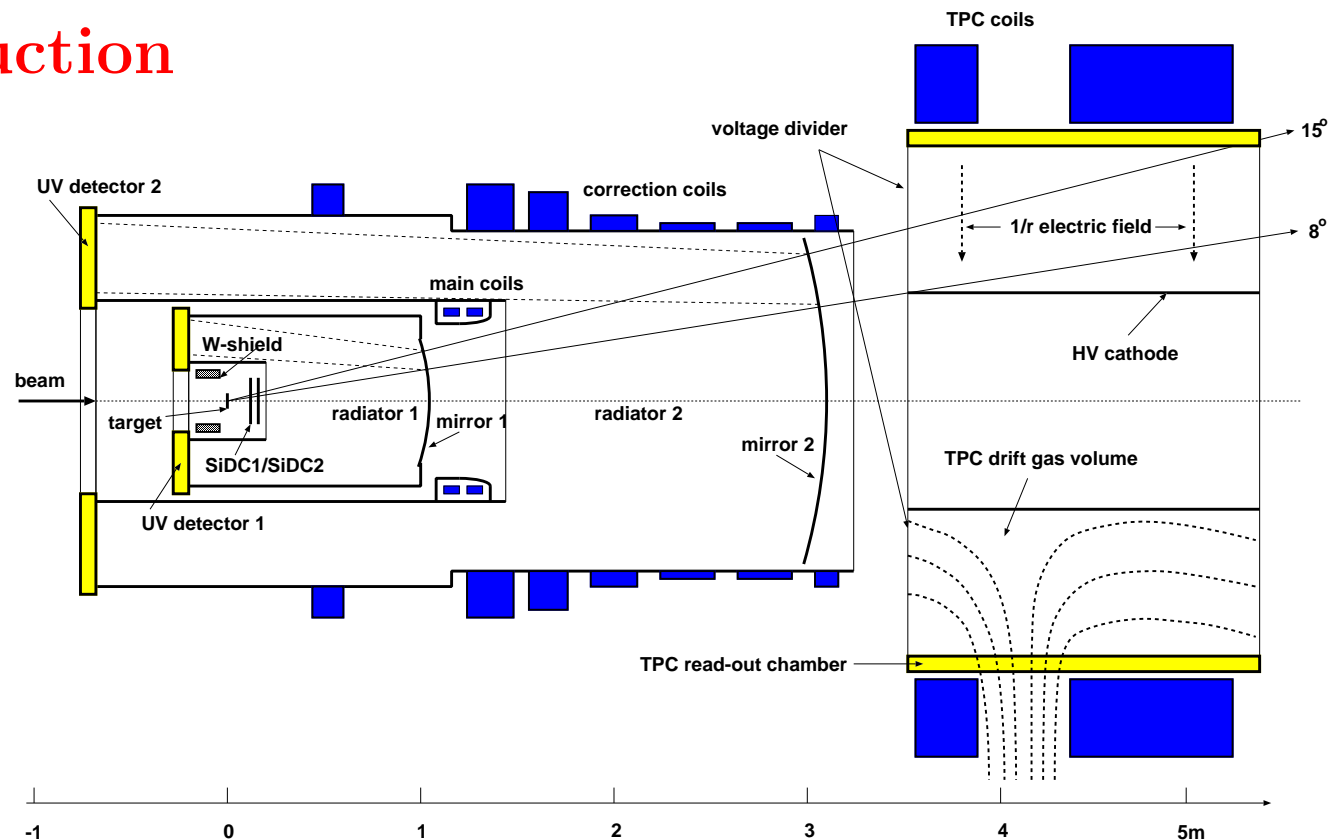
with large area and very fine granularity

3. Electron Identification

in high hadron density environment (RICH and TRD development)

# NA45/CERES Experiment at CERN SPS

## Study of $e^+e^-$ Production

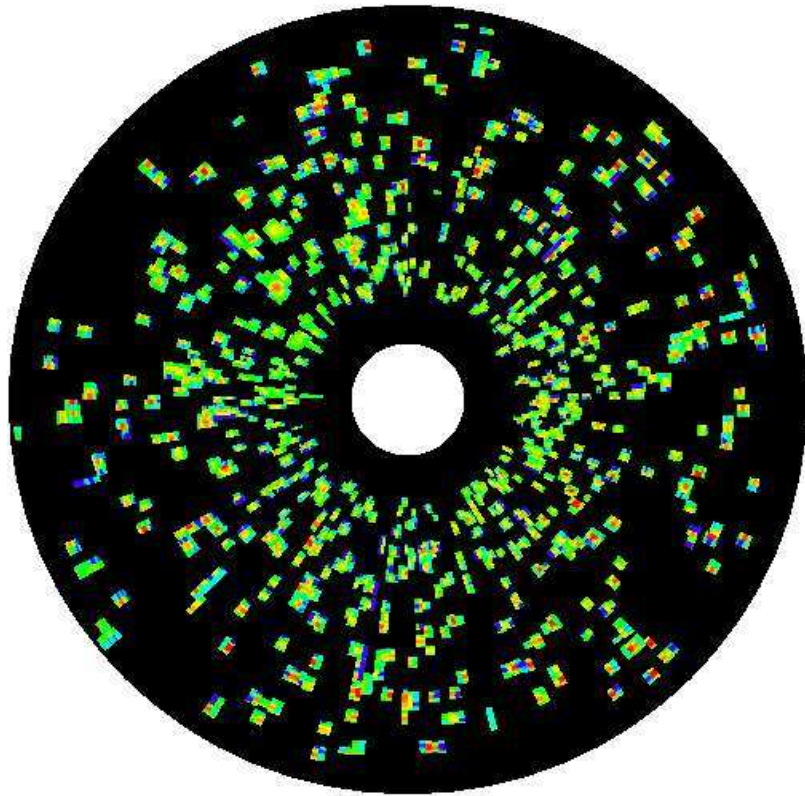


Since 1999:

also hadronic observables

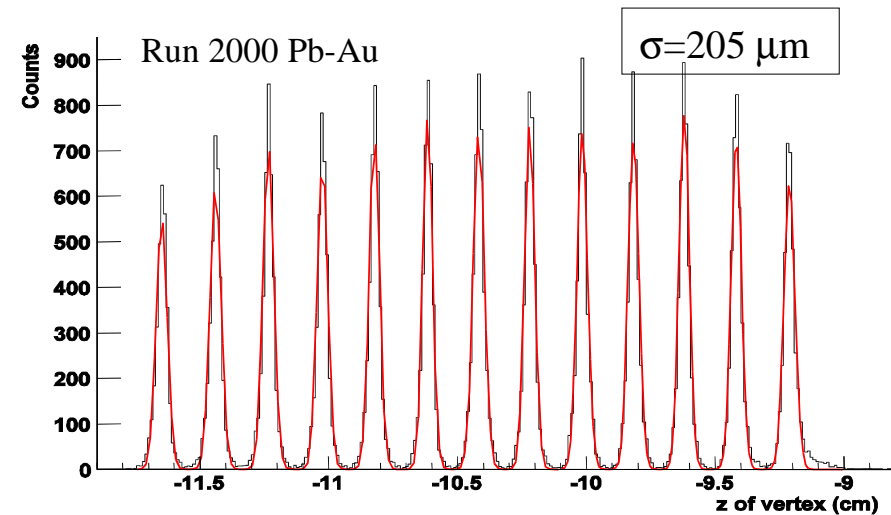
all novel detectors: 2 Si Drift detectors, 2 RICHes, large radial TPC

# CERES Silicon Drift Detectors



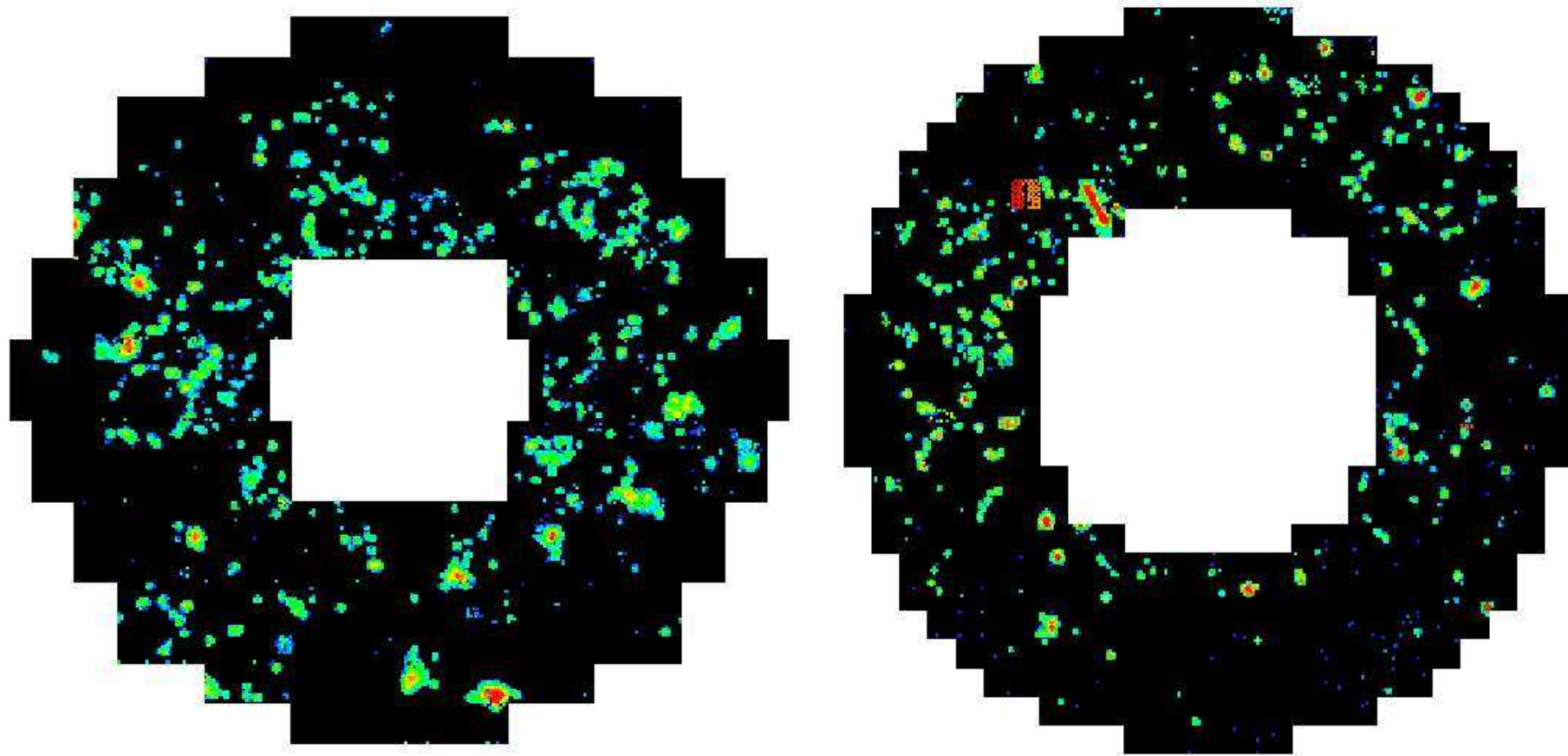
two 4" Silicon wafers

- charged particle tracking
- vertex reconstruction



combination of 2 or more:  
form telescopes

# CERES Ring Imaging Cherenkov Counters RICH1/2



**electron identification via ring signature  
about 10 photons per electron ring**

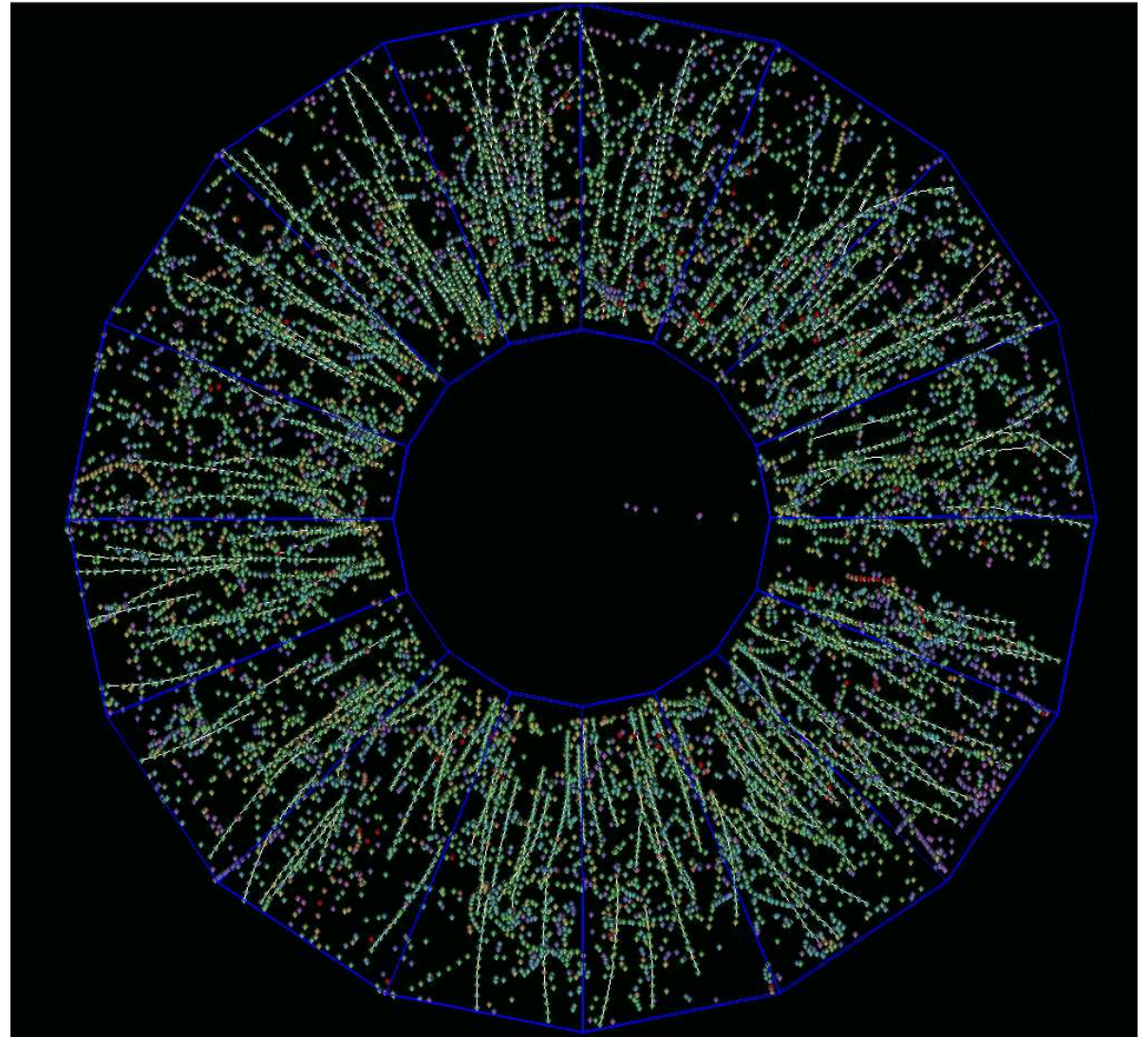
# CERES Event Display

---

charged particle tracking  
with TPC

$10 \text{ m}^3$ ,  $4 \cdot 10^6$  pixels

up to 400 charged particles





# Time Projection Chamber (TPC) Principle

3-dimensional tracking

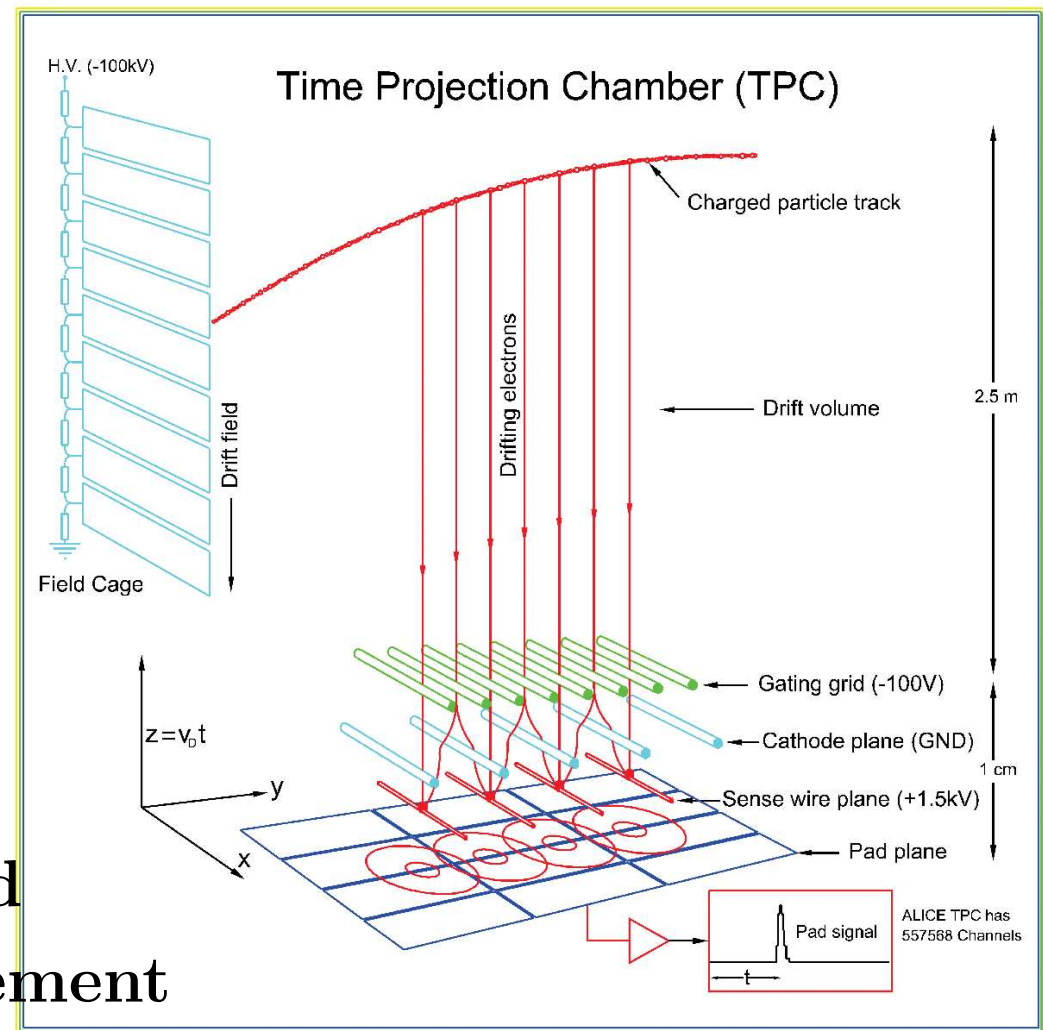
large volumes possible

90 m<sup>3</sup> and

3·10<sup>8</sup> read out pixels

for ALICE TPC

information from drift time and  
2-dimensional position measurement



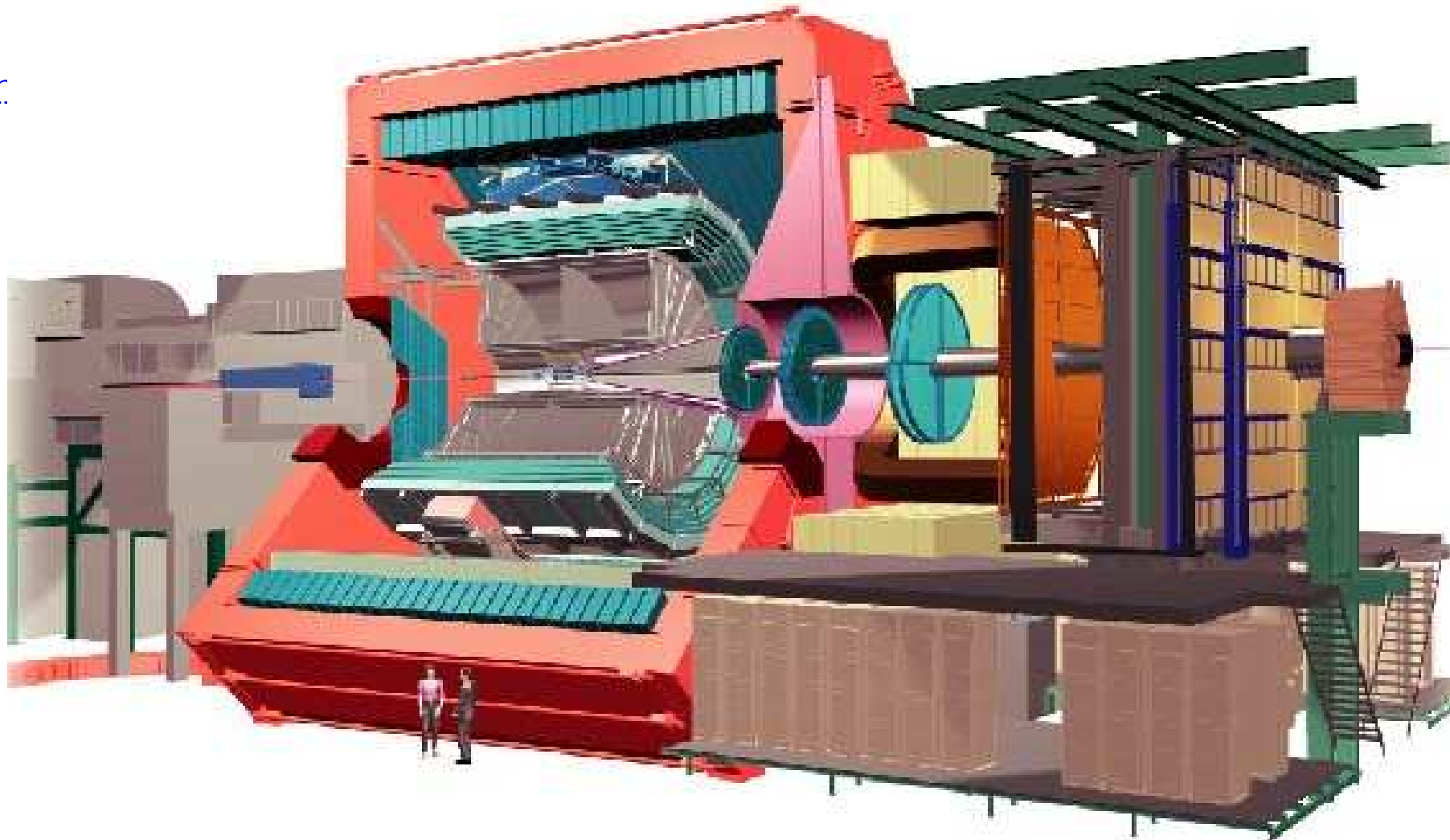
# STAR Experiment at RHIC



# The ALICE Experiment at LHC

---

running from  
2007



central barrel: ITS, TPC, TRD, TOF +  
forward muon detector

# The ALICE TPC field cage

