

News from Herwig++

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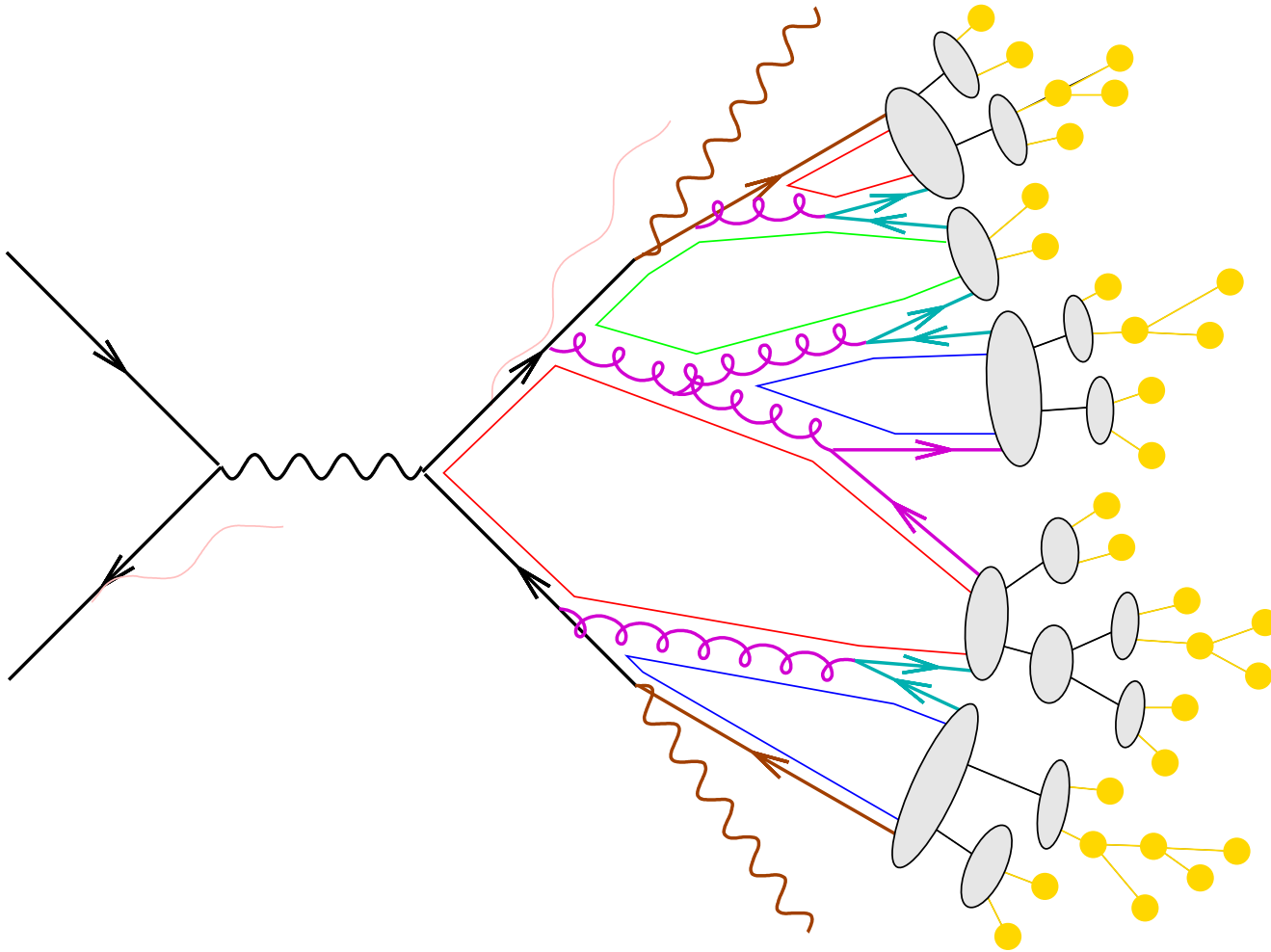
work with A Ribon, P Richardson, MH Seymour, P Stephens, BR Webber (Cambridge, Durham, CERN)

- Quick tour of Herwig++ (mainly e^+e^-)
- Jet physics, results for e^+e^- Annihilation
- Initial state shower — towards a full hadronic event generator
- New Decays
- Summary and Future

SG, P. Stephens and B. Webber, JHEP **0312** (2003) 045 [hep-ph/0310083]

SG, A. Ribon, M. H. Seymour, P. Stephens and B. Webber, JHEP **0402** (2003) 005 [hep-ph/0311208]

e^+e^- Event Generator

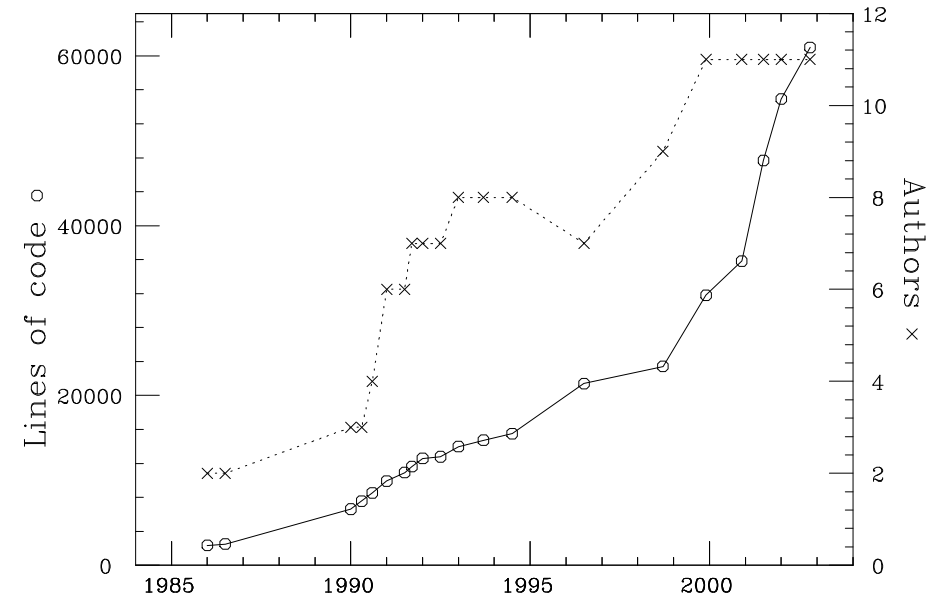


- hard scattering
- (QED) initial/final state radiation
- partonic decays, e.g. $t \rightarrow bW$
- parton shower evolution
- nonperturbative gluon splitting
- colour singlets
- colourless clusters
- cluster fission
- cluster \rightarrow hadrons
- hadronic decays

The new generator Herwig++

Complete rewrite of HERWIG in C++

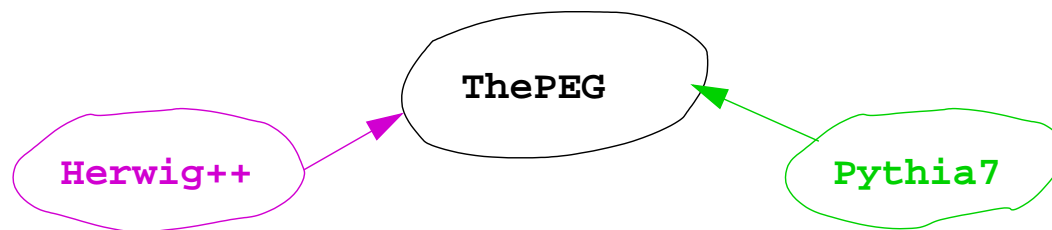
- aiming at full multi-purpose generator for LHC and future colliders.
- Preserve main features of HERWIG such as
 - angular ordered parton shower
 - Cluster Hadronization
- New features and improvements
 - improved parton shower evolution for heavy quarks
 - consistent radiation from unstable particles



HERWIG's growth. . .

Use of ThePEG in Herwig++

ThePEG = Toolkit for high energy Physics Event Generation



Won't re-invent the wheel

Share administrative overhead, common to event generators with Pythia7

Independent *physics* implementation

Large but very flexible implementation

Common basis for Pythia7/Herwig++:

- ✗ Lack of independence.
- ✗ Miss the possibility to test codes against each other.
- ✓ Physics, however, is still independent.
- ✓ Beneficial for the user to have the same framework.
- ✓ Running Herwig++ with the Lund String Fragmentation from Pythia7 is very simple!

Hard interactions

- Basic ME's included in **ThePEG**, such as:

$$e^+e^- \rightarrow q\bar{q}, \text{ partonic } 2 \rightarrow 2,$$

we use them.

- Soft and hard **matrix element corrections** implemented for $e^+e^- \rightarrow q\bar{q}g$.
- **AMEGIC++** will provide arbitrary ME's for multiparton final states via **AMEGICInterface**.
- **LesHouchesFileReader** enables to read in and process *any* hard event generated by parton level event generators (MadGraph/MadEvent, AlpGen, CompHEP, ...).
- CKKW ME+PS foreseen.
- Other authors can easily include their own matrix elements (\rightarrow *safety* of OO code)

New/Future: HELAS like structures are already implemented for decays and spin correlations \longrightarrow allows us to code simple processes efficiently.

Quasi-Collinear Limit (Heavy Quarks)

Sudakov-basis p, n with $p^2 = M^2$ ('forward'), $n^2 = 0$ ('backward'),

$$p_q = zp + \beta_q n - q_\perp$$

$$p_g = (1 - z)p + \beta_g n + q_\perp$$

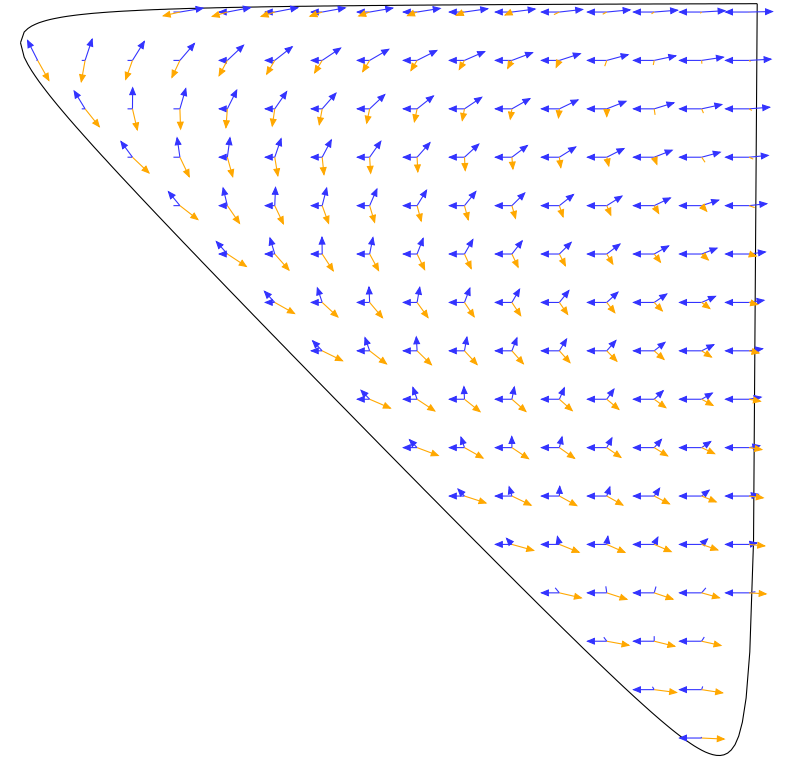
Collinear limit for radiation off heavy quark,

$$P_{gq}(z, \mathbf{q}^2, m^2) = C_F \left[\frac{1 + z^2}{1 - z} - \frac{2z(1 - z)m^2}{\mathbf{q}^2 + (1 - z)^2 m^2} \right]$$

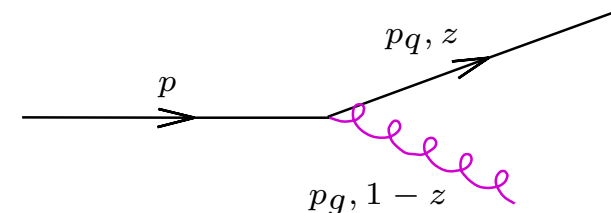
$$= \frac{C_F}{1 - z} \left[1 + z^2 - \frac{2m^2}{z\tilde{q}^2} \right]$$

→ $\tilde{q}^2 \sim \mathbf{q}^2$ may be used as evolution variable.

$q\bar{q}g$ -Phase space (x, \bar{x})

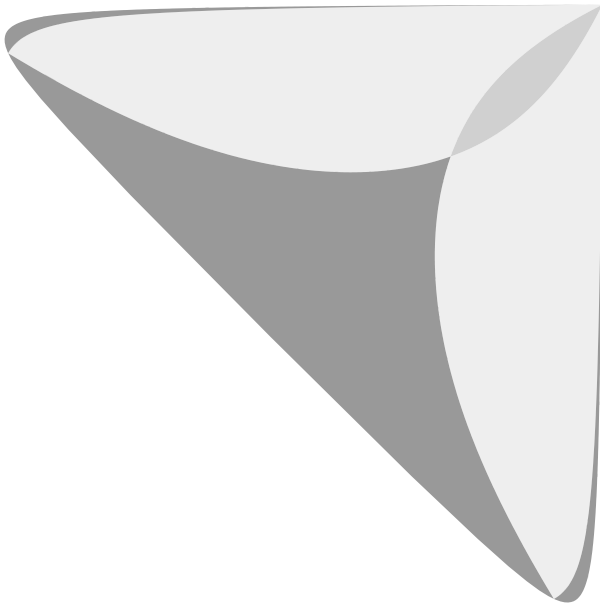


Single emission:

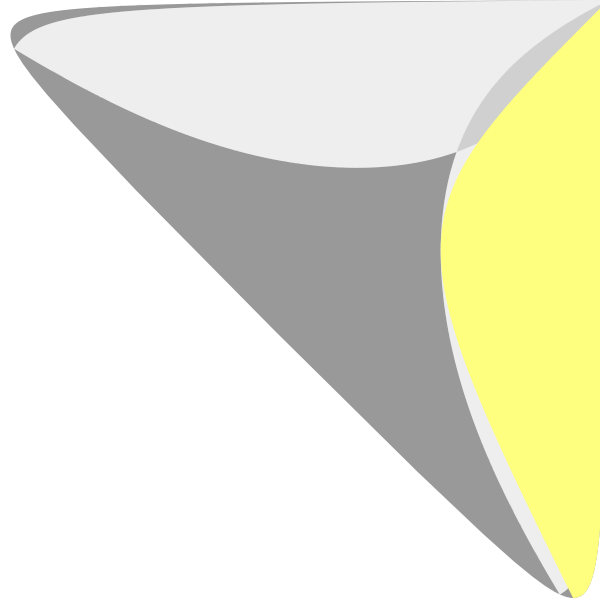


$q\bar{q}g$ Phase Space old vs new variables

Consider (x, \bar{x}) phase space for $e^+e^- \rightarrow q\bar{q}g$



HERWIG



Comparison

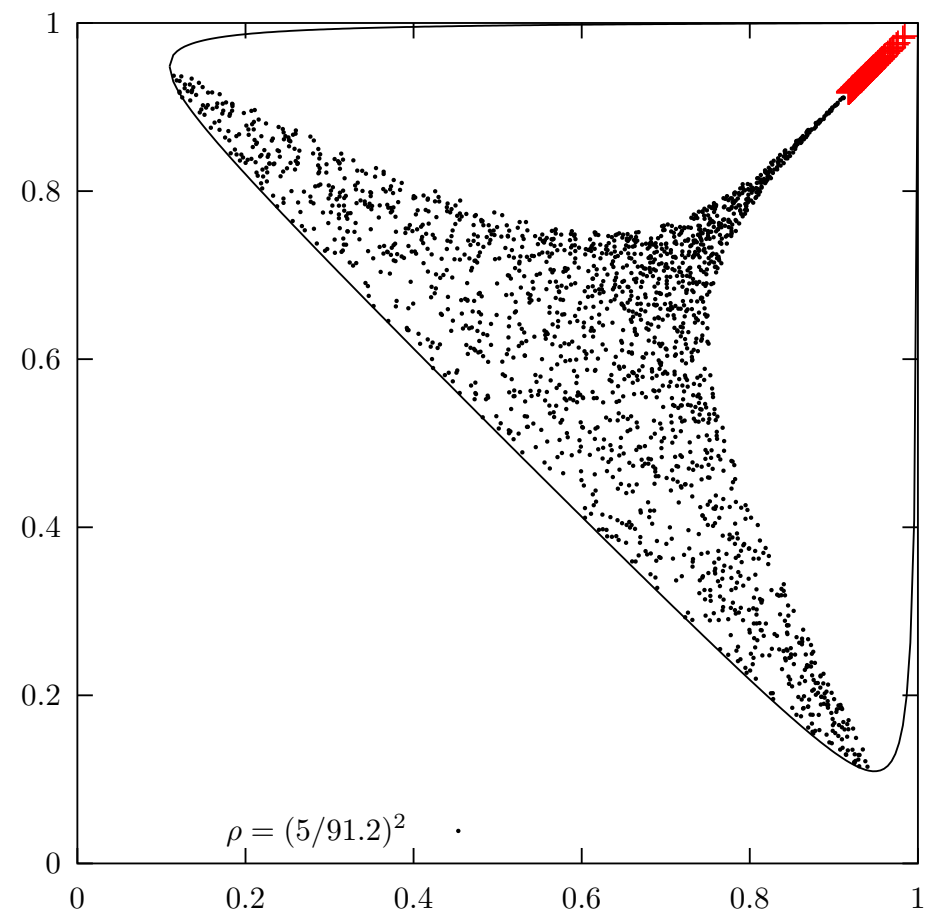


Herwig++

- ✗ Larger dead region with new variables.
- ✓ Smooth coverage of soft gluon region.
- ✓ No overlapping regions in phase space.

Hard Matrix Element Corrections

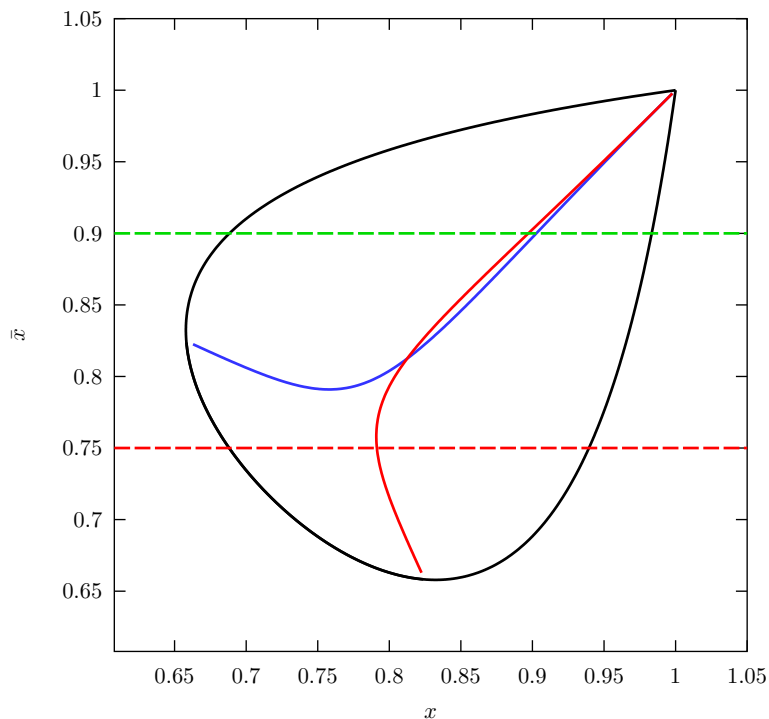
- Points (x, \bar{x}) in **dead region** chosen acc to LO $e^+e^- \rightarrow q\bar{q}g$ matrix element and accepted acc to ME weight.
- About **3%** of all events are actually hard $q\bar{q}g$ events.
- Red points have **weight > 1** , practically no error by setting weight to one.
- Event **oriented** according to given $q\bar{q}$ geometry. Quark direction is kept with weight $x^2/(x^2 + \bar{x}^2)$.



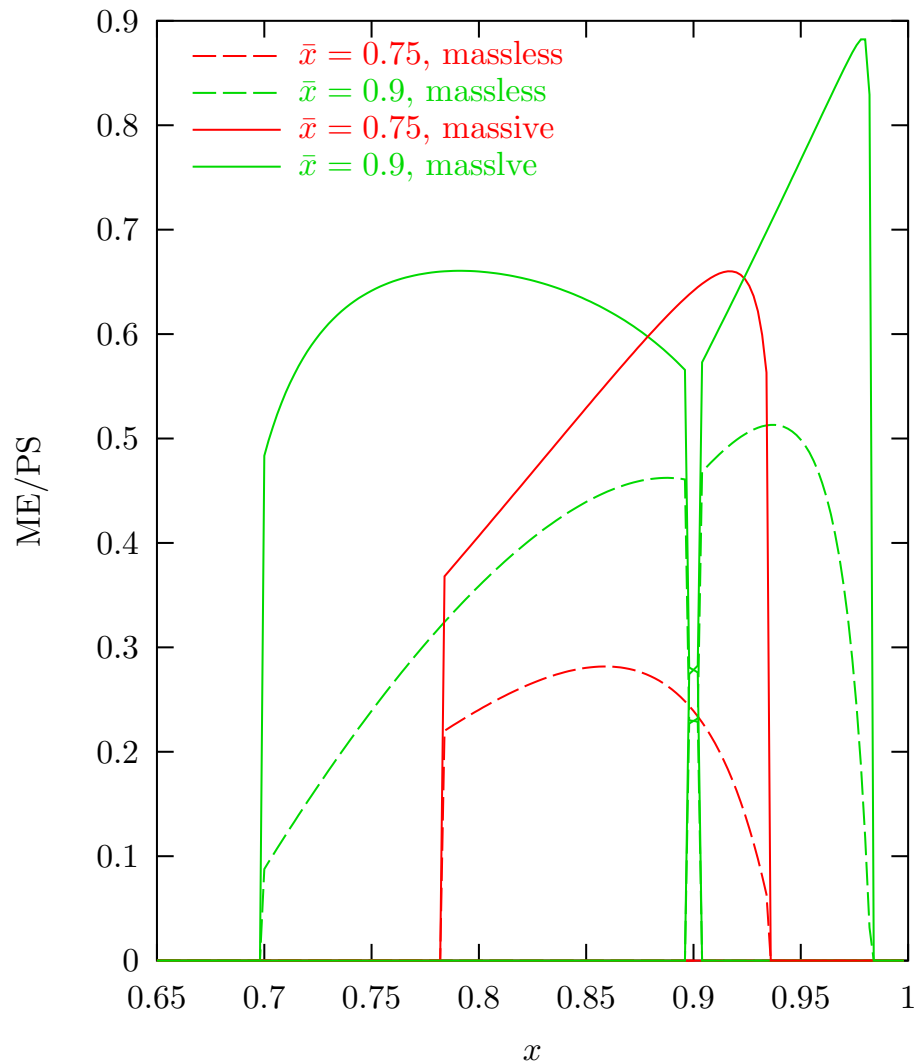
Soft Matrix Element Corrections

- Ratio ME/PS compares emission with result from true ME if slightly away from soft/collinear region.
- **Veto** on 'hardest emission so far' in p_{\perp} .
- **Massive splitting function** *very important!*

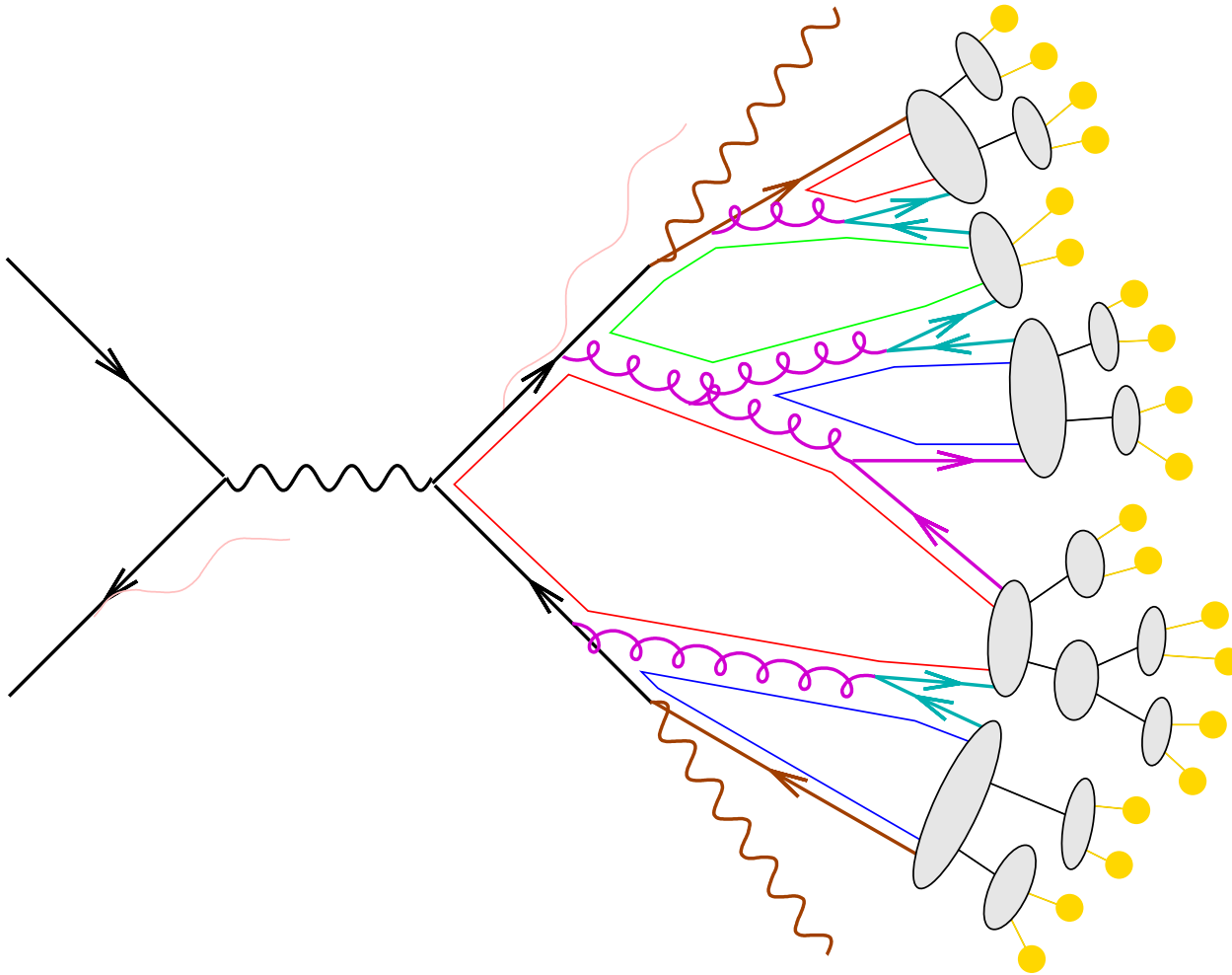
Example with heavy quark, $m^2/Q^2 = 0.1$,
 ($t\bar{t}$, $Q = 500$ GeV):



Comparison with massless splitting function



e^+e^- Event Generator



- hard scattering
- (QED) initial/final state radiation
- partonic decays, e.g. $t \rightarrow bW$
- parton shower evolution
- nonperturbative gluon splitting
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- cluster \rightarrow hadrons

Cluster hadronization in a nutshell

- **Nonperturbative $g \rightarrow q\bar{q}$ splitting** ($q = uds$) isotropically.
Here, $m_g \approx 750 \text{ MeV} > 2m_q$.
- **Cluster formation**, universal spectrum (see below)
- **Cluster fission**, until

$$M^P < M_{\text{max}}^P + (m_1 + m_2)^P$$

where masses are chosen from

$$M_i = \left[\left(M^P - (m_i + m_3)^P \right) r_i + (m_i + m_3)^P \right]^{1/P},$$

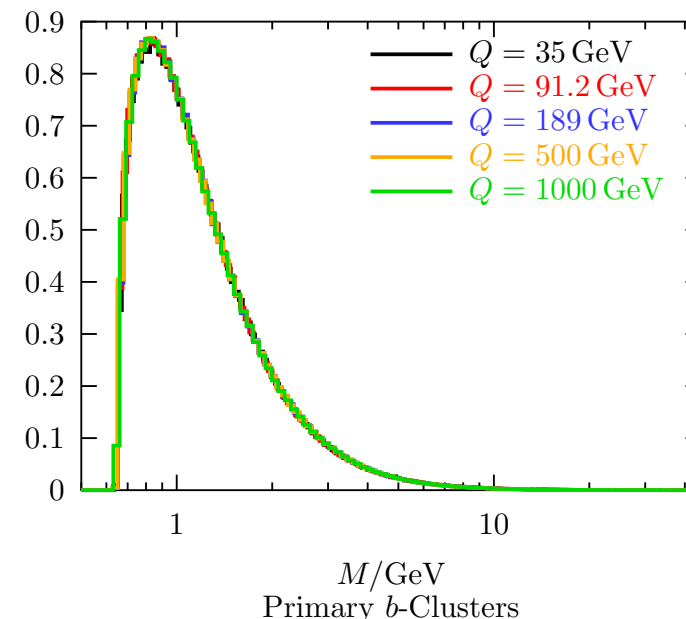
with additional phase space constraints. Constituents keep moving in their original direction.

- **Cluster Decay**

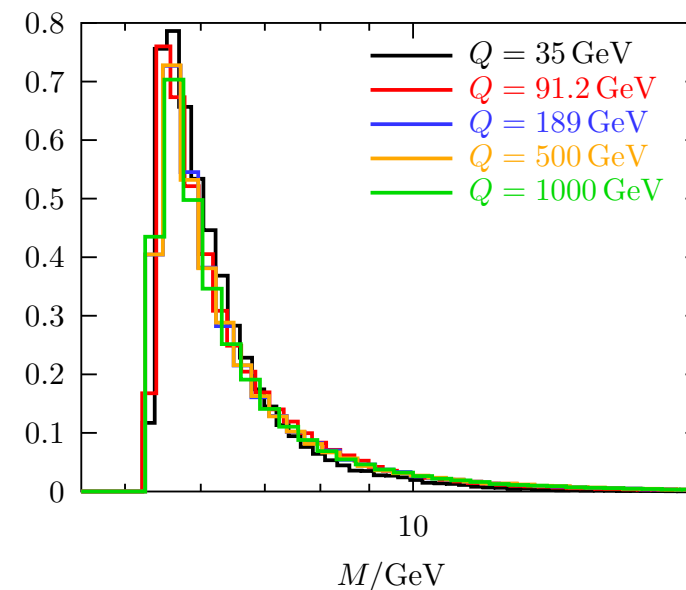
$$P(a_{i,q}, b_{q,j} | i, j) = \frac{W(a_{i,q}, b_{q,j} | i, j)}{\sum_{M/B} W(c_{i,q'}, d_{q',j} | i, j)}.$$

New! Meson/Baryon ratio is parametrized in terms of diquark weight. In HERWIG the sum ran over all possible hadrons.

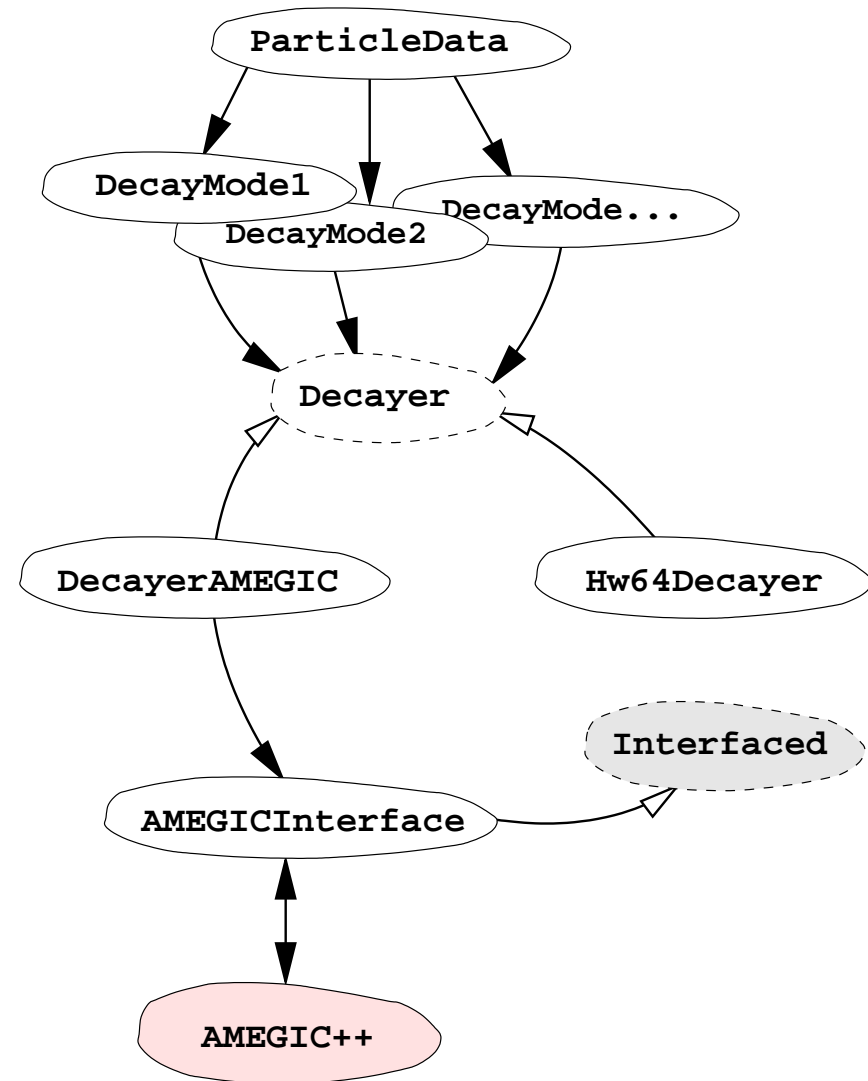
Primary Light Clusters



Primary b -Clusters



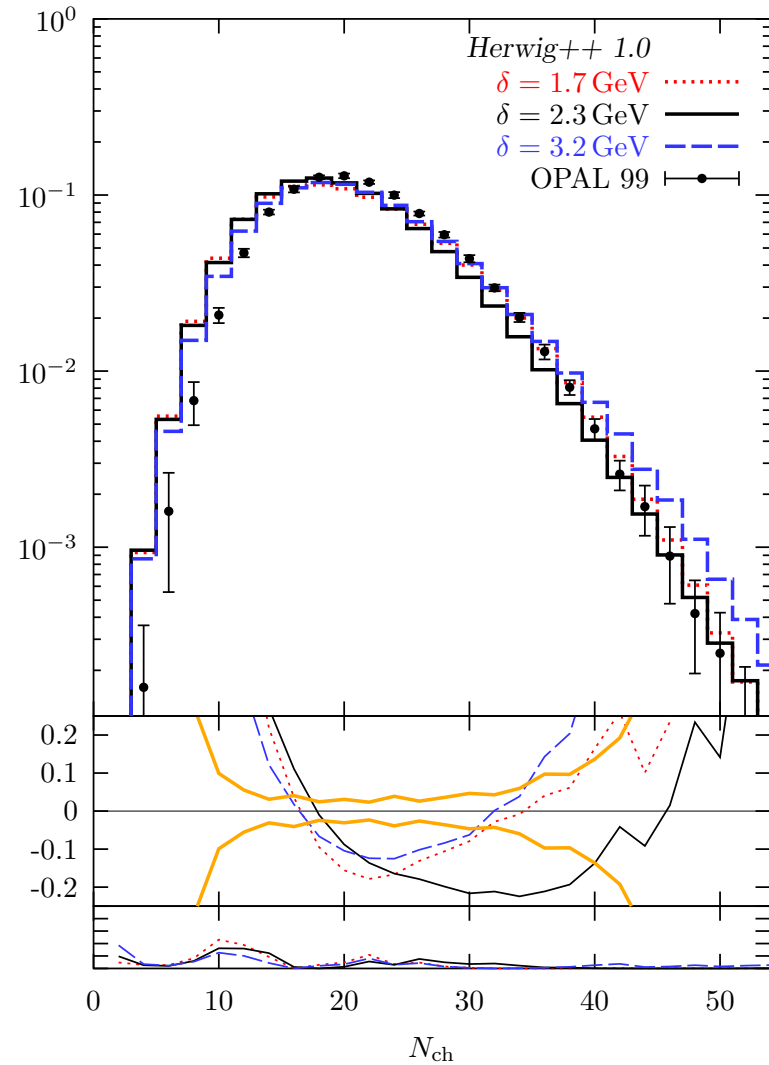
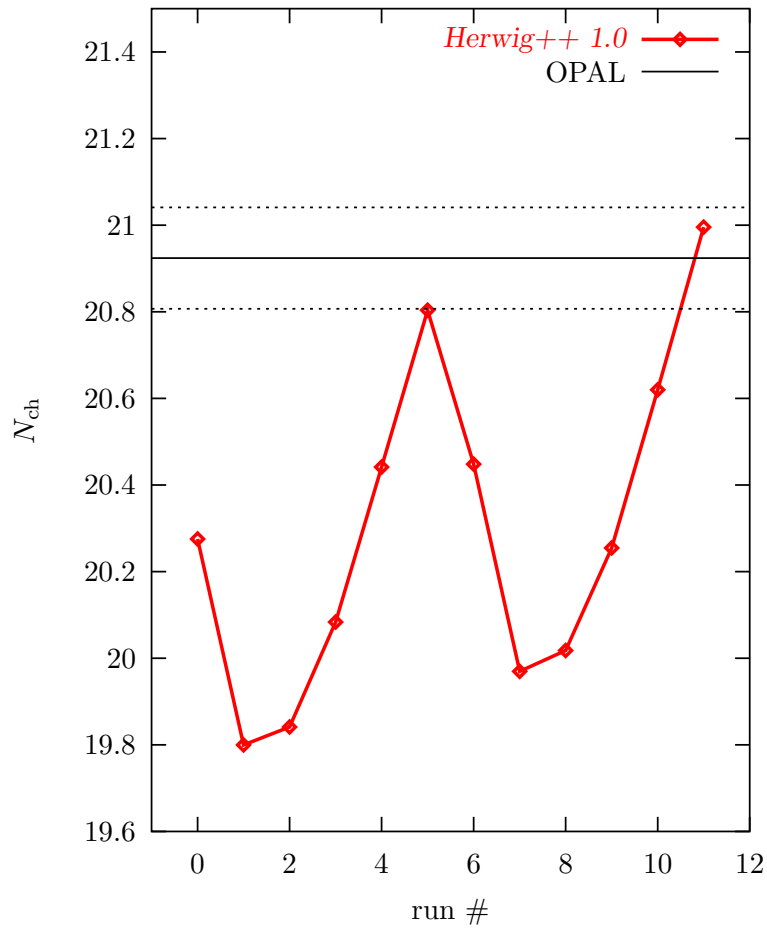
Decays



- FORTRAN HERWIG is reproduced with **Hw64Decayer** using the same Matrix element codes as before (will be used for hadronic decays right now)
- **DecayerAMEGIC** gets final states for a decay mode directly from **AMEGIC++**

Charged Particle Multiplicity

Good indicator for quality of hadronization. Still very sensitive on shower cutoff:



Hadron Multiplicities

Particle	Experiment	Measured	Old Model	Herwig++	Fortran
All Charged	M,A,D,L,O	20.924 ± 0.117	20.22*	20.814	20.532*
γ	A,O	21.27 ± 0.6	23.032	22.67	20.74
π^0	A,D,L,O	9.59 ± 0.33	10.27	10.08	9.88
$\rho(770)^0$	A,D	1.295 ± 0.125	1.235	1.316	1.07
π^\pm	A,O	17.04 ± 0.25	16.30	16.95	16.74
$\rho(770)^\pm$	O	2.4 ± 0.43	1.99	2.14	2.06
η	A,L,O	0.956 ± 0.049	0.886	0.893	0.669*
$\omega(782)$	A,L,O	1.083 ± 0.088	0.859	0.916	1.044
$\eta'(958)$	A,L,O	0.152 ± 0.03	0.13	0.136	0.106
K^0	S,A,D,L,O	2.027 ± 0.025	2.121*	2.062	2.026
$K^*(892)^0$	A,D,O	0.761 ± 0.032	0.667	0.681	0.583*
$K^*(1430)^0$	D,O	0.106 ± 0.06	0.065	0.079	0.072
K^\pm	A,D,O	2.319 ± 0.079	2.335	2.286	2.250
$K^*(892)^\pm$	A,D,O	0.731 ± 0.058	0.637	0.657	0.578
$\phi(1020)$	A,D,O	0.097 ± 0.007	0.107	0.114	0.134*
p	A,D,O	0.991 ± 0.054	0.981	0.947	1.027
Δ^{++}	D,O	0.088 ± 0.034	0.185	0.092	0.209*
Σ^-	O	0.083 ± 0.011	0.063	0.071	0.071
Λ	A,D,L,O	0.373 ± 0.008	0.325*	0.384	0.347*
Σ^0	A,D,O	0.074 ± 0.009	0.078	0.091	0.063
Σ^+	O	0.099 ± 0.015	0.067	0.077	0.088
$\Sigma(1385)^\pm$	A,D,O	0.0471 ± 0.0046	0.057	0.0312*	0.061*
Ξ^-	A,D,O	0.0262 ± 0.001	0.024	0.0286	0.029
$\Xi(1530)^0$	A,D,O	0.0058 ± 0.001	0.026*	0.0288*	0.009*
Ω^-	A,D,O	0.00125 ± 0.00024	0.001	0.00144	0.0009

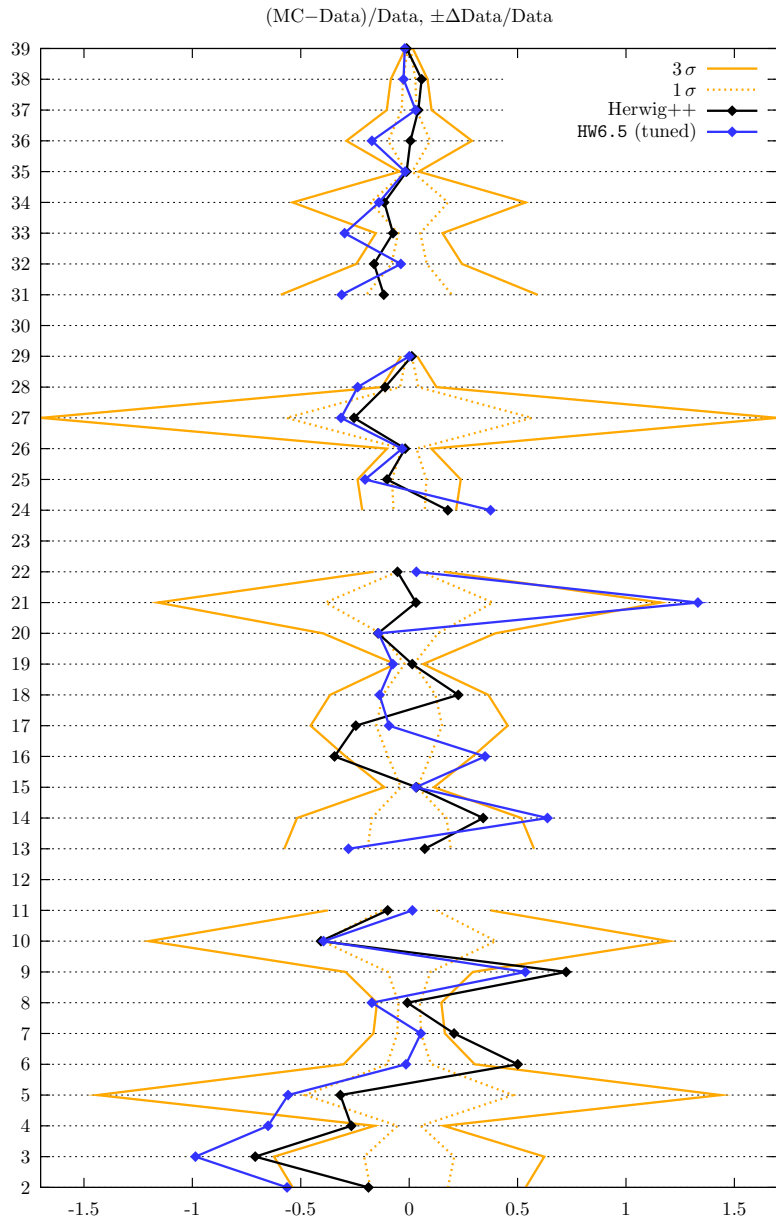
Hadron Multiplicities (ctd')

Particle	Experiment	Measured	Old Model	Herwig++	Fortran
$f_2(1270)$	D,L,O	0.168 ± 0.021	0.113	0.150	0.173
$f_2'(1525)$	D	0.02 ± 0.008	0.003	0.012	0.012
D^\pm	A,D,O	0.184 ± 0.018	0.322*	0.319*	0.283*
$D^*(2010)^\pm$	A,D,O	0.182 ± 0.009	0.168	0.180	0.151*
D^0	A,D,O	0.473 ± 0.026	0.625*	0.570*	0.501
D_s^\pm	A,O	0.129 ± 0.013	0.218*	0.195*	0.127
$D_s^{*\pm}$	O	0.096 ± 0.046	0.082	0.066	0.043
J/Ψ	A,D,L,O	0.00544 ± 0.00029	0.006	0.00361*	0.002*
Λ_c^+	D,O	0.077 ± 0.016	0.006*	0.023*	0.001*
$\Psi'(3685)$	D,L,O	0.00229 ± 0.00041	0.001*	0.00178	0.0008*

of *'s = observables with more than 3σ deviation:

OldModel : Herwig++ : Fortran = 9 : 7 : 13

Hadron Multiplicities (ctd')

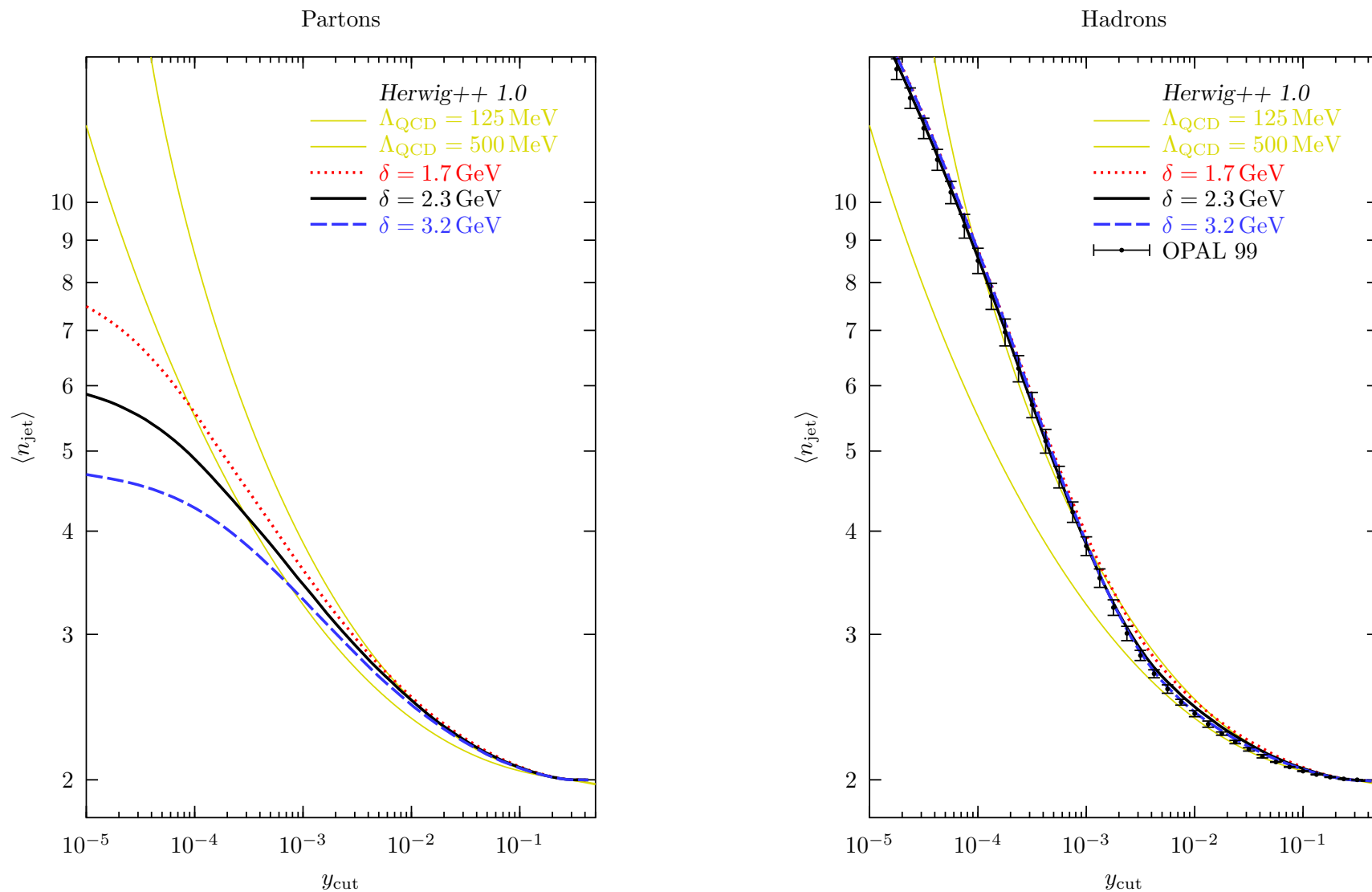


We can compare χ^2 's:

model	$\sum \chi^2 / \text{dof} =$
DKMode 0:	543.84/35 = 15.54
DKMode 1:	3644.33/35 = 104.12
Herwig++:	277.16/35 = 7.92
no D^\pm :	= 6.54
HW65d:	7151.13/35 = 204.32
HW65t:	490.52/35 = 14.01
no J/ψ :	= 4.38

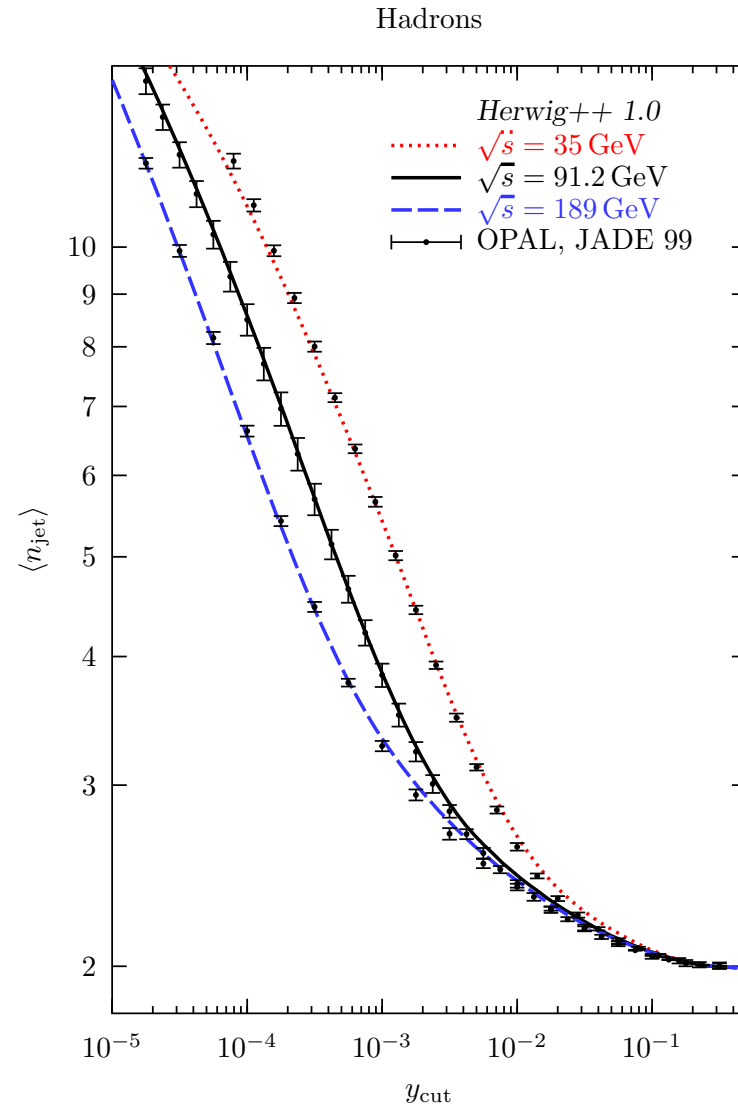
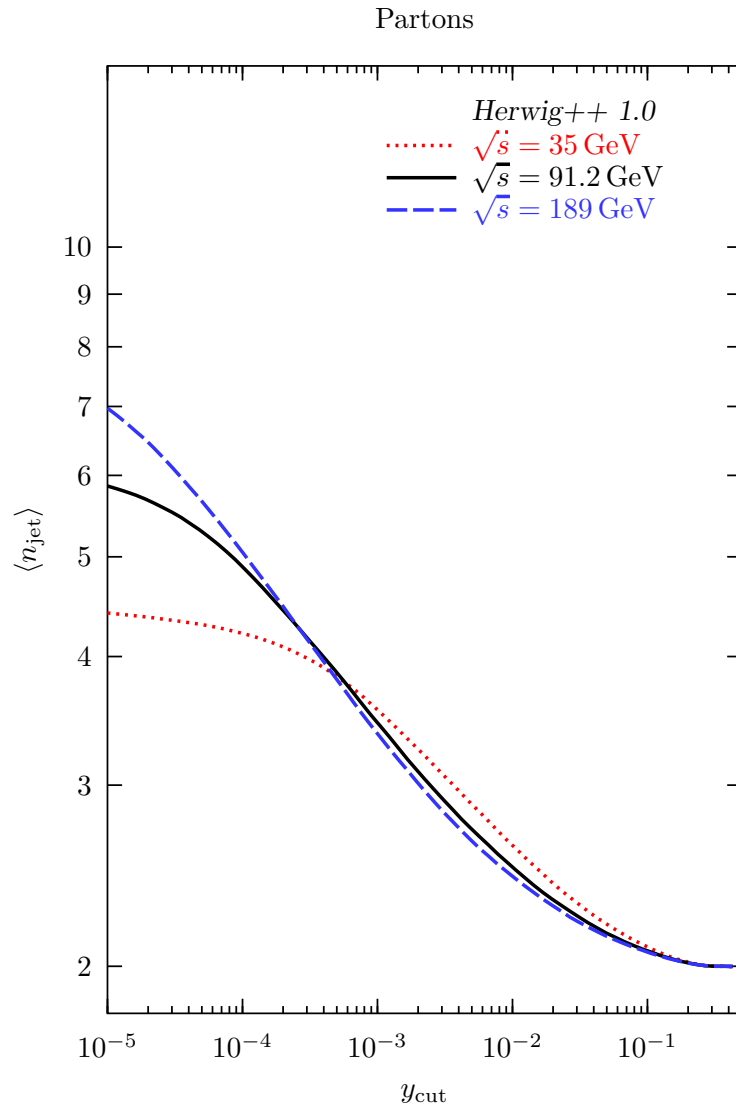
Jet Multiplicity

Durham algorithm. Smooth interplay between shower and hadronization.



Jet Multiplicity (PETRA, LEP, LEP II)

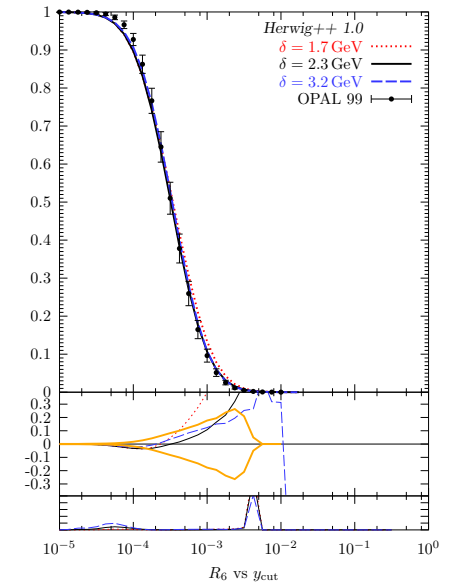
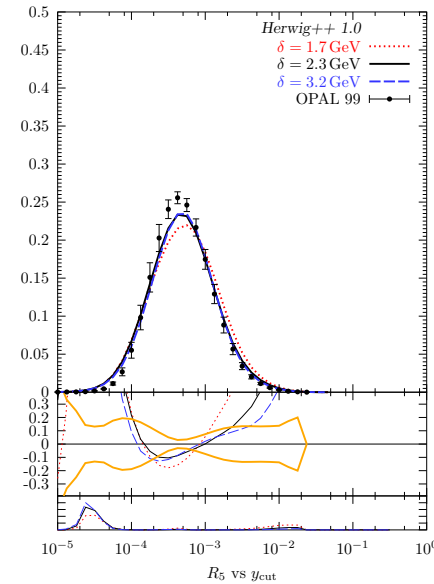
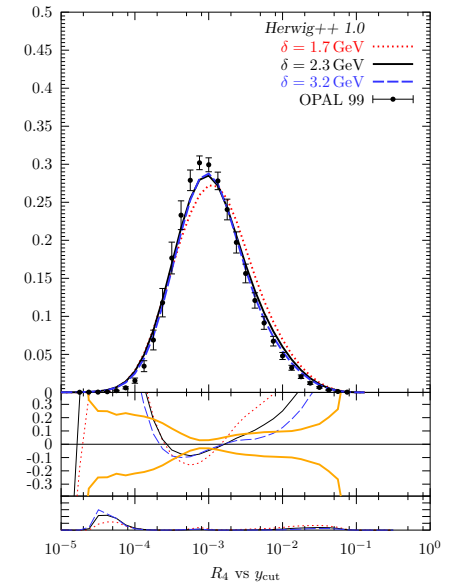
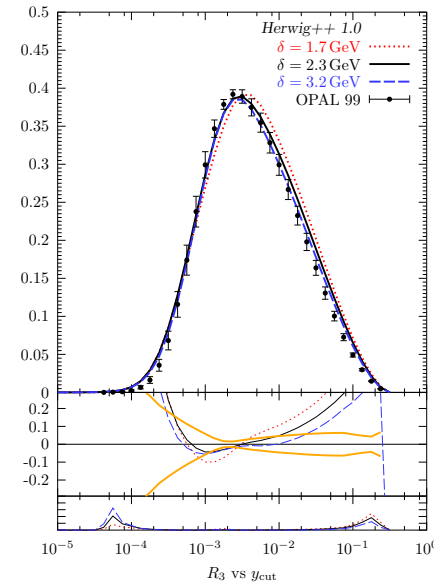
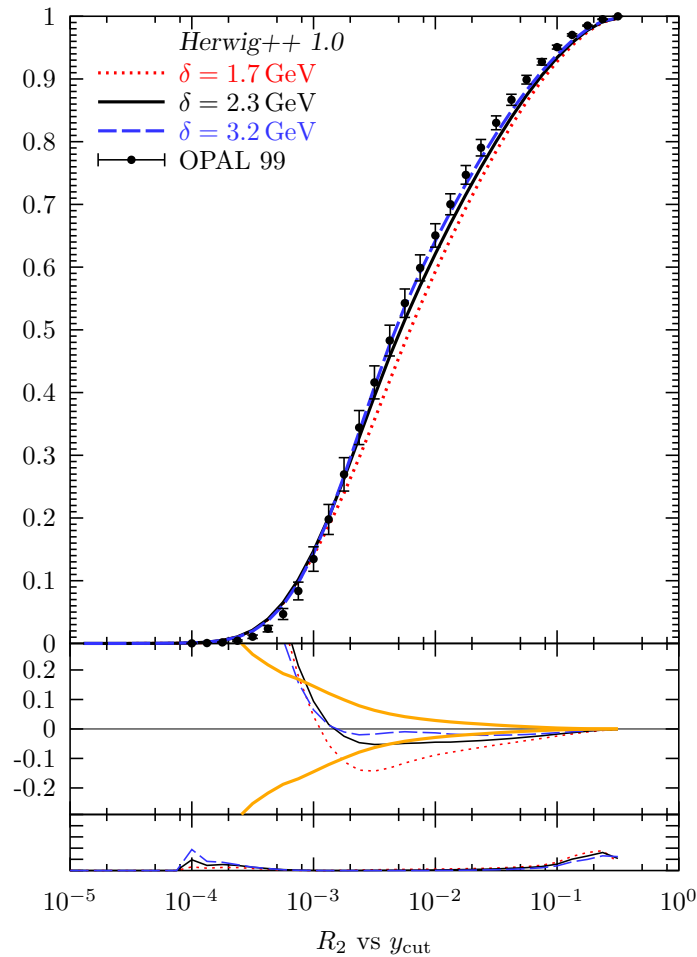
$$\sqrt{s} = \{35, 91.2, 189\} \text{ GeV}$$



Jet Rates

$$R_n = \sigma(n\text{-jets})/\sigma(\text{jets}) \quad (n = 2..5)$$

$$R_6 = \sigma(> 5\text{-jets})/\sigma(\text{jets})$$



Event Shape Variables, Definition

Thrust

$$F(\mathbf{n}) = \frac{\sum_{\alpha} |\mathbf{p}_{\alpha} \cdot \mathbf{n}|}{\sum_{\alpha} |\mathbf{p}_{\alpha}|}$$

Find \mathbf{n} , such that thrust

$$\begin{aligned} T &= \max_{\mathbf{n}} F(\mathbf{n}) \\ &= F(\mathbf{n}_T) , \end{aligned}$$

thrust major

$$\begin{aligned} M &= \max_{\mathbf{n} \perp \mathbf{n}_T} F(\mathbf{n}) \\ &= F(\mathbf{n}_M) , \end{aligned}$$

thrust minor

$$\begin{aligned} \mathbf{n}_m &= \mathbf{n}_T \times \mathbf{n}_M \\ m &= F(\mathbf{n}_m) \end{aligned}$$

Sphericity

$$Q_{ij} = \frac{\sum_{\alpha} (\mathbf{p}_{\alpha})_i (\mathbf{p}_{\alpha})_j}{\sum_{\alpha} \mathbf{p}_{\alpha}^2}$$

Diagonalize, eigenvalues

$$\begin{aligned} \lambda_1 &> \lambda_2 > \lambda_3 \\ \lambda_1 + \lambda_2 + \lambda_3 &= 1 \end{aligned}$$

Then

$$\begin{aligned} S &= \frac{3}{2}(\lambda_2 + \lambda_3) \\ P &= \lambda_2 - \lambda_3 \\ A &= \frac{3}{2}\lambda_3 \end{aligned}$$

Eigenvector \mathbf{n}_S sphericity axis
etc.

C, D parameter

$$L_{ij} = \frac{\sum_{\alpha} (\mathbf{p}_{\alpha})_i (\mathbf{p}_{\alpha})_j / |\mathbf{p}_{\alpha}|}{\sum_{\alpha} |\mathbf{p}_{\alpha}|}$$

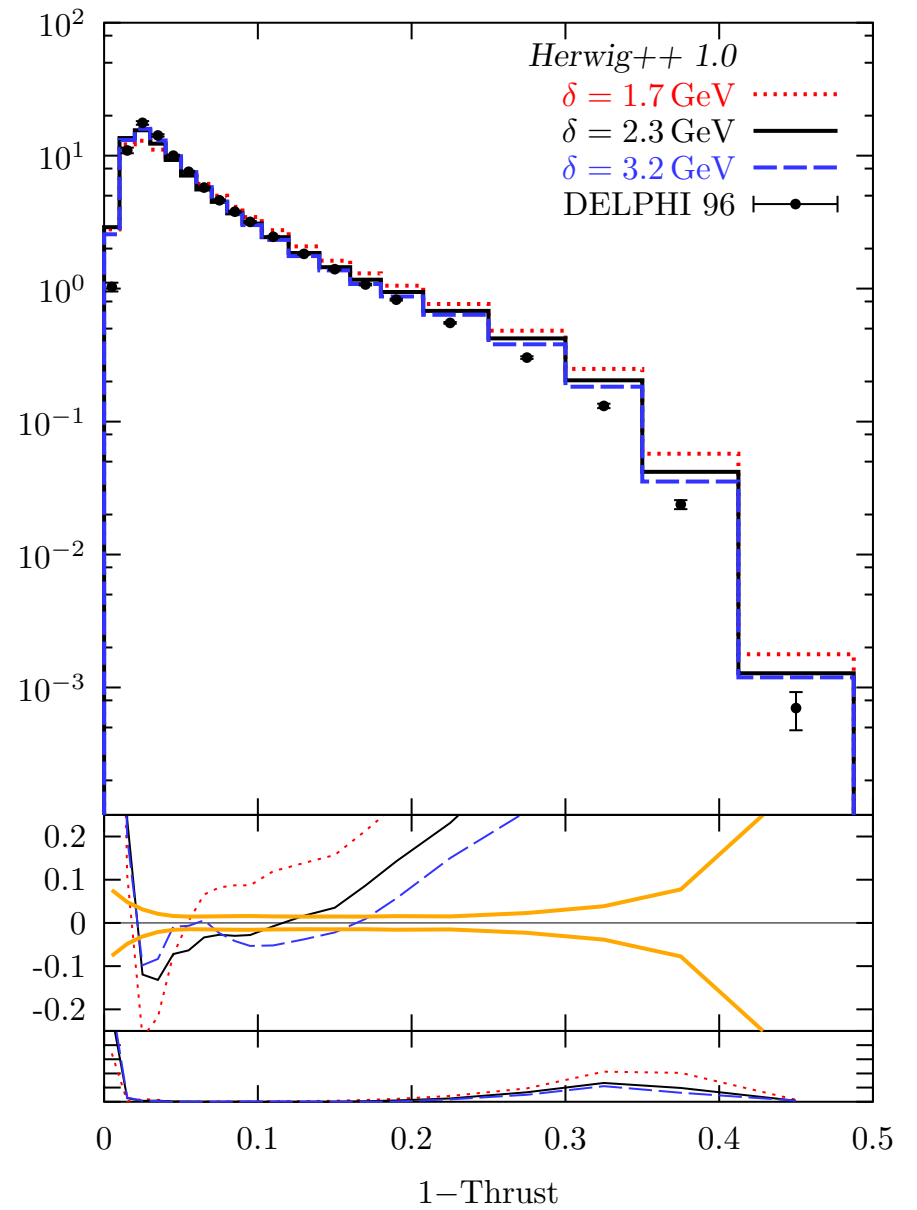
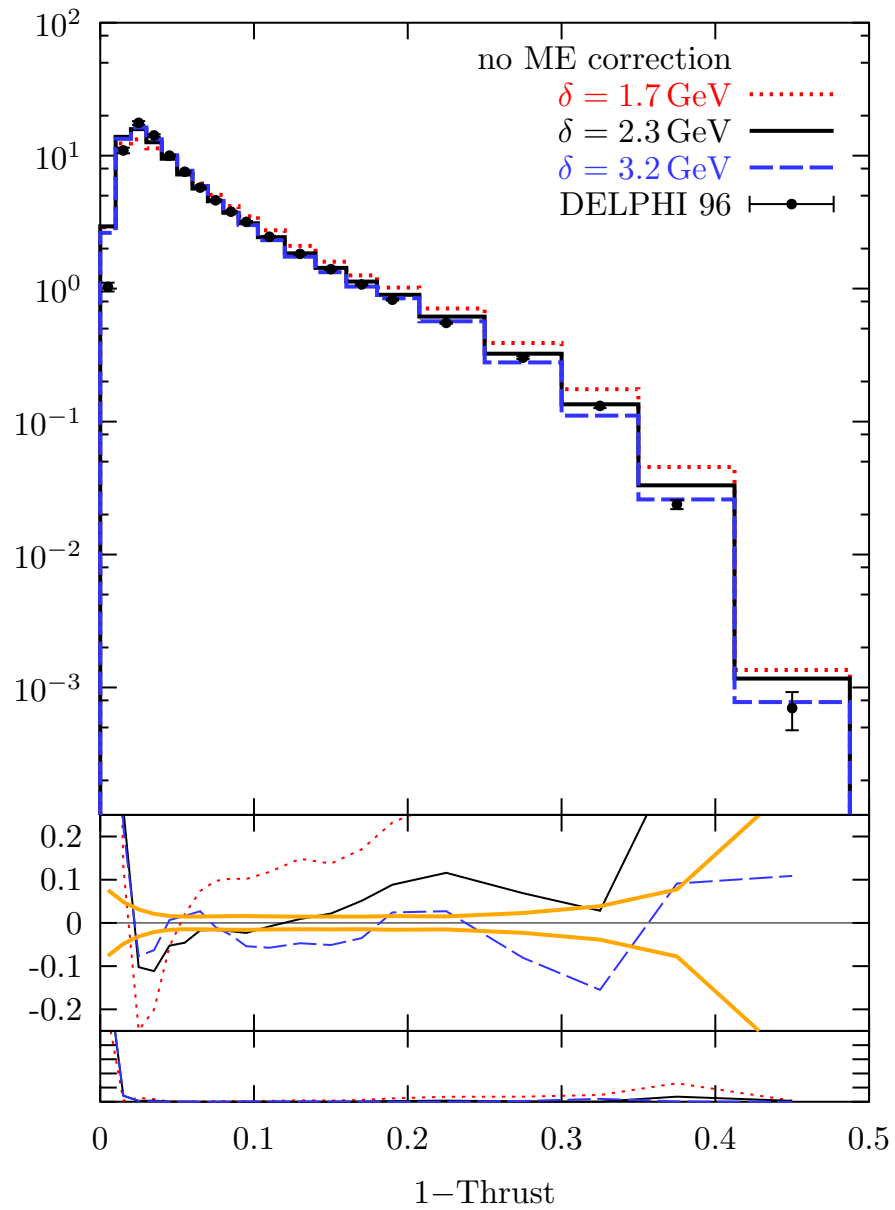
Diagonalize, eigenvalues

$$\lambda_1 + \lambda_2 + \lambda_3 = 1$$

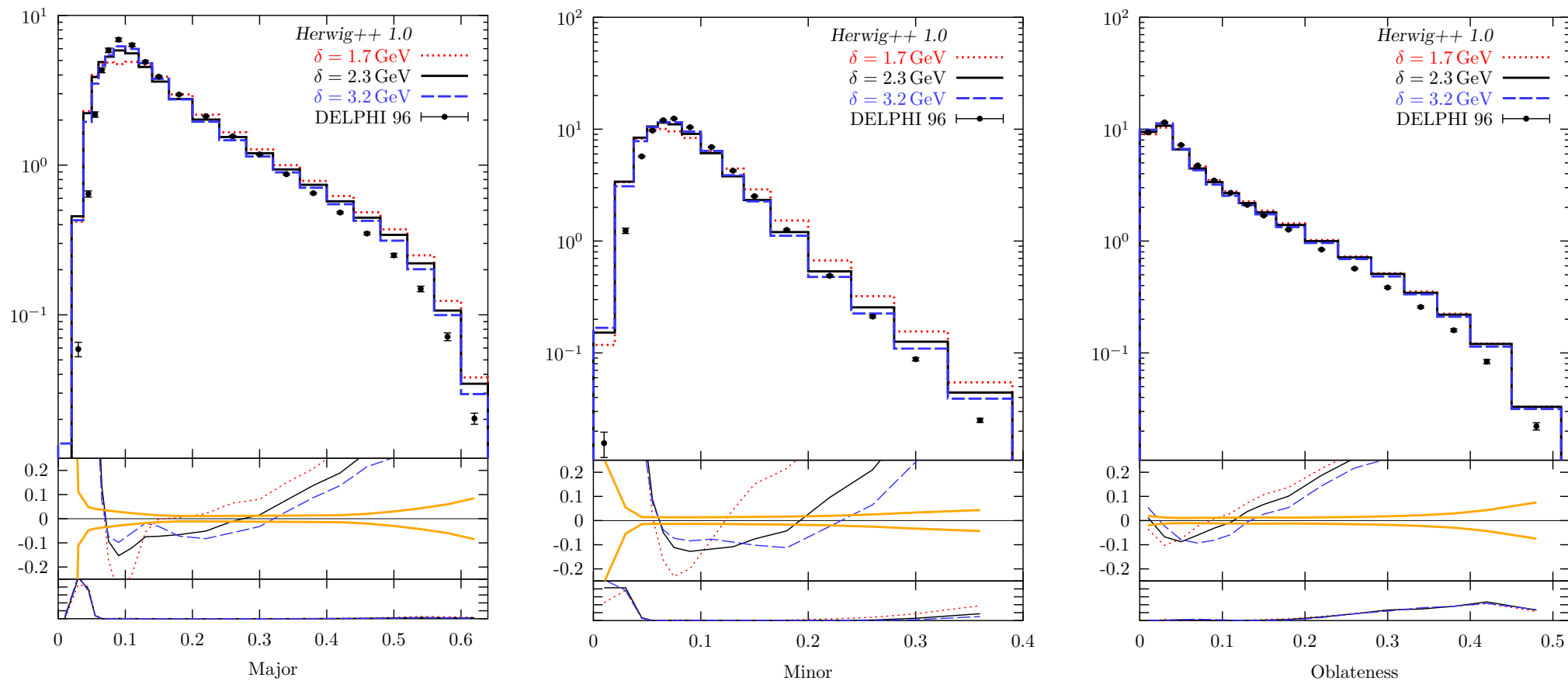
and define

$$\begin{aligned} C &= 3(\lambda_1 \lambda_2 + \lambda_2 \lambda_3 + \lambda_3 \lambda_1) \\ D &= 27 \lambda_1 \lambda_2 \lambda_3 \end{aligned}$$

Thrust — ME Corrections off/on

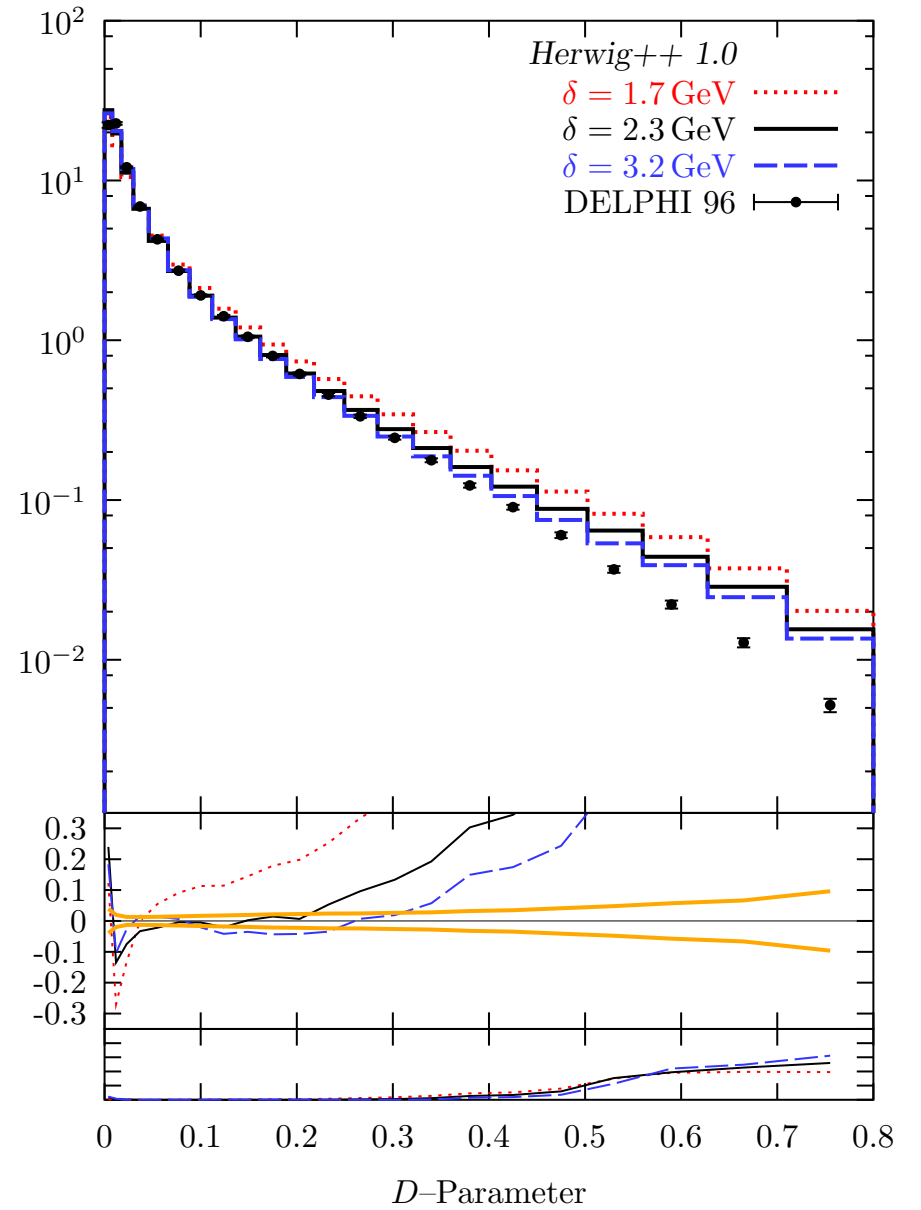
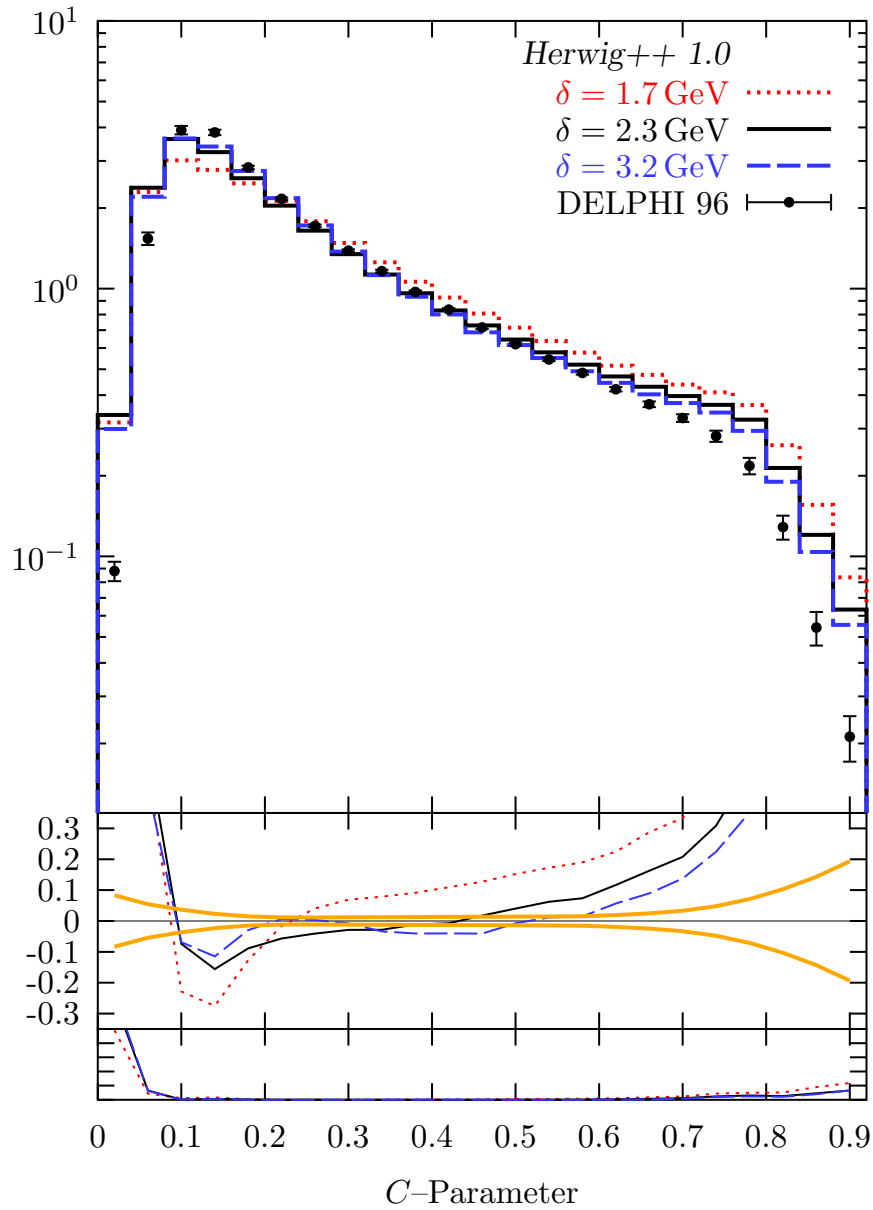


Major, Minor, Oblateness



All Thrust-related distributions slightly wide, ie too many 2-jet like on one side and too many spherical events on the other side.

C and D parameter



Four Jet Angles — Definitions

Bengtsson–Zerwas angle

$$\chi_{BZ} = \angle(\mathbf{p}_1 \times \mathbf{p}_2, \mathbf{p}_3 \times \mathbf{p}_4)$$

Körner–Schierholz–Willrodt angle

$$\Phi_{KSW} = \frac{1}{2} [\angle(\mathbf{p}_1 \times \mathbf{p}_3, \mathbf{p}_2 \times \mathbf{p}_4) + \angle(\mathbf{p}_1 \times \mathbf{p}_4, \mathbf{p}_2 \times \mathbf{p}_3)]$$

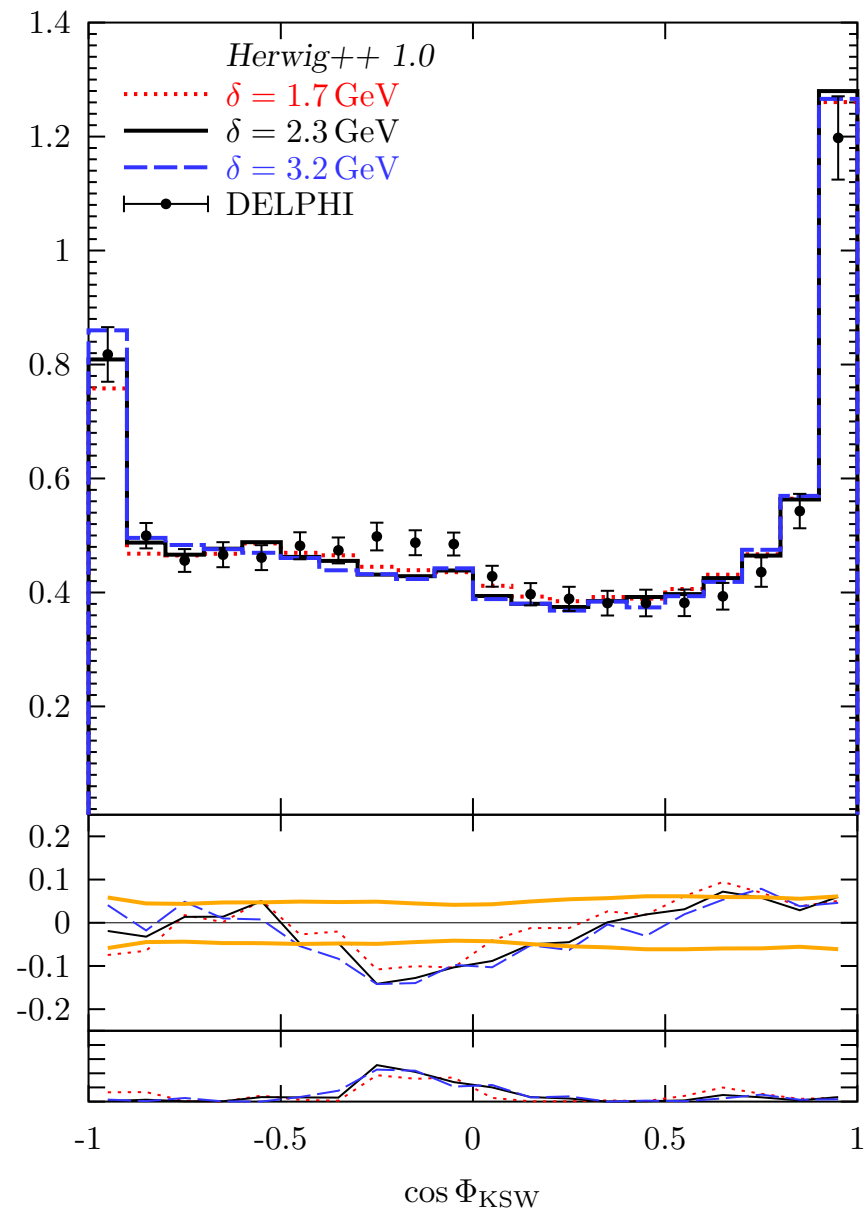
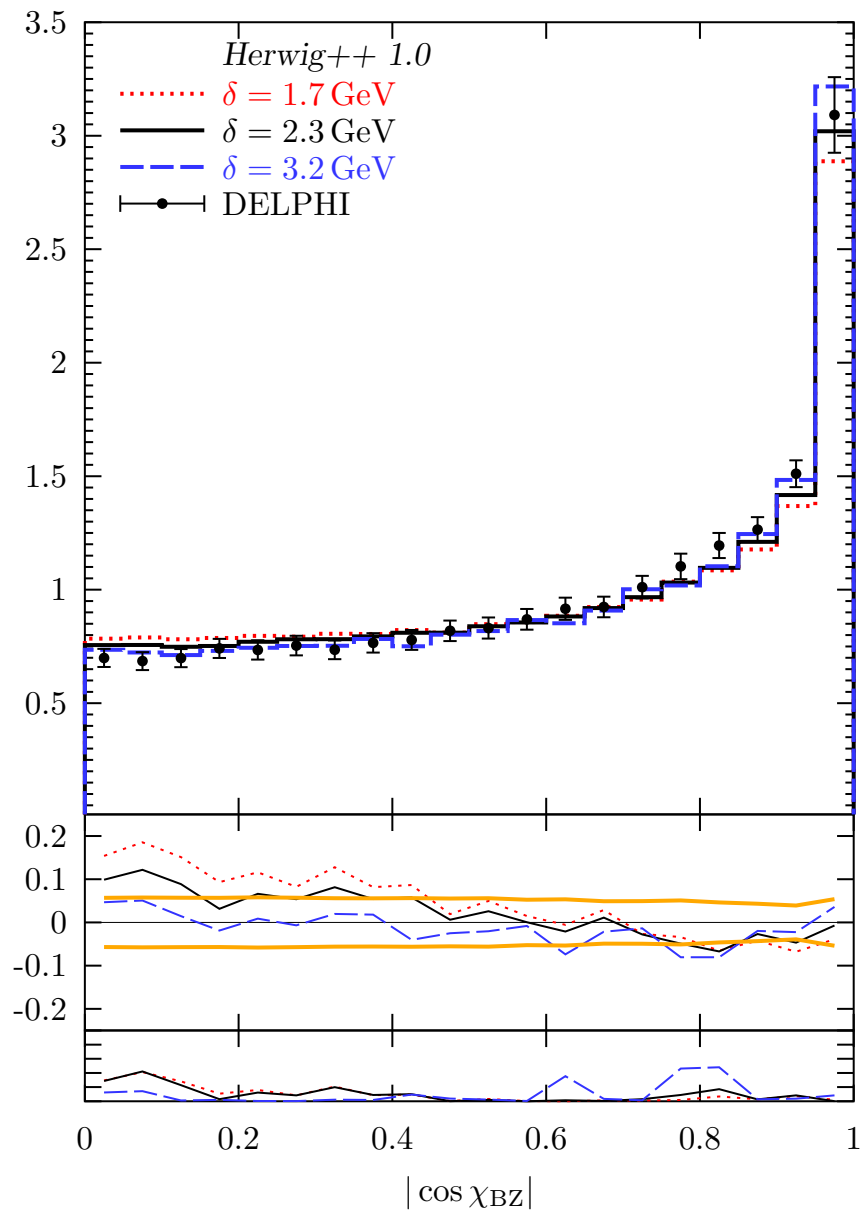
(modified) Nachtmann–Reiter angle

$$\theta_{NR}^* = \angle(\mathbf{p}_1 - \mathbf{p}_2, \mathbf{p}_3 - \mathbf{p}_4)$$

α_{34} :

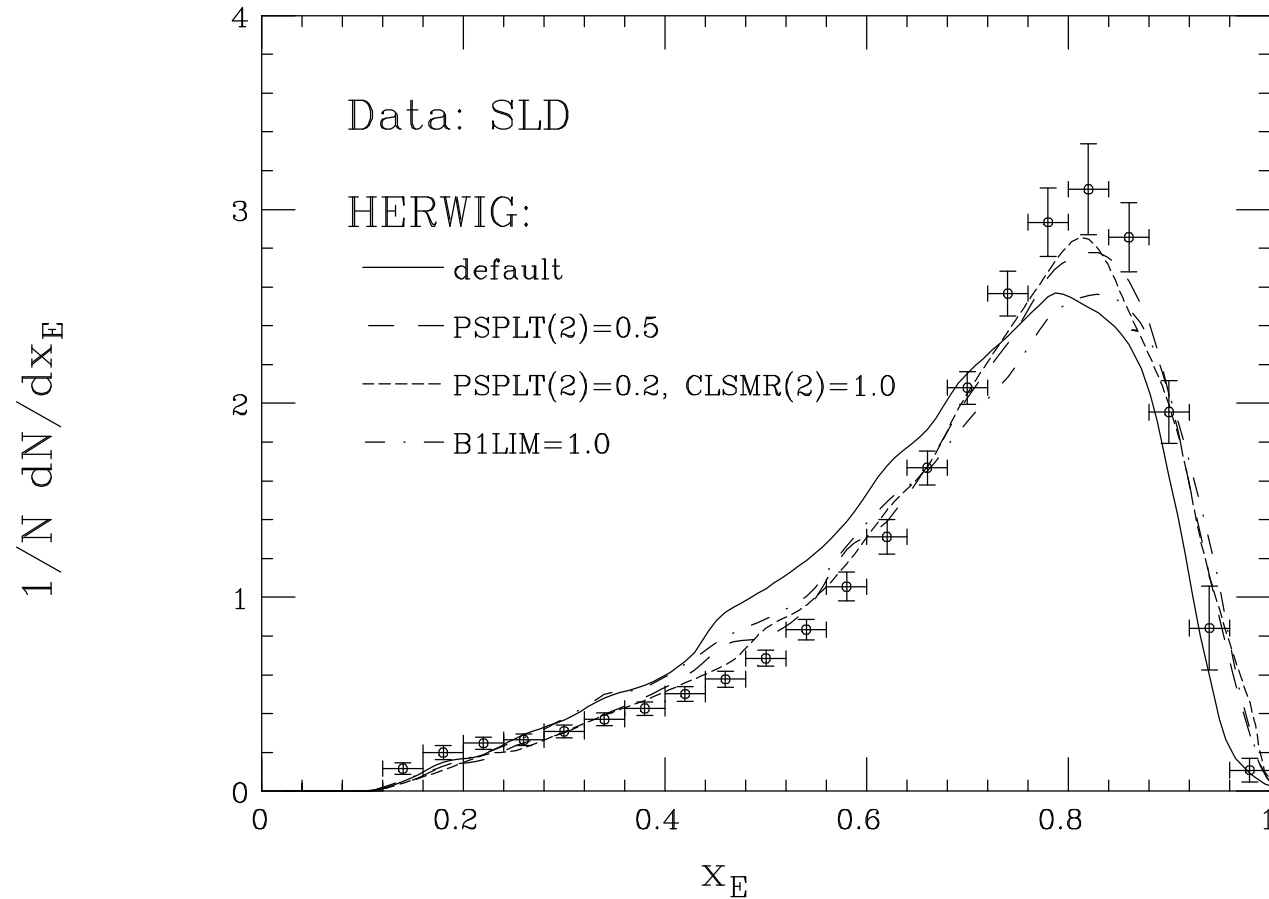
$$\alpha_{34} = \angle(\mathbf{p}_3, \mathbf{p}_4)$$

Four Jet Angles I



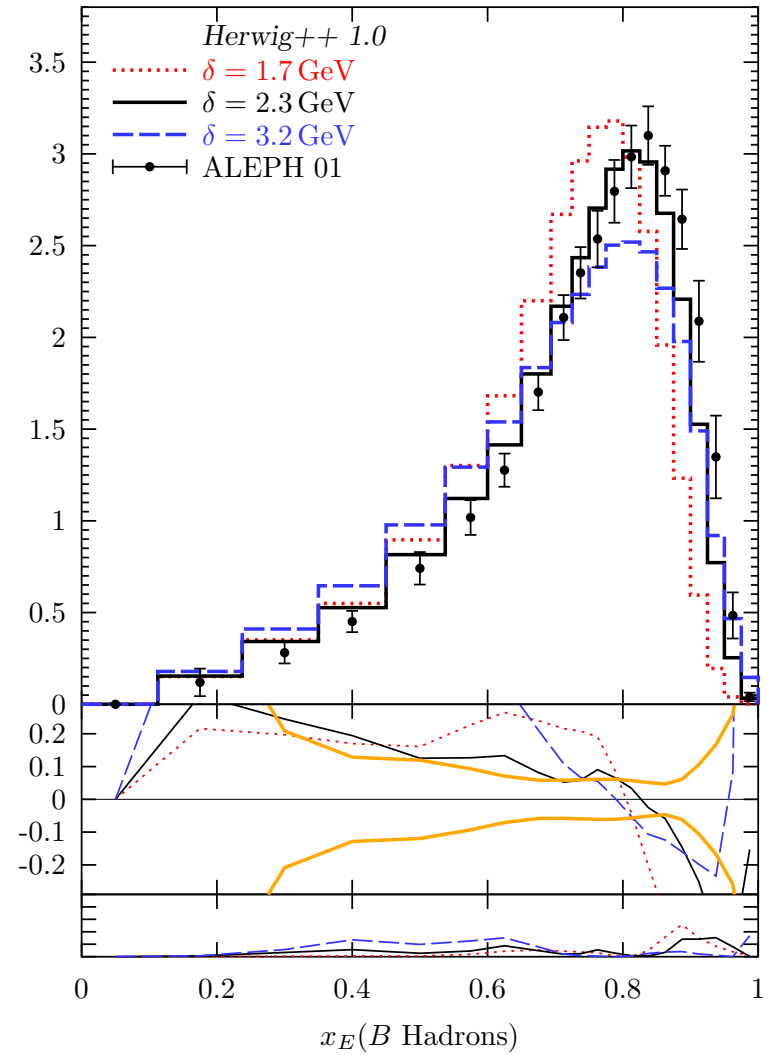
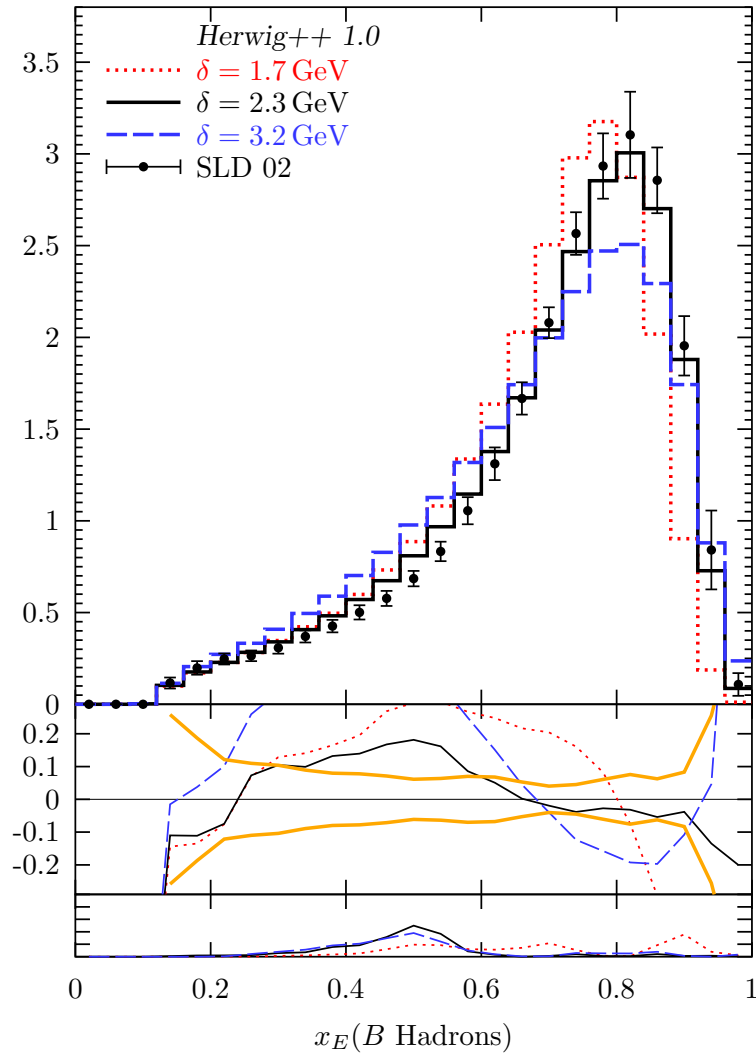
B-fragmentation function

Weakly decaying *b* hadrons



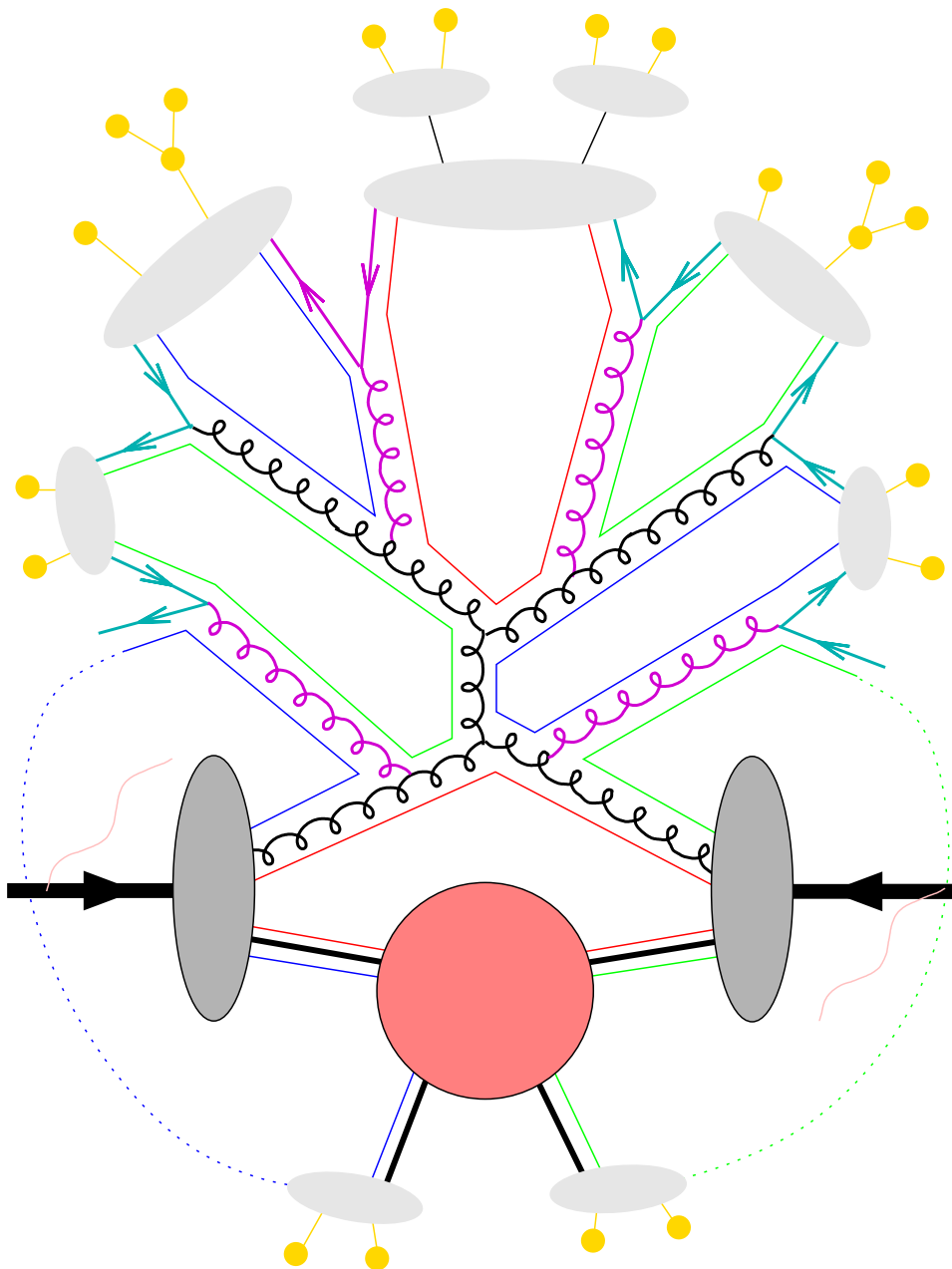
HERWIG 6.4, *B* specific hadronization parameters needed!

B-fragmentation function



Only parton shower parameters varied!

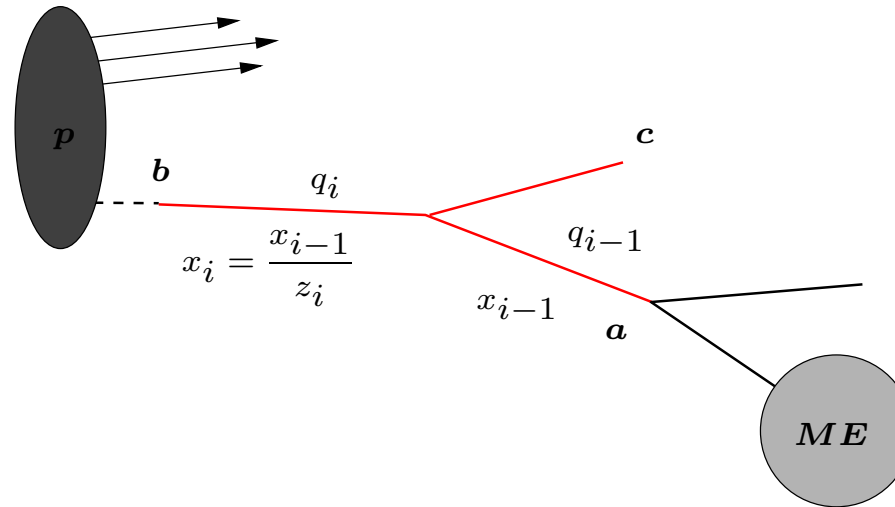
Additional Complications in $pp/p\bar{p}$



- + backward parton evolution
- + underlying event

Backward branching kinematics in Herwig++

Consider only single branching $b \rightarrow ac$:



Sudakov decomposition $q_i = \alpha_i p + \beta_i n + q_{\perp i}$. Basis $(p, n) \parallel$ proton direction. Kinematics of shower reconstructed from

$$\alpha_i = \frac{\alpha_{i-1}}{z}, \quad \mathbf{q}_{\perp i} = \frac{\mathbf{q}_{\perp i-1} - \mathbf{p}_{\perp i}}{z_i} .$$

$$\mathbf{p}_{\perp i}^2 = (1 - z_i)^2 \tilde{q}_i^2 - z_i Q_g^2 .$$

Q_g closely related to parton shower cutoff.

Sudakov form factor for space-like branchings

The Sudakov form factor for spacelike backward evolution of a parton a from the hard scale \tilde{q}_{\max} down to some scale \tilde{q} ,

$$S_a(\tilde{q}, \tilde{q}_{\max}; x, \tilde{q}_0) = \exp \left[- \sum_b \mathcal{I}_{ba}(\tilde{q}, \tilde{q}_{\max}; x, \tilde{q}_0) \right] . \quad (1)$$

The sum on the right hand side (rhs) is over all possible splittings into partons of type b and

$$\mathcal{I}_{ba}(\tilde{q}, \tilde{q}_{\max}; x, \tilde{q}_0) = \int_{\tilde{q}^2}^{\tilde{q}_{\max}^2} \frac{d\tilde{q}^2}{\tilde{q}^2} \int_{z_0}^{z_1} dz \frac{\alpha_s(z, \tilde{q}^2)}{2\pi} \frac{x' f_b(x', \tilde{q}^2)}{x f_a(x, \tilde{q}^2)} P_{ba}(z, \tilde{q}^2) . \quad (2)$$

Choosing the argument of $\alpha_s(Q)$ as $Q = (1 - z_i)\tilde{q}_i$ we may now rewrite the integral (2) as

$$\mathcal{I}_{ba}(\tilde{q}, \tilde{q}_{\max}; x, Q_g) = \int_{\tilde{q}^2}^{\tilde{q}_{\max}^2} \frac{d\tilde{q}^2}{\tilde{q}^2} \int_0^1 dz \frac{\alpha_s[(1 - z)\tilde{q}]}{2\pi} \frac{x' f_b(x', \tilde{q}^2)}{x f_a(x, \tilde{q}^2)} P_{ba}(z, \tilde{q}^2) \Theta(\text{P.S.}) . \quad (3)$$

Numerical study

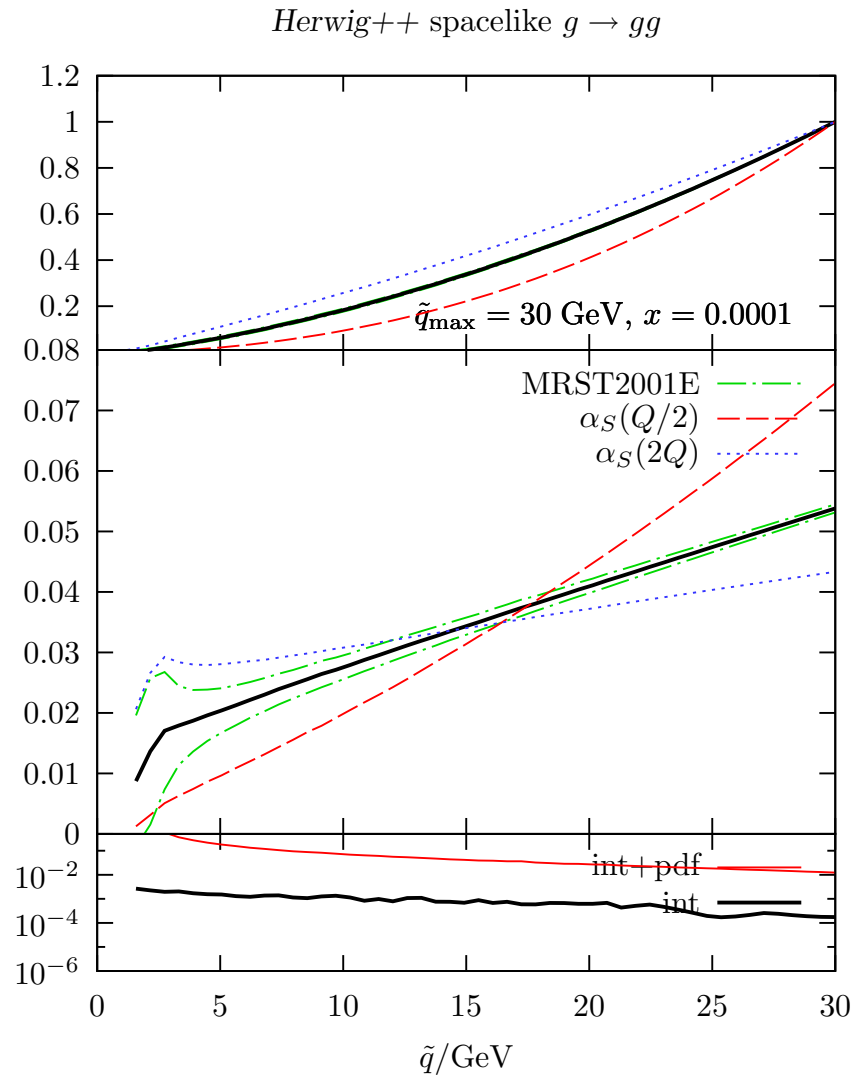
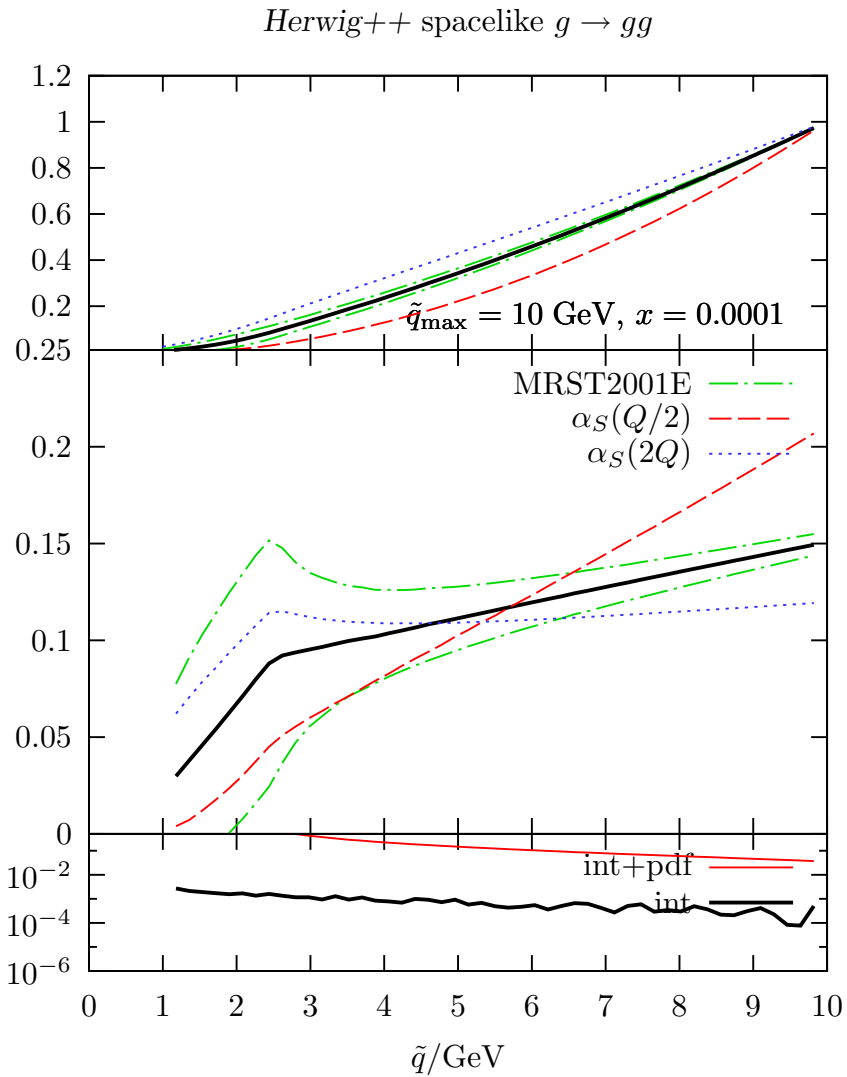
We consider

- different types of splittings.
- low and high x and \tilde{q}_{\max} .
- pdf errors from MRST/CTEQ,
- $\alpha_s(Q)$ errors from scale variation in comparison.
- NP treatment of $\alpha_s(Q)$.
- no study of effects beyond NLL.
- no kinematics from other generators
- strictly only first emission (vetos. . .)

We always show


- Sudakov form factor (top panel)
- Branching probability density (middle panel)
- Error information (bottom panel)

$g \rightarrow gg$, lower x , higher \tilde{q}_{\max}



Quite sizable at very small x . Shrinks again for larger \tilde{q}_{\max} .

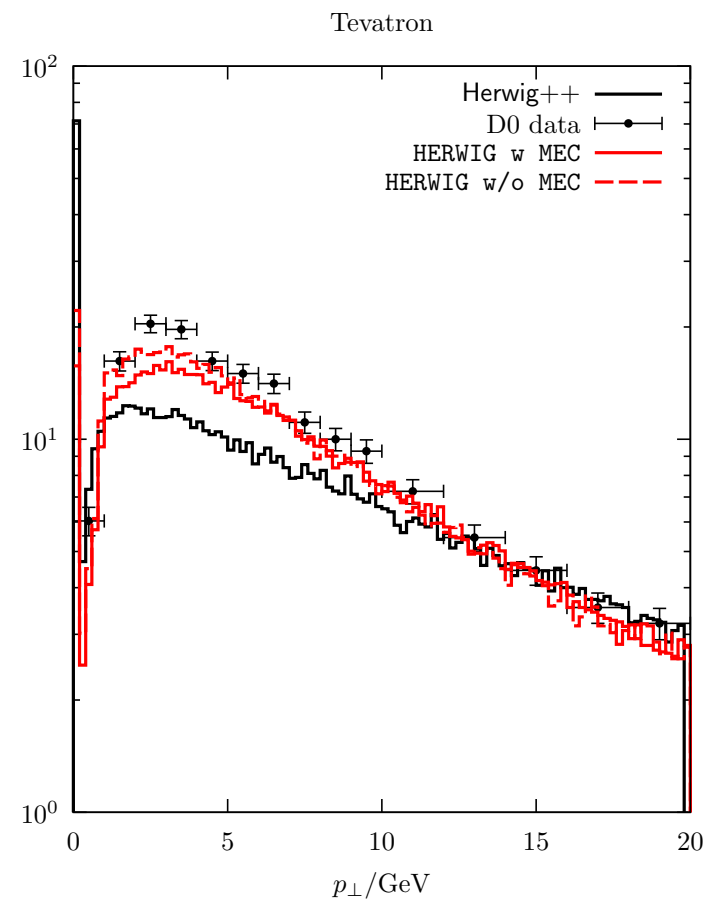
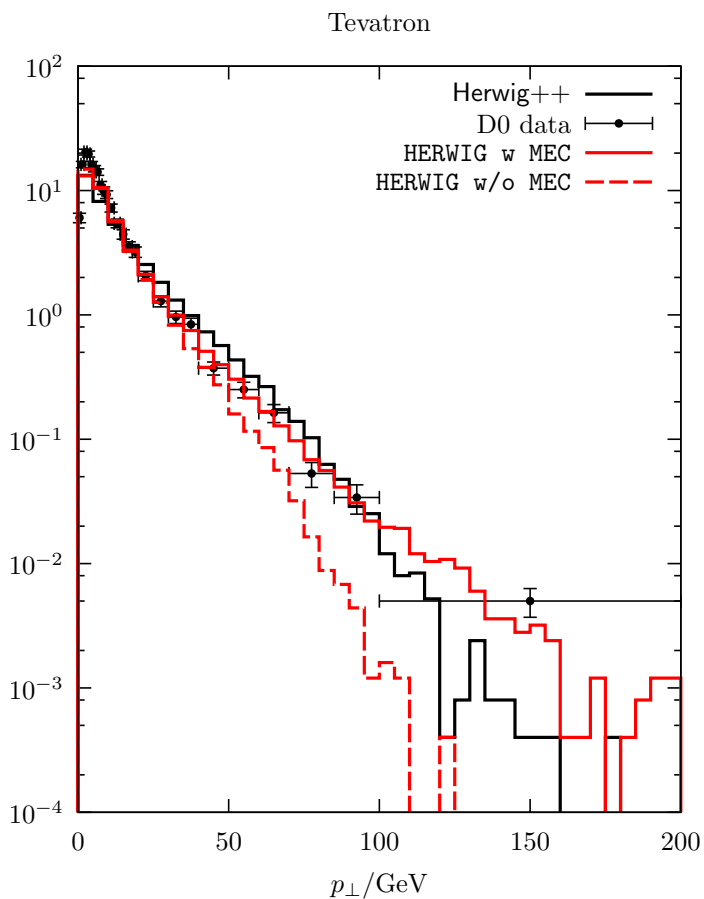
Some remarks

- Sudakov FF can be a useful tool for understanding certain effects.
- effect of pdf errors mostly small.
- *BUT* can be large in places  $t\bar{t}$?
- all compared to α_s scale uncertainties.
- very sensitive to non-perturbative α_s and scale variations in general (used for tuning. . .).
- NLL effects may be interesting to look at in greater detail?!

—→ *talk at parallel session*

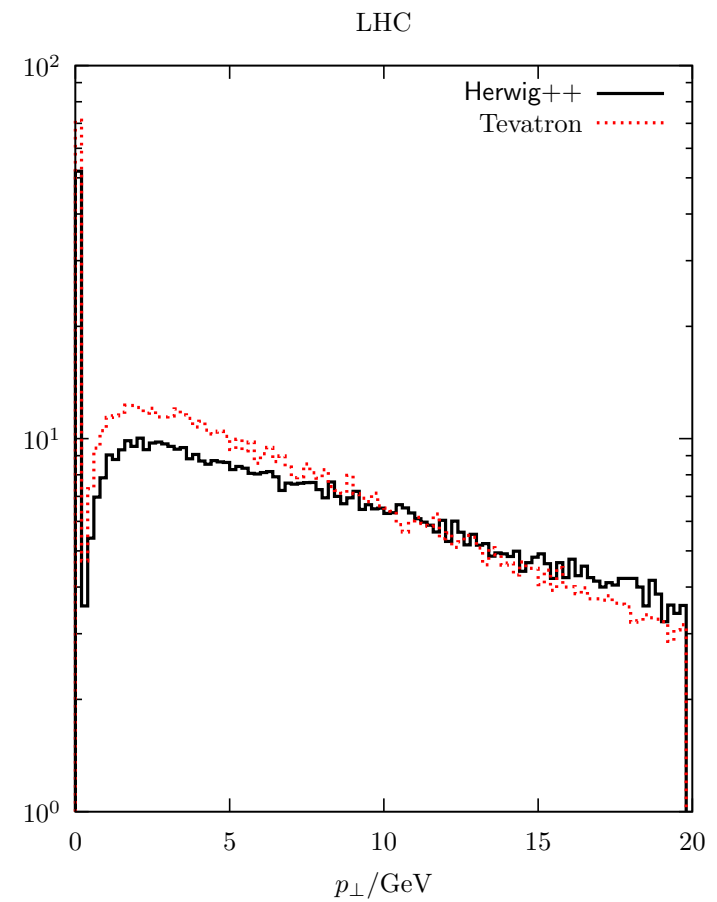
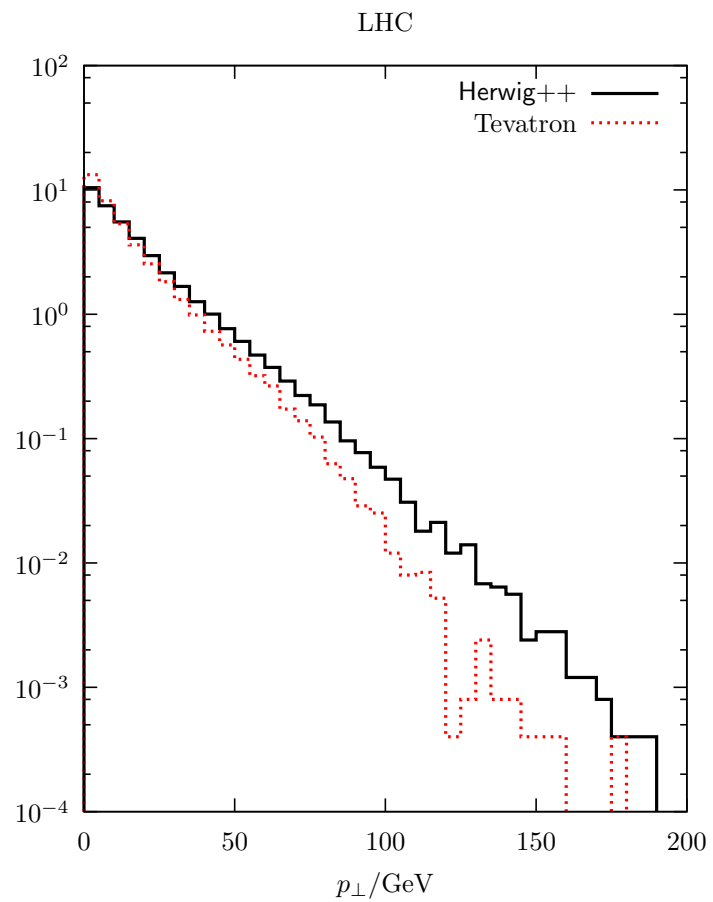
Currently working on initial state shower. . .

- Parton shower implementations of evolution in our 'new variables' (hep-ph/0310083) ongoing.
- First results for Drell–Yan coming up.
- Decays.



Currently working on initial state shower. . .

- same for LHC, compared to Tevatron.



New Decays!

- Better decayers are being developed for almost all decay modes.
- $\rightarrow B$ decays.
- Spin correlations will be included.
- Major effort ongoing
 - a universal database is being set up.
 - contains 448 particles and 2607 decay modes at present.
 - possibility to generate configuration files for different generators (they need to write their own code however. . .).
- Particle data book as guideline.

\longrightarrow *look at examples. . .*

What's next?

Near Future. . .

- ★ Initial state shower:
 - Complete implementation and tests.
- ★ Refine e^+e^- :
 - Full CKKW ME+PS matching.
 - Precision tune to LEP data should be possible.
- ★ with IS and FS showers running:
 - we can start to test Drell–Yan and jets in pp collisions.
 - cross check with Tevatron data and finally make predictions for the LHC.
- ★ Underlying Event.
- ★ Hadronic Decays: *NEW!* many new decayers, τ -decays, Spin correlations (P Richardson).
- ★ *New Ideas*: soft gluons, improved shower algorithm, NLO, . . .

Schedule?

- Ready for LHC!