

Hadronic MC generators for colliders and cosmic rays

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QCD at Cosmic Energies - II

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- Introduction: models for colliders and models for cosmic rays
- Conventional structure:
 - Gribov's Reggeon approach and multiple scattering
 - QCD and hard processes
 - color connections and hadronization
- “Dense” partonic systems: non-linear effects
- Air shower characteristics and related quantities
- Cosmic ray interactions: remaining puzzles
- Outlook

Introduction: models for colliders and models for cosmic rays

MC generators at colliders and in CRs:

- planning new experiments
- analysis & interpretation of data
- testing theoretical ideas

Contemporary models:

- similar physics input
- guided by accelerator data

But: models for colliders or models for CRs?

Model \equiv approximation of the reality; has to mimic its essential features

Essential for colliders:

- detailed simulation of the interaction pattern
- close detailed agreement with experimental data
- high p_t physics of special importance (pQCD tests, background for new physics)

Possible simplifications:

- models applicable to **particular** (not all) event classes, e.g.,
 - high p_t jet triggered
 - central heavy ion collisions
- models can be **re-tuned** for a particular experiment

Typical collider models:

- PITHYA (Sjostrand et al.)
- HERWIG (Webber et al.)
- HIJING (Wang & Gyulassy)

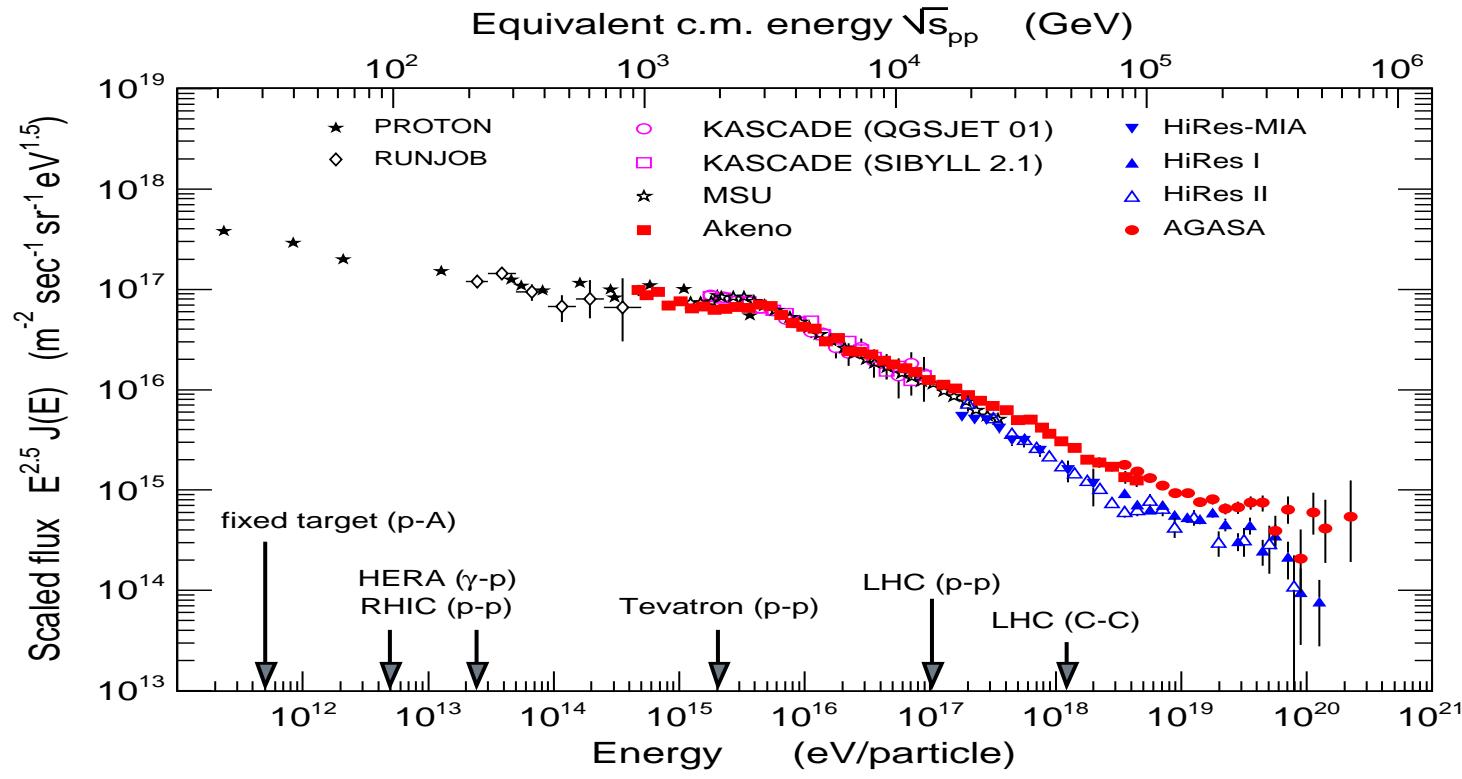
Representative CR models:

- DPMJET (Engel, Ranft & Roesler)
- neXus (Drescher et al.)
- QGSJET (Kalmykov & SO)
- SIBYLL (Engel, Gaisser, Lipari & Stanev)

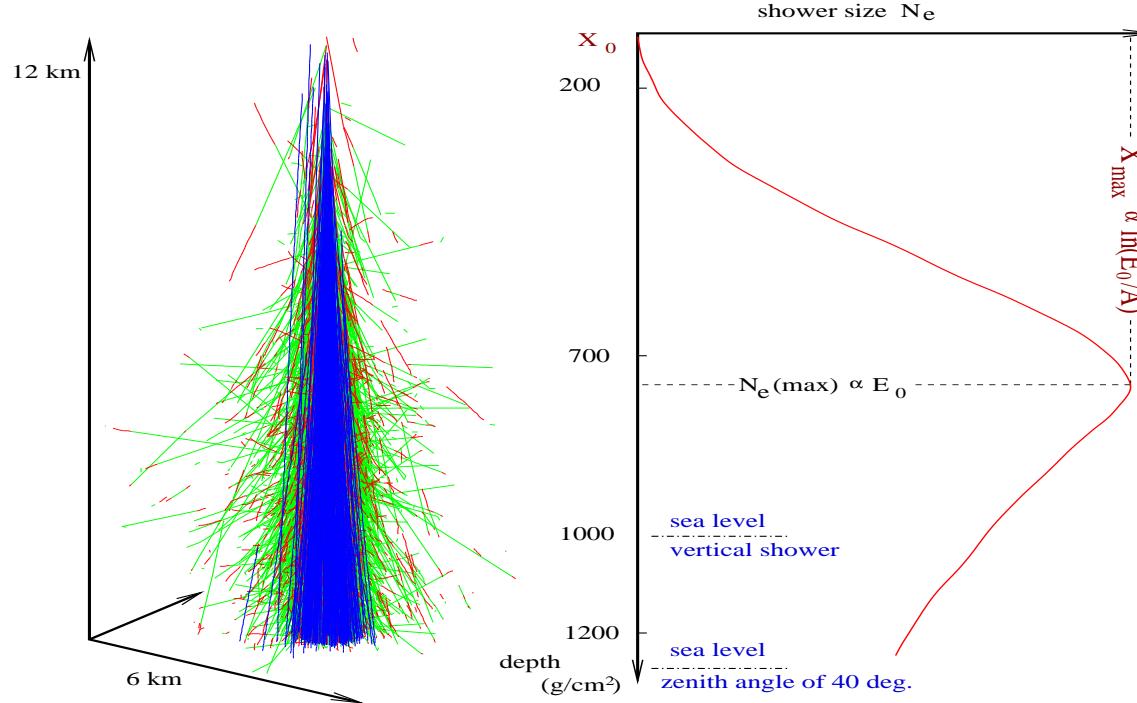
What is different?

High energy cosmic ray spectrum:

- extends over 10 energy decades!
- steeply falling down: $\sim E^{-2.7}$ ($E^{-3.1}$) before (after) the “knee” ($\sim 4 \cdot 10^{15}$ eV)
- \Rightarrow very few particles at highest energies



Detection: extensive air showers (EAS)



EAS development:

- guided by few interactions of the initial (fastest secondary) particle
 \Rightarrow main source of fluctuations (interaction point X_0 , energy loss K_{inel})
- many sub-cascades of secondaries \Rightarrow well averaged

\Rightarrow requirements to CR interaction models:

- cross section predictions
- description of minimum bias hA- and AA-collisions
- importance of “forward” region
- predictive power (to extrapolate over many energy decades)

But:

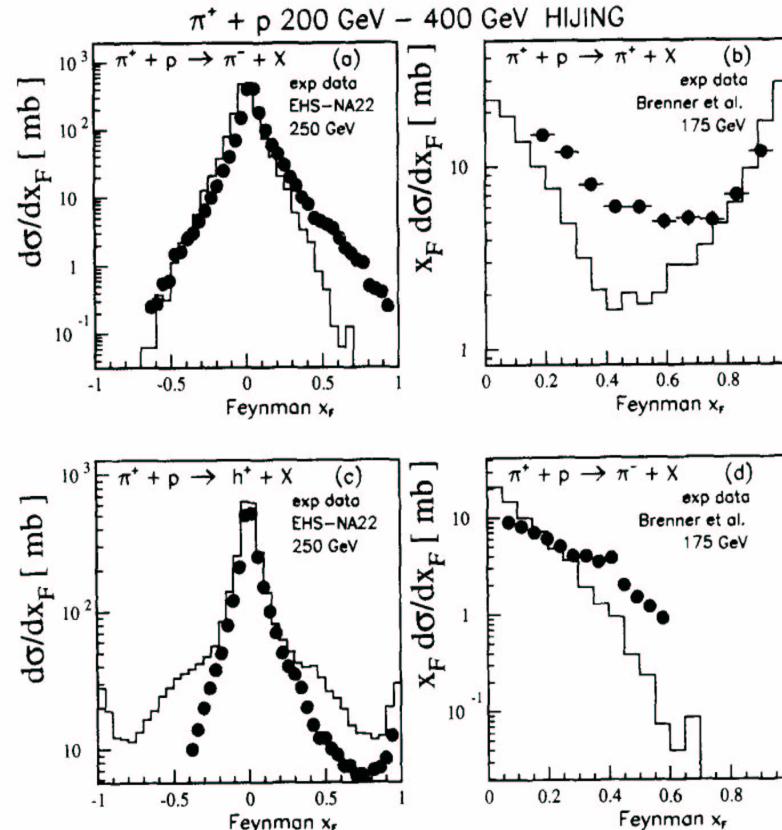
- low sensitivity to “fine” details (smoothed by EAS development)
- high p_t s - irrelevant, e.g., $p_t = 10 \text{ GeV}$, $E_0 = 10^5 \text{ GeV} \Rightarrow \Theta \simeq p_t/E_0 = 10^{-4}$
- charm, bottom, ... new rare processes - also irrelevant:
 - much smaller inclusive cross sections
 - produced mainly at central rapidities

Why not PYTHIA, HIJING, ... ?

Most models not
designed/tuned for simulating
forward particle production

Most models cannot handle
different projectiles/targets
and energies

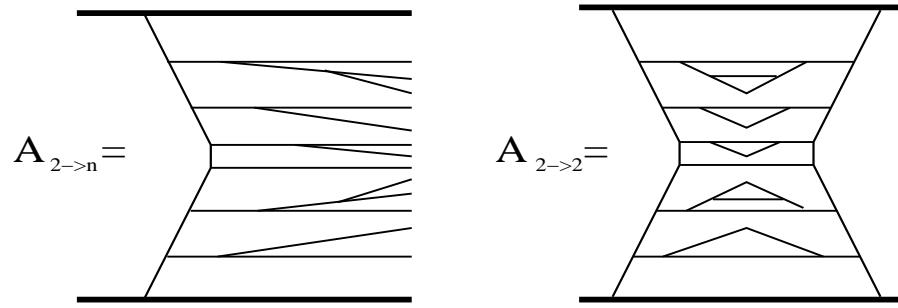
Example: comparison of
HIJING to fixed target data



(Pop, Gyulassy & Rebel, Astropart. Phys. 10 (1999) 211)

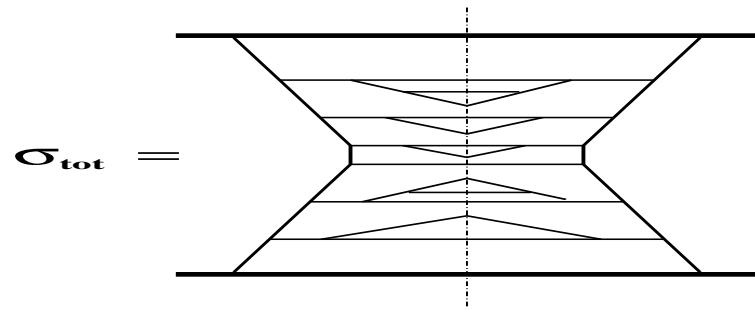
Gribov's Reggeon approach and multiple scattering

Elementary interaction - inelastic&elastic amplitudes:



Cross section - optical theorem:

$$\sigma_{\text{tot}} = \sum_n \int d\tau_n A_{2 \rightarrow n} \cdot A_{2 \rightarrow n}^* = \frac{1}{2s} 2 \text{Im } A_{2 \rightarrow 2} \Big|_{t=0}$$



Pomeranchuk: elementary interaction \equiv Pomeron exchange

Pomeron amplitude:

$$f_{ad}^P(s, t) = 8\pi i \gamma_a \gamma_d s^{\alpha_P(0)} \exp(-\lambda_{ad}(s)t)$$

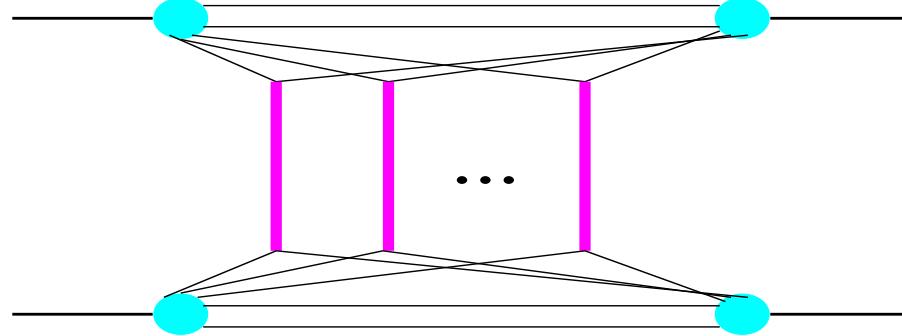
$$\lambda_{ad}(s) = R_a^2 + R_d^2 + \alpha'_P(0) \ln s$$

Pomeron intercept $\alpha_P(0) > 1$ - energy increase

Pomeron slope $\alpha'_P(0)$ - increasing spatial size of the interaction

$\sigma_{ad}^P(s) = \frac{1}{2s} 2\text{Im } f_{ad}^P(s, 0) \sim s^{\alpha_P(0)}$ - violates unitarity bound?

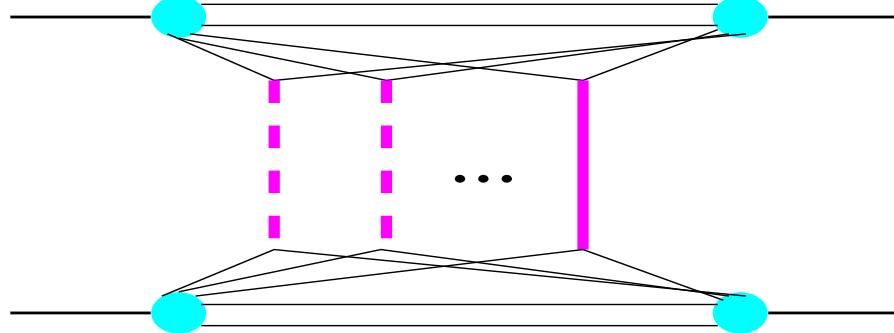
\Rightarrow multiple scattering (multi-Pomeron exchange):



$$\sigma_{ad}^{\text{tot}}(s) = 2 \int d^2 b \left[1 - e^{-\chi_{ad}^P(s, b)} \right] \sim \ln^2 s, \quad s \rightarrow \infty$$

$$\chi_{ad}^P(s, b) = \frac{1}{8\pi^2 s} \int d^2 q_\perp e^{-i\vec{q}_\perp \cdot \vec{b}} \text{Im } f_{ad}^P(s, q_\perp^2) = \frac{\gamma_a \gamma_d s^{\alpha_P(0)-1}}{\lambda_{ad}(s)} \exp\left(\frac{-b^2}{4\lambda_{ad}(s)}\right)$$

Particle production - **AGK cutting rules** (Abramovskii, Gribov & Kancheli):
 no interference between different classes of the interaction \Rightarrow cross sections:



\Rightarrow “topological” cross sections (n “cut” Pomerons):

$$\sigma_{ab}^{(n)}(s) = \int d^2 b \frac{[2\chi_{ab}^P(s, b)]^n}{n!} e^{-2\chi_{ab}^P(s, b)}$$

$$\sigma_{ab}^{\text{inel}}(s) = \sum_{n=1}^{\infty} \sigma_{ab}^{(n)}(s) = \int d^2 b \left[1 - e^{-2\chi_{ab}^P(s, b)} \right]$$

Particle production (Capella et al.; Kaidalov & Ter-Martyrosyan):

“cut” Pomeron \Rightarrow string formation & break up \Rightarrow hadronization

QCD and hard processes

What QCD tells us about high energy interactions?

- (mini-)jet production ($p_t > p_t^{\min} = Q_0$) - increases with energy
- small coupling ($\alpha_s(p_t^2)$) - compensated by large logarithms $\ln \frac{x_i}{x_{i+1}}$, $\ln \frac{p_{t,i+1}^2}{p_{t,i}^2}$
⇒ “leading-log” re-summations (n -parton “ladders”): $\sum_n \prod_{i=1}^n \left(\int \alpha_s \frac{dx_i}{x_i} \right)$; $\sum_n \prod_{i=1}^n \left(\int \alpha_s \frac{dp_{t,i}^2}{p_{t,i}^2} \right)$

QCD “collinear” factorization ⇒ inclusive (leading-log) jet-pair cross section:

$$\sigma_{ad}^{\text{jet}}(s, Q_0^2) = K \sum_{I,J=q,\bar{q},g} \int_{p_t^2 > Q_0^2} dp_t^2 \int dx^+ dx^- \frac{d\sigma_{IJ}^{2 \rightarrow 2}(x^+ x^- s, p_t^2)}{dp_t^2} f_{I/a}(x^+, M_F^2) f_{J/d}(x^-, M_F^2)$$

$d\sigma_{IJ}^{2 \rightarrow 2}/dp_t^2$ - differential parton-parton cross section;

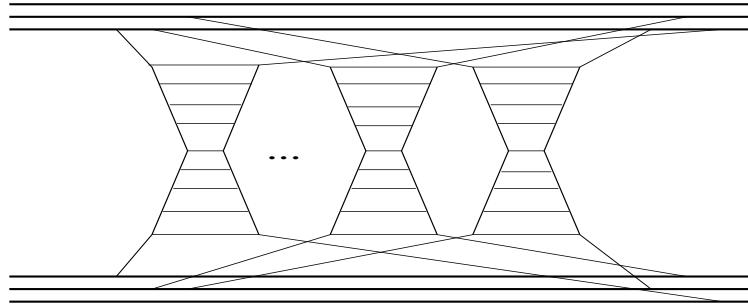
$f_{I/a}(x^+, Q^2)$ - parton I momentum distribution, “probed” at scale Q^2

Not sufficient to construct a MC model: pQCD tells nothing about

- jet production in an individual event
- interaction cross sections
- “soft” (low p_t) particle production, e.g., about leading particles

⇒ Mini-jet scheme (Gaisser & Halsen, Pancheri & Srivastava)

- “soft” physics \equiv scaling
- energy increase of $\sigma_{ad}^{\text{tot}}(s)$, $N_{ad}^{\text{ch}}(s)$ - due to mini-jet production
- $\sigma_{ad}^{\text{jet}} > \sigma_{ad}^{\text{tot}}$ ⇒ multiple scattering - eikonal approach



“Hard” eikonal - product of $\sigma_{ad}^{\text{jet}}(s, Q_0^2)$ and hadronic overlap function $A_{ad}(b)$:

$$\begin{aligned}\chi_{ad}^{\text{hard}}(s, b) &= \frac{1}{2} \sigma_{ad}^{\text{jet}}(s, Q_0^2) A_{ad}(b) \equiv \frac{1}{2} \langle n_{ad}^{\text{jet}}(s, b) \rangle \\ A_{ad}(b) &= \int d^2 s T_a^{\text{e/m}}(\vec{s}) T_d^{\text{e/m}}(|\vec{b} - \vec{s}|)\end{aligned}$$

Number of jet pairs per event (for given b) - Poisson:

$$W(n_{\text{jet}}) = \frac{1}{n_{\text{jet}}!} [2\chi_{ad}^{\text{hard}}(s, b)]^{n_{\text{jet}}} \exp(-2\chi_{ad}^{\text{hard}}(s, b))$$

To get cross sections - also “soft” eikonal:

$$\chi_{ad}^{\text{soft}}(s, b) = \frac{1}{2} \sigma_{ad}^{\text{soft}}(s) A_{ad}(b)$$

⇒ inelastic cross section:

$$\sigma_{ad}^{\text{inel}}(s) = \int d^2b \left[1 - e^{-2\chi_{ad}^{\text{soft}}(s,b) - 2\chi_{ad}^{\text{hard}}(s,b)} \right]$$

Conversion of partons into hadrons:

- color field connections between final partons
- hadronization: string or cluster procedures

Employed in PITHYA, HERWIG, HIJING, SIBYLL,...

Main differences to Gribov’s scheme:

- high energy scattering - dominated by “hard” eikonal
⇒ (believed to be) governed by pQCD
- multiple scattering - only due to “semi-hard” ($p_t > Q_0$) processes
- initial state emission - starts at $p_t = Q_0$ (or a similar scale)

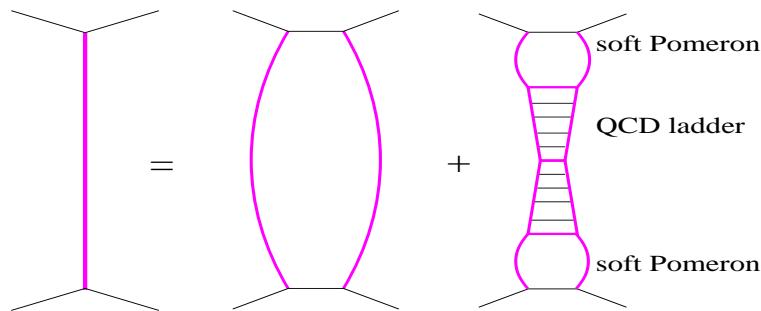
Alternative: matching Gribov's scheme with QCD

⇒ “semi-hard” (“heterotic”) Pomeron scheme (Levin & Tan, Kalmykov & SO):

- introduce a “threshold” scale Q_0^2
- use “soft” Pomeron below Q_0^2
- use DGLAP ladder for $|p_t^2| > Q_0^2$

⇒ Gribov's scheme based on a “general Pomeron”:

$$\chi_{ab}^P(s, b) = \chi_{ab}^{P\text{soft}}(s, b) + \chi_{ab}^{P\text{sh}}(s, b)$$



⇒ similar to the mini-jet approach

Employed in QGSJET, neXus

Differences from the mini-jet scheme:

- multiple scattering - due to both “soft” and “semi-hard” Pomerons
- parton (particle) production extends to “soft” (low p_t) region (“soft pre-evolution”)
- low- x partons - distributed over larger transverse area

Presently: no sharp border between mini-jet / semi-hard Pomeron models:

- SIBYLL 2.1 - multiple “soft” interactions (“soft” Pomerons)
- DPMJET - each mini-jet process accompanied by “soft” Pomeron exchange
- PITHYA - hardest scattering is color connected to valence quarks & diquarks
⇒ mimics “soft pre-evolution”
- HERWIG - initial state emission may (optionally) continue till Λ_{QCD} scale

Important: in both schemes elementary processes proceed independently

Rapidly comes to its limits: realistic parton momentum distributions (PDFs)
⇒ too rapid energy increase of cross sections & hadron multiplicities

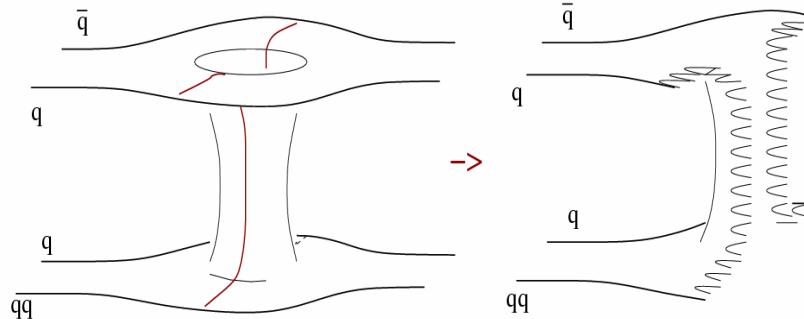
Energy-dependent p_t -cutoff: $p_t^{\min} \equiv Q_0 = Q_0(s)$? Why?

Color connections and hadronization

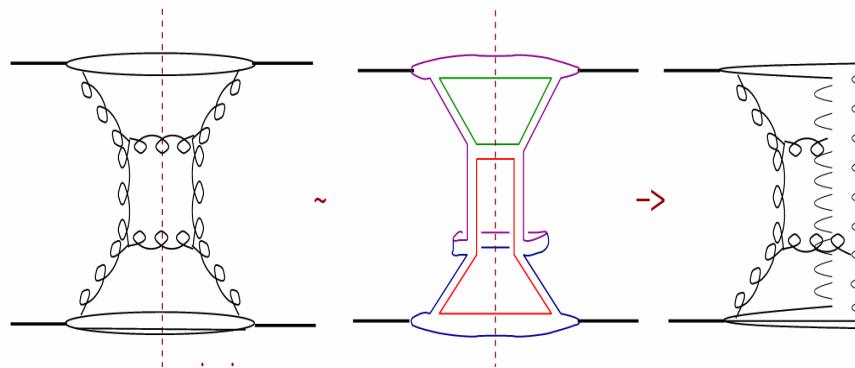
Dual topological unitarization scheme, $N_c \rightarrow \infty$, $N_f \rightarrow \infty$ (Veneziano):

Pomeron \equiv cylinder

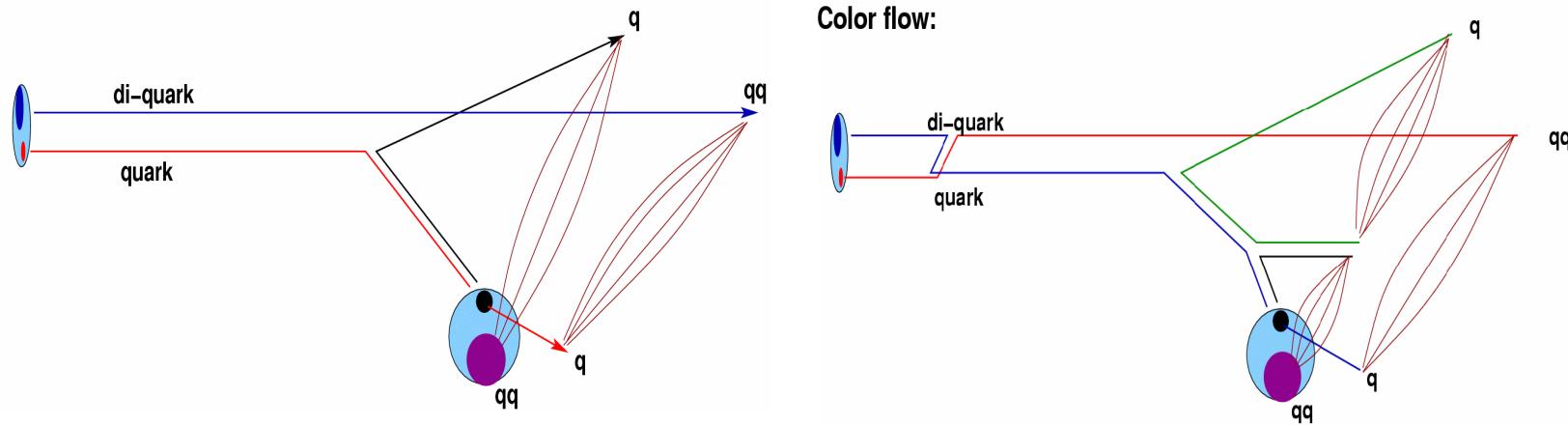
\Rightarrow “cut” Pomeron \equiv cut cylinder \Rightarrow 2 chains of secondaries:



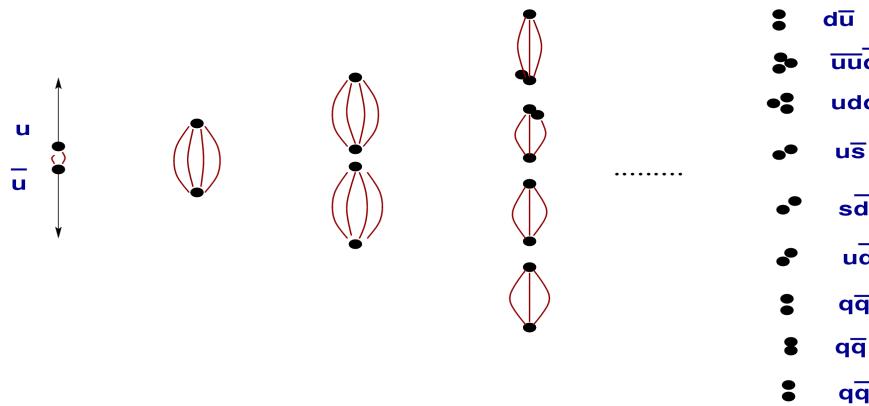
Or via gluon exchange:



Can be used to establish string picture of hadronization (Capella et al., Kaidalov & Ter-Martyrosyan):



String fragmentation procedure:



Mostly LUND fragmentation procedures used - “area law” decay
(PITHYA, HIJING, DPMJET, SIBYLL,...)

HERWIG: $g \rightarrow \bar{q}q$ splittings and isotropic cluster decays
recently - fission of long clusters (similar to string procedure)

QGSJET: fragmentation of string-end partons ($q(\bar{q}), qq, \dots$);
parameters - Regge intercepts (Kaidalov)

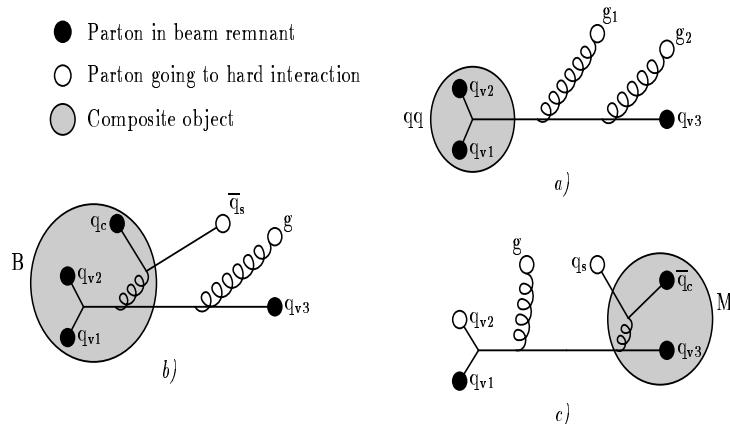
Important aspect - hadronic “remnants”:

- PITHYA:
 - 1st (“hardest”) process is color-connected to valence q, qq
 - all other hard processes decoupled
 - composite remnants (new option): may contain many (anti-)quarks
 - if no quarks left \Rightarrow remnant = gluon
- HERWIG:
 - all hard processes decoupled
 - “soft” processes = “soft” gluon emission (also decoupled)

- HIJING:
 - all hard processes decoupled
 - “soft” processes = (multiple) longitudinal remnant excitation (dM^2/M^2)
- SIBYLL: similar to PITHYA but with multiple “soft” Pomeron exchanges
- DPMJET: multiple “soft” and “hard” interactions coupled to remnants
- QGSJET: multiple “soft” and “semi-hard” Pomerons coupled to constituent (valence and sea) (anti-)quarks ($f_{q(\bar{q})}(x) \sim 1/\sqrt{x}$)

Additional baryon stopping - “diquark splitting” (junction) (PITHYA, HIJING)

Also black disk limit (BDL) stopping mechanism (Drescher, Dimitru & Strikman)



“Dense” partonic systems: non-linear effects

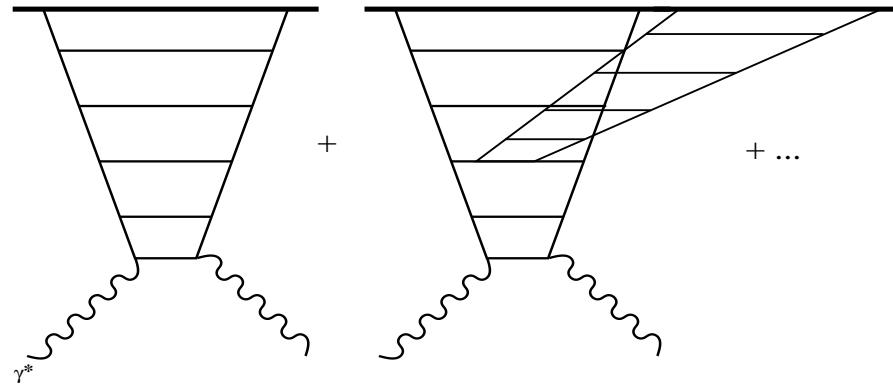
Independent interaction picture is **inadequate** for large s , small b , large A :

- many partons closely packed
- \Rightarrow expected to interact with each other

QCD approach (Gribov, Levin & Ryskin) - asymptotic picture:

- parton saturation at some scale $Q_{\text{sat}}^2(x) \Rightarrow$ “soft” contribution suppressed
- QCD parton dynamics for $p_t^2 > Q_{\text{sat}}^2(x)$
- non-linear effects - interaction between QCD ladders

Structure function (SF) $F_2(x)$, $x \rightarrow 0$:



Provides formal justification for the energy-dependent p_t -cutoff:

saturation-based picture; $Q_0^2 = Q_0^2(s)$ - effective saturation scale

However: no explicit connection to GLR (QCD) \Rightarrow loss of predictive power
ad hoc parameterizations:

- SIBYLL: $Q_0(s) = p_t^{\min}(s) = 1 + 0.065 \exp[0.9\sqrt{\ln s}]$ (GLR-inspired)
- PITHYA: $p_t^{\min}(s) \sim \sqrt{s}^{0.25}$ (“like Pomeron intercept”)
- HERWIG: p_t^{\min} - free parameter
- HIJING: $p_t^{\min}(s) = 3.91 - 3.34 \ln(\ln \sqrt{s}) + 0.98 \ln^2(\ln \sqrt{s}) + 0.23 \ln^3(\ln \sqrt{s})$

Still no account for:

- no saturation in peripheral interactions
- saturation being different in $hh-$, $hA-$, $AA-$ collisions
- screening effects in non-saturation regime (shadowing)

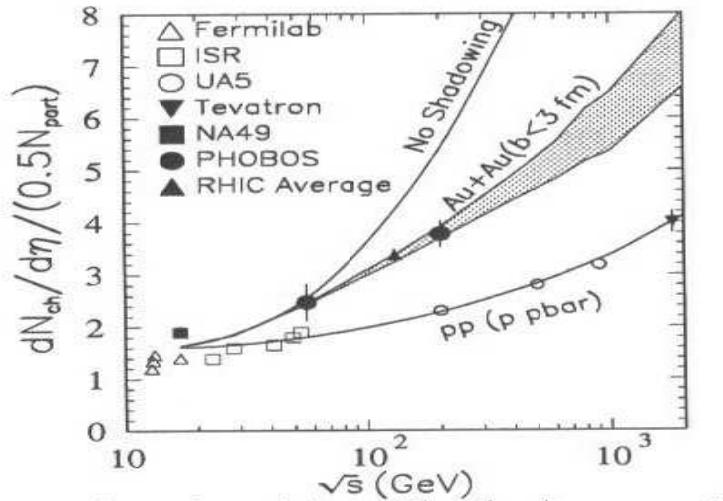
Additional non-linear effects may be introduced at particle production level, e.g., color re-arrangement in PITHYA, HERWIG (optional)

HIJING (Li & Wang, 2001): parameterized nuclear shadowing of PDFs, e.g.

$$f_{g/A}(x, Q^2, b, A) = A f_{g/p}(x, Q^2) \left[1 + 1.19 \ln^{1/6} A (x^3 - 1.2 x^2 + 0.21 x) - s_g(b) (A^{1/3} - 1)^{0.6} (1 - 1.5 x^{0.35}) \exp(-x^2/0.004) \right]$$

$$s_g(b) = (0.24 \div 0.28) \frac{5}{3} (1 - b^2/R_A^2)$$

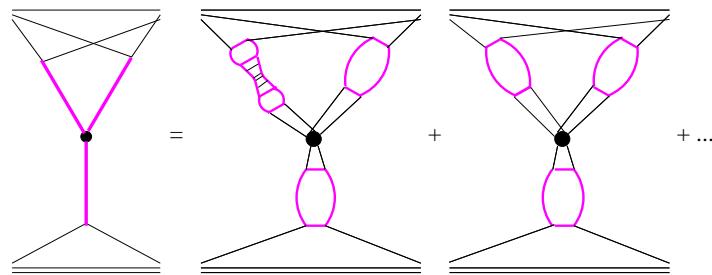
appears to be decisive to get agreement with RHIC:



In general: treatment of **realistic** (not asymptotic) conditions needed!

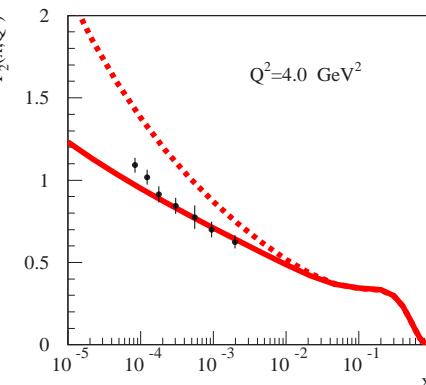
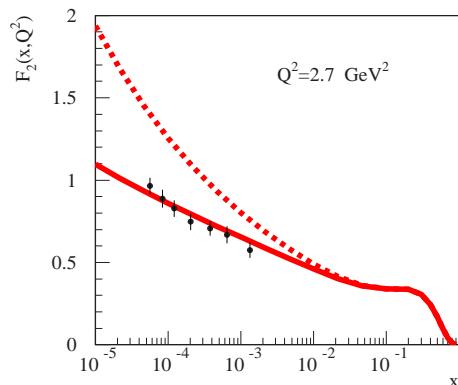
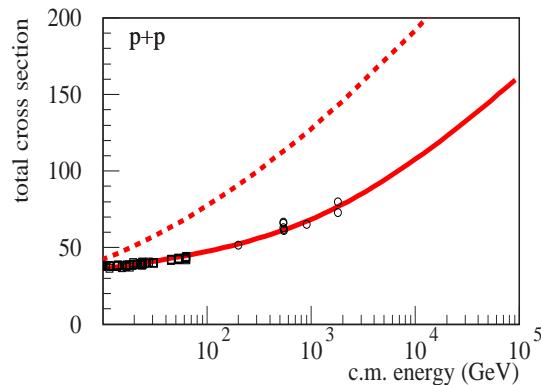
Alternative approach - QGSJET-II model (SO, 2004) :

- assumes no saturation at a fixed Q_0^2 scale
- \Rightarrow non-linear effects = interactions between “soft” Pomerons



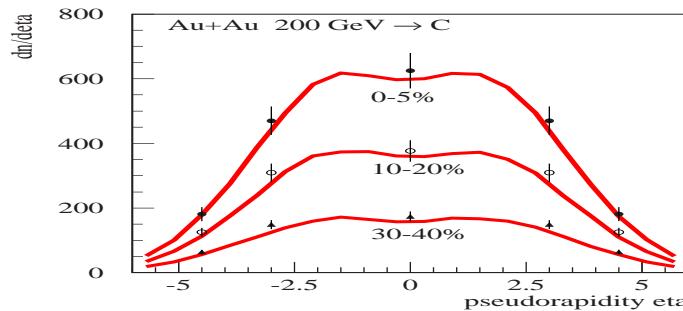
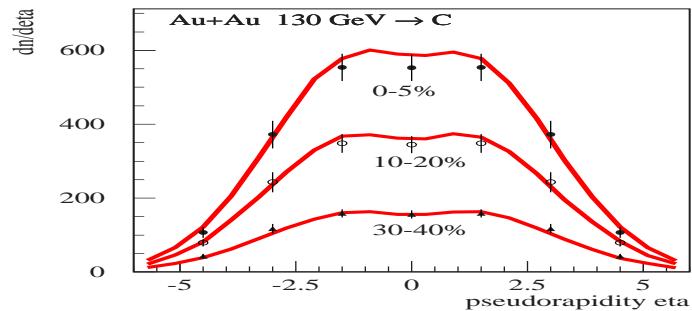
- \Rightarrow Gribov’s Reggeon scheme (all order re-summation of “enhanced” graphs)

Total cross section and SF $F_2(x, Q^2)$ with (without) enhanced graphs:



hA, AA : “enhanced” (multi-Pomeron) graphs connected to different nucleons
 $\Rightarrow A$ -enhancement of screening effects

Charged multiplicity for different centralities at RHIC:



Main differences to the linear scheme:

- screening of the “soft” particle production
- in the “dense” limit (large s , small b , large A) -
 re-normalization of the “soft” Pomeron intercept: $\alpha_P(0) \rightarrow \tilde{\alpha}_P(0) < 1$
 $\Rightarrow \chi_{ab}^{P_{\text{soft}}}(s, b)$ - decreasing with s - **saturation at the Q_0^2 scale!**
- \Rightarrow approaches “mini-jet” picture in the “dense” limit

Drawback: does not treat **screening & saturation** effects at $p_t^2 > Q_0^2$!

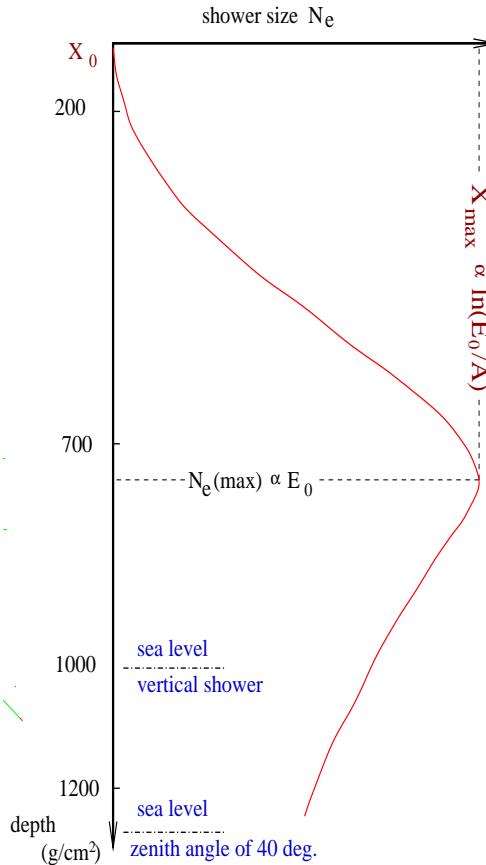
Air Shower Predictions

Basic EAS characteristics - sensitivity to hadronic interactions:

- X_{\max} - mainly defined by $\sigma_{h\text{-air}}^{\text{inel}}$, $K_{h\text{-air}}^{\text{inel}}$
 - position of the first interaction X_0 : $\sigma_{p\text{-air}}^{\text{inel}}$
 - profile shape: $K_{p\text{-air}}^{\text{inel}}$, $\sigma_{\pi\text{-air}}^{\text{inel}}$, $K_{\pi\text{-air}}^{\text{inel}}$
 - X_{\max} fluctuations: mainly from X_0 , $K_{p\text{-air}}^{\text{inel}}$
- N_e - correlated with X_{\max}
- N_μ - depends on $N_{h\text{-air}}^{ch}$ (especially, $N_{\pi\text{-air}}^{ch}$)

Energy (mass) dependence:

- $X_{\max} \sim \ln(E_0/A)$
- $N_e \sim A (E_0/A)^{\alpha_e}$, $\alpha_e > 1$
- $N_\mu \sim A (E_0/A)^{\alpha_\mu}$, $\alpha_\mu < 1$

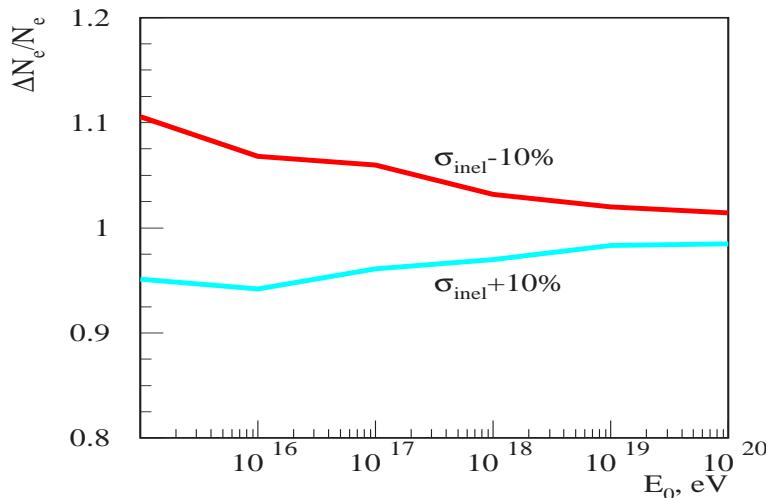
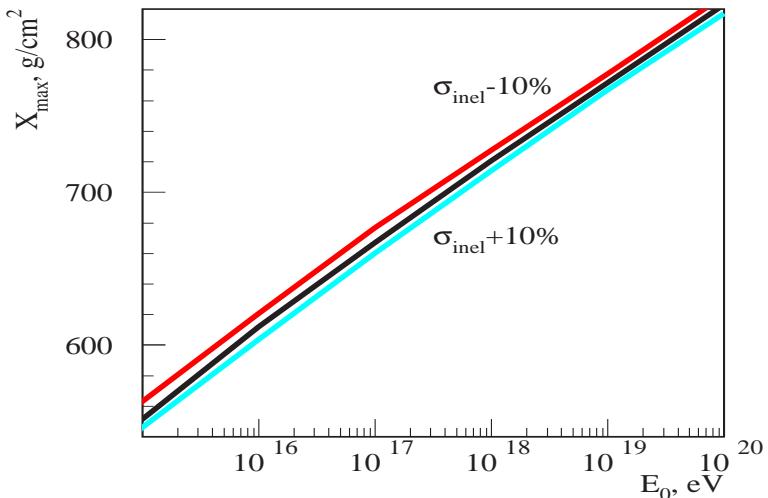


Münchhausen's problem: disentangle energy, mass, and hadronic models

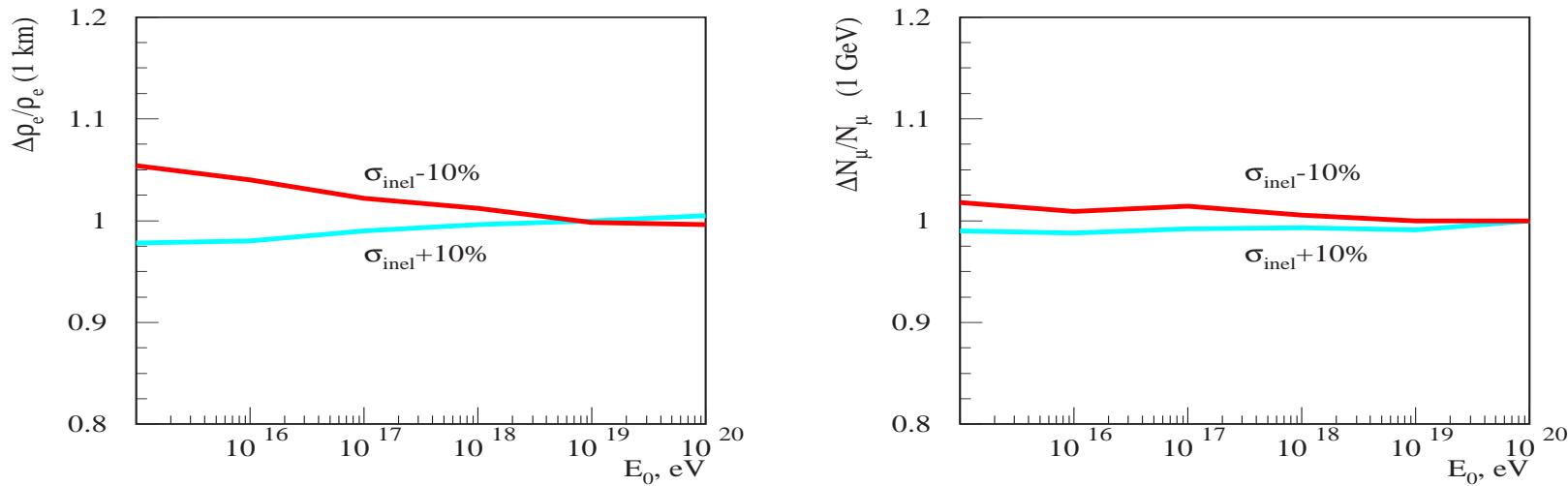
Let us make simple tests...

Change $\sigma_{p\text{-air}}^{\text{inel}}$ by $\pm 10\%$:

- X_{\max} changes by $\pm 5 \div 10 \text{ g/cm}^2$
- electron number at ground - by $\pm 5 \div 10\%$

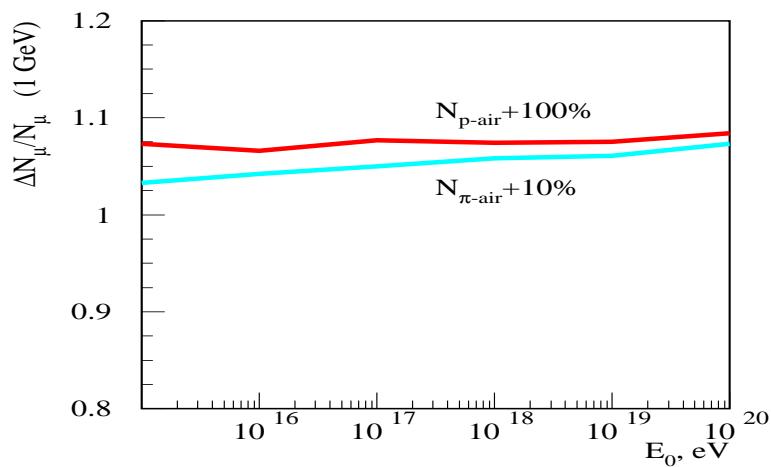


But electron density at large distance (1 km) and muon number - more stable



Now we increase p – air multiplicity by 100% or π – air multiplicity by 10%

- nearly same effect at highest energies



Let us compare models...

SIBYLL 2.1:

- mini-jet approach + multiple “soft” Pomerons
- GRV PDFs + floating p_t -cutoff ($Q_0(s)$)

QGSJET:

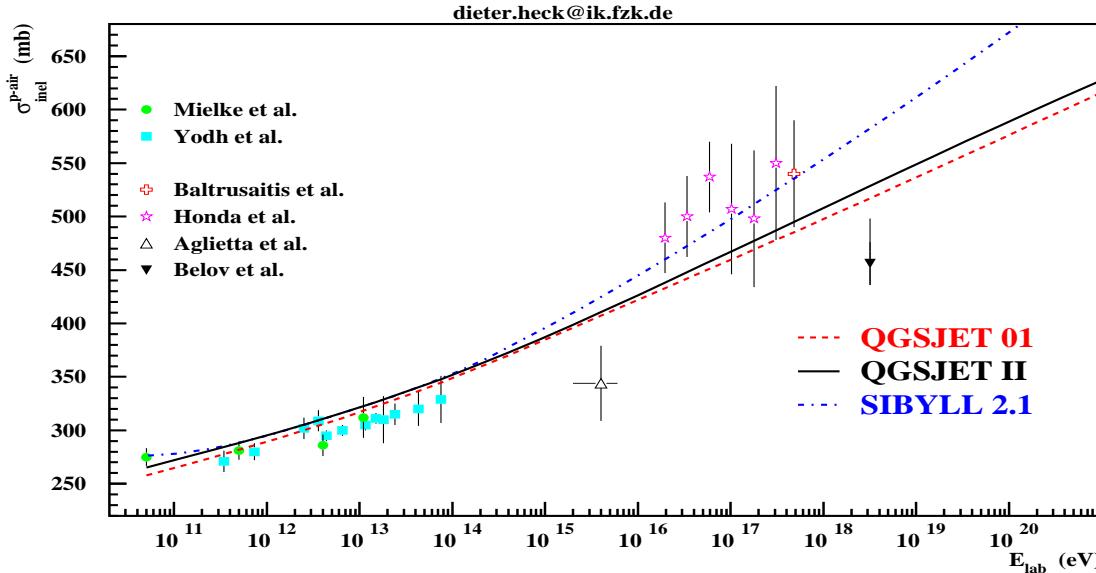
- multiple “soft” and “semi-hard” Pomerons
- “flat” (pre-HERA) PDFs & fixed p_t -cutoff (2 GeV)

QGSJET-II / QGSJET:

- bigger Pomeron intercept (1.18 instead of 1.07)
- steeper PDFs (now in agreement with HERA)
- non-linear screening effects (multi-Pomeron vertices)

Impact on $\sigma_{h\text{-air}}^{\text{inel}}$, $K_{h\text{-air}}^{\text{inel}}$, $N_{h\text{-air}}^{ch}$?

Proton-air cross section

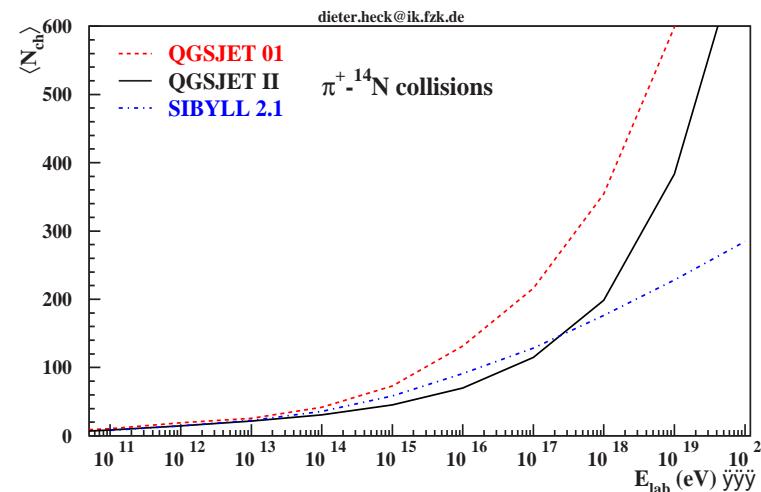
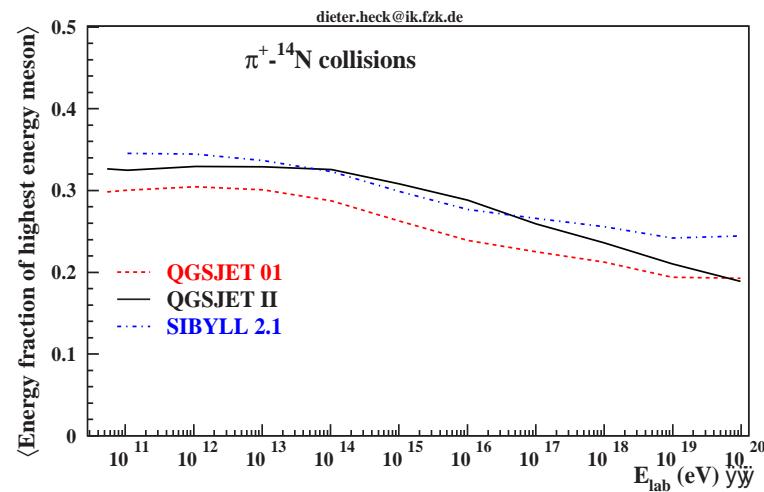
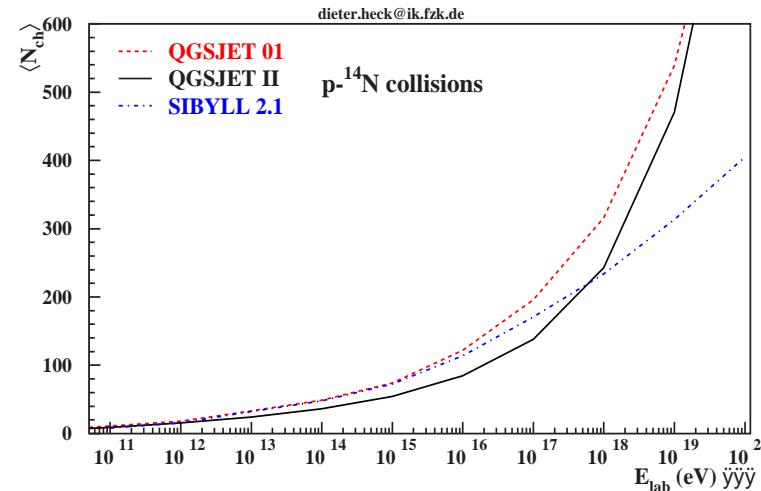
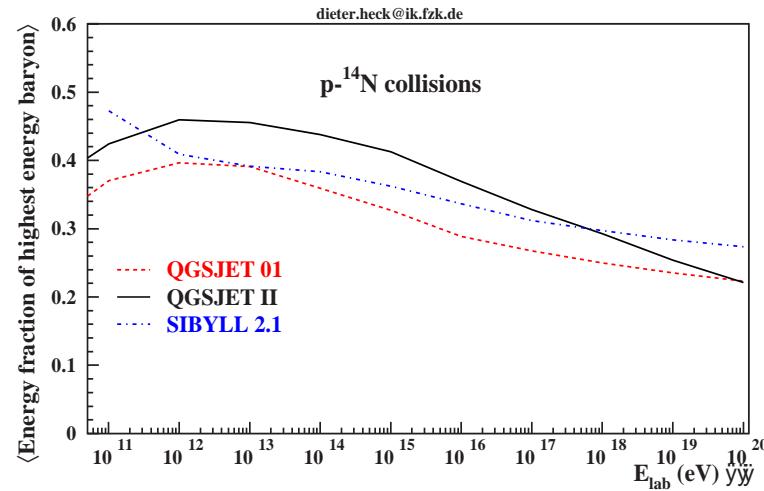


SIBYLL / QGSJET - faster energy increase:

- steeper PDFs in SIBYLL
- inelastic screening in QGSJET
- beware: also depends on the $Q_0(s)$ -parameterization & overlap function

QGSJET-II / QGSJET: steeper PDFS compensated by screening effects

Leading baryon (meson) energy share ($1 - K_{\text{h-air}}^{\text{inel}}$) and charged multiplicity



QGSJET / SIBYLL: “soft” parton production in addition to mini-jets

⇒ faster energy increase of $K_{h\text{-air}}^{\text{inel}}$, $N_{h\text{-air}}^{\text{ch}}$

QGSJET-II / QGSJET: suppression of “soft” production in the “dense” limit

⇒ much smaller $K_{h\text{-air}}^{\text{inel}}$, $N_{h\text{-air}}^{\text{ch}}$

QGSJET-II / SIBYLL: same effect

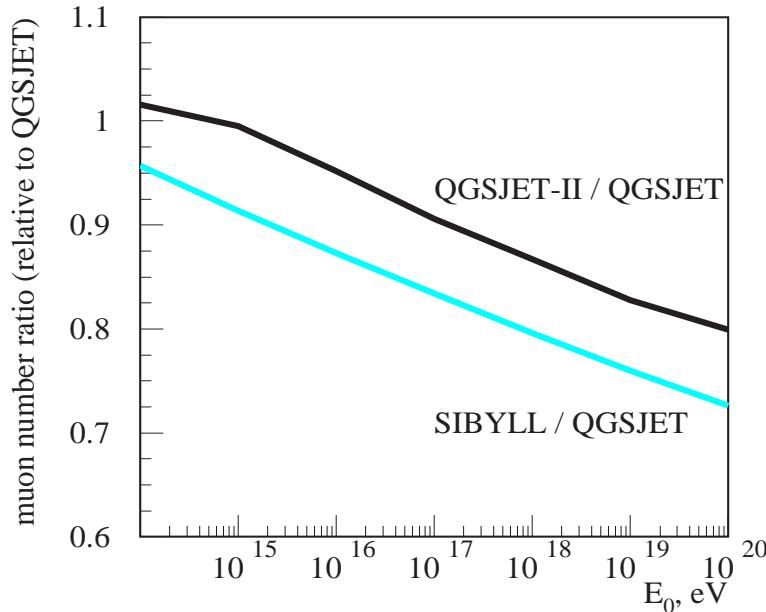
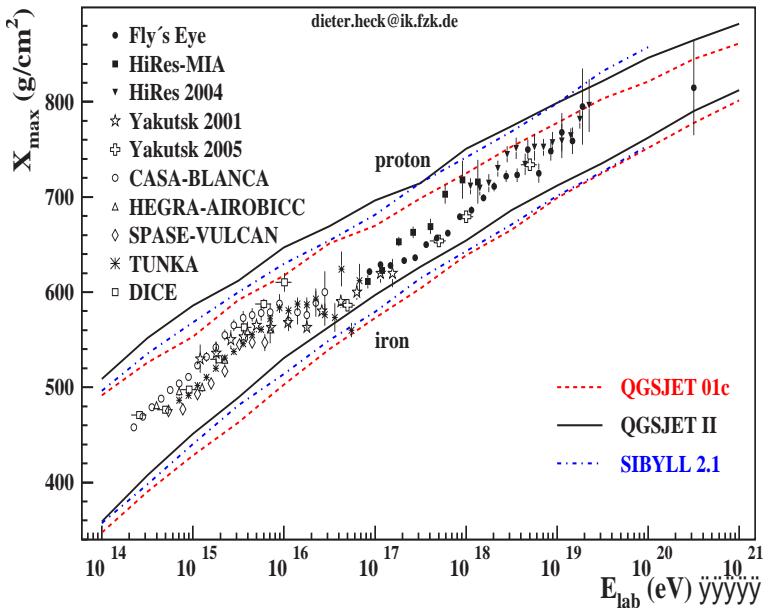
At highest energies - faster increase of $K_{h\text{-air}}^{\text{inel}}$, $N_{h\text{-air}}^{\text{ch}}$ in QGSJET-II:

too strong $Q_0(s)$ increase in SIBYLL or absence of GLR-effects in QGSJET-II?

Summary of model differences

- $\sigma_{h\text{-air}}^{\text{inel}}$: increasing with energy, reaching **10-15%** at $10^{19} - 10^{20}$ eV
- $K_{h\text{-air}}^{\text{inel}}$: **10-20%** between QGSJET / SIBYLL over the whole energy range
- $N_{h\text{-air}}^{\text{ch}}$ - increasing with energy, up to a **factor of 2** at $10^{19} - 10^{20}$ eV

Shower maximum position (X_{\max}) and muon number N_μ ($E_\mu > 1$ GeV)



QGSJET:

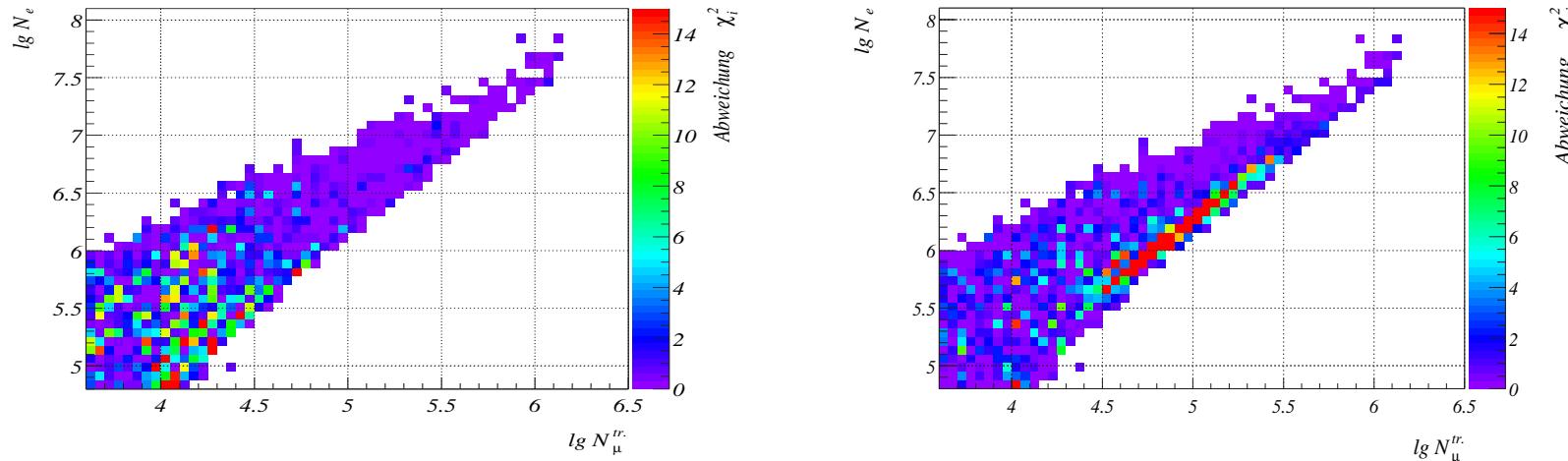
- largest $K_{h-\text{air}}^{\text{inel}}$ \Rightarrow highest shower maximum
- much bigger $N_{h-\text{air}}^{ch}$ compared to SIBYLL \Rightarrow higher N_μ (up to 30% at 10^{20})

QGSJET-II / QGSJET - strong reduction of $K_{h-\text{air}}^{\text{inel}}$, $N_{h-\text{air}}^{ch}$
 \Rightarrow deeper X_{\max} , smaller N_μ (only 10% difference with SIBYLL)

Remaining puzzles

Solving Münchhausen's problem - KASCADE studies of N_e - N_μ correlations:

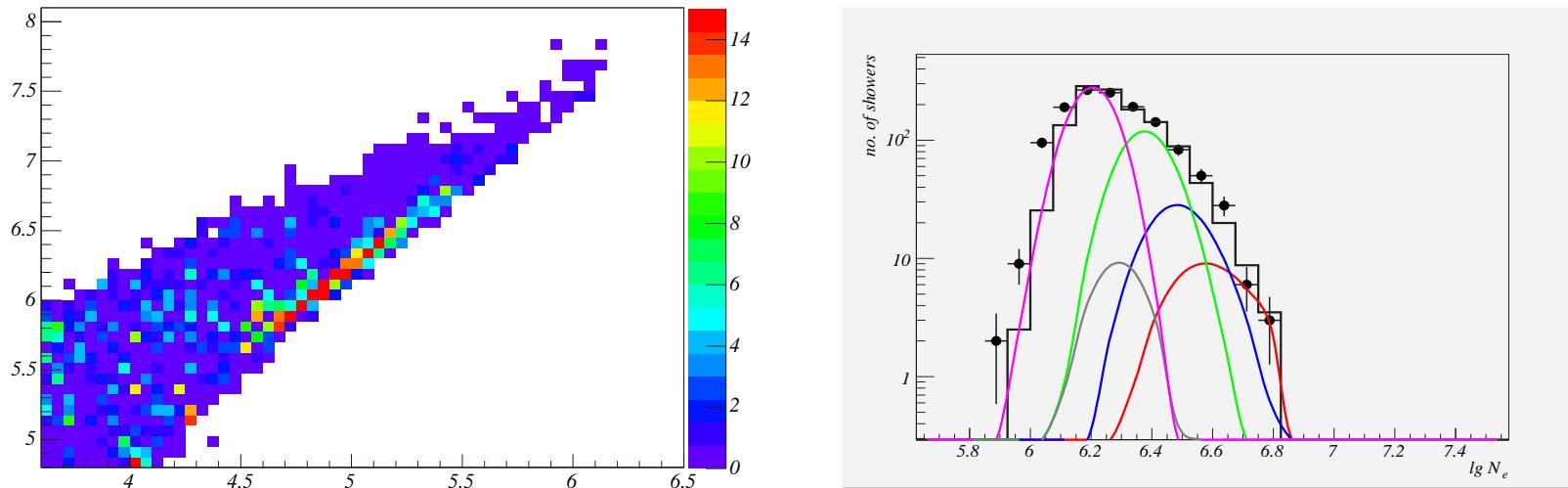
- reconstruction of CR spectra and composition using a hadronic MC model
- testing model consistency with the obtained spectra
(H. Ulrich et al., 2005)



Result: “true” model is between QGSJET and SIBYLL:

- either smaller N_μ than in QGSJET
- or (more probable) bigger $N_e \Rightarrow$ deeper X_{\max} ?

QGSJET-II goes in the right direction... but too far:

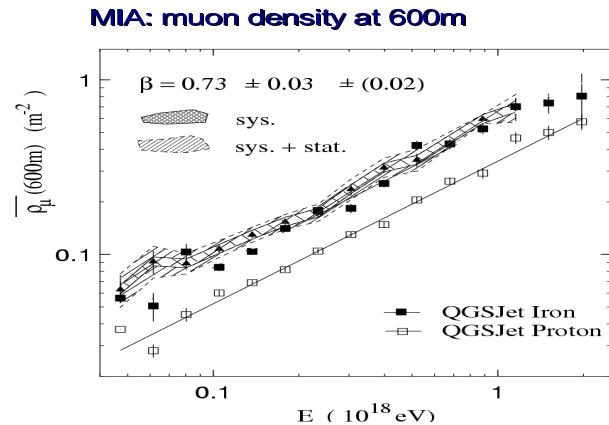


Now few possibilities:

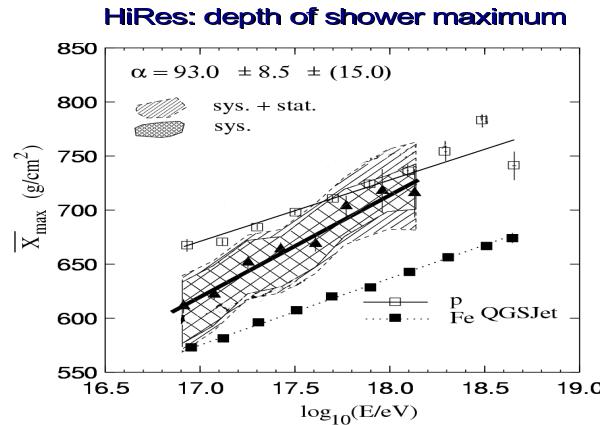
- larger $K_{\text{h-air}}^{\text{inel}}$, increasing with energy - supported by RHIC (baryon stopping) & theoretical ideas (diquark breaking (baryon junction), BDL-scenario,...)
- larger cross section
- “exotic” option: significantly bigger multiplicity
(how to accommodate with RHIC data?)

The last option could help solving composition puzzles at higher energies

Example: HiRes-MIA measurement



Composition iron dominated,
no significant change with energy



Composition changes to proton
dominated one

Seems to be a general problem:

- ground arrays favor iron-dominated composition
- fluorescence arrays: light (proton-dominated) composition

Way to solve: deeper X_{\max} and large N_μ (\Rightarrow huge multiplicity)

May be we don't understand πA -interaction?

Outlook

Contemporary models - “conventional” structure well established

Still significant technical differences

Theoretical challenge:

combined description of “hard” and “soft” screening (saturation) effects

Hadronic leading states - phenomenological approaches \Rightarrow data should decide

CR experiments can test general model consistency

Accelerator data are of great help to solve Münchhausen’s problem:

- LHC measurements of σ_{pp}^{tot} , B_{pp}^{el} could resolve cross section uncertainty $\Rightarrow X_{\max}$
- LHC measurements of N_{pp}^{ch} , N_{pA}^{ch} \Rightarrow key to the multiplicity problem $\Rightarrow N_{\mu}$
- RHIC studies of baryon “stopping” for different “centralities”
 \Rightarrow insight into hadronic leading state behavior

Can πA -interaction be very different from pA ? Any ideas?