



# Status of the LAr Shower Parameterisation



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LAr Simulation Meeting

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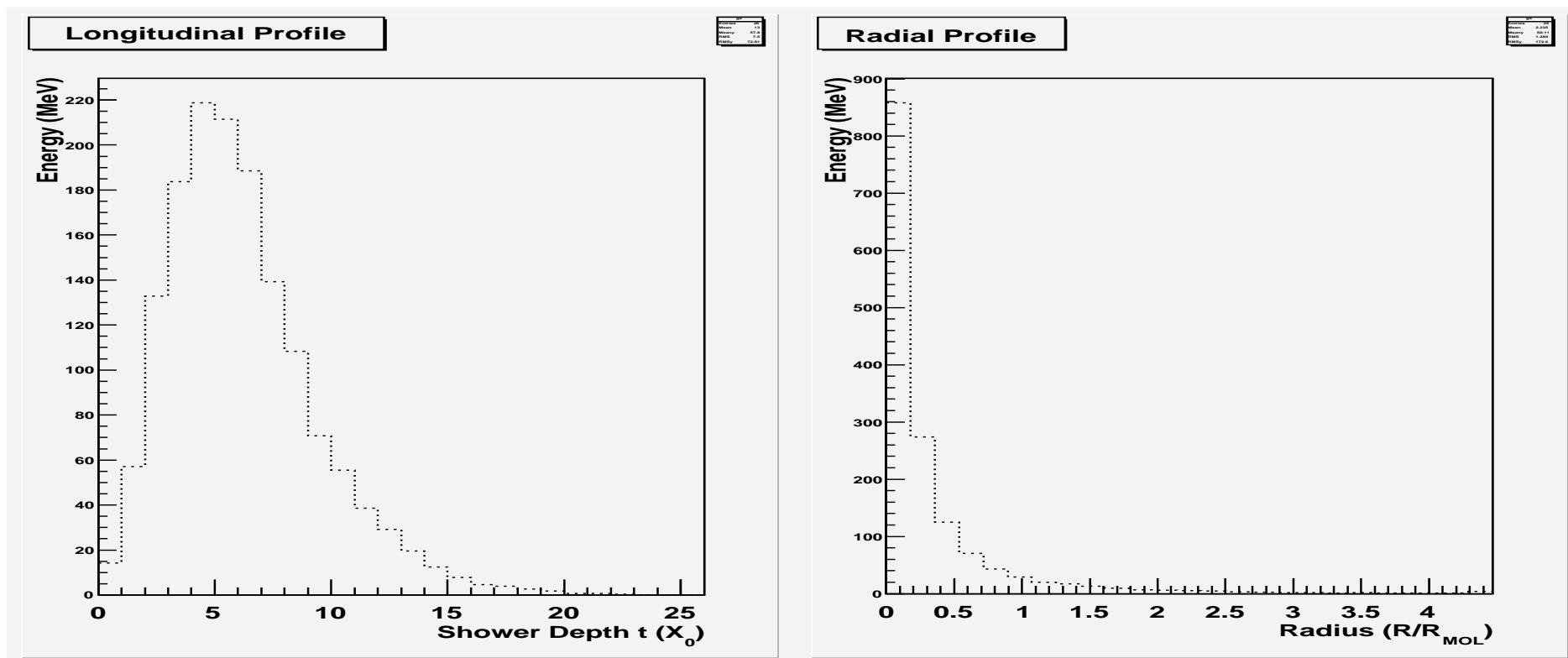


## Motivation for Shower Parameterisation

- For Geant4 simulation, one of the biggest users of CPU time is electromagnetic showers.
- One proton - proton event can contain many high energy photons and electrons
- To estimate background for rare interactions we require millions of simulated events
- We wish to find a set of equations which describe the shape of the shower, given only the 4 vector of the incoming electron
- Parameterisation used is based on Grindhammer & Peters  
*arXiv:hep-ex/0001020v1*



# Energy Profiles



Longitudinal and radial profiles of a single 10 GeV electron shower in the EM barrel.



## Longitudinal Profile

$$\left\langle \frac{1}{E} \frac{dE(t)}{dt} \right\rangle = \frac{(\beta t)^{\alpha-1} \beta \exp(-\beta t)}{\Gamma(\alpha)}$$

$t$  = longitudinal depth into shower

$\alpha$  = shape parameter

$\beta$  = scaling parameter

$$T = \frac{\alpha-1}{\beta} = \text{depth of shower energy maximum}$$

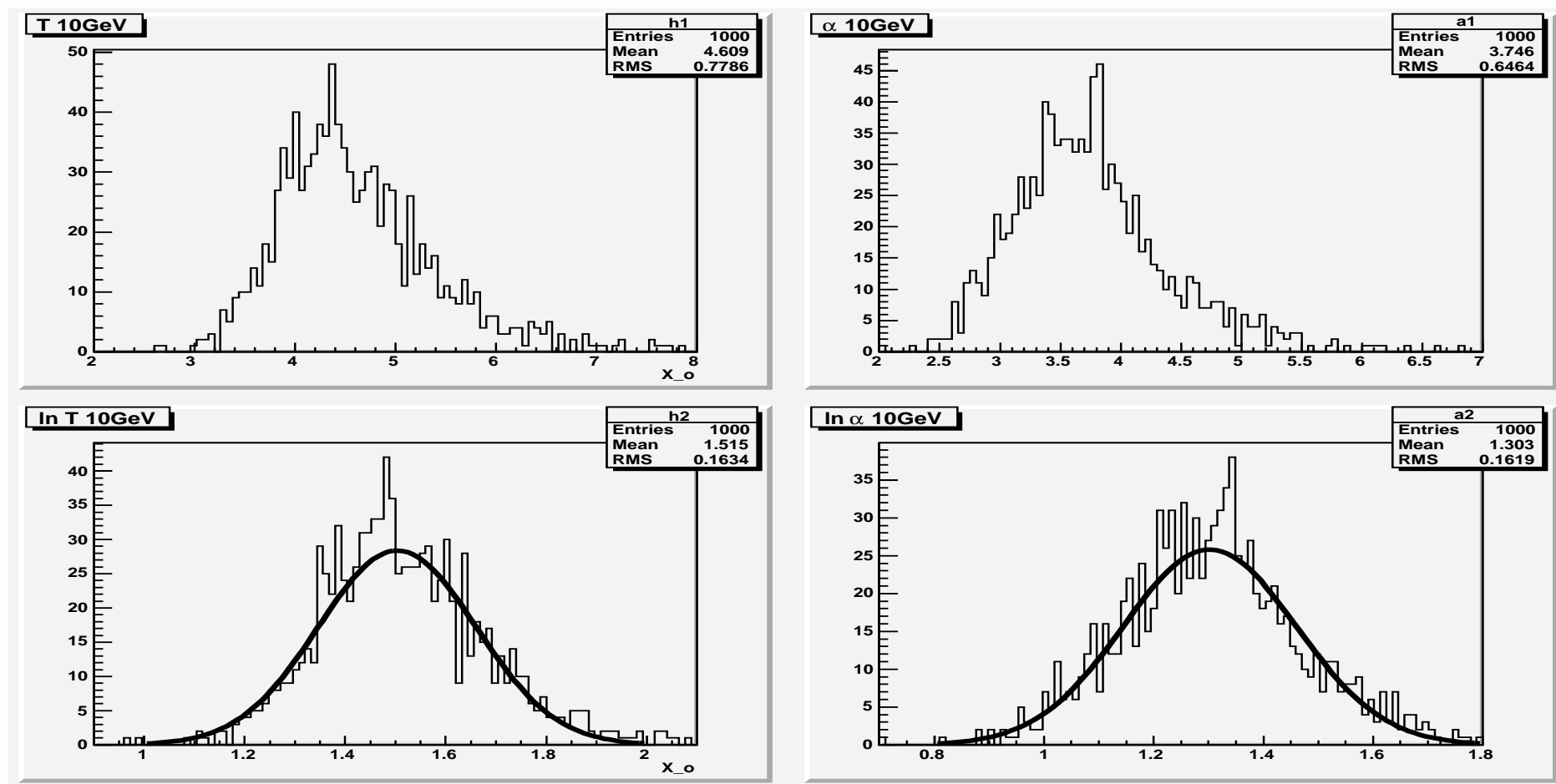
$$T_i = \frac{2Z_1^2 - Z_2}{Z_1}$$

$$\alpha_i = \frac{Z_1^2}{Z_2 - Z_1^2}$$

$$Z_n = \int_0^\infty t^n f_L(t) dt$$



# Fitting the Longitudinal Profile



Gaussian fits for  $\log T$  and  $\log \alpha$  at  $E = 10\text{GeV}$



## Fitting the Longitudinal Profile

$$\langle \ln T \rangle = \ln(c_1 + \ln y)$$

$$\langle \ln \alpha \rangle = \ln(c_2 + c_3 \ln y)$$

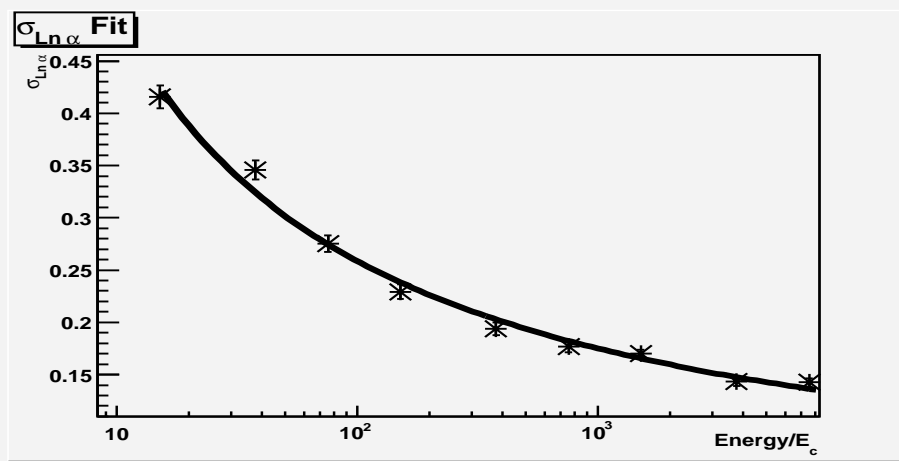
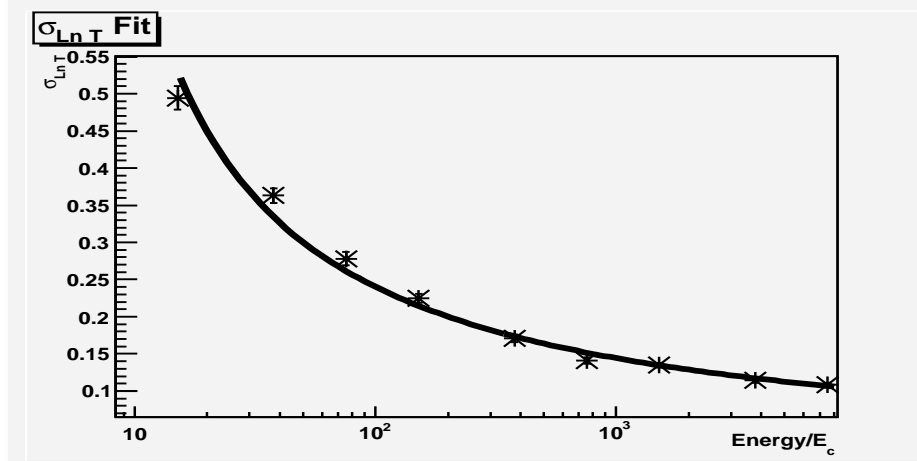
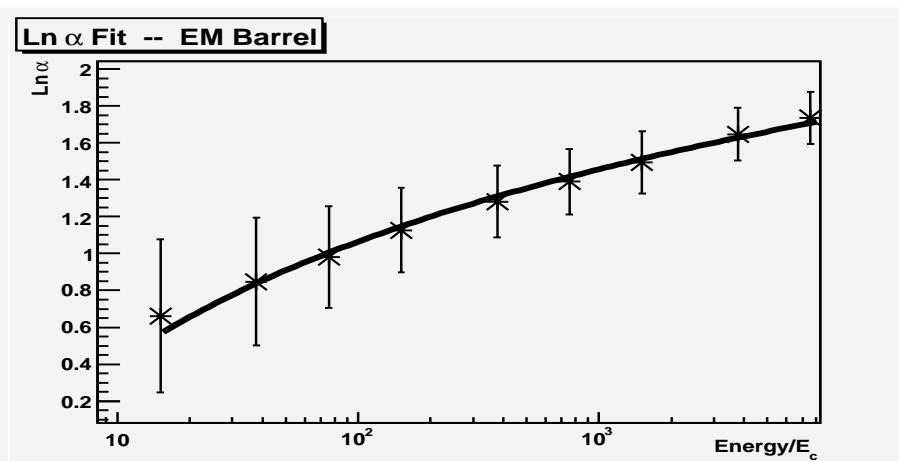
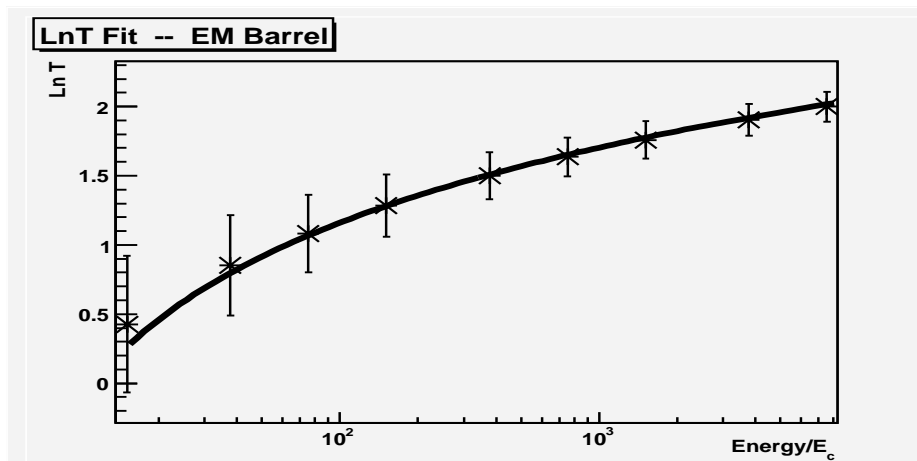
$$\sigma_{\ln T} = (c_4 + c_5 \ln y)^{-1}$$

$$\sigma_{\ln \alpha} = (c_6 + c_7 \ln y)^{-1}$$

$$y = E/E_{critical}$$



# Fitting the Longitudinal Profile



Longitudinal profile fits for the EM barrel



## Radial Profile

- Divide shower in length in units of  $X_0$
- Fit radial energy profile for each length

$$\left\langle \frac{1}{E(t)} \frac{dE(t,r)}{dt} \right\rangle = p \frac{2rR_C^2}{(r^2 + R_C^2)^2} + (1 - p) \frac{2rR_T^2}{(r^2 + R_T^2)^2}$$

- $R_C(t)$  = the median of the energy distribution of the core of the shower
- $R_T(t)$  = the median of the energy distribution of the tail of the shower
- $p$  is a weighting function

$$p(t) = E_{core}(t) / E_{tail}(t)$$

- Core is the radial interval containing 90% of the total energy
- Tail is the radial interval between Core and the radius containing 99% of the energy





## Fitting the Radial Profile

$$R_C(y, \tau) = (c_{10} + c_{11} \ln y + c_{12} \tau)$$

$$R_C(y, \tau) = (c_{12} (\exp(c_{13}(\tau - c_{14}) + \exp(c_{15} - c_{16} \ln y)) (\tau - c_{14})))$$

$$p(y, \tau) = c_{17} \exp\left(\frac{c_{18} - \tau}{c_{19} - c_{20} \ln y} \exp\left(\frac{c_{18} - \tau}{c_{19} - c_{20} \ln y}\right)\right)$$

$$\tau = R/R_{MOLIERE}$$



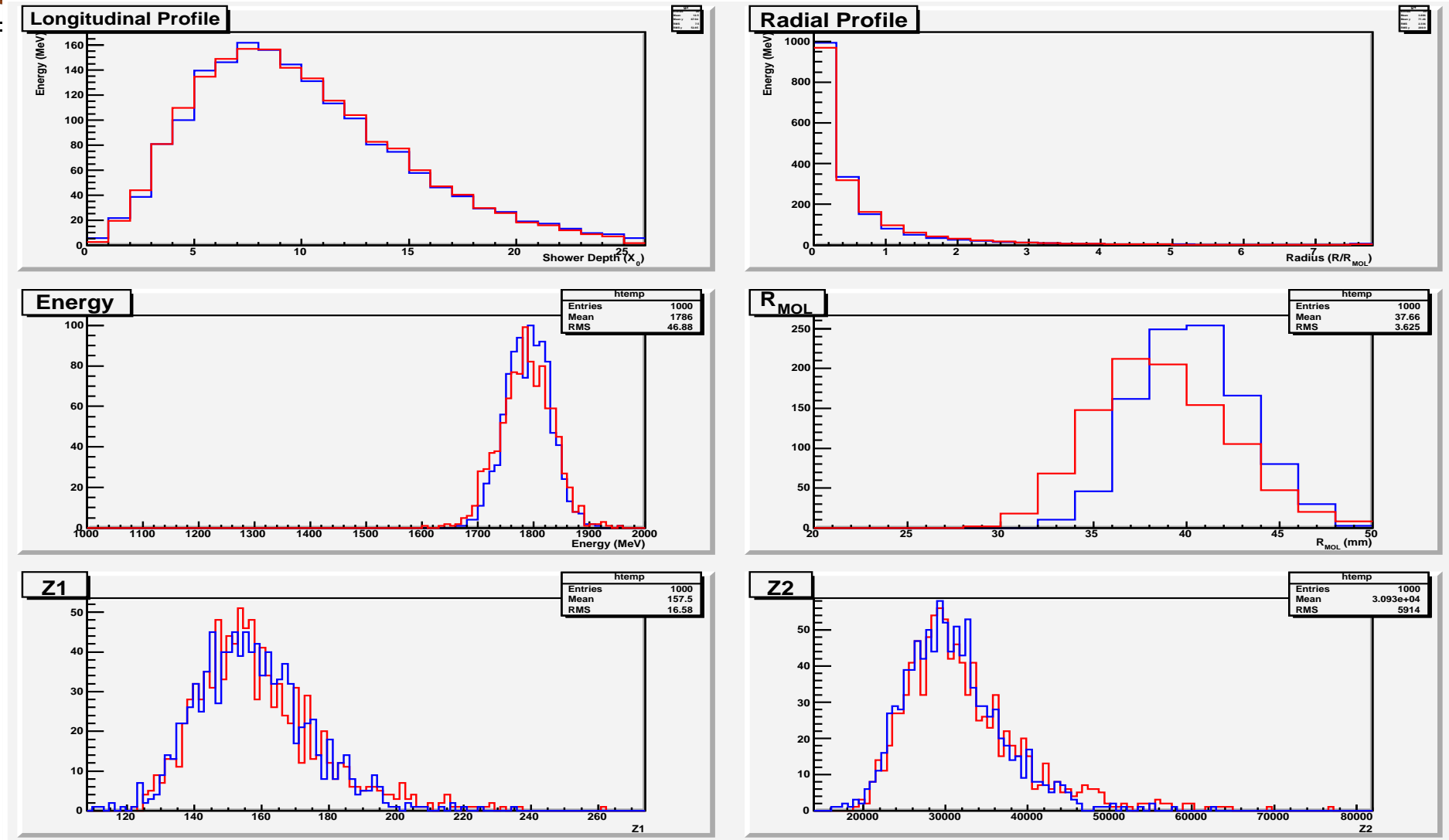
## Fast Simulation Scheme

- Conditions for parameterisation
  - Only electrons/positrons are parameterized. Photons are returned to full sim and the first electron produced is parameterised.
  - Particle must be within allowable energy range, if not it is returned to full simulation
  - Shower must be contained within the calorimeter, checked at  $Z(95\%)$  and  $R(95\%)$ .
- Handling of Leakage
  - If shower not contained, returned to full simulation; when the shower produces a fully contain electron, it is parameterised
- Showers starting before the calo
  - Particles are tracked using full simulation until they enter the calo, then each is parameterised separately

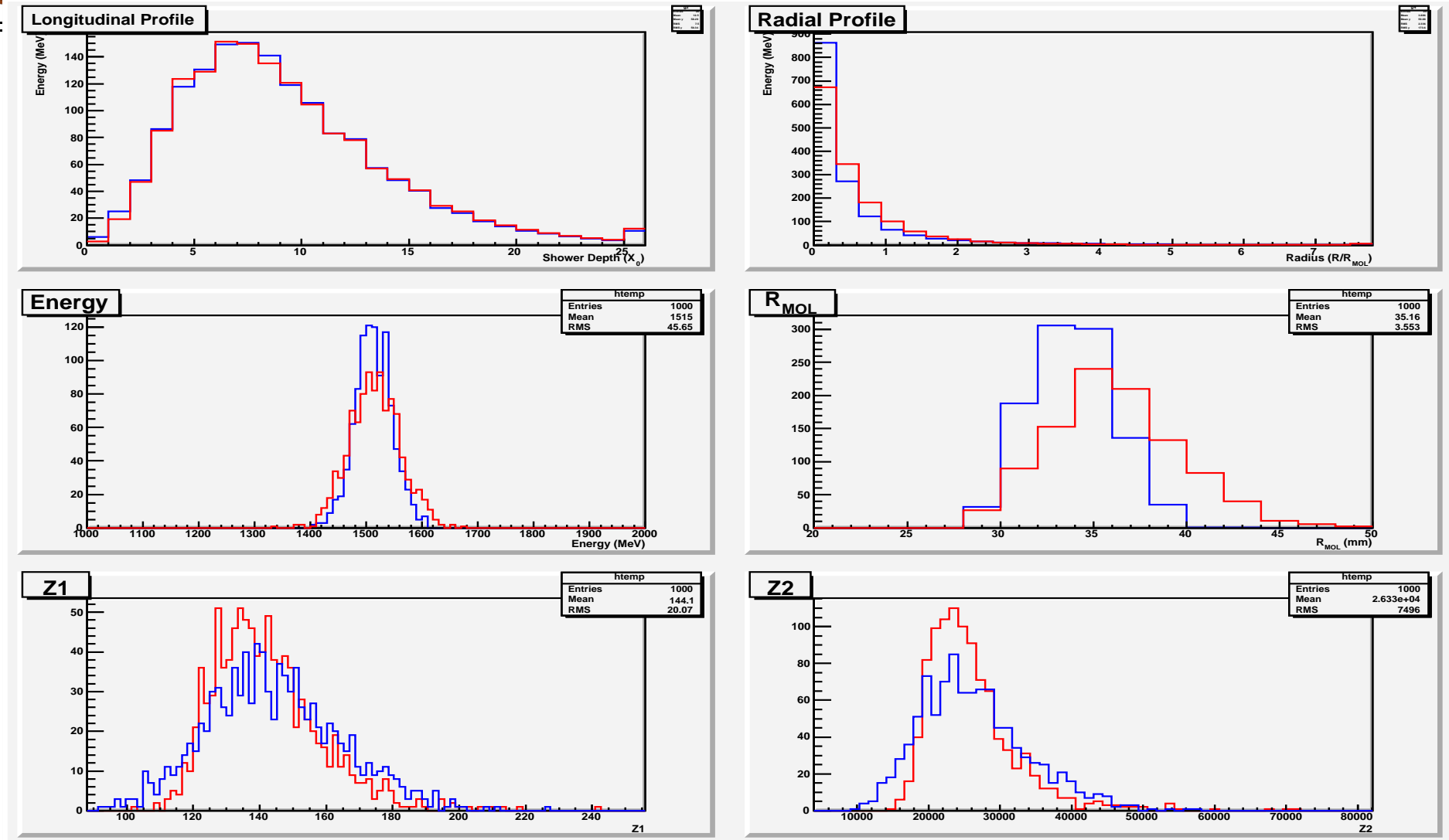


## Fast Simulation Scheme cont...

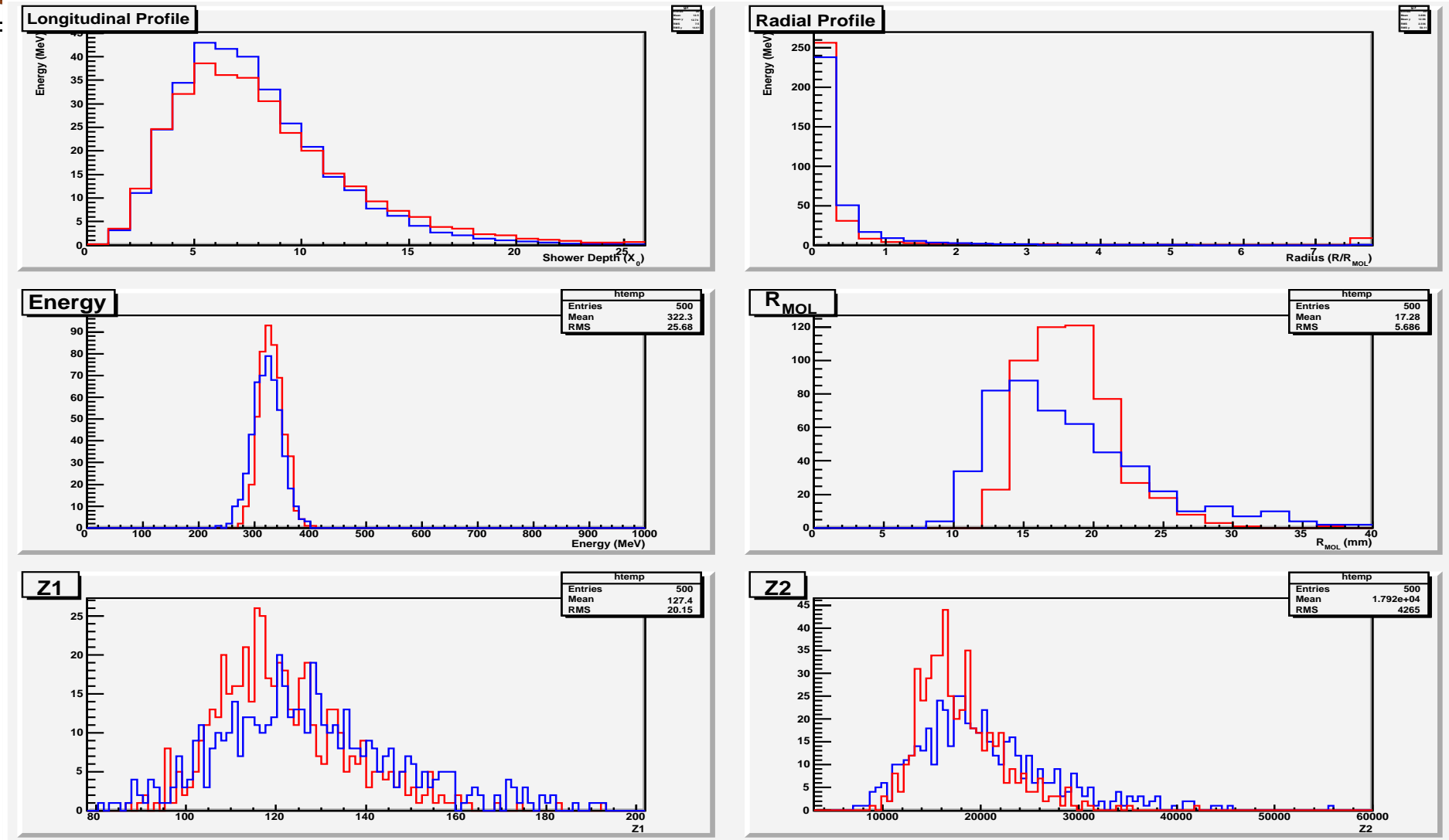
- If the conditions are satisfied
  - the track is killed
  - generate fake steps of a chosen length ( $10\mu m$ ) along the initial electron trajectory; calculate energy deposited and number of spots for each step
  - applying sampling fluctuation, taking into account the calorimeter resolution
  - calculate energy and position of each spot
  - generate hits and fill fake step to feed the sensitive detector
  - follow the full simulation chain to process the hits
  - loop until the total shower energy is deposited



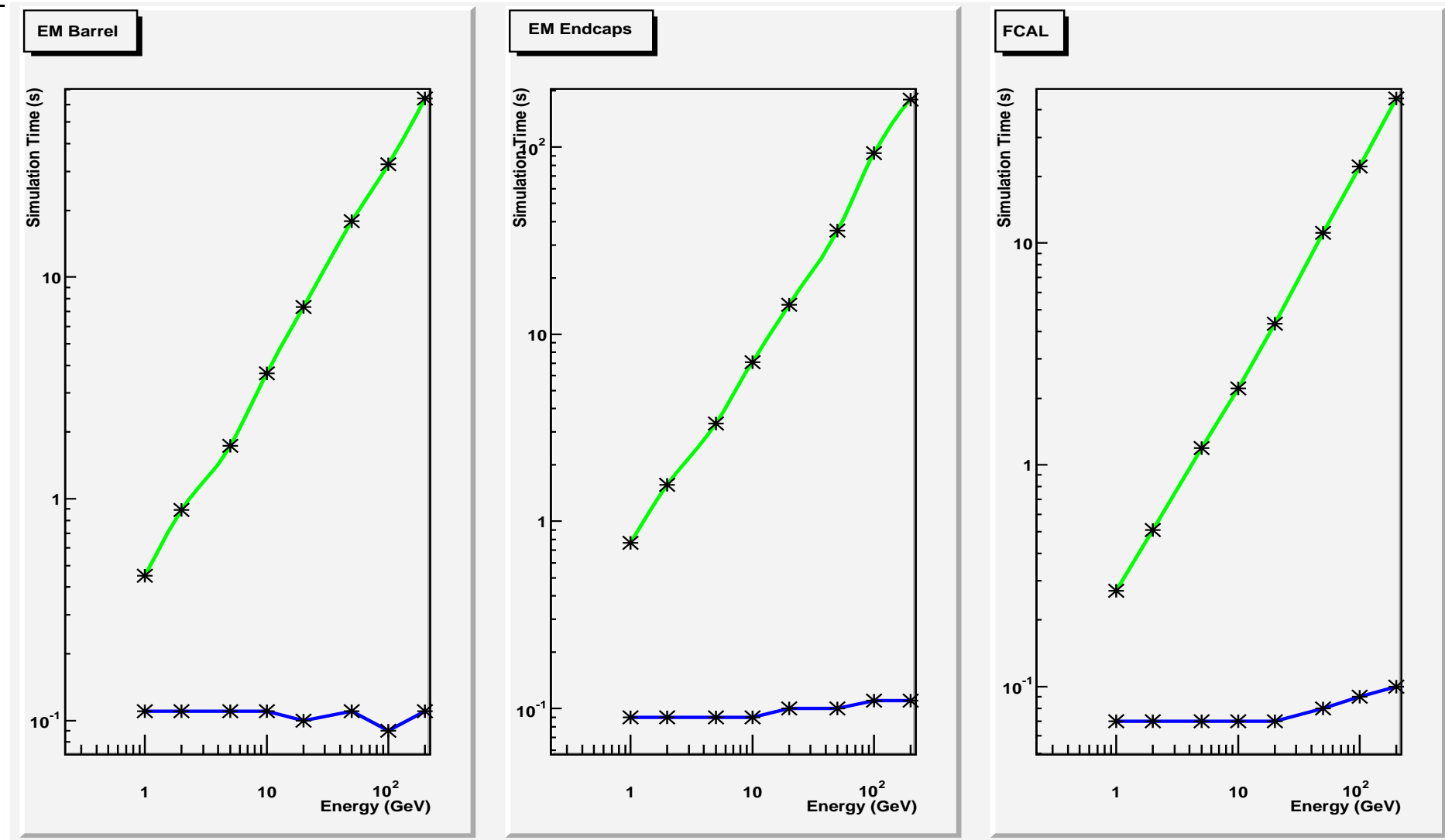
- Shower profiles for EMBARrel (1000 10GeV electrons) - using GEANT4 hits
- BLUE — Full simulation RED — Fast simulation



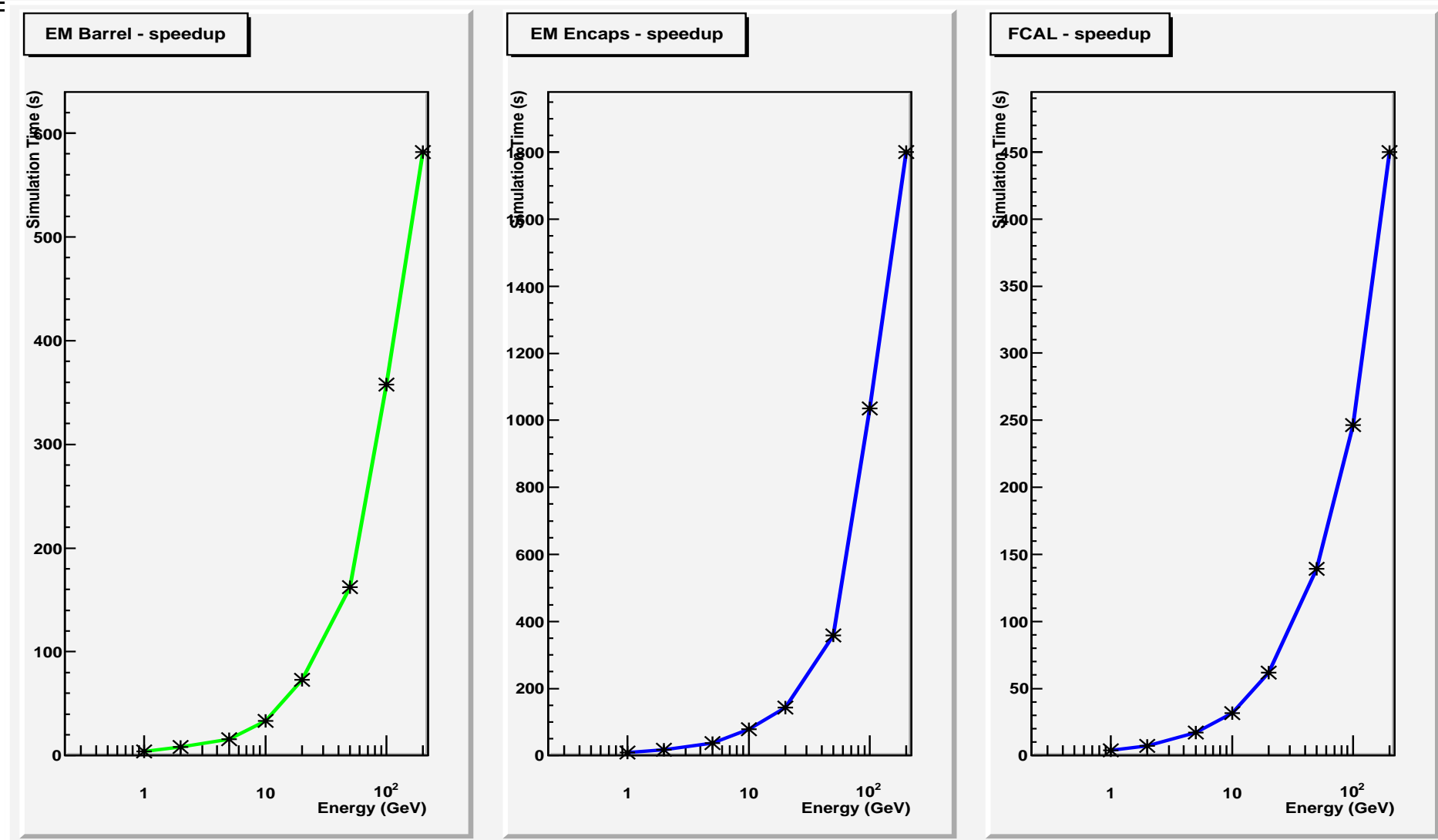
- Shower profiles for EM Endcap (1000 10GeV electrons) - using GEANT4 hits
- BLUE — Full simulation RED — Fast simulation



- Shower profiles for FCAL (500 10GeV electrons) - - using GEANT4 hits
- BLUE — Full simulation RED — Fast simulation



- electron shower simulation time (EM calorimeter only) for fast simulation and full simulation



- electron shower speedup (EM calorimeter only) for full simulation vs fast simulation





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## Validation

- Parallel production with athena 12.0.1
- To be validated by e-gamma person - blind analysis?
- Initially: single electrons, Z and W events.
- Down the track: jets, minimum bias events, susy



## Current/Future Work

- Maintenance of code; significant changes to geometry or athena require refit
- Extend parameterisation to hadron calorimeter and modules 2 and 3 of fcal to speed up simulation of EM component of hadron showers
- Feasibility of parameterising pion showers
- GEANT4.8



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## Conclusion

- EM calorimeter has been parameterised and fast simulation implemented
- Comparisons show reasonable agreement between full and fast simulations
- Timing is significantly improved
- Small production for validation using 12.0.1