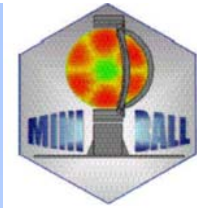
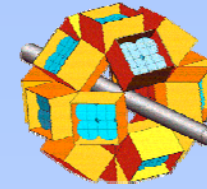


ISOLDE  
CERN



# Exotic shapes in exotic nuclei: Shape coexistence in unstable nuclei studied by Coulomb excitation

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Emmanuel Clément  
*CERN-PH/IS*

# Plan

- Nucleus, **shape**, deformation, shape coexistence ??
- **How to measure** the shape of the nucleus ?
- **Radioactive** ions beams
- Coulomb excitation of radioactive **Kr beams**
- **Shape coexistence** in light Kr isotopes
- Coulomb excitation of radioactive **Se beams**
- Shape coexistence **at CERN-ISOLDE**

# Nuclear deformation

- The **shape** is a **fundamental property** of the nucleus

Quantic system composed by **A nucleons** and driven by the **nuclear interaction** and the **electromagnetic interaction**

⇒ Minimum of the potential energy for a **non-spherical shape** (shell effect)

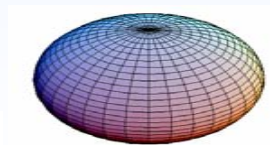
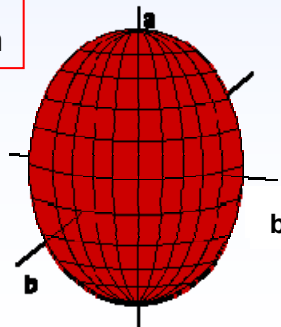
- The **sphere** is not the most common shape for a nucleus !!!  
 ⇒ Most of the nuclei are “deformed”



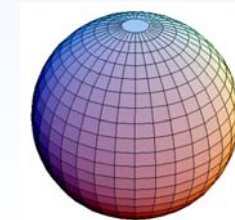
Picture of the ellipsoid : a, b, c, semi-axes

Axial symmetry  $b=c$  :  
 Pure quadrupole deformation

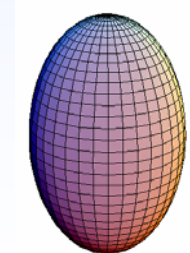
$$\beta = \frac{4}{3} \sqrt{\frac{\pi}{5}} \left( \frac{a-b}{R} \right)$$



$a < b$   
 $\beta < 0$  : oblate



$a = b$   
 $\beta = 0$  : sphère



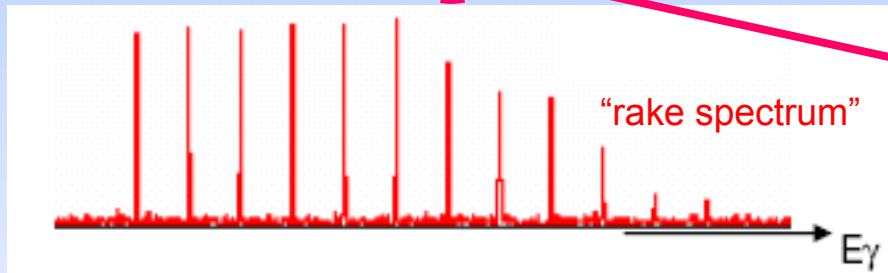
$a > b$   
 $\beta > 0$  : prolate

# Rotation of a deformed nucleus

- A deformed nucleus has a **rotational spectra**

$$E(I) = \frac{\hbar^2}{2\mathcal{J}^{(0)}} I(I + 1)$$

**Rotor** energy sequence

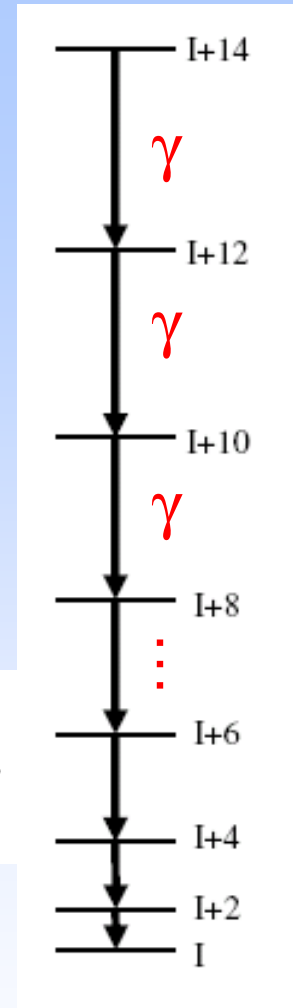


**Static** moment of inertia

$$\mathcal{J}^{(2)} = \left( \frac{\partial^2 E}{\partial I^2} \right)^{-1} = \frac{\partial I}{\hbar \partial \omega} \approx \frac{(\Delta I)^2}{\Delta E_\gamma}$$

**dynamic** moment of inertia : **variation of the rigid rotor**

**CONSTANT**



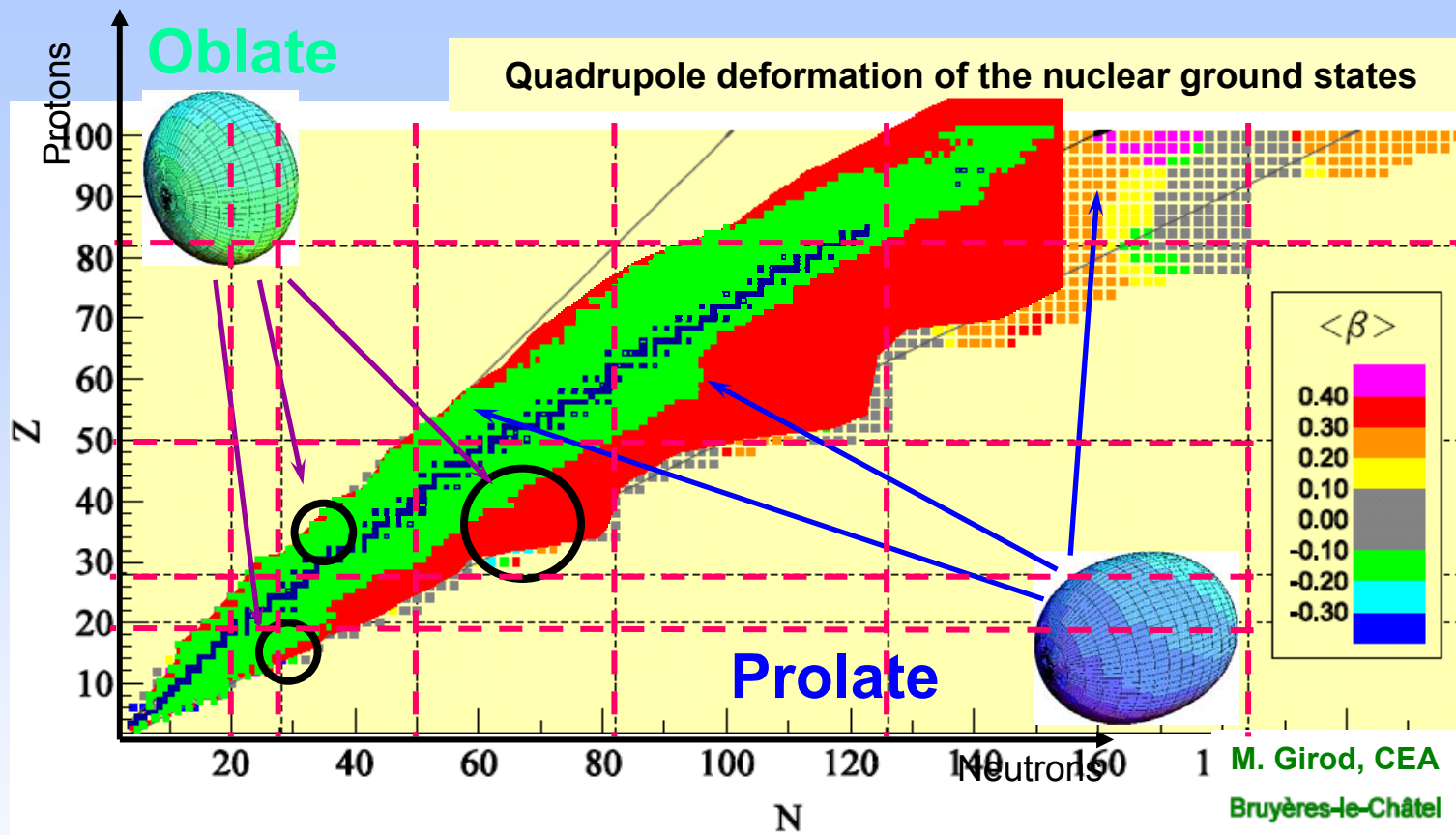
$$B(E\lambda, I_i \rightarrow I_f) = \frac{|\langle I_f || M(E\lambda) || I_i \rangle|^2}{2I_i + 1}$$

**Reduced** transition probability (collectivity)

$$eQ_0 = \sqrt{\frac{16\pi}{5}} \frac{1}{\sqrt{2I_i + 1}} \frac{\langle I_f || M(E2) || I_i \rangle}{\langle I_i K 2 0 | I_f 0 \rangle}$$

**Quadrupole** moment (intrinsic properties)

# The deformed world ...



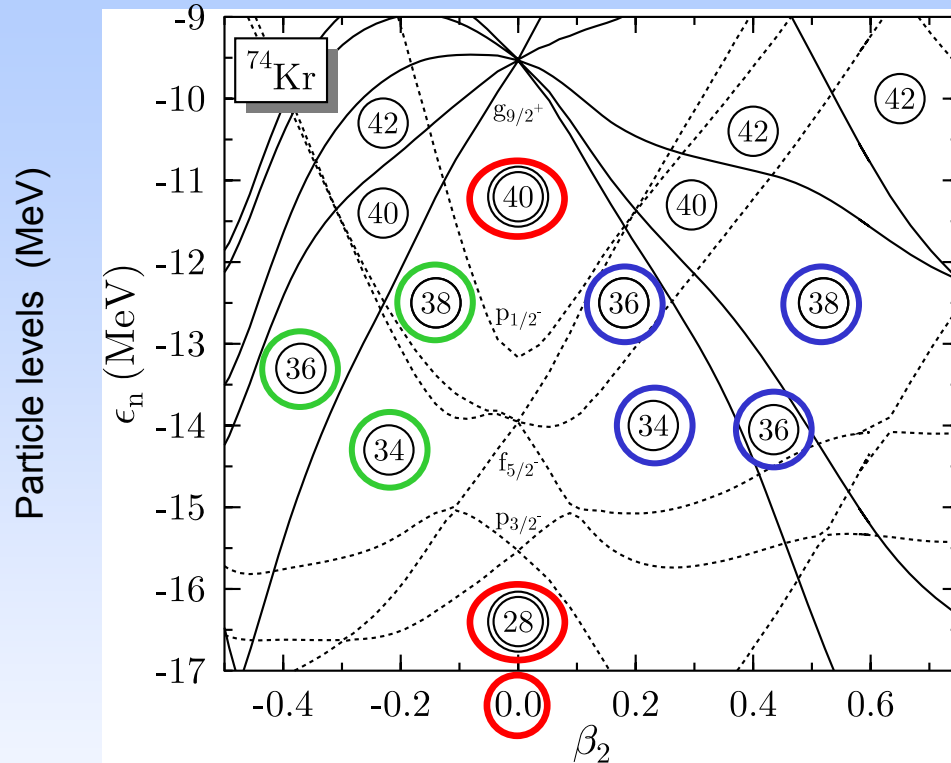
- For the **magic numbers** of the nuclear physics, the nucleus is **spherical**
- **Between** the magic number the nucleus is **deformed**

Deformation describe in term of magnetic dipole and quadrupole moments which are very **sensitive to all types of correlations**



Important **benchmarks** for nuclear models / theory

# The mass region $A=70-80$ close to $N=Z$ line



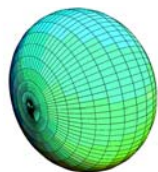
One particle level scheme in a phenomenological potential  
 → Nilsson scheme

The nucleus chooses a configuration which **minimizes** its energy and presents a maximal gap with the next orbital  
 → energy gap

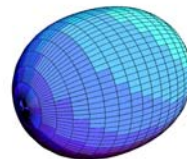
- Spherical nuclei

➔ Magic number

For nucleons number **34,36,38**



Deformation parameter  $\beta$



- Gap for **prolate** deformation
- Gap for **oblate** deformation

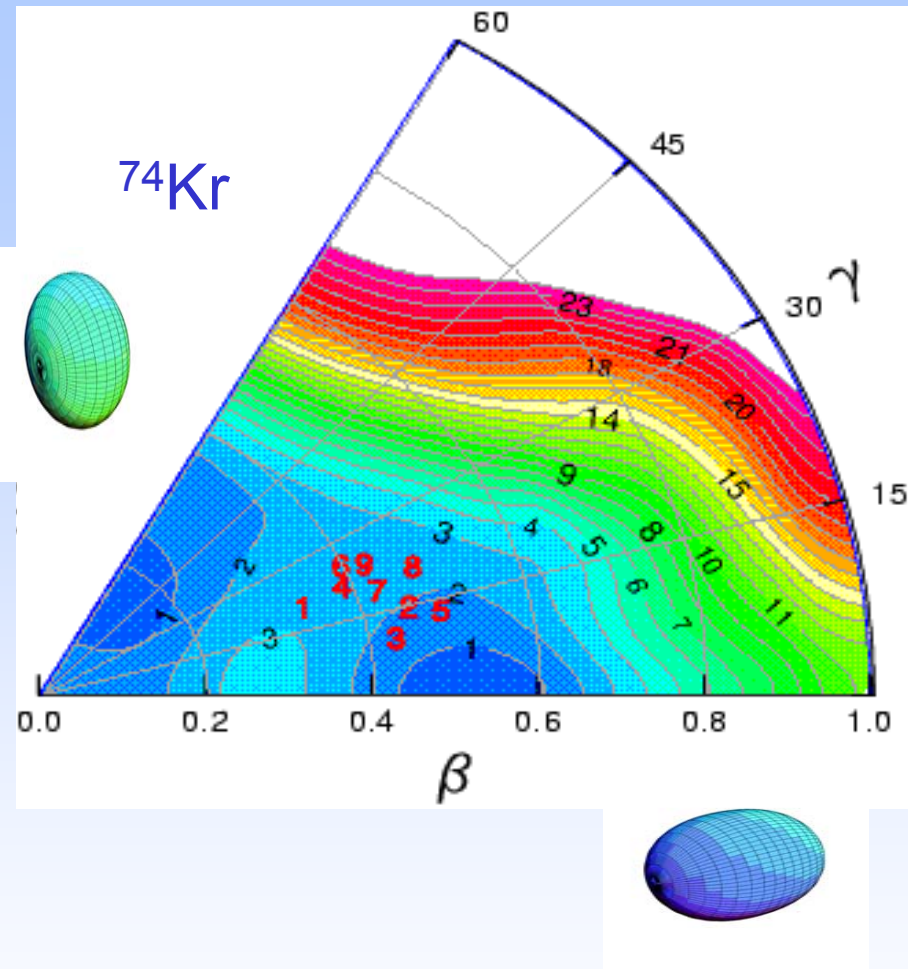
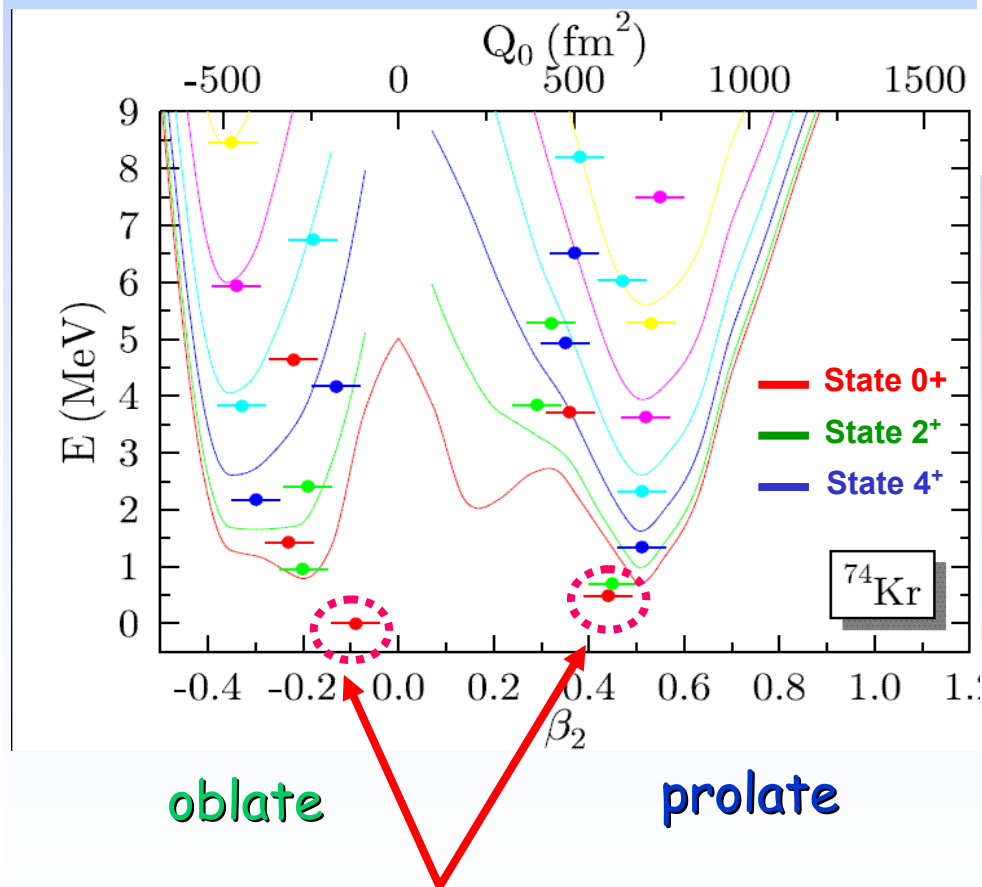
✓ **Shape coexistence** expected in nuclei  $Z = 34, 36, 38$



✓ Possibility to study the **oblate deformation**

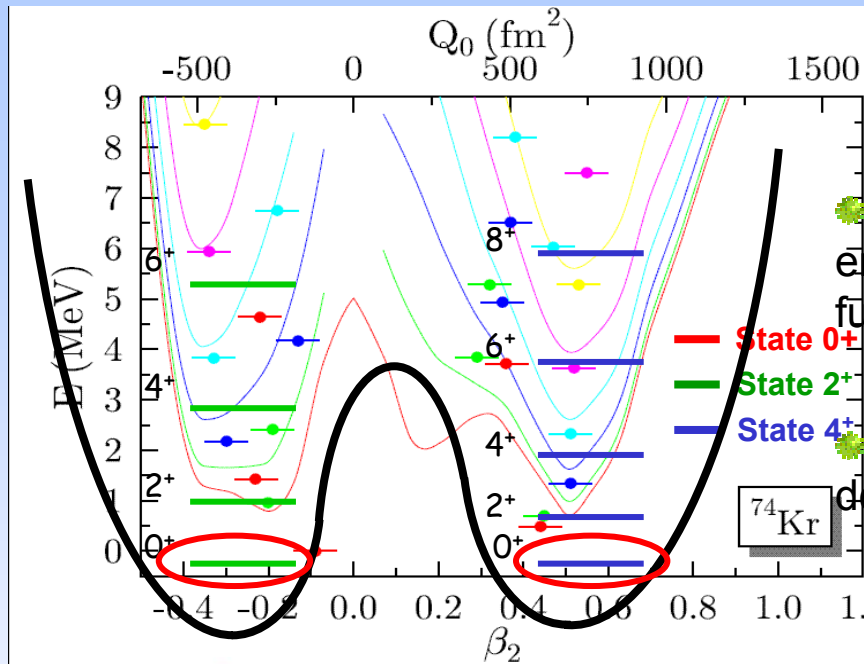
# Shape coexistence in the light krypton

HFB+Gogny D1S  
M. Girod *et al.*



GCM-HFB (SLy6)  
M. Bender, P. Bonche et P.H. Heenen,

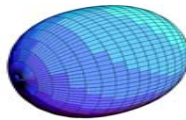
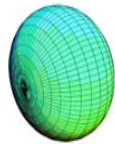
# The mass region $A=70-80$ close to $N=Z$ line



A low lying  $0^+$  state is expected at low energy, with a high mixing of the wave function

GCM-HFB (SLy6)  
M. Bender, P. Bonche et P.-H. Heenen,

2 rotational bands with an opposite deformation built on each  $0^+$  state



- What is the relative position of the rotational states ?
- Low lying  $0^+_2$  state ?
- Deformation of the rotational band ?
- Mixing of the wave function ?

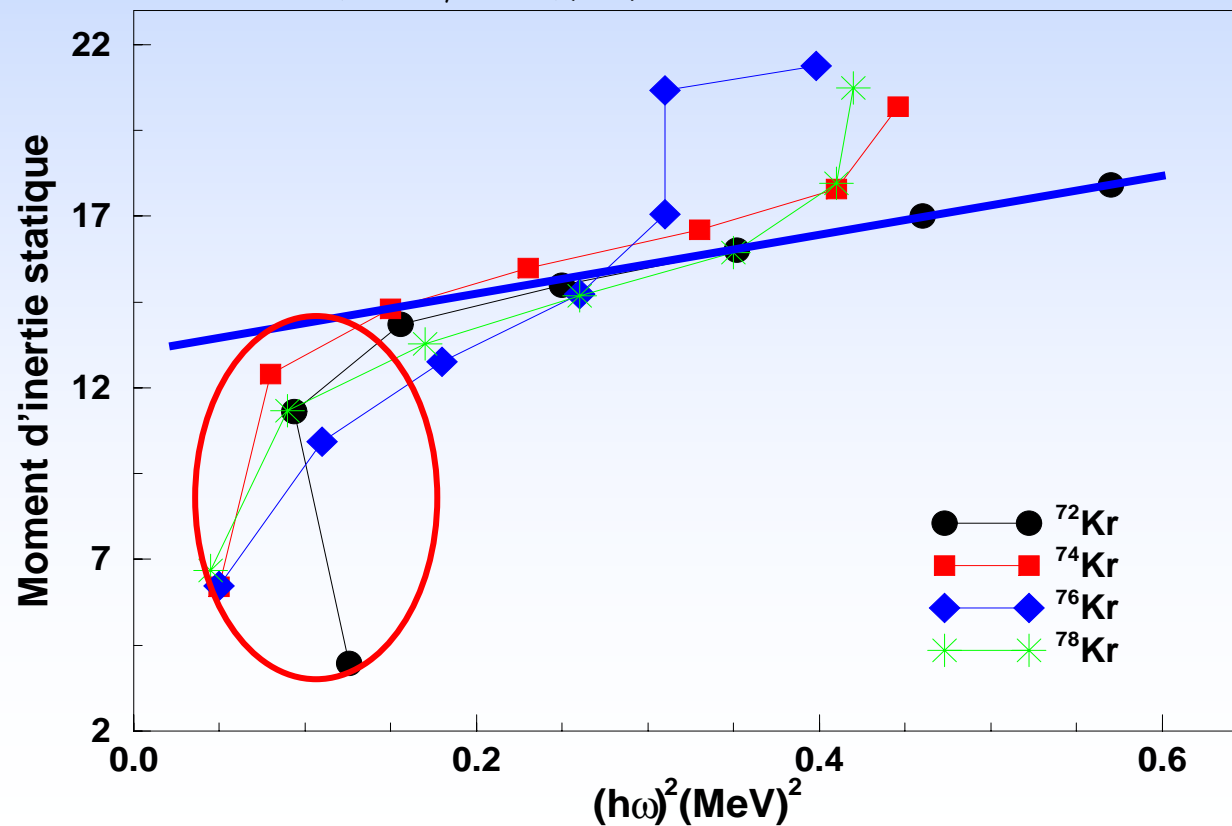


# First studies on Shape Coexistence in Kr isotopes

High spins studies populated by fusion-evaporation reaction

Measure of the static moment of inertia of :  $^{72}\text{Kr}$ ,  $^{74}\text{Kr}$ ,  $^{76}\text{Kr}$  et  $^{78}\text{Kr}$

S. M. Fischer et al., Phys. Rev. Lett. **87**, (2001)  
 N. S. Kelsall et al., Phys. Rev. C **64**, (2001)  
 D. Rudolph et al., Phys. Rev. C **56**, (1998)  
 C. J. Gross et al., Nucl. Phys. A **501**, (1989)



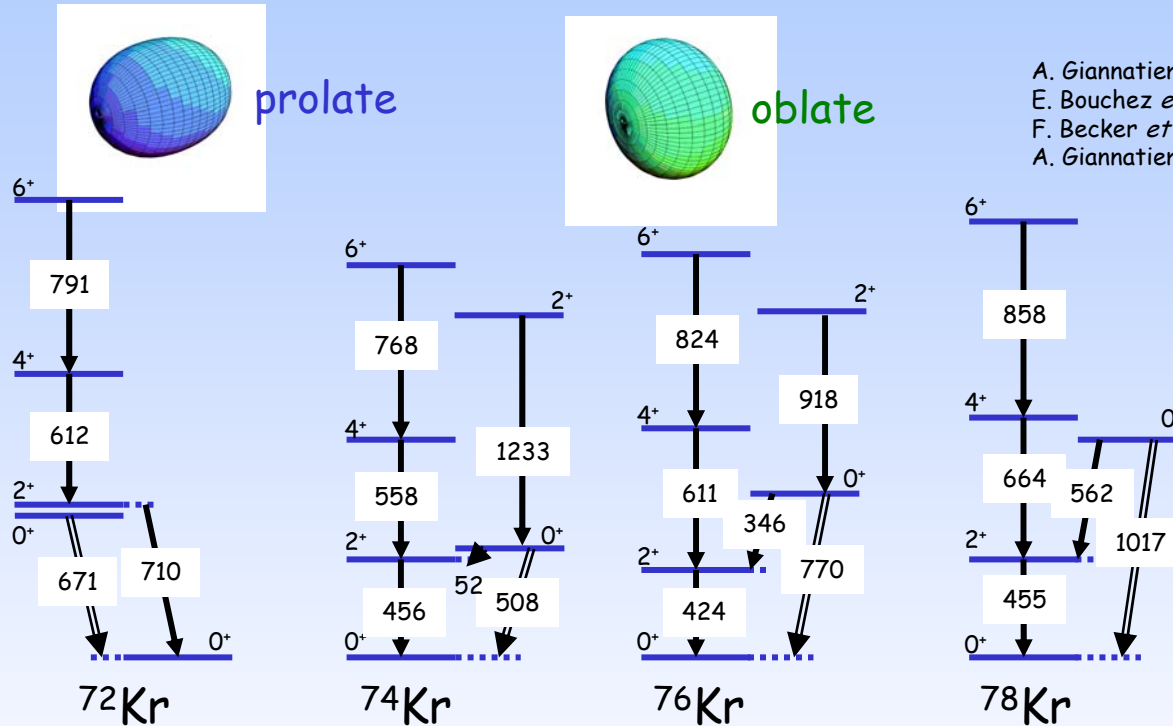
Static moment of inertia for a **rotor = constant**

In a normal nucleus :  
 $\sim a + b (\hbar\omega)^2$

Perturbation of the collectivity at low spins

# First studies on Shape Coexistence in Kr isotopes

- Identification of the low lying  $0^+$  state, possible candidate for the shape isomer.



A. Giannatiempo *et al.*, Phys. Rev. C **72** (2005)  
 E. Bouchez *et al.* Phys. Rev. Lett., **90** (2003)  
 F. Becker *et al.*, Eur. Phys. J. A **4** (1999)  
 A. Giannatiempo *et al.*, Phys. Rev. C **52** (1995)

72(6)

84(18)

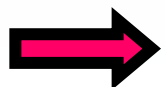
79(11)

47(13)

Transition strength:  
 $\rho^2(E_0) \cdot 10^{-3}$

► **Shape inversion** for  $^{72}\text{Kr}$

►  **$^{74}\text{Kr}$  is a transitional nucleus** where the mixing of the wave function is maximal



Complete measure of reduced **transition probability**  $B(E2)$  and **static quadrupole moment**



Coulomb excitation

# Plan

- Nucleus, shape, deformation, shape coexistence ??
- How to measure the shape of the nucleus ?
- Radioactive ions beams
- Coulomb excitation of radioactive Kr beams
- Shape coexistence in light Kr isotopes
- Coulomb excitation of radioactive Se beams
- Shape coexistence at CERN .....

# How to measure the shape of the nucleus ?

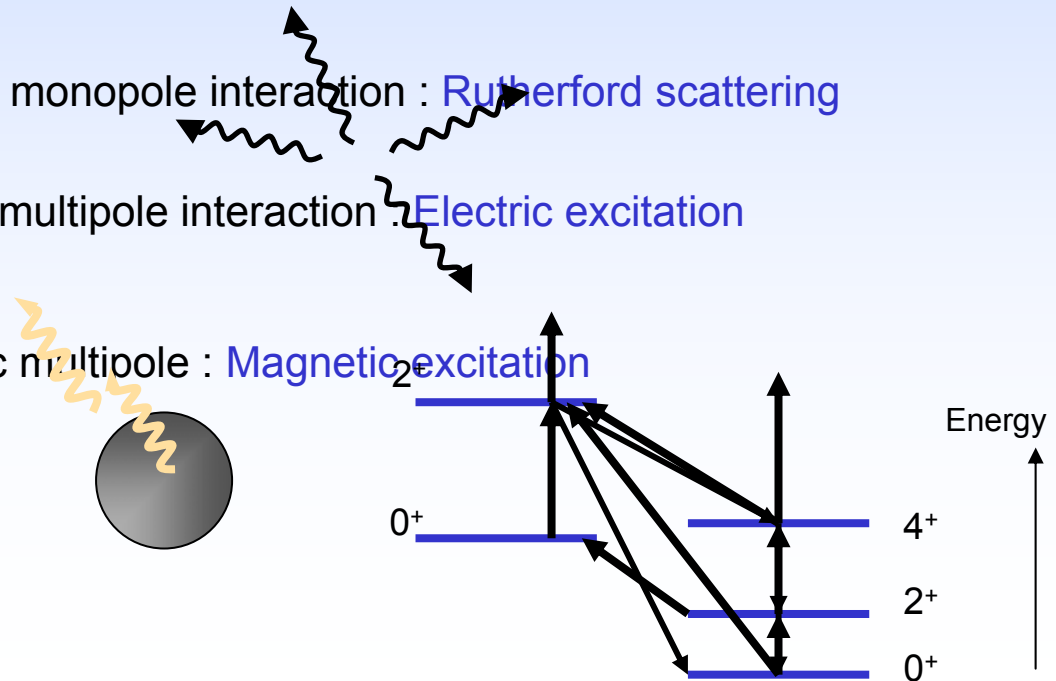
..... by Coulomb excitation

- ▶ The electric quadrupole moment of a nucleus is measured through its **interaction with an electromagnetic field** created by a probe nucleus
- ▶ The electromagnetic interaction is the **only forces** involved in the collision



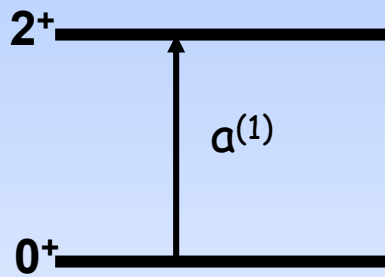
**NO nuclear reaction**

- ▶ Electric monopole – Electric monopole interaction : Rutherford scattering
- ▶ Electric monopole – Electric multipole interaction : Electric excitation  
 $E1, E2, \dots, E\lambda$
- ▶ Electric monopole – Magnetic multipole : Magnetic excitation  
 $M1, M2, \dots, M\lambda$



# Coulomb excitation et re-orientation effect

1<sup>er</sup> order:



$$\frac{d\sigma^{(1)}}{d\Omega} \propto \frac{\langle I_f \| M(E2) \| I_i \rangle}{d\sigma_{Ruth}} \propto \frac{B(E2)}{d\sigma} \propto Q^2$$

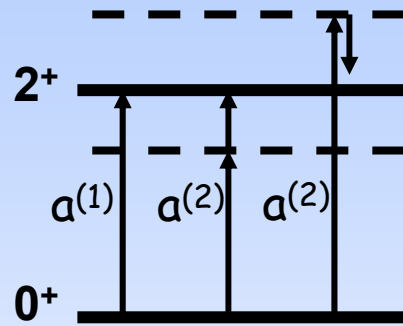
$P_{i \rightarrow f}$

absolute deformation !

↳ Particle detector covering a large range in scattering angle

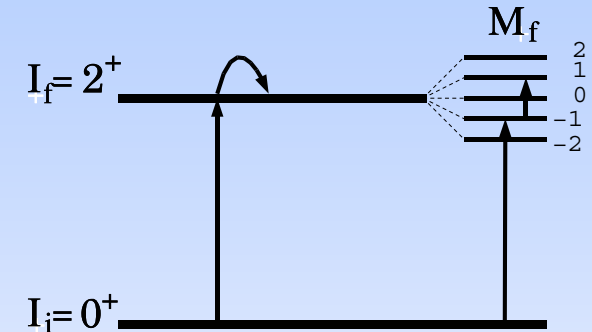
↳ High efficiency and selectivity

2<sup>nd</sup> order:

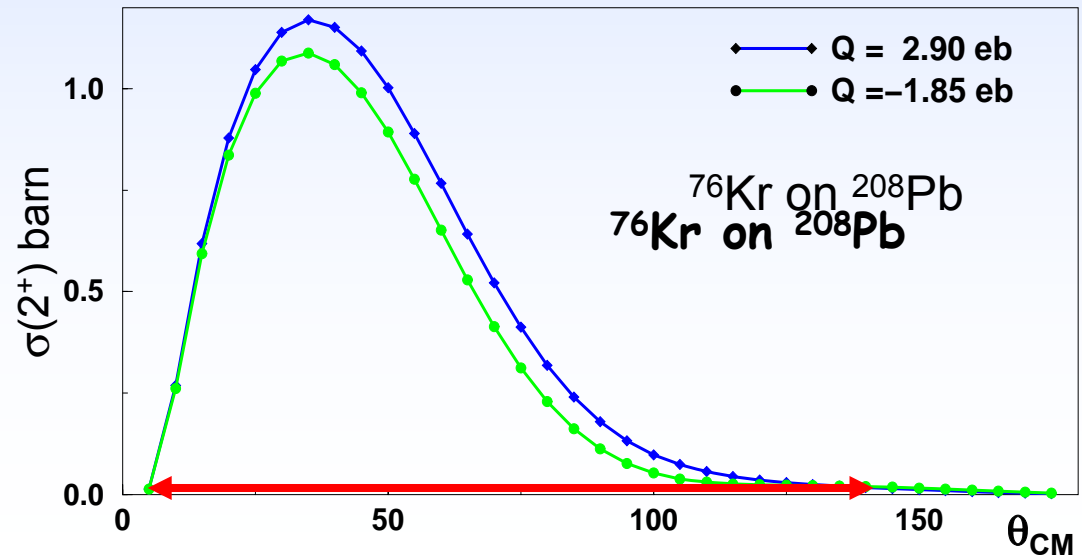


$$a^{(2)} \propto \sum_j \langle I_f \| M(E2) \| I_j \rangle \langle I_j \| M(E2) \| I_i \rangle$$

Re-orientation effect



Cross section  $\rightarrow Q_0$

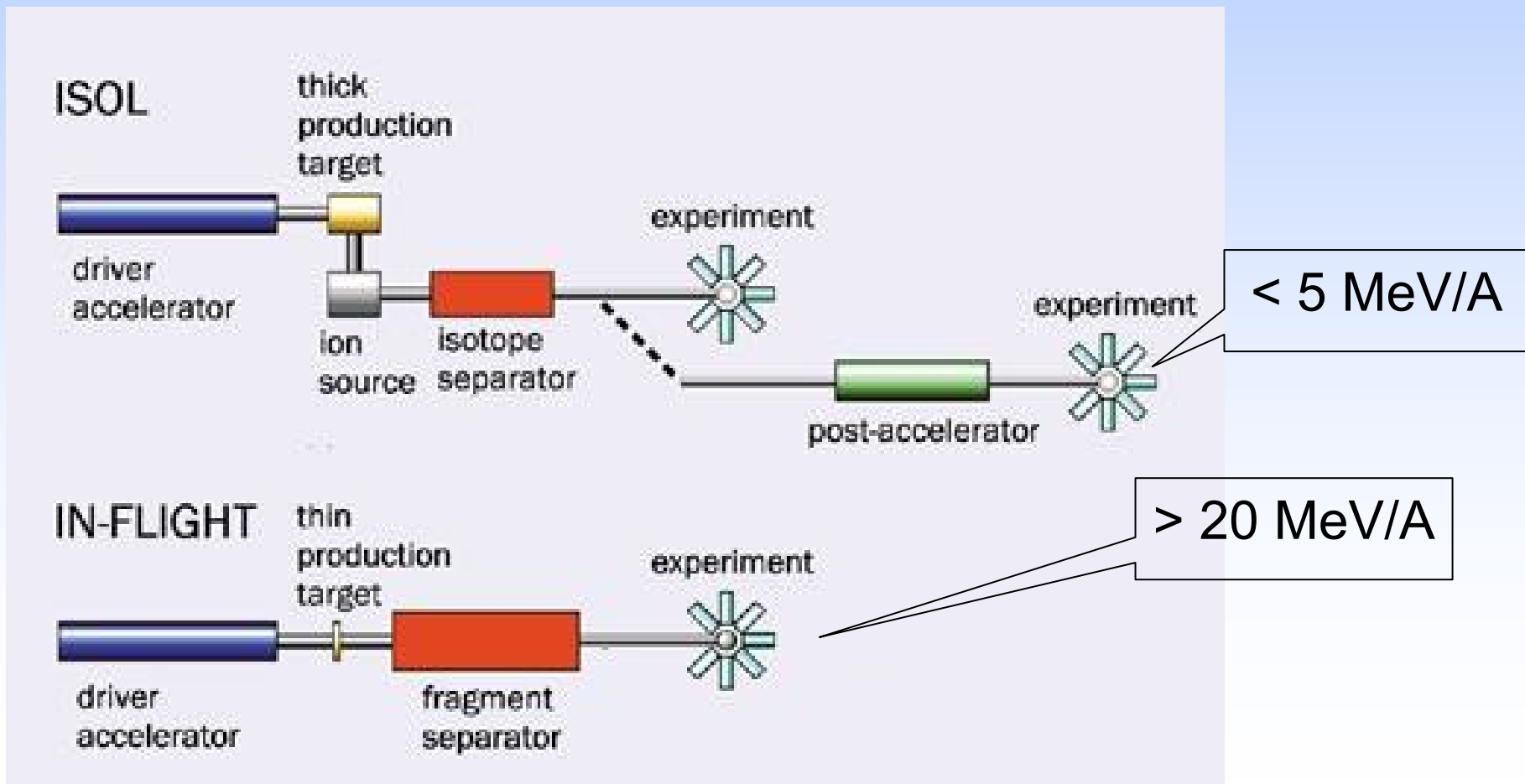


# Plan

- Nucleus, shape, deformation, shape coexistence ??
- How to measure the shape of the nucleus ?
- **Radioactive ions beams**
- Coulomb excitation of radioactive Kr beams
- Shape coexistence in light Kr isotopes
- Coulomb excitation of radioactive Se beams
- Shape coexistence at CERN .....

# Radioactive ions beam

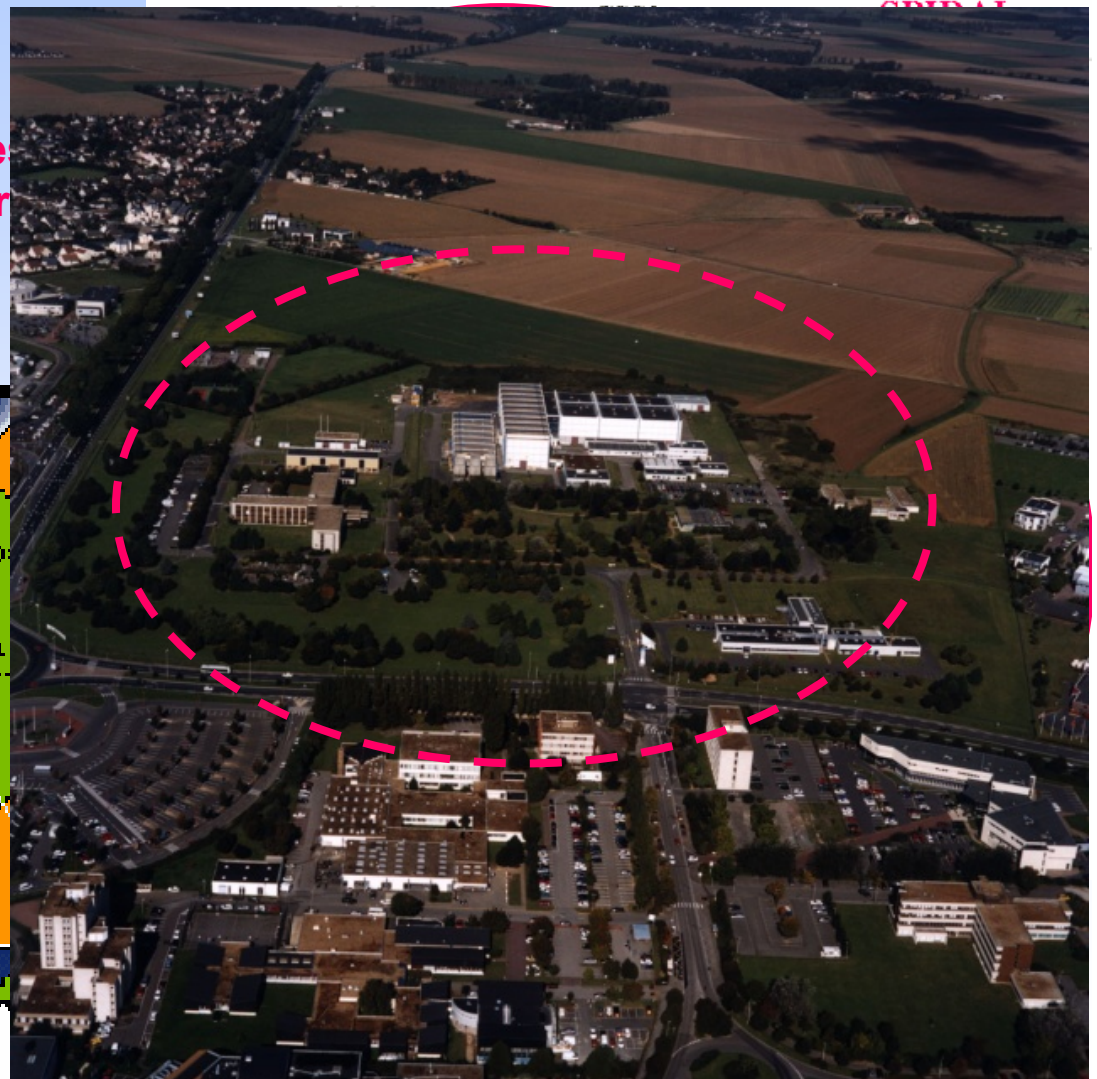
radioactive target is not possible so we need a  
radioactive ions beams below the coulomb barrier



# ISOL beam @ SPIRAL –GANIL France

ISOL beam production  
and post-acceleration  
Primary beam  
acceleration

Ions source  
and injector



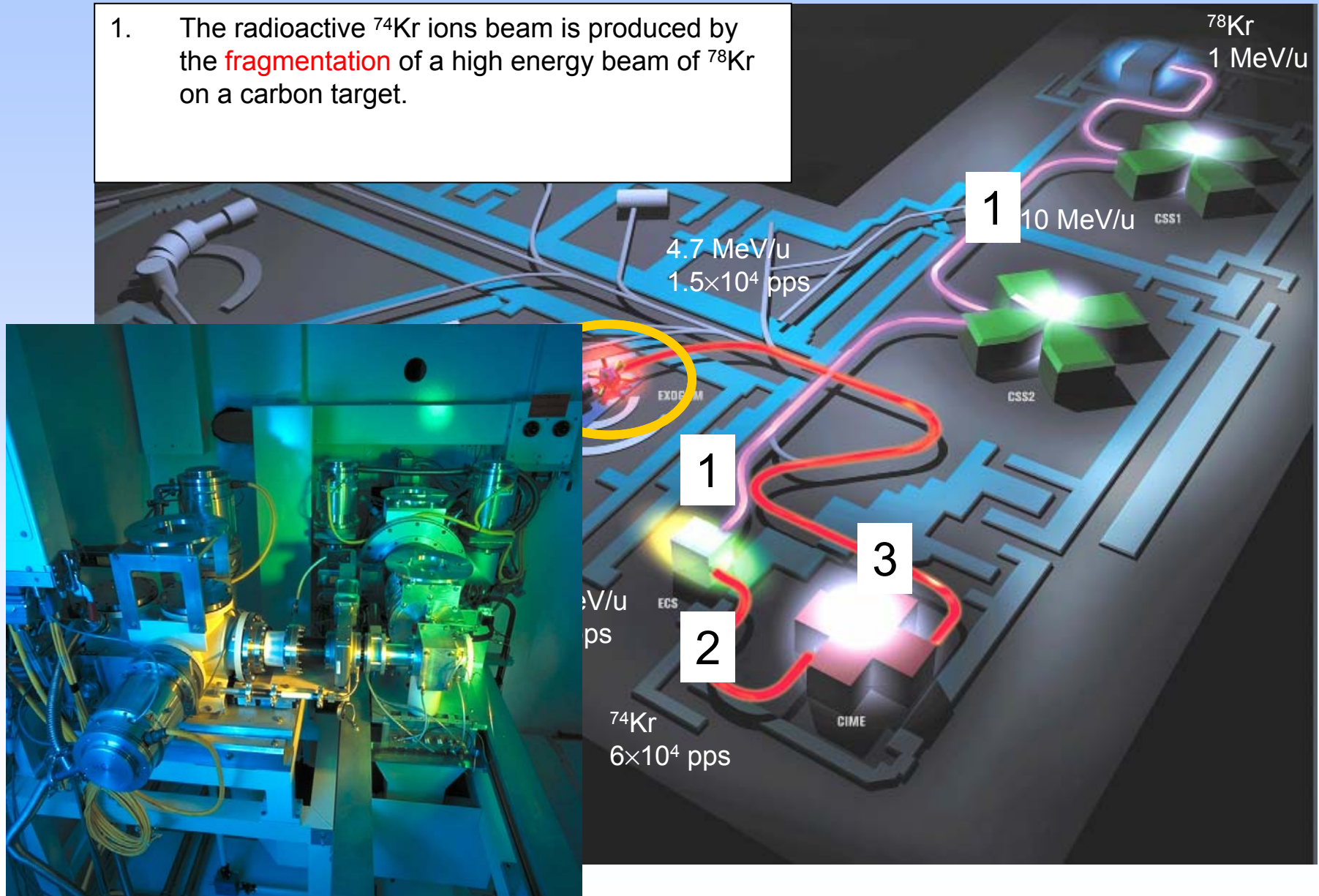


# Plan

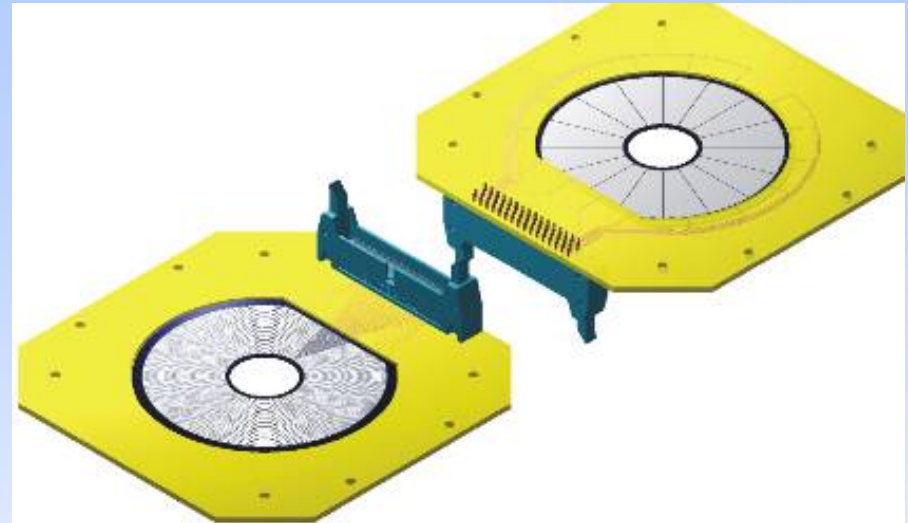
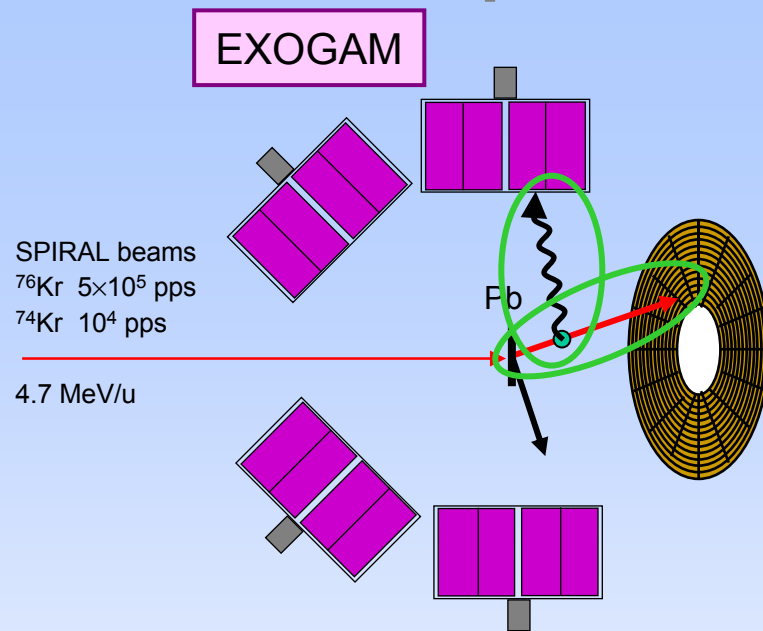
- Nucleus, shape, deformation, shape coexistence ??
- How to measure the shape of the nucleus ?
- Radioactive ions beams
- Coulomb excitation of radioactive Kr beams
- Shape coexistence in light Kr isotopes
- Coulomb excitation of radioactive Se beams
- Shape coexistence at CERN .....

# $^{74}\text{Kr}$ and $^{76}\text{Kr}$ beam @ SPIRAL

1. The radioactive  $^{74}\text{Kr}$  ions beam is produced by the **fragmentation** of a high energy beam of  $^{78}\text{Kr}$  on a carbon target.



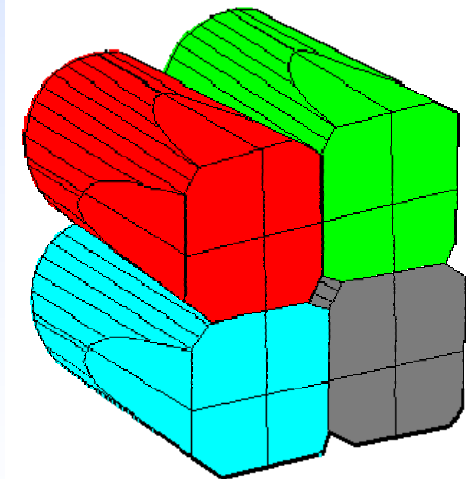
# Experimental setup



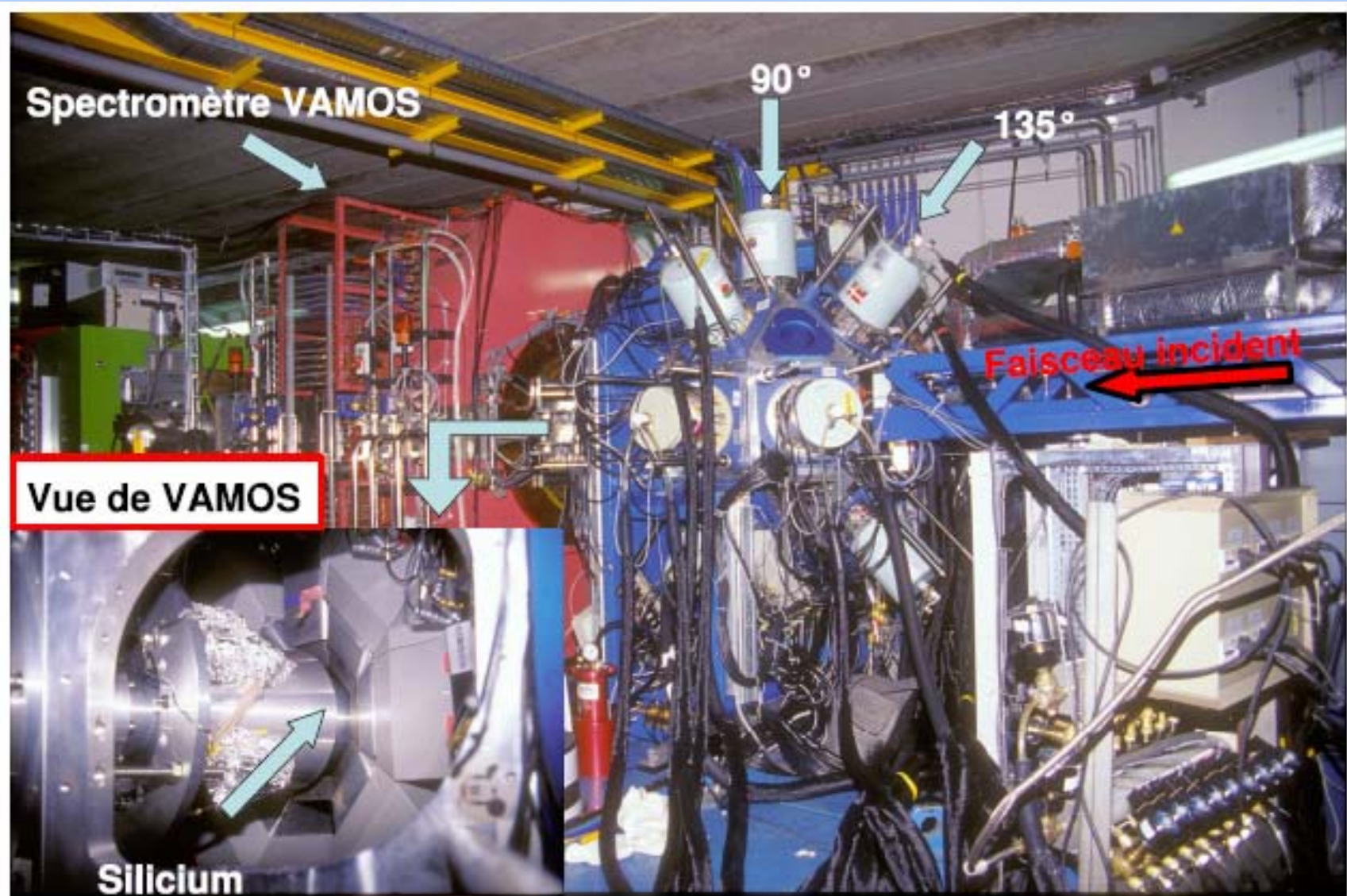
➤ Highly segmented particle detector 16 concentric ring and 16 sector :

➤ Segmentation of the Silicon + Segmentation of EXOGAM  
→ Doppler Correction

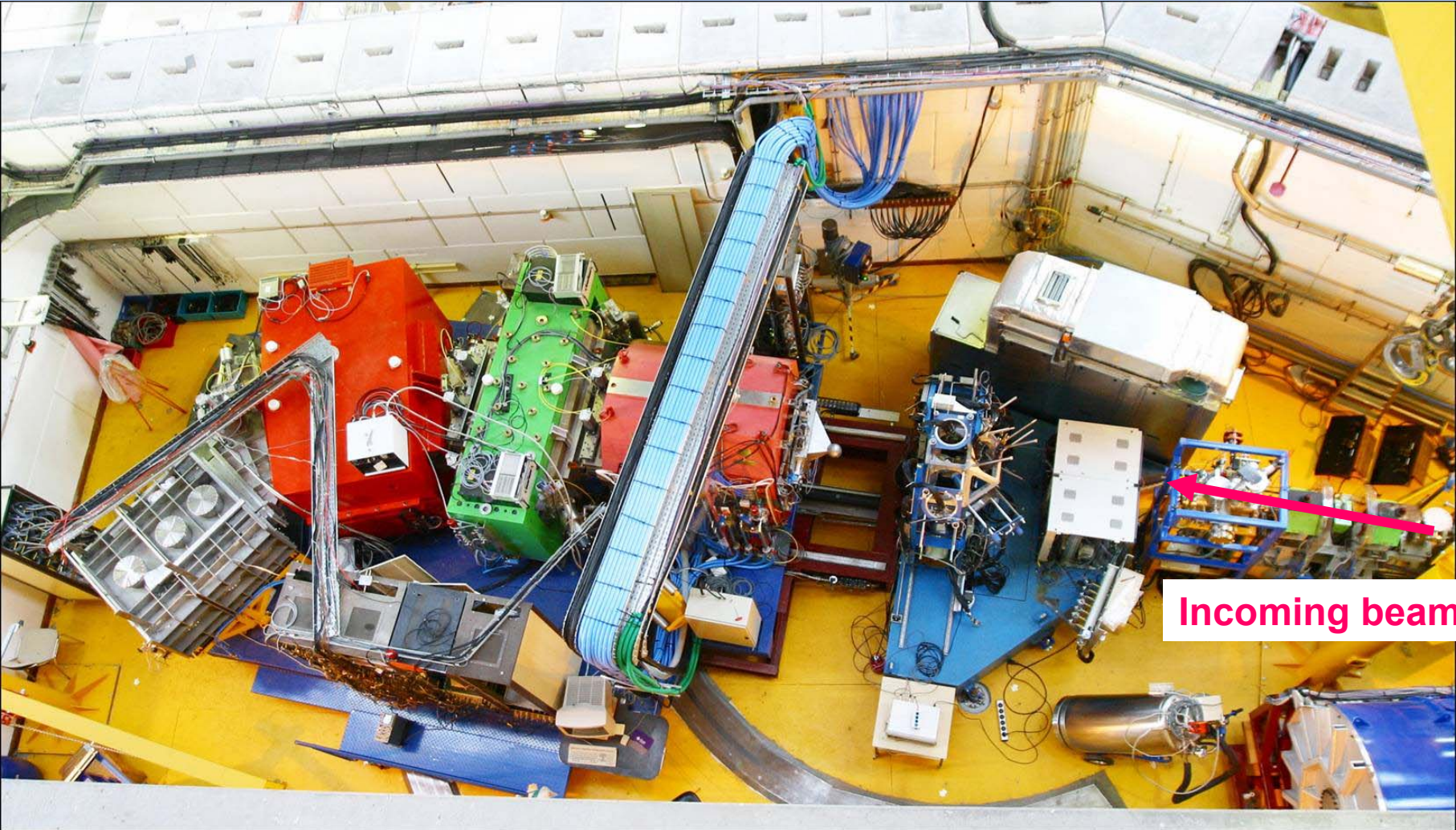
➤ Differential cross section



# Experimental setup

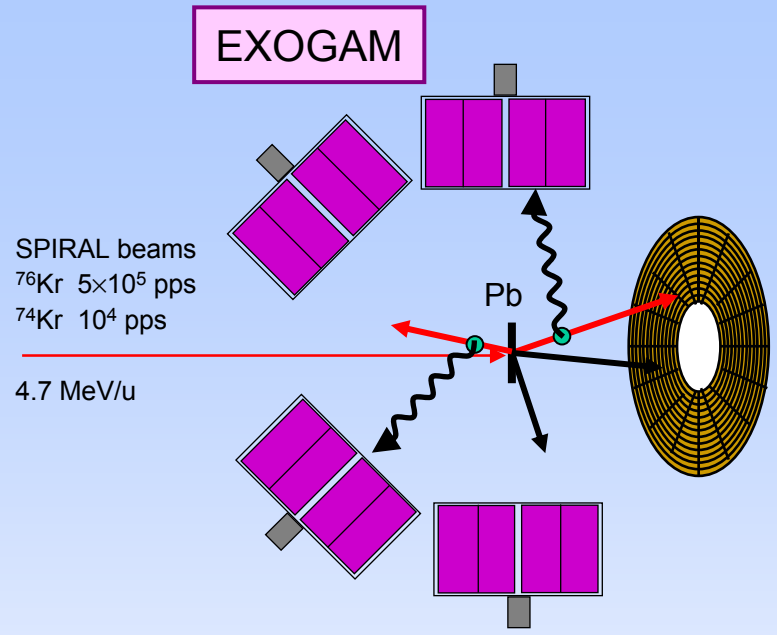


# Experimental setup

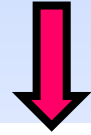
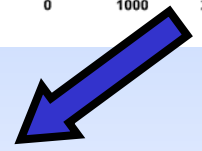
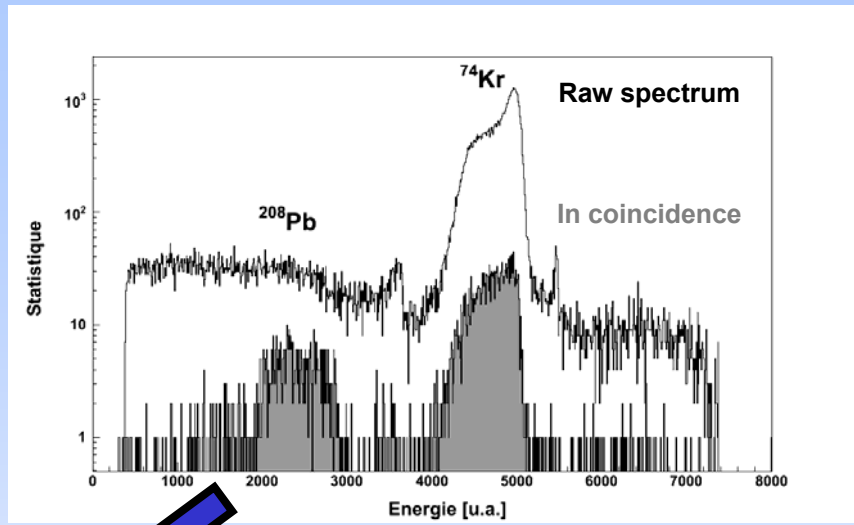


Incoming beam

# Experimental results

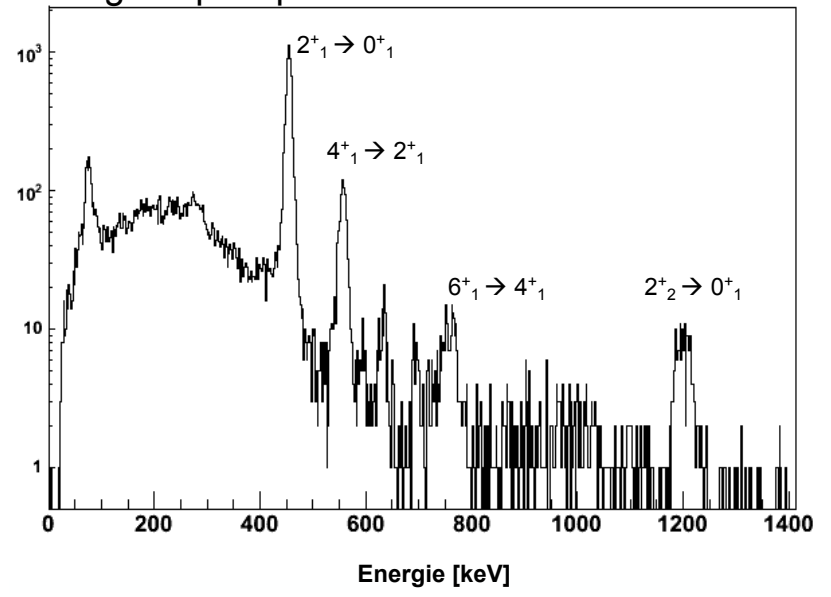


Silicon spectrum



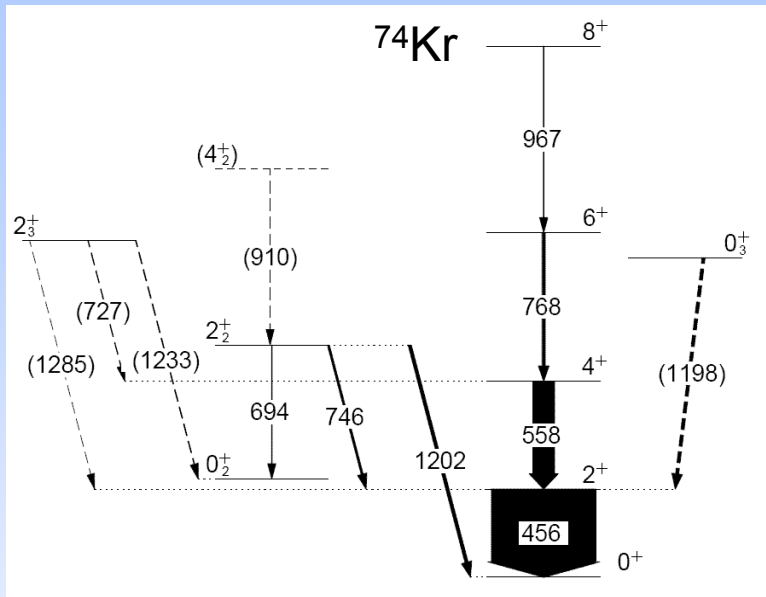
Small impact parameter  $\rightarrow$  Pb detected

Large impact parameter  $\rightarrow$  Kr detected



# Coulomb excitation analysis with GOSIA\*

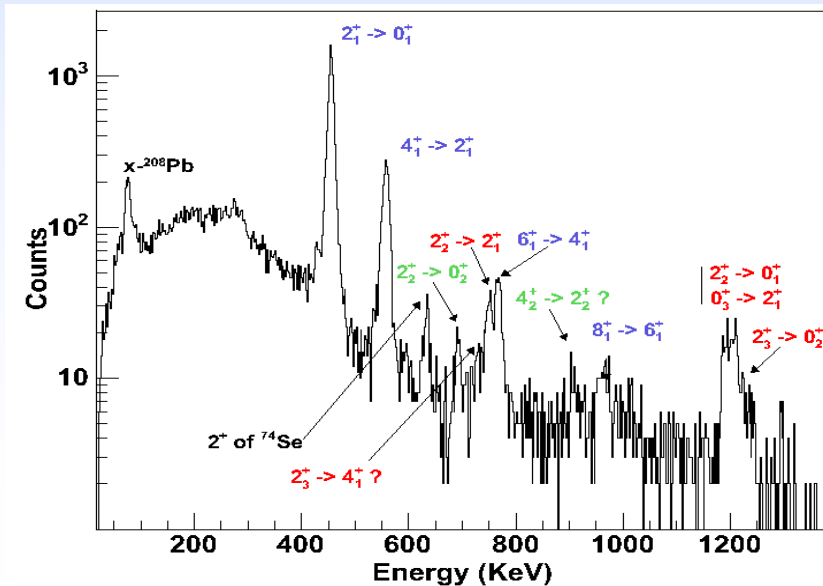
\*D. Cline, C.Y. Wu, T. Czosnyka; Univ. of Rochester



Matrix elements adjustment (transitional and diagonal) in order to reproduce the experimental data :  $I_\gamma(\theta_{\text{Kr}})$

•  $I_\gamma(\theta_{\text{Kr}})$  : differential cross section

$\theta_{\text{cm}} \rightarrow [24, 144.5]$  degrees



Weak constraint due to the limited statistic

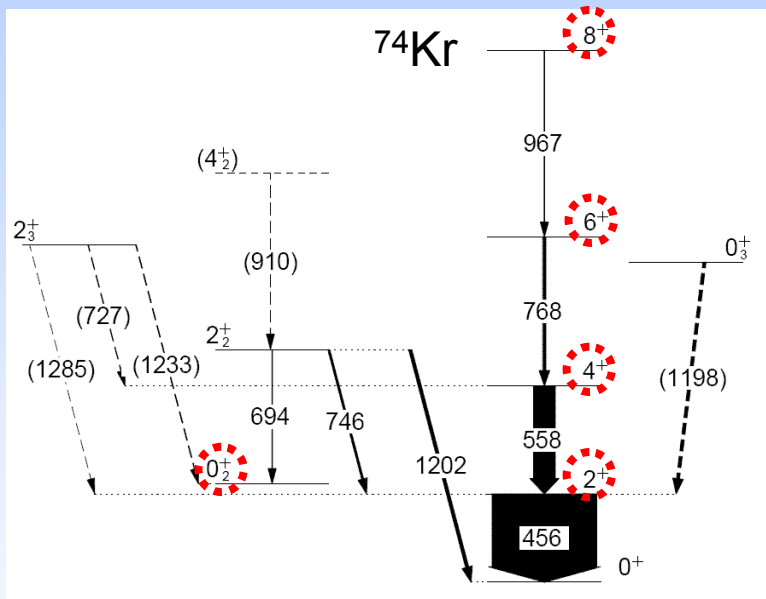
• Additional constraints : spectroscopic data

- ✘ Lifetime
- ✘ Branching ratio
- ✘ Mixing E2/M1

# Coulomb excitation analysis with GOSIA\*

\*D. Cline, C.Y. Wu, T. Czosnyka; Univ. of Rochester

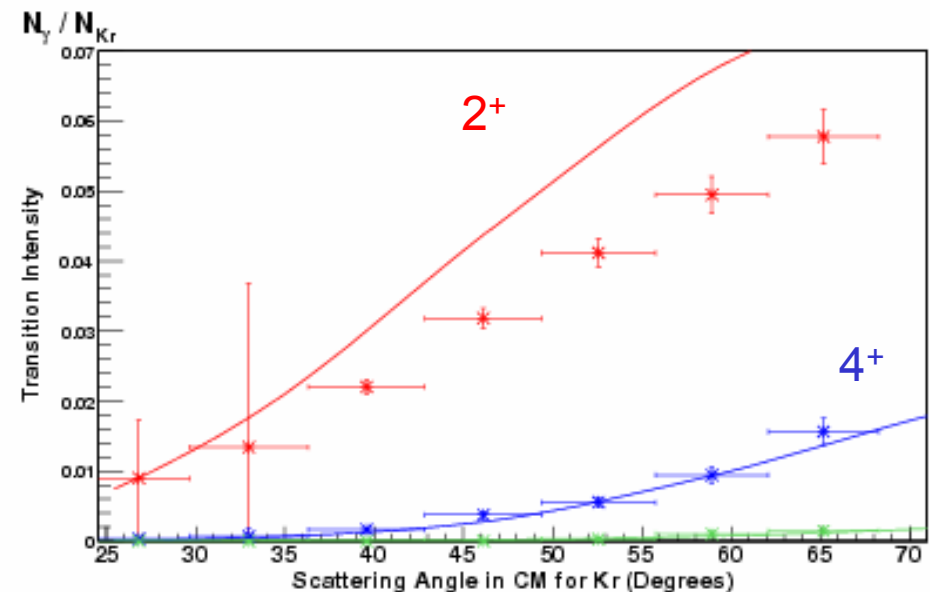
- **Lifetime** are the strongest constraints because directly linked to the **transitional matrix elements** (transition probability)



5 lifetime involving populated states were already measured

→ compatible with our measure ?

Published lifetime are **incompatible** with our data

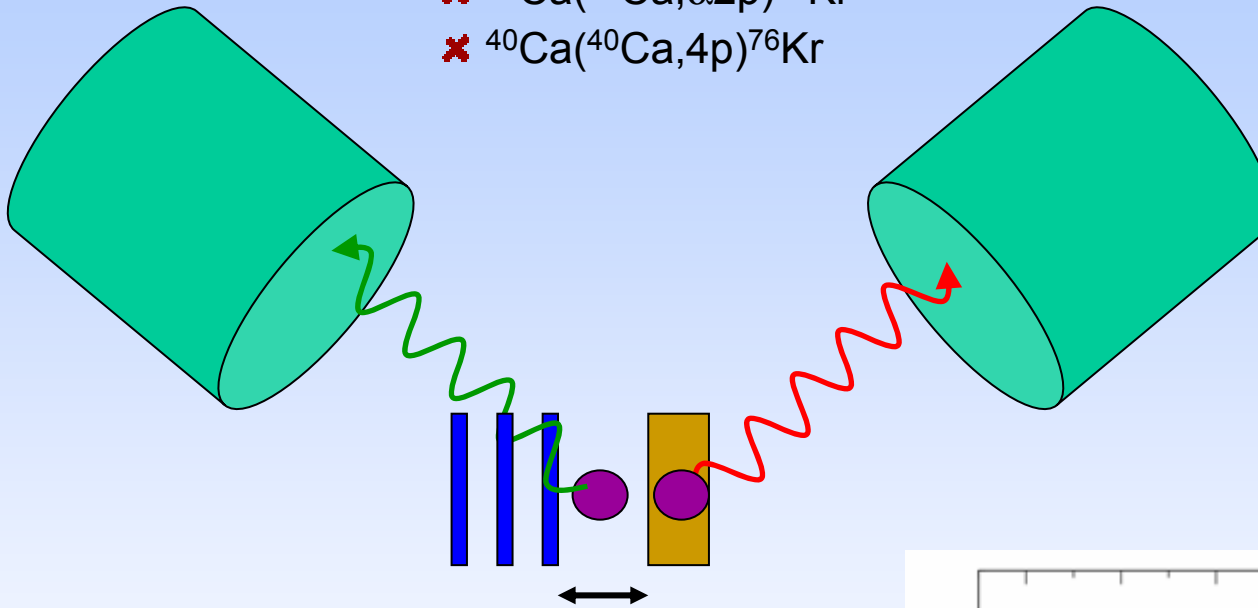
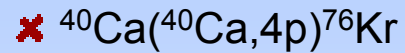




# Pico-second lifetime measurement using RDDS

Recoil Distance Doppler Shift

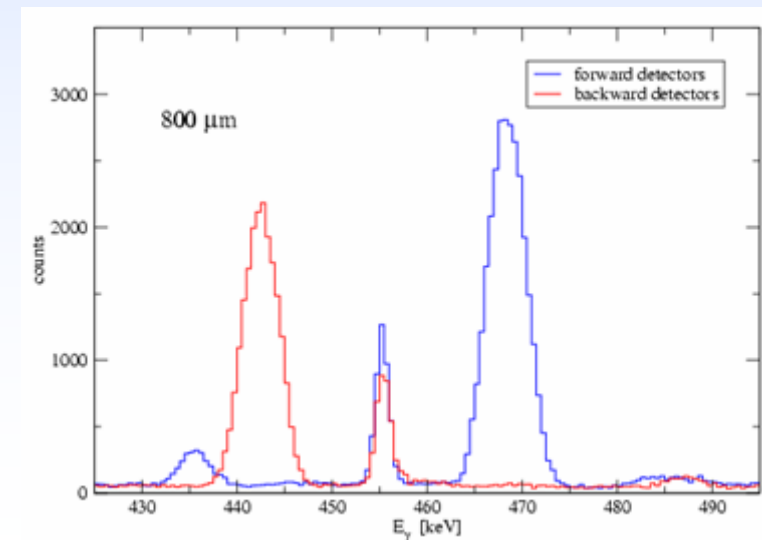
The  $^{74}\text{Kr}$  and  $^{76}\text{Kr}$  nuclei are populated at high spins by a fusion-evaporation reaction :



Target and stopper separated by a fix distance

$\gamma$  rays of desexcitation emitted :

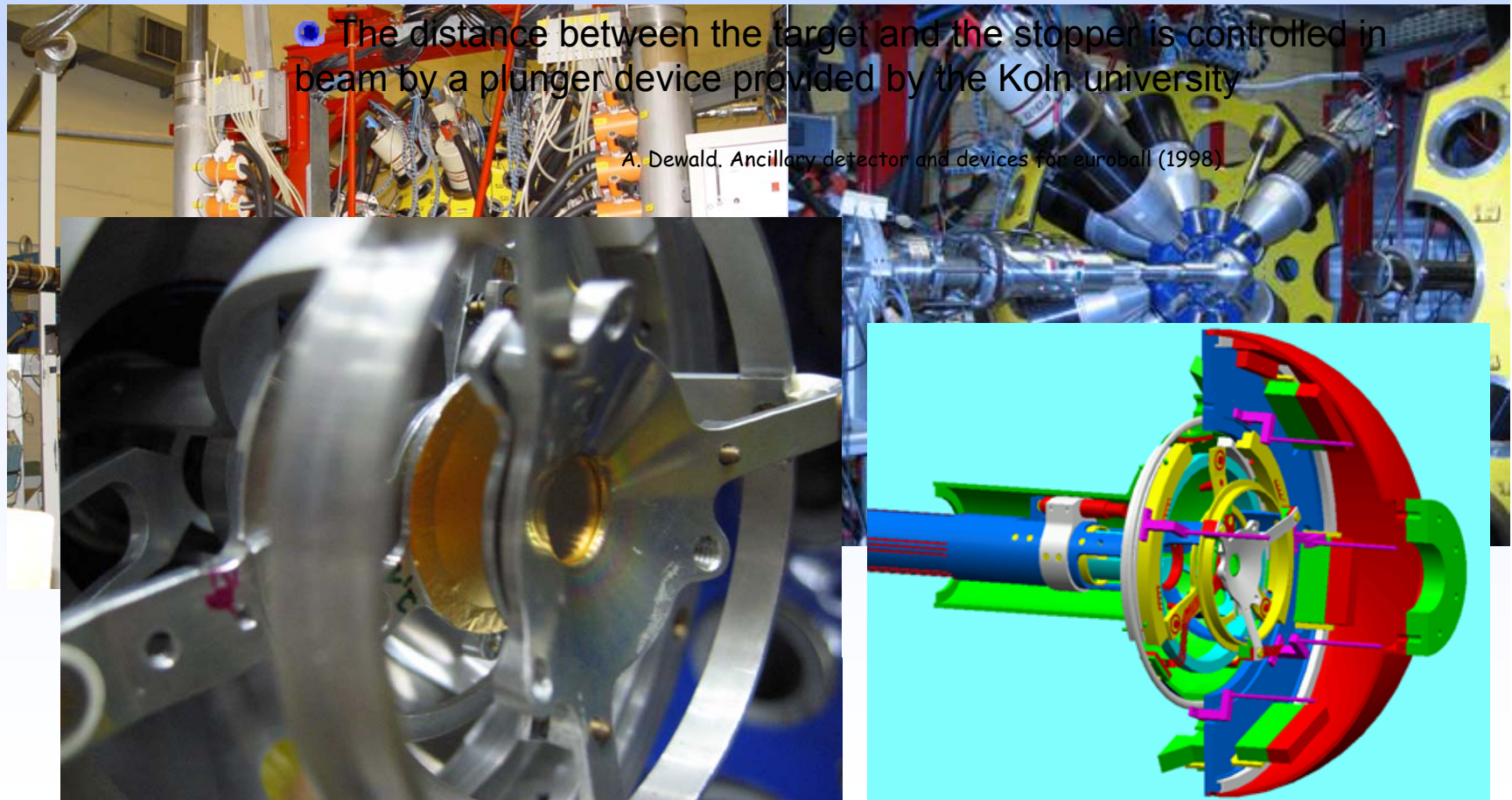
- In flight  $\Rightarrow$  shifted by the Doppler effect
- Stopped  $\Rightarrow$  Energy  $E_0$



# Pico-second lifetime measurement using RDDS

Experiment performed at the **tandem accelerator of Legnaro** in November 2004

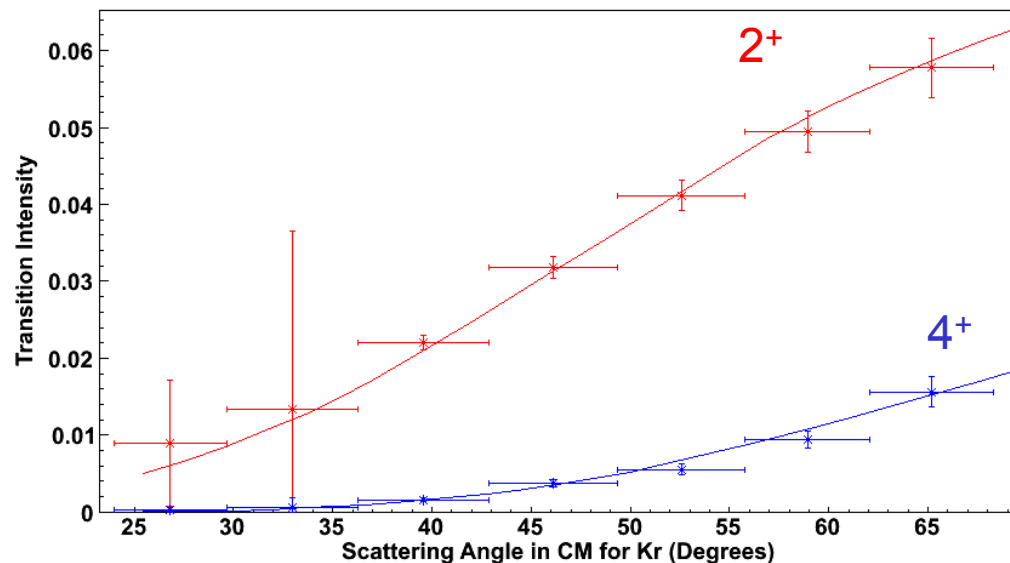
- The  $\gamma$  rays are detected in the GASP spectrometer (32 HPGe germanium detectors)



# Pico-second lifetime measurement using RDDS

	$\tau_{Nucl.Data.}$	$\tau_{Param\grave{e}tre\ libre\ GOSIA}$	$\tau_{Plunger}$
$^{76}Kr$			
$2_1^+$	35.9(10)	38	41.5(8)
$4_1^+$	4.8(4)	4.4	3.67(9)
$6_1^+$	0.86(10)	0.8	0.97(29)
$^{74}Kr$			
$2_1^+$	23.5(2.0)	29.6	33.8(6)
$4_1^+$	13.2(7)	5.9	5.2(2)
$6_1^+$	1.08(14)	1.4	1.09(23)

A. Gorgen, E. Clement *et al.*, EPJA **26** (2005)



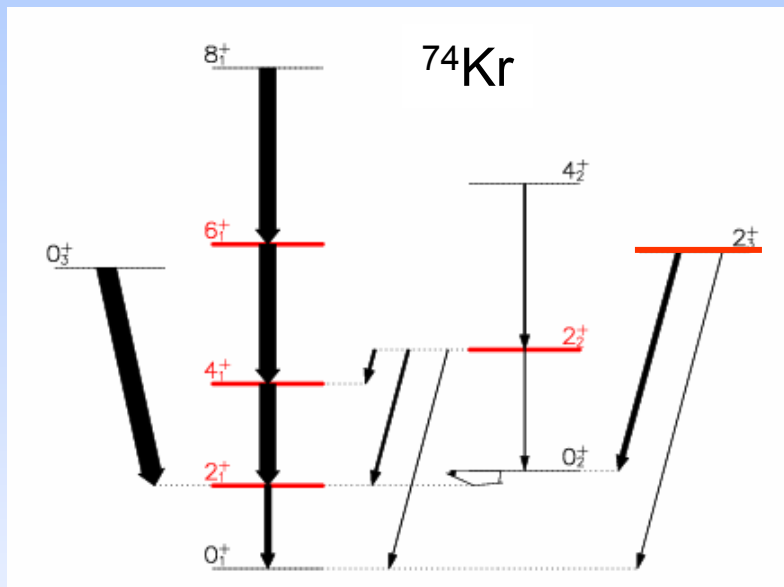
• The measured lifetime **are compatible** with the coulomb excitation data

The high precision provides **strong constraints** on the GOSIA minimization

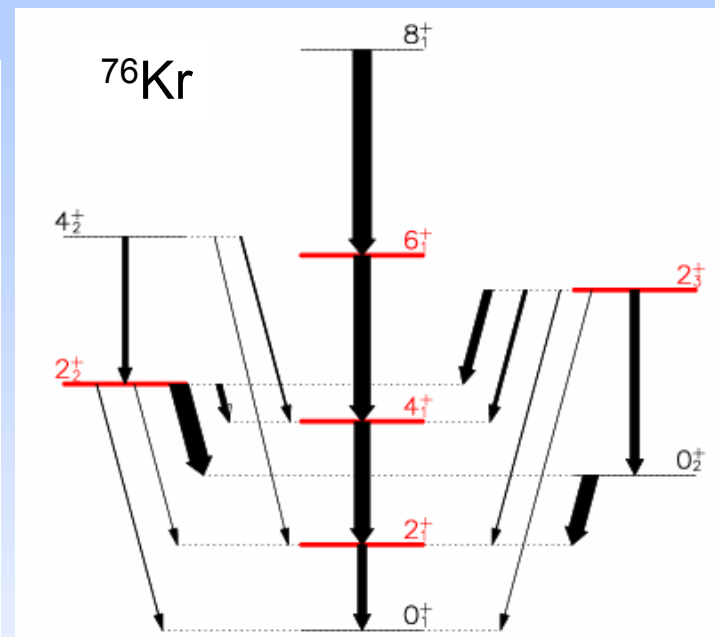
# Plan

- Nucleus, shape, deformation, shape coexistence ??
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# Coulomb excitation analysis with GOSIA



➤ 14 E2 transitional matrix elements



➤ 18 E2 transitional matrix elements

In  $^{74}\text{Kr}$  and  $^{76}\text{Kr}$ , a **prolate** ground state coexists with an **oblate** excited configuration  
 Transition probability : describe the coupling between states

➤ 5 E2 diagonal matrix element **First direct experimental proof of the shape coexistence in light Kr isotopes** ➤ 5 E2 diagonal matrix element

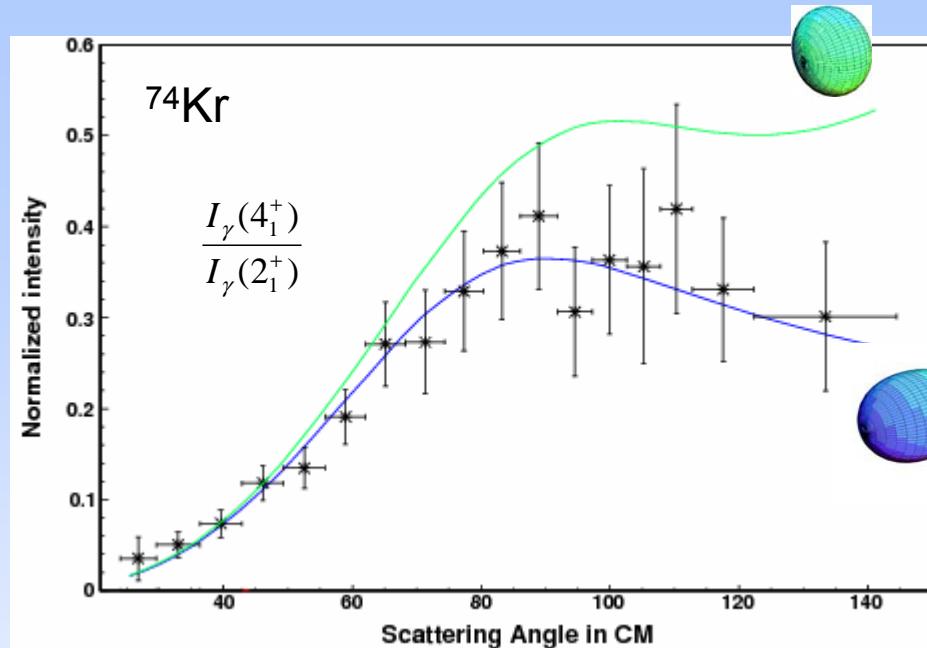
Spectroscopic quadrupole moment : intrinsic properties of the nucleus

E. Bouchez These SPN 2003

E. Clément These SPN 2006

E. Clément et al. Submitted to PRC

# Sensitivity to the static quadrupole moment



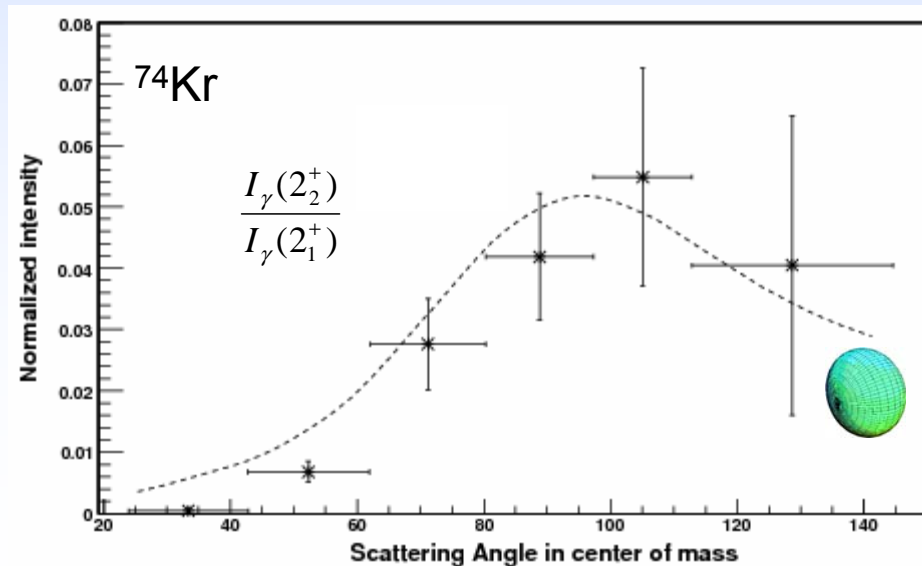
$\chi^2$  minimization:

$$\langle 2_1^+ \| \mathbf{M}(E2) \| 2_1^+ \rangle = -0.70_{-0.30}^{+0.33}$$

$$\langle 4_1^+ \| \mathbf{M}(E2) \| 4_1^+ \rangle = -1.02_{-0.21}^{+0.59}$$

Negative matrix element  
(positive quadrupole moment  $Q_0$ )

$\Rightarrow$  prolate deformation



$$\langle 2_2^+ \| \mathbf{M}(E2) \| 2_2^+ \rangle = +0.33_{-0.23}^{+0.28}$$

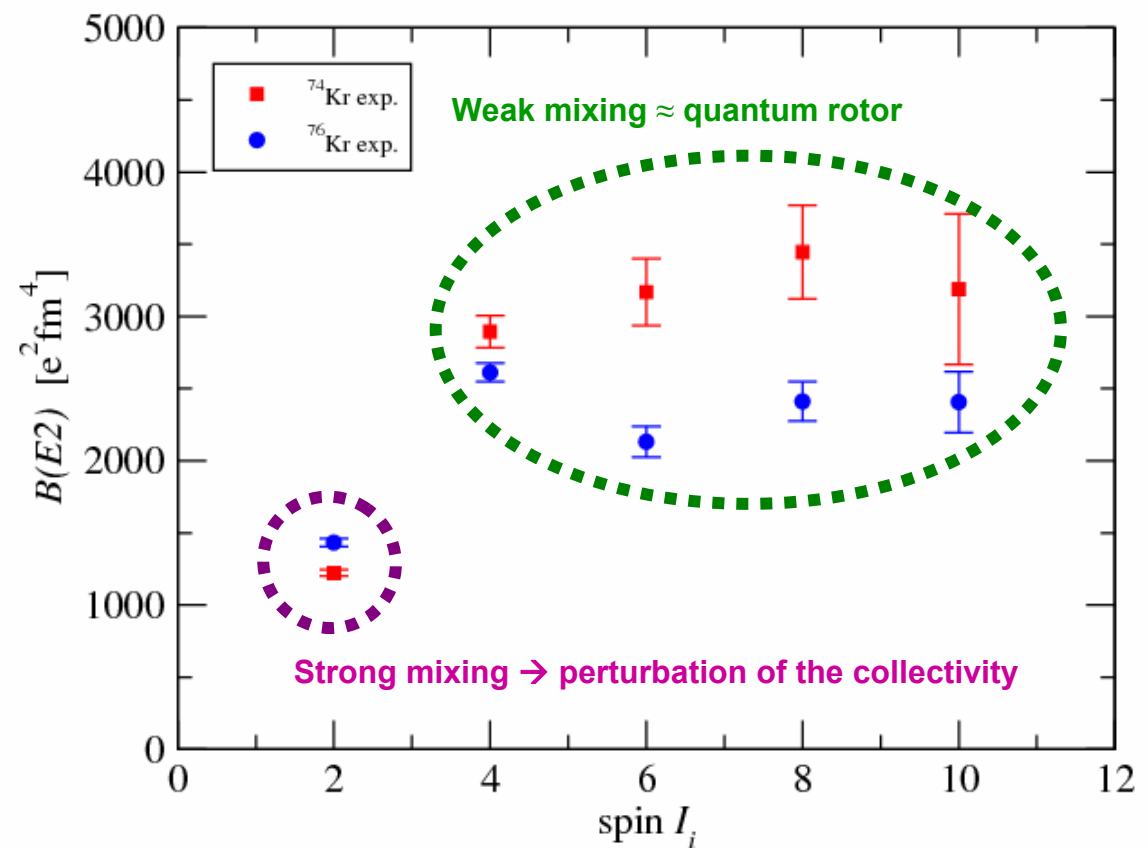
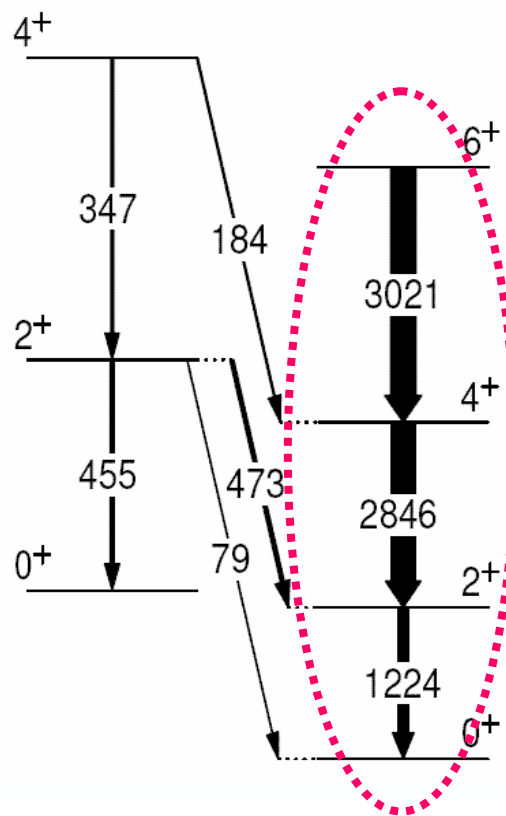
Positive matrix element  
(negative quadrupole moment  $Q_0$ )

$\Rightarrow$  oblate deformation

# Configurations mixing (1)

➔ For the shape-coexisting states, prolate and oblate wave functions are **highly mixed**

$$B(E\lambda, I_i \rightarrow I_f) = \frac{|\langle I_f || M(E\lambda) || I_i \rangle|^2}{2I_i + 1} \quad \text{CONSTANT}$$



# Configurations mixing (2)

Shape coexistence in a **two-state mixing model**

$$\begin{aligned} |I_1\rangle &= +\cos\theta_I |I_{pr}\rangle + \sin\theta_I |I_{ob}\rangle \\ |I_2\rangle &= -\sin\theta_I |I_{pr}\rangle + \cos\theta_I |I_{ob}\rangle \end{aligned}$$

Perturbed states

Pure states

Extract **mixing** and **shape** parameters from set of experimental **matrix elements**.

Ⓢ **Energy perturbation of  $0^+_2$  states**

E. Bouchez *et al.* Phys. Rev. Lett., **90** (2003)

	$^{76}\text{Kr}$	$^{74}\text{Kr}$	$^{72}\text{Kr}$
$\cos^2\theta_0$	0.73(1)	0.48(1)	0.10(1)

Ⓢ **Full set of matrix elements :**

E. Clément, A. Görge, W. Korten *et al.*  
Submitted to PRC

$\cos^2\theta_0$	0.69(4)	0.48(2)
------------------	---------	---------

**Model describes mixing of  $0^+$  states well, but ambiguities remain for higher-lying states. Two-band mixing of prolate and oblate configurations is too simple.**

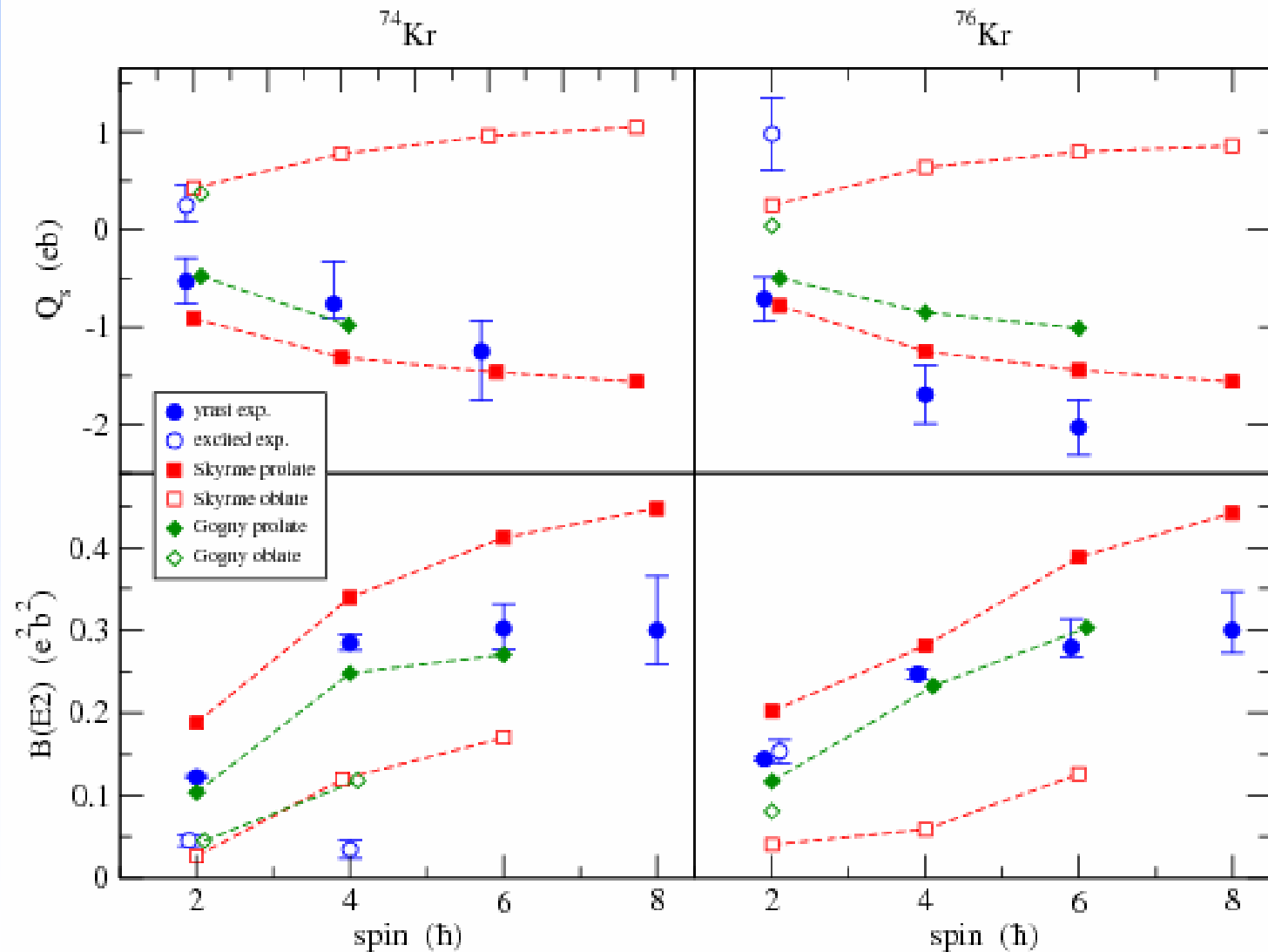


# Shape coexistence in mean-field models (1)

⊗ In-band reduced transition probability and spectroscopic quadrupole moments

GCM-HFB (SLy6) M. Bender,  
P. Bonche et P.H. Heenen,  
Phys. Rev. C 74, 024312 (2006)

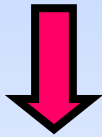
GCM-HFB (Gogny-D1S)  
E. Clément *et al.*,  
submitted to PRC  
J-P. Delaroche *et al.*  
In preparation



# Shape coexistence in mean-field models (2) Skyrme

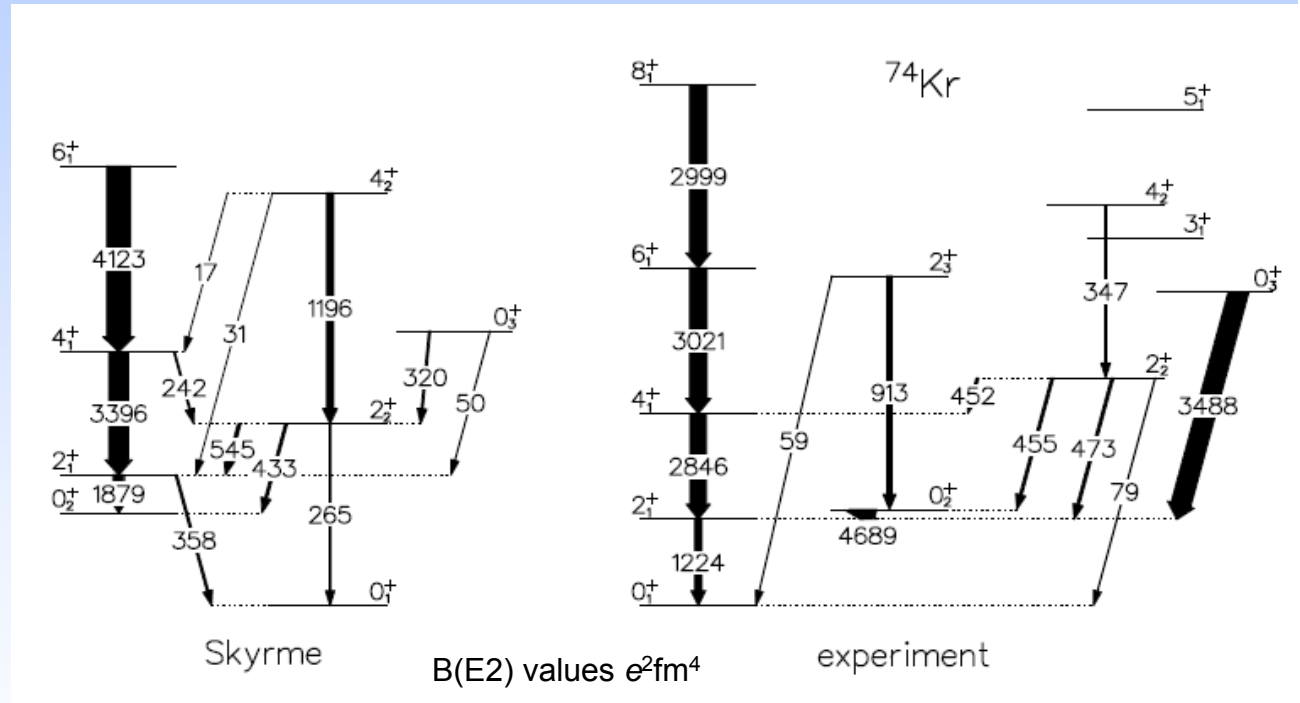
GCM-HFB (SLy6)  
 M. Bender, P. Bonche et P.H. Heenen,  
 Phys. Rev. C 74, 024312 (2006)

HFB+GCM method  
 Skyrme SLy6 force  
 density dependent pairing  
 interaction



Restricted to **axial symmetry** : no K=2 states

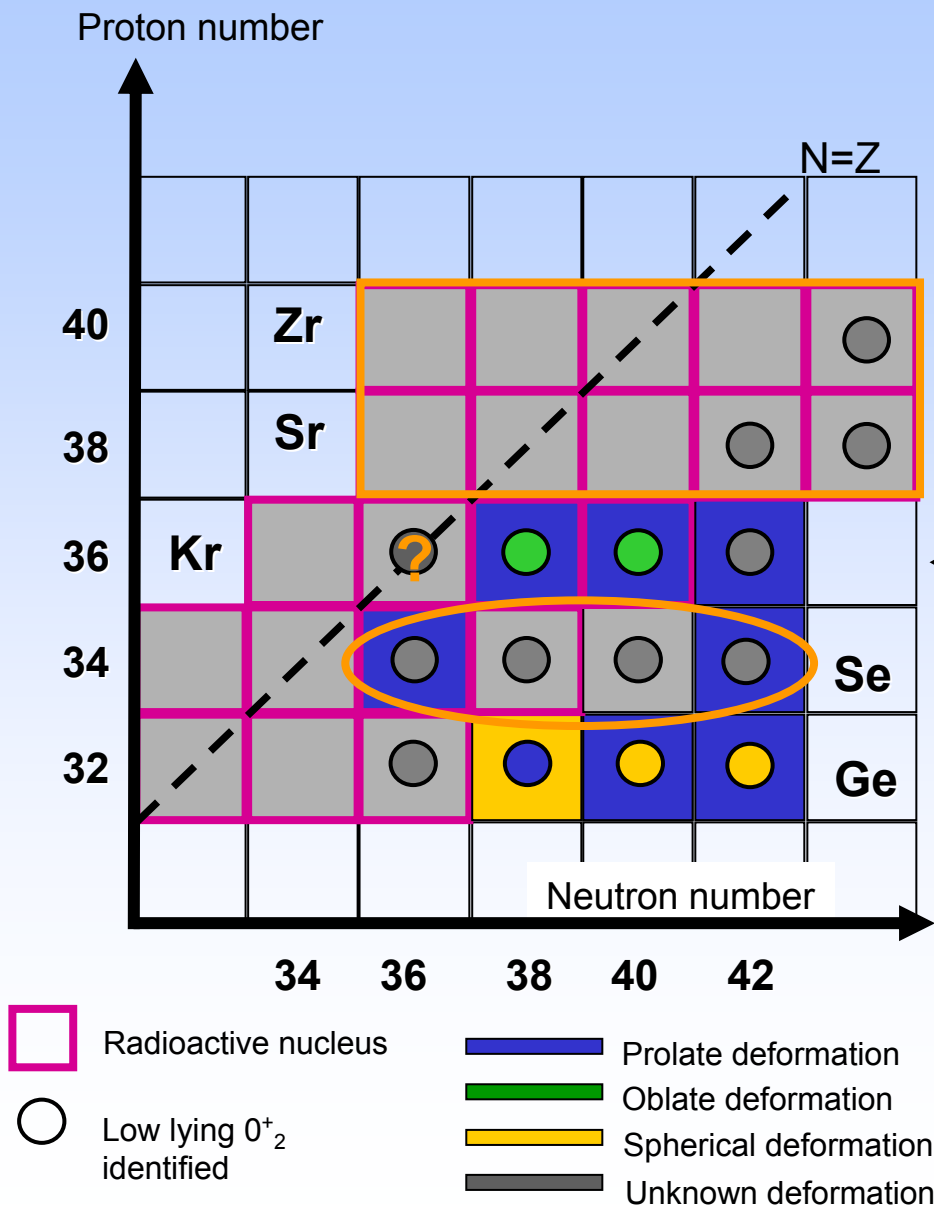
- **Inversion** of oblate and prolate states
- Collectivity of the **prolate rotational band** is correctly reproduced
- **Interband B(E2)** are under estimated



Same conclusion for <sup>76</sup>Kr



# The mass region A=70-80 close to N=Z line



✗ Shape inversion in  $^{70}\text{Kr}$  ground state and oblate  $0^+_2$  with high mixing

• The  $^{70}\text{Se}$  ground state is purely prolate  
✗ Shape coexistence in selenium isotopes? (REX-ISOLDE)

•  $^{74}\text{Ge}$  and  $^{72}\text{Ge}$ : prolate ground state and shape coexistence in  $^{70}\text{Ge}$  and  $^{72}\text{Ge}$   
(sub shell closure at  $Z=40$ ? Spherical shape?)  
 $^{70}\text{Ge} \rightarrow$  Shape Inversion  
 $^{72}\text{Ge} \rightarrow$  maximal mixing

→ The structure evolves rapidly with the proton and neutron number

→ Strong constraint for modern nuclear t



The  $^{72}\text{Kr}$  SPIRAL beam is delivered with a too low intensity (< 100 pps)



The Se, Sr and Zr beam are not available at SPIRAL



Radioactive ions beam of Se and Sr are available at REX-ISOLDE

# Plan

- Nucleus, shape, deformation, shape coexistence ??
- How to measure the shape of the nucleus ?
- Radioactive ions beams
- Coulomb excitation of radioactive Kr beams
- Shape coexistence in light Kr isotopes
- Coulomb excitation of radioactive Se beams
- Shape coexistence at CERN .....

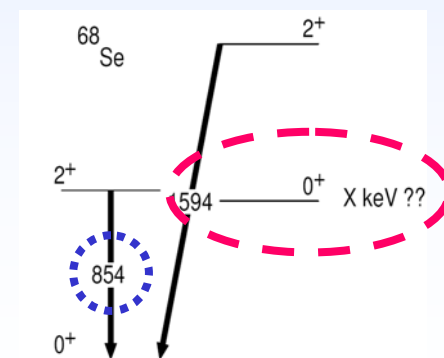
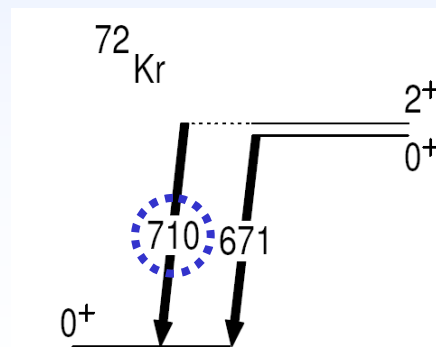
# Coulomb excitation at intermediate energy

For radioactive ions **very far from the stability**, i.e. very low beam intensity **~ 100 pps**, one can take advantage of a **higher beam energy** (20-40 MeV/A) in order to use **thicker target** to increase the interaction probability

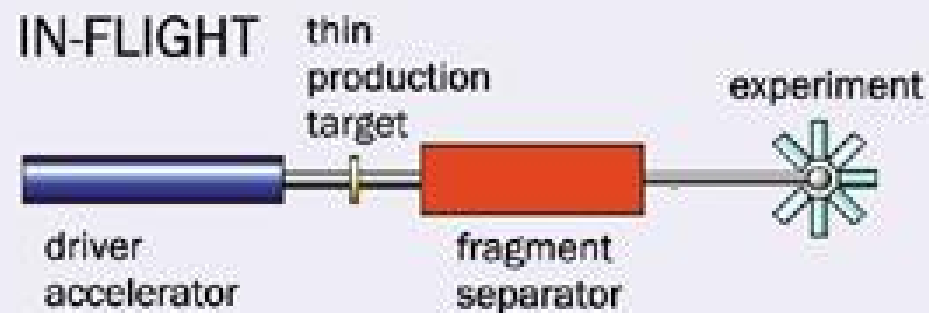
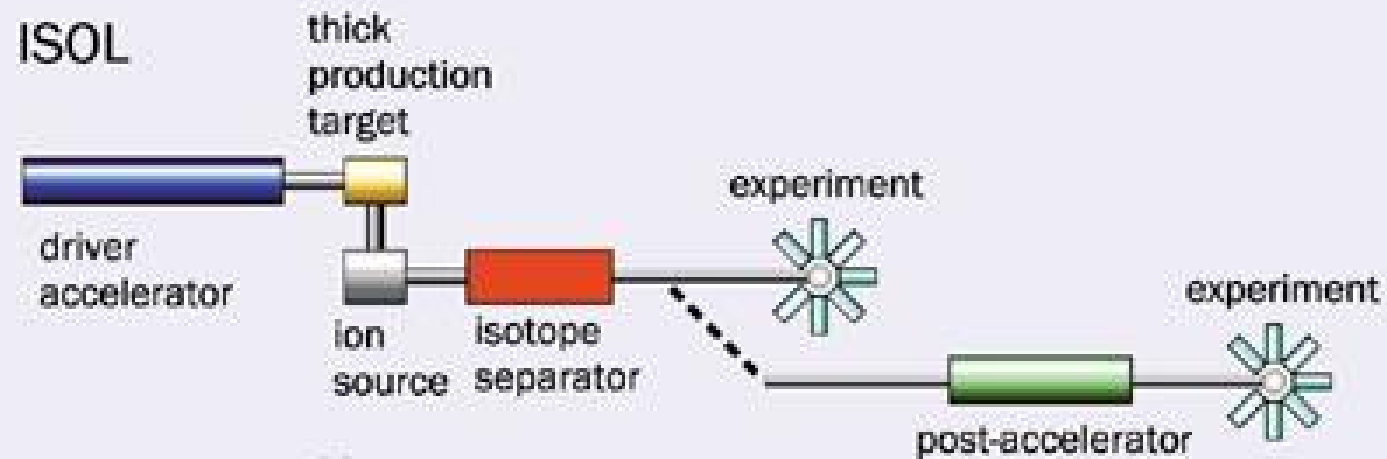
- **One step** excitation ( $0^+ \rightarrow 2^+_i$ )
- **No sensitivity** to the quadrupole moment
- **Low beam quality** (optic, purity, ...)

➡ However it is a first estimation of the nucleus collectivity

- ✓  $^{72}\text{Kr}$  collectivity
- ✓  $^{68}\text{Se}$  collectivity
- ✓ Shape isomer in  $^{68}\text{Se}$

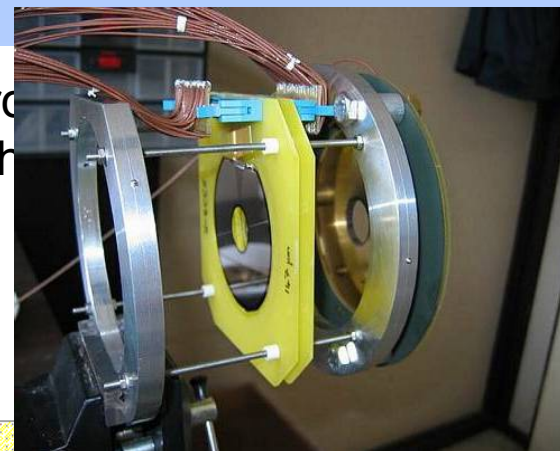
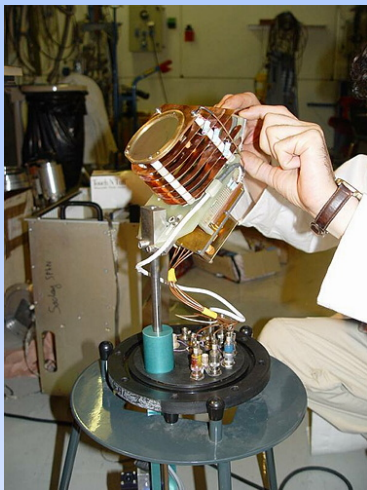


# Radioactive ions beam



20-30  
MeV/A

# Experimental setup



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Second dispersive plane  
Second achromatic focal point

4 Clover Exogam

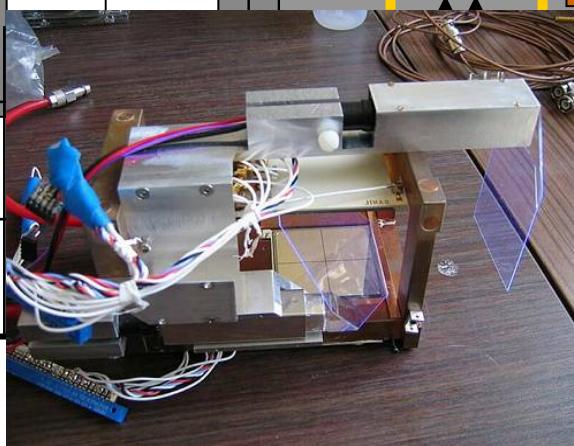
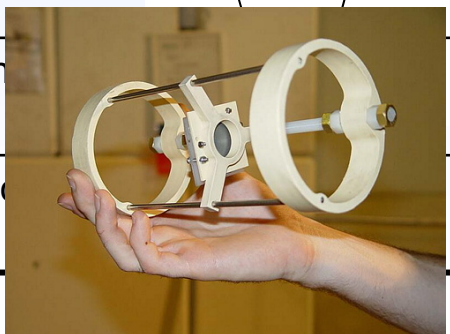
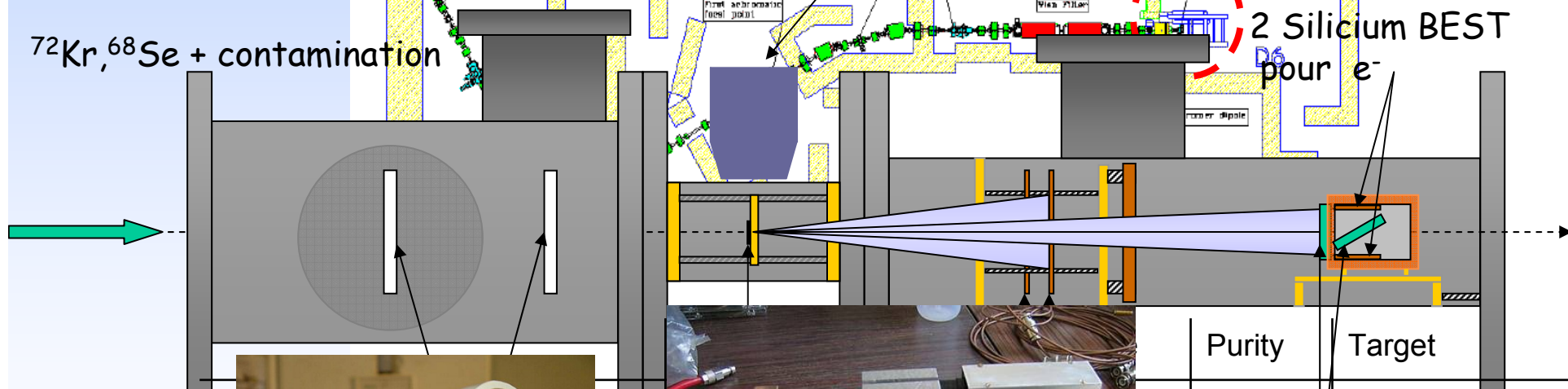
First achromatic focal point

Wien filter

2 Silicium BEST pour  $e^-$

quadrupole

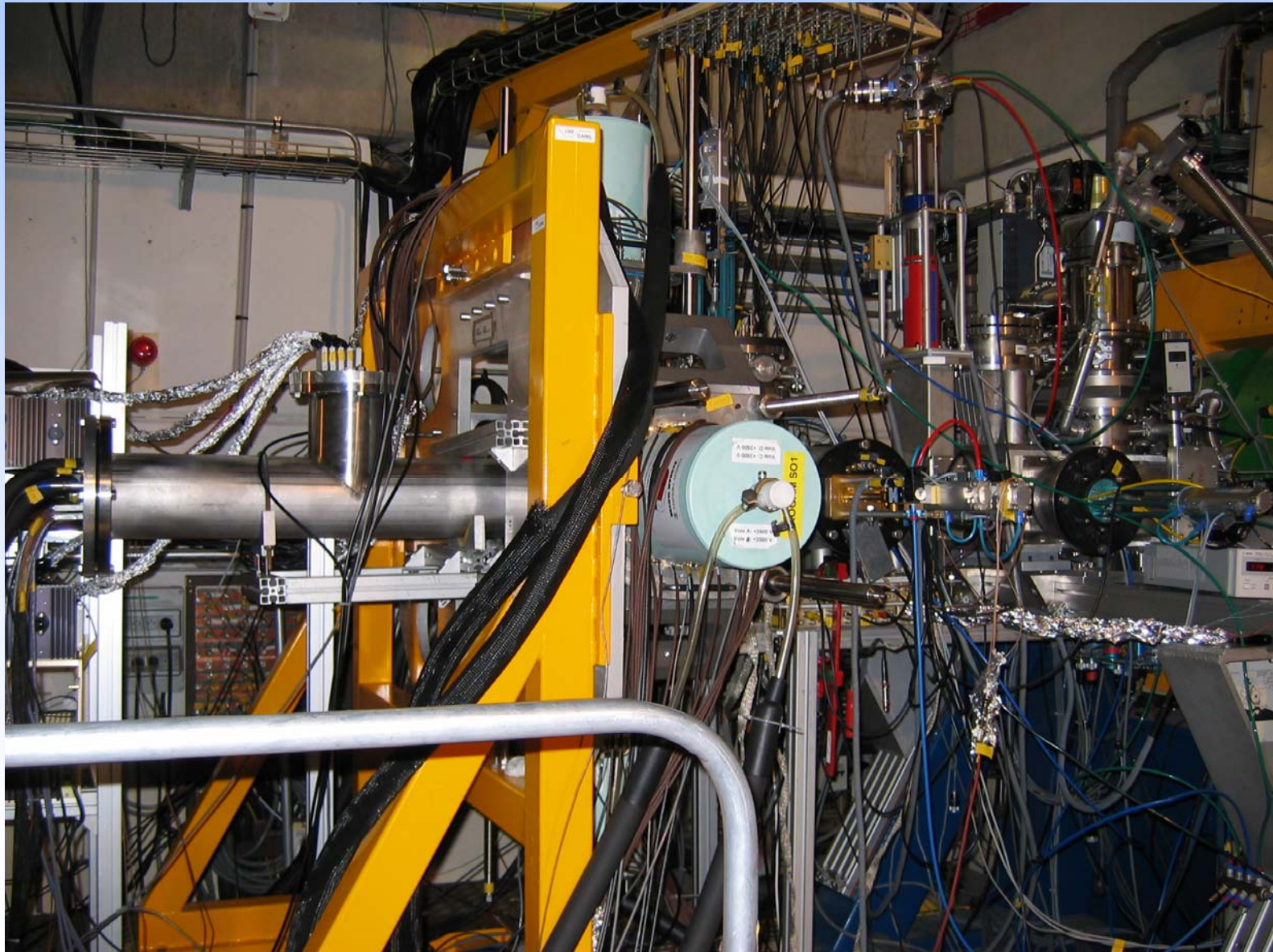
$^{72}\text{Kr}, ^{68}\text{Se}$  + contamination



	Purity	Target
/A	1%	220 $\text{mg}\cdot\text{cm}^{-2}$
	2 100% fillateurs	1 $\text{mg}\cdot\text{cm}^{-2}$
	plastiques de 300 $\mu\text{m}$	

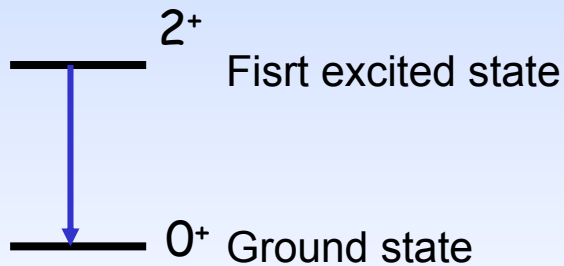


# Experimental setup



# Experimental results

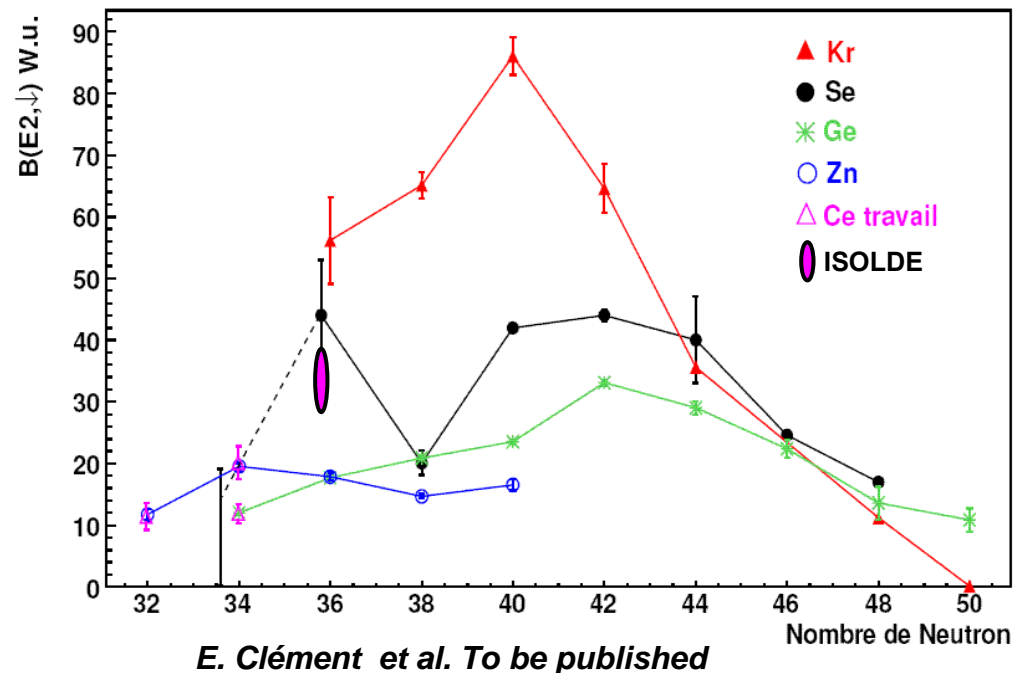
- Coulomb excitation of  $^{78}\text{Kr}$ ,  $^{72}\text{Ge}$  and  $^{64}\text{Zn}$  for **normalization**
- Too low intensity in  $^{72}\text{Kr}$  case ( $< 54$  pps)
- Coulomb excitation of  $^{62}\text{Zn}$ ,  $^{66}\text{Ge}$  and  $^{68}\text{Se}$  radioactive ions



- No **electron** or  $\gamma$  transition corresponding to the decay of an **isomeric  $0^+_{2}$**  observed

⇒ No low lying  $0^+_{2}$  state

Noyau	B(E2) Référence	B(E2) déduit [W.u]
$^{66}\text{Ge}$	12.0 (23)	11.7 (1.5)
$^{62}\text{Zn}$	11.7 (9)	10.2 (2.1)
$^{68}\text{Se}$		$\leq 19$
$^{64}\text{Zn}$	19.5 (6)	21.7 (2.8)



# Plan

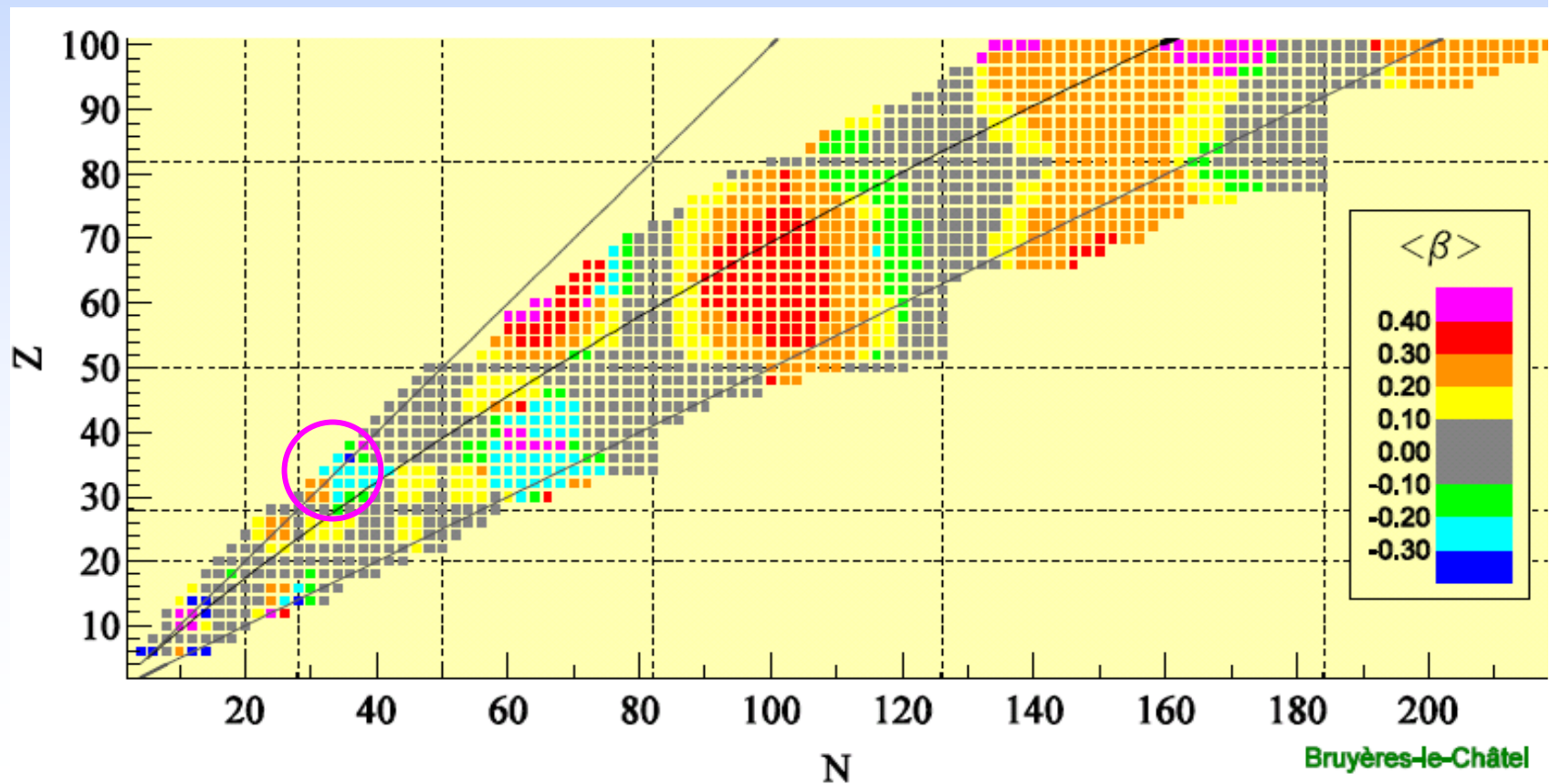
- Nucleus, shape, deformation, shape coexistence ??
- How to measure the shape of the nucleus ?
- Radioactive ions beams
- Coulomb excitation of radioactive Kr beams
- Shape coexistence in light Kr isotopes
- Coulomb excitation of radioactive Se beams
- Shape coexistence at CERN .....

# New area of investigation

All theoretical calculations predict a **sudden onset of quadrupole** deformation at the neutron number  $N=60$

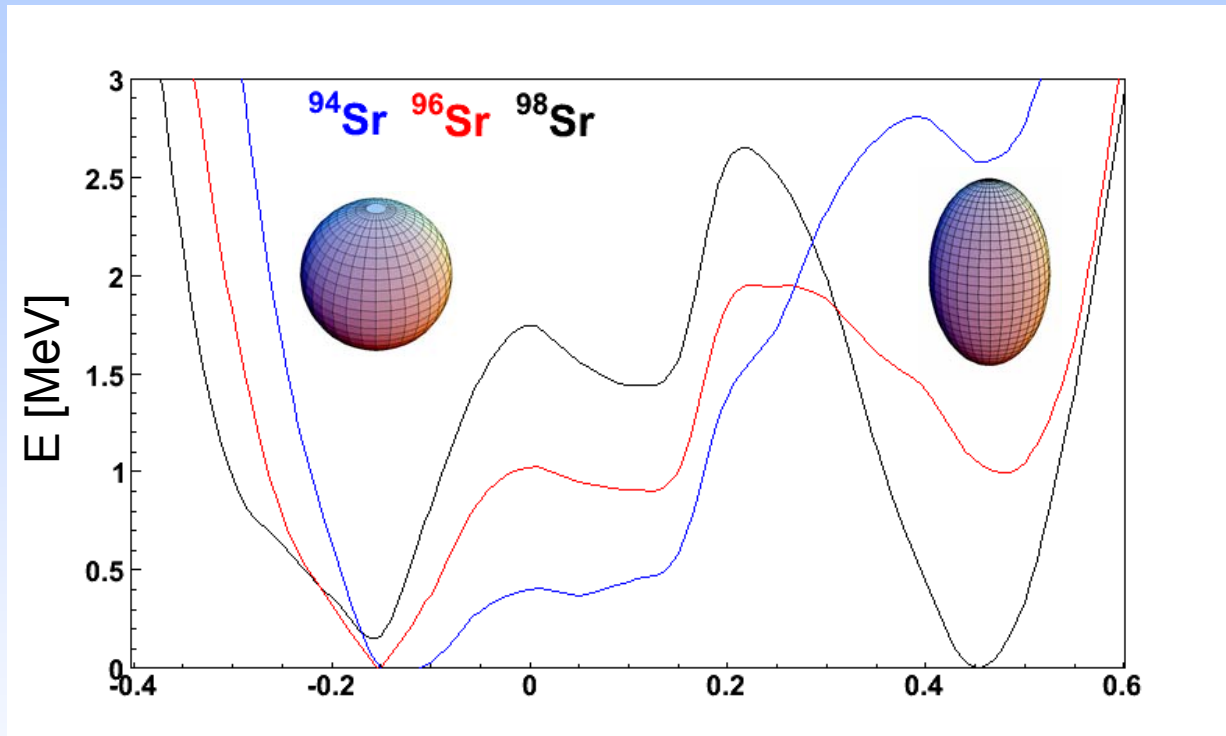
Neutron rich **Sr & Zr isotopes** are accessible by fission of an  $UC_x$  target

Coulomb excitation of such nuclei can be performed at **REX-ISOLDE**



# N-rich Sr and Zr isotopes

Sudden onset of quadrupole deformation at the neutron number N=60



HFB Gogny D1S

M. Girod

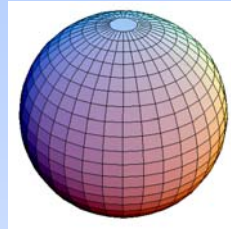
CEA Bruyères-le-Châtel

$^{96}\text{Sr}$  is a transitional nucleus

- Both deformations should coexist at low energy
  - ▶ Shape coexistence between highly deformed and quasi-spherical shapes
- Important constraints for modern nuclear structure theories :
  - ☞ Predicted values of  $\beta_2$
  - ☞  $E(0^+_2)$ ,  $\rho^2(E0)$ ,  $B(E2)$ ,  $Q_0$  ...
  - ☞ Mixing of wave function  $\rightarrow$  GCM

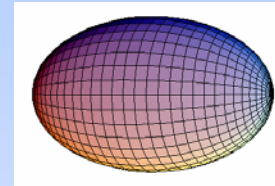
# N-rich Sr and Zr isotopes

The first evidence is the energy of the  $2^+_1$  state

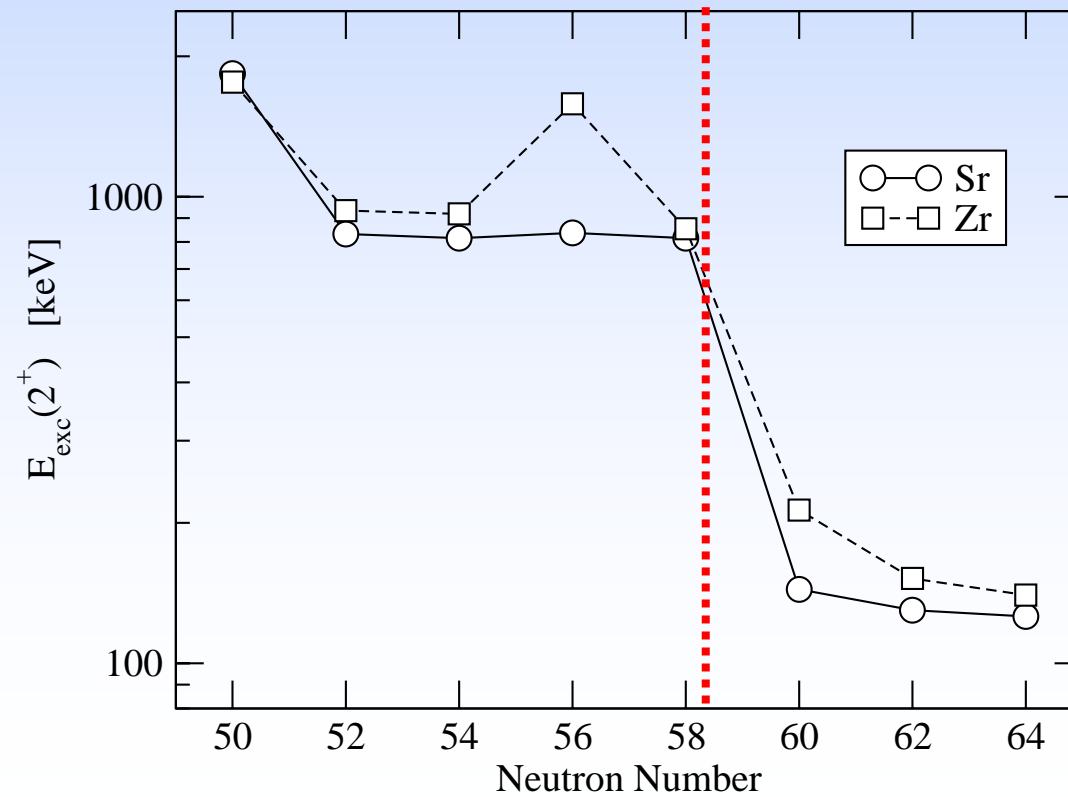


$|\beta| \ll 1$  : Quasi-spherical

N=58



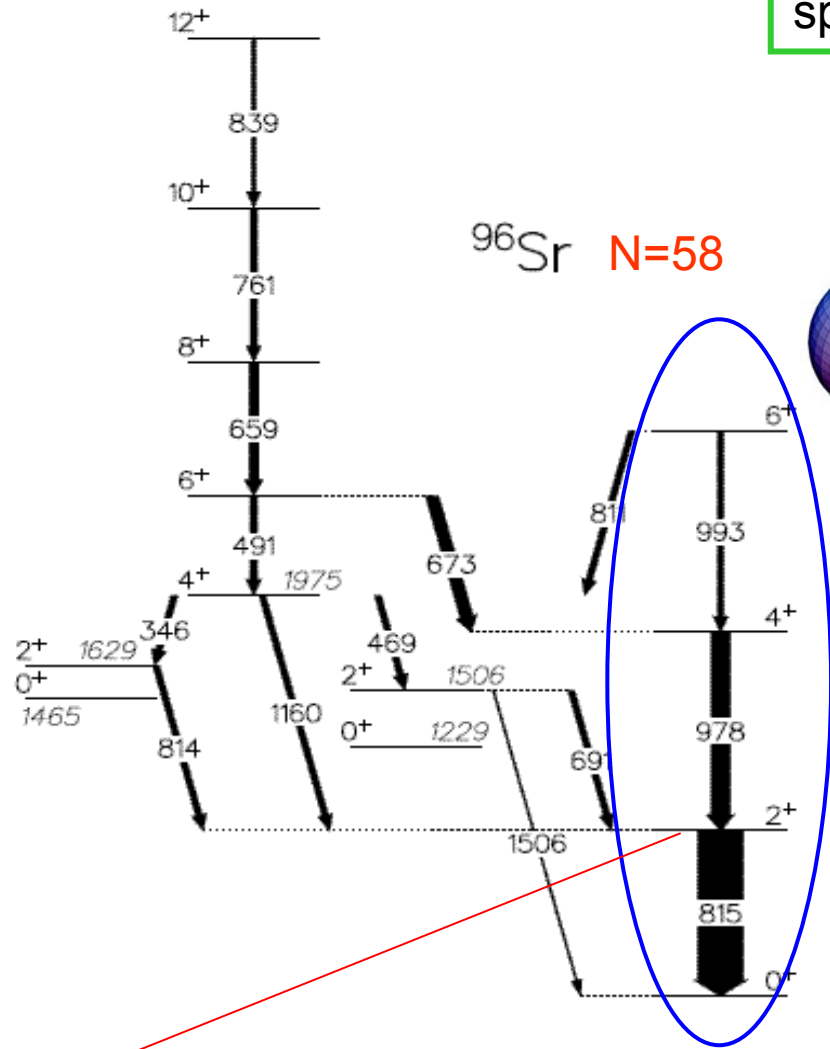
$|\beta| > 0$  : deformed state



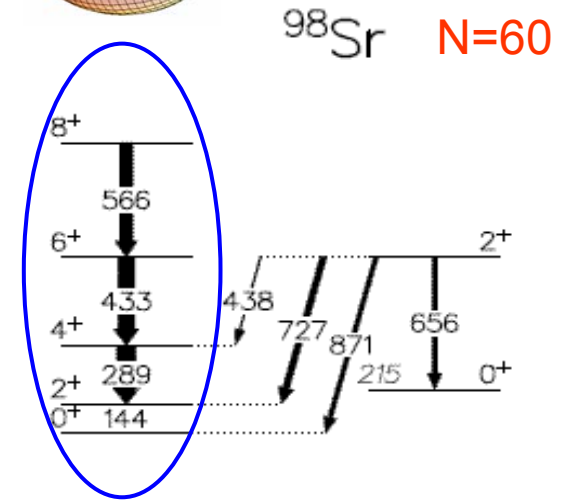
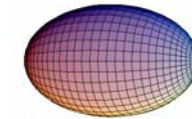
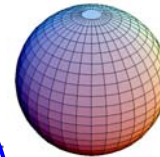
# N-rich Sr isotopes

Level scheme established by spectroscopic experiments

● Ground state band

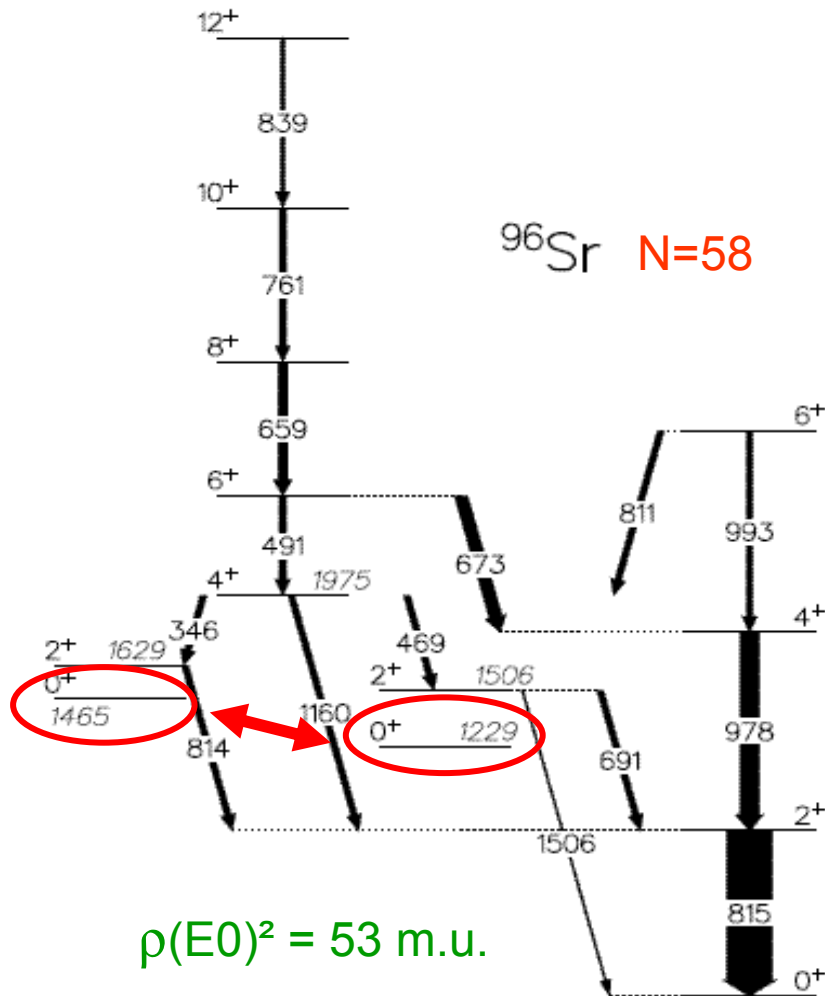


$\tau = 7(4)$  ps  $\rightarrow$  Nearly spherical ground state

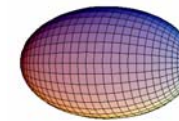
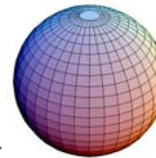


Highly deformed rotational band  $\beta \approx 0.4$

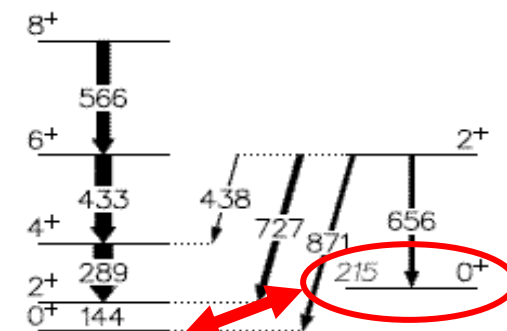
# N-rich Sr isotopes



Excited configuration



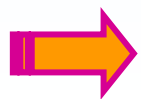
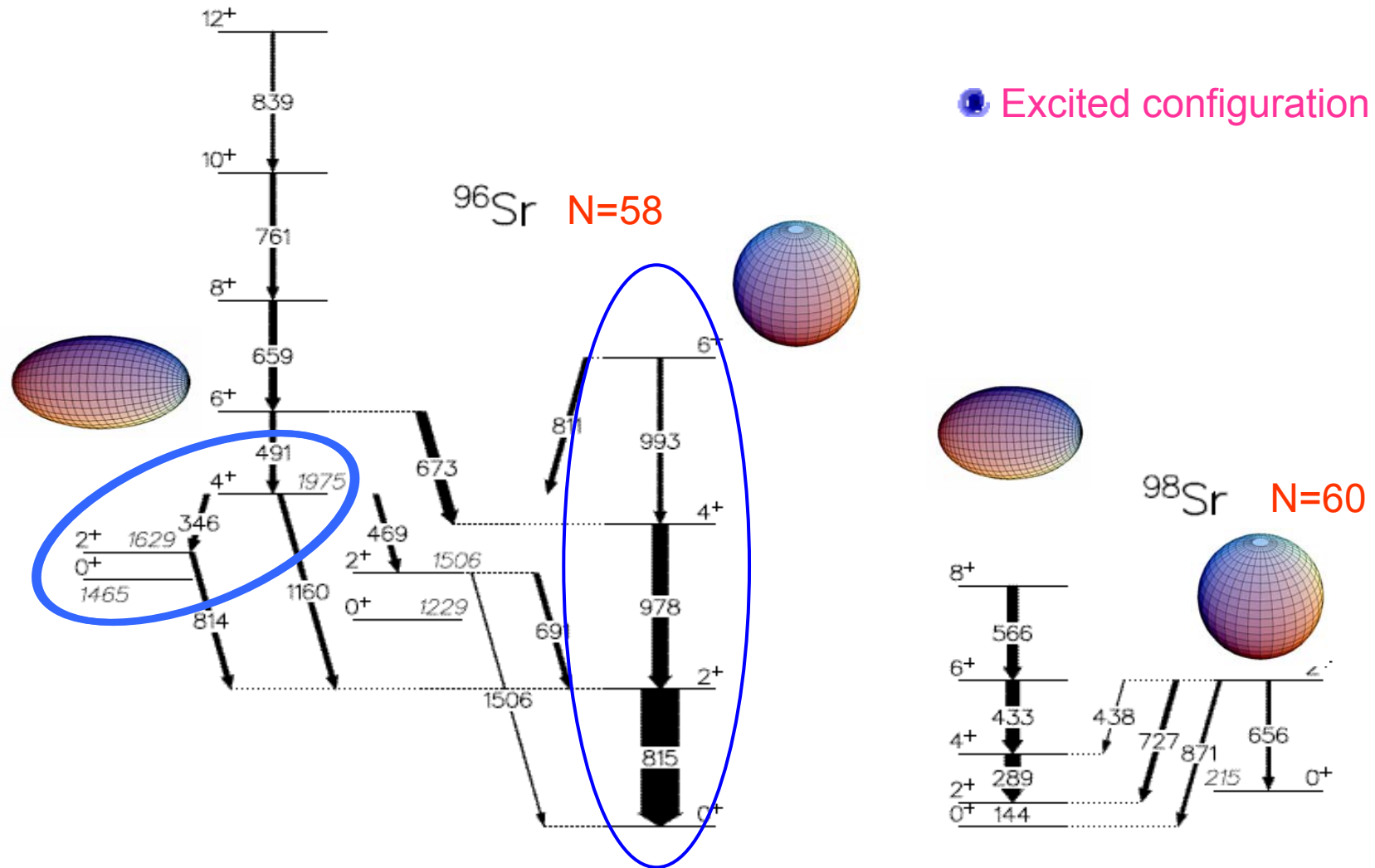
$^{98}\text{Sr}$   $N=60$



$\rho(E0)^2$  is directly linked to deformation and mixing configuration

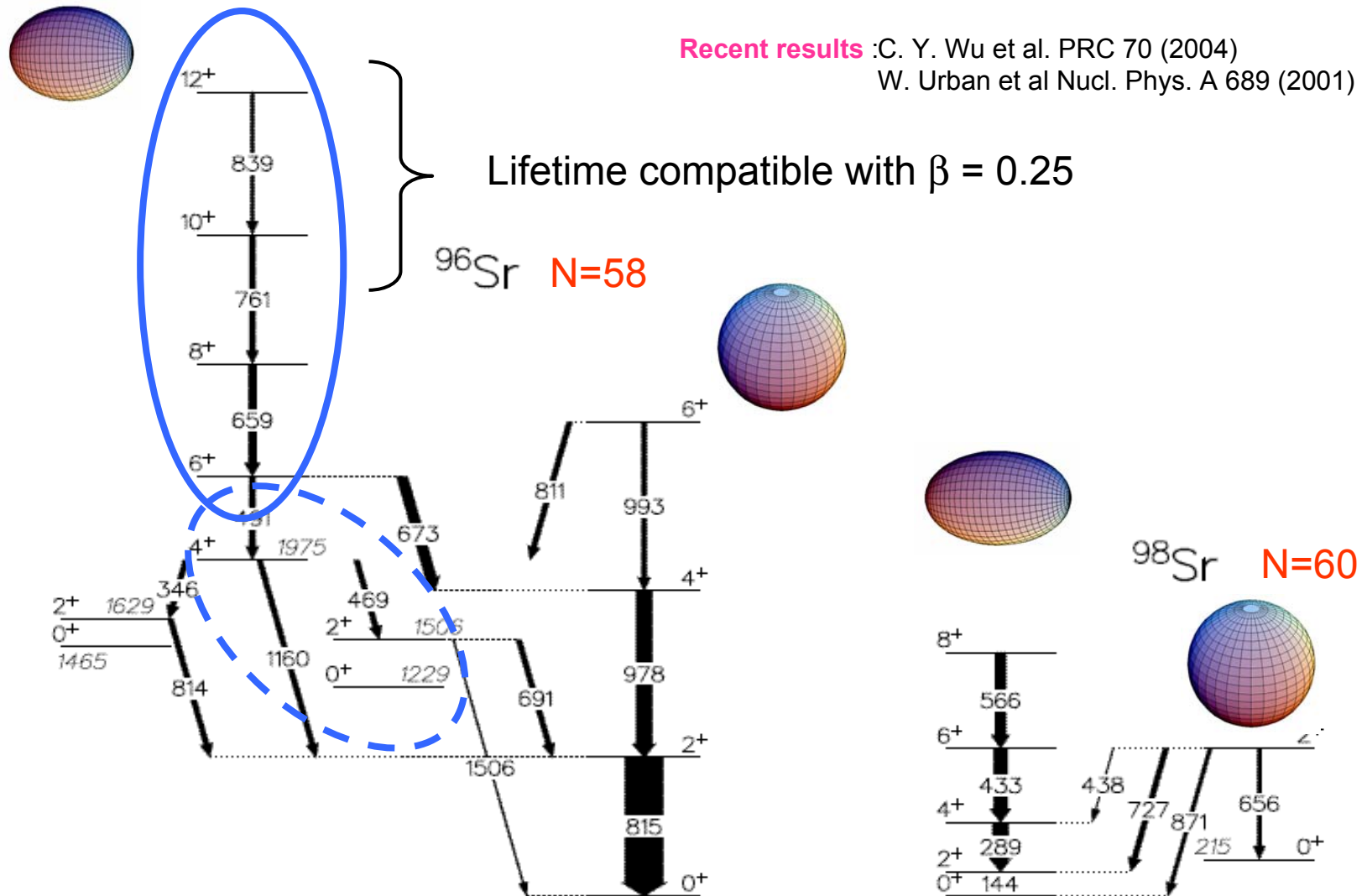


# N-rich Sr isotopes



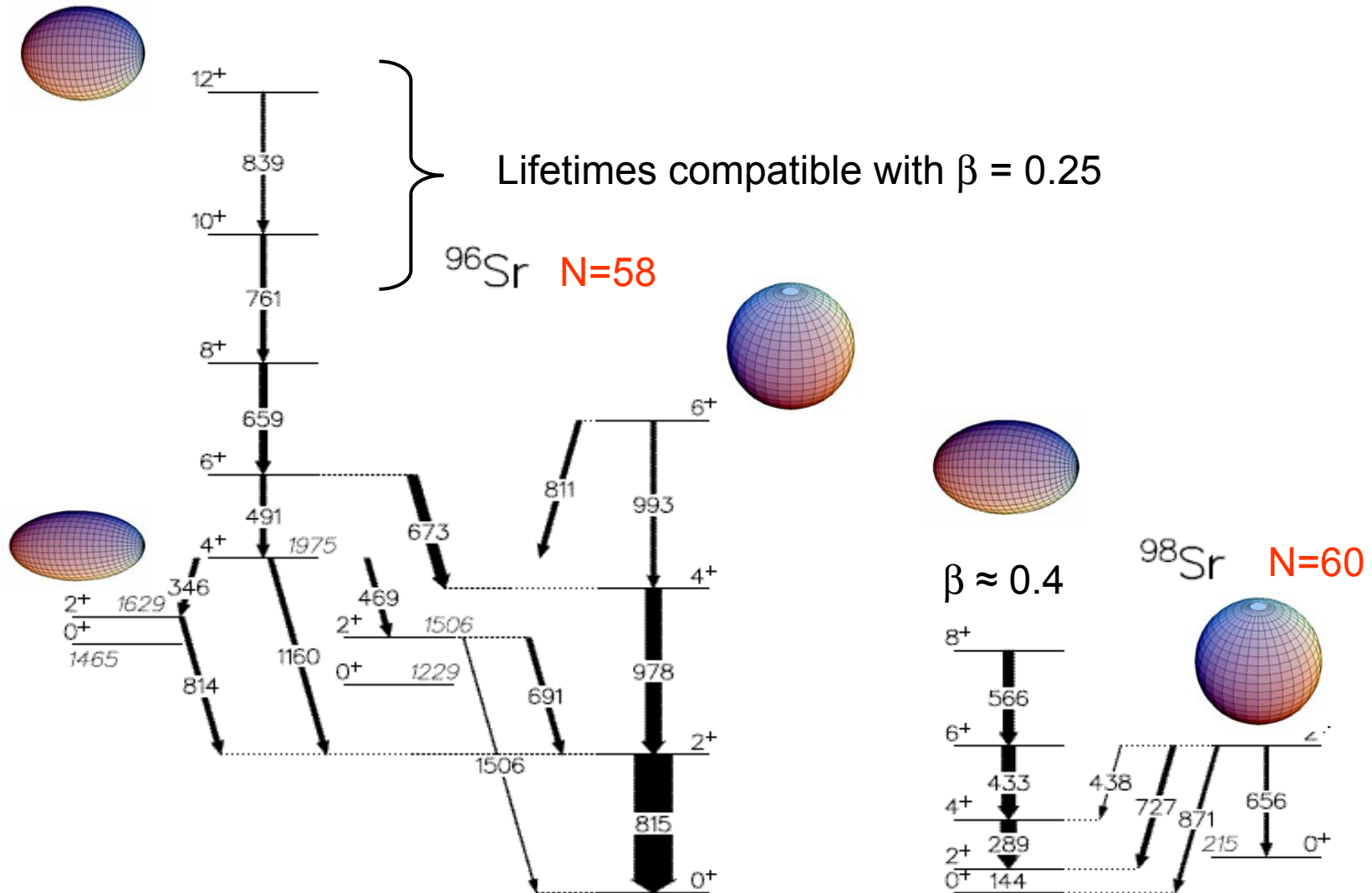
The highly deformed band  $0^+_3 \rightarrow 2^+_3 \rightarrow 4^+_2$  becomes the ground state band in  $^{98}\text{Sr}$

# N-rich Sr isotopes



➡ The onset of deformation around N=58 is **maybe more gradual**

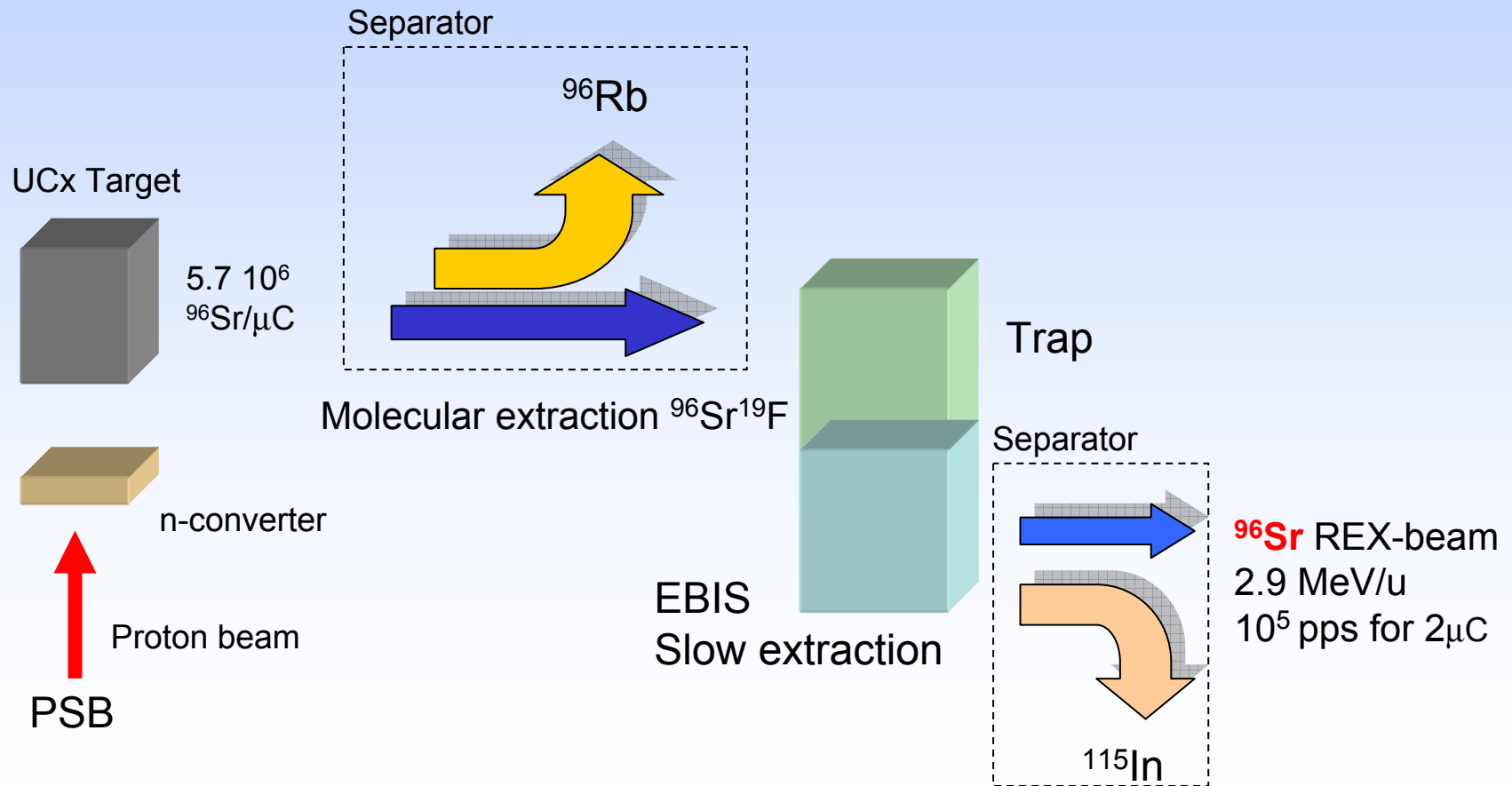
# N-rich Sr isotopes



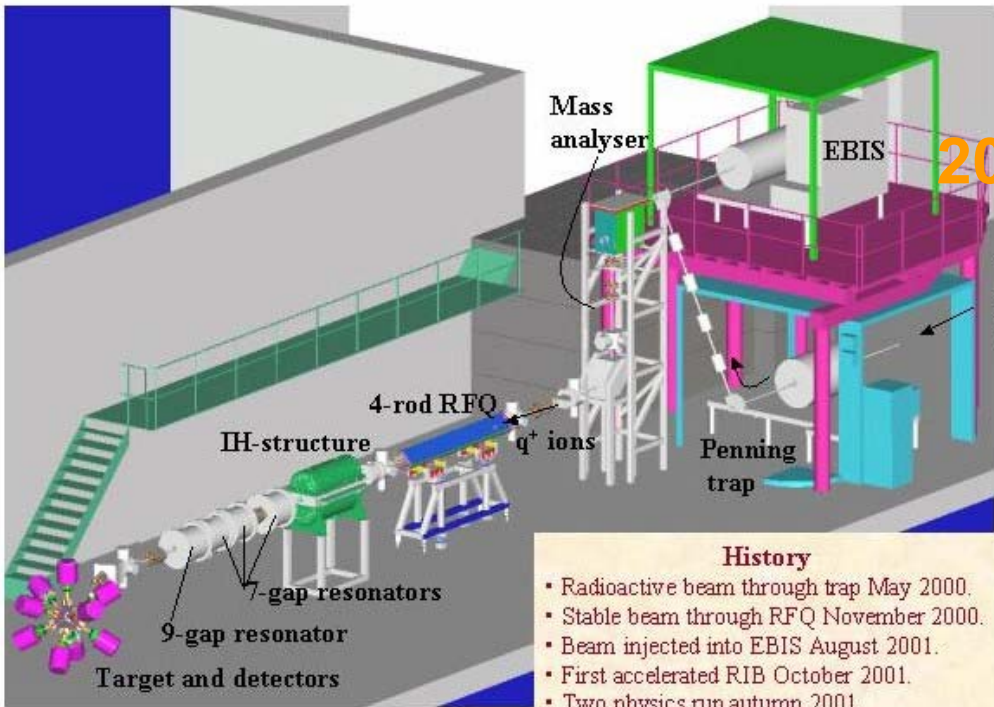
The measure of transition strength and intrinsic quadrupole moments is essential to understand the complex shape coexistence in Sr isotopes → **Coulomb excitation**

# Coulomb excitation of a Sr beam at Rex-ISOLDE

- First Sr beam at REX-ISOLDE → need **new development**
  - ▶ **Molecular beam** has shown the efficiency of this technique in term of purity and intensity...



# Coulomb excitation of a Sr beam at Rex-ISOLDE



**2007 summer campaign**

**1<sup>+</sup> ions from ISOLDE**

**PSB beam**

**Mass analyser**

**EBIS**

**Penning trap**

**4-rod RFQ**

**q<sup>+</sup> ions**

**IIH-structure**

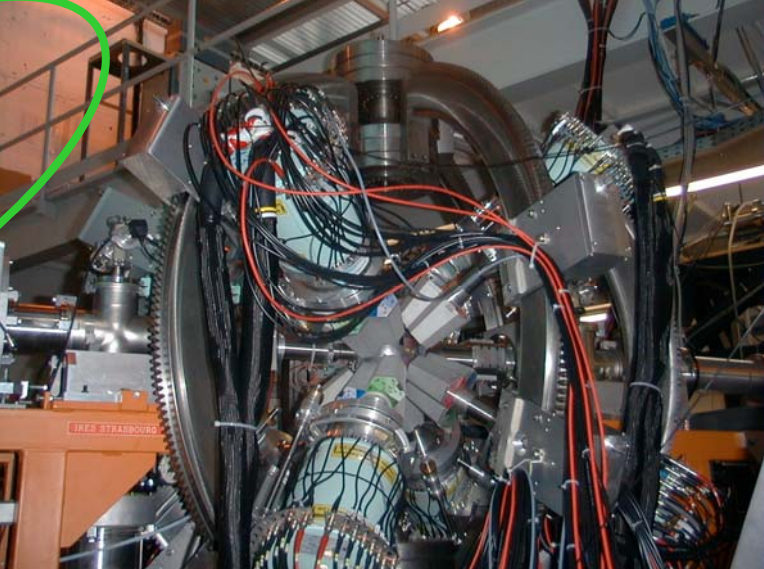
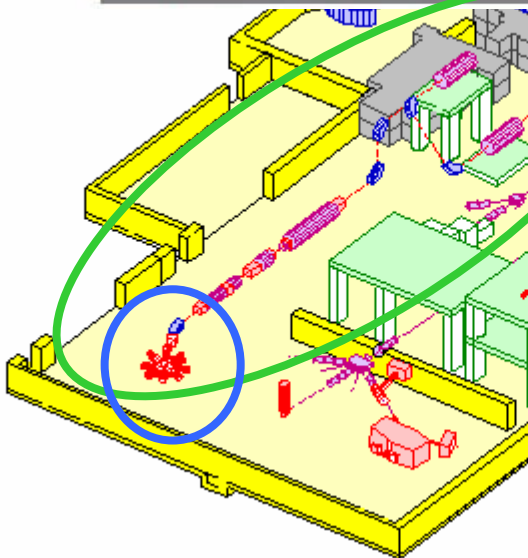
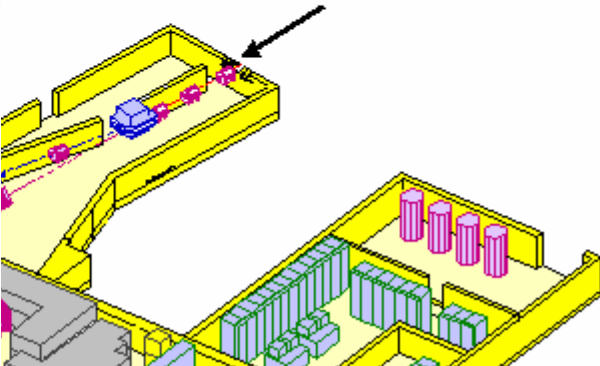
**7-gap resonator**

**9-gap resonator**

**Target and detectors**

**History**

- Radioactive beam through trap May 2000.
- Stable beam through RFQ November 2000.
- Beam injected into EBIS August 2001.
- First accelerated RIB October 2001.
- Two physics run autumn 2001.



# Conclusion

## • Coulomb excitation of radioactive $^{74}\text{Kr}$ and $^{76}\text{Kr}$ ions beams

- Extraction of the diagonal matrix element, 1<sup>ère</sup> measure of the **sign of quadupole moment in radioactive beam**

↳ **prolate** ground state coexists with an **oblate** excited configuration

- Extraction transitional matrix element

↳ In contradiction with published lifetime

• **re-measured by plunger**

↳ Very complex coupling between all configurations .... Triaxiality

## • Coulomb excitation at high energy of $^{68}\text{Se}$

- First estimation of the collectivity

↳  $B(E2 ; 2^+_1 \rightarrow 0^+_1) < 19 \text{ W.u}$  (low collectivity)

- No low-lying  $0^+_2$  state

↳ Shape coexistence ??

## • Coulomb excitation of radioactive $^{96}\text{Sr}$ ions beams at Rex-ISOLDE

Thanks for your attention

E. Clément,<sup>1</sup> A. Görge, <sup>1</sup> W. Korten,<sup>1</sup> E. Bouchez,<sup>1</sup> A. Chatillon,<sup>1</sup> Y. Le Coz,<sup>1</sup> Ch. Theisen,<sup>1</sup> J.N. Wilson,<sup>1</sup>  
M. Zielinska,<sup>5,1</sup> C. Andreik,<sup>2</sup> F. Becker,<sup>3</sup> J.M. Casandjian,<sup>4</sup> W. Catford,<sup>9</sup> T. Czosnyka,<sup>5</sup> G. de France,<sup>4</sup> J.  
Gerl,<sup>3</sup> J. Iwanicki,<sup>5</sup> P. Napiorkowski,<sup>5</sup> G. Sletten,<sup>8</sup> C. Timis<sup>9</sup>

## Collaboration “temps de vie”

A. Görge,<sup>1</sup> E. Clément,<sup>1</sup> A. Chatillon,<sup>1</sup> A. Dewald,<sup>6</sup> W. Korten,<sup>1</sup> Y. Le Coz,<sup>1</sup> N. Marginean,<sup>7</sup> B. Melon,<sup>6</sup>  
R. Menegazzo,<sup>7</sup> O. Möller,<sup>6</sup> Ch. Theisen,<sup>1</sup> D. Tonev,<sup>7</sup> C.A. Ur,<sup>7</sup> K.O. Zell<sup>6</sup>

## Collaboration “E410”

E. Clément,<sup>1</sup> A. Bürger,<sup>1,12</sup> A. Chatillon,<sup>1</sup> A. Görge,<sup>1</sup> W. Korten,<sup>1</sup> Y. Le Coz,<sup>1</sup> Ch. Theisen,<sup>1</sup> M. Zielinska,<sup>5,1</sup>  
B. Blank,<sup>12</sup> S. Fox,<sup>10</sup> G. Georgiev,<sup>7</sup> S. Grevy,<sup>4</sup> D.G. Jenkins,<sup>10</sup> F. Johnston-Theasby,<sup>10</sup> P. Joshi,<sup>10</sup> I. Matea,<sup>12</sup>  
P. Napiorkowski,<sup>5</sup> F. de Oliveira Santos,<sup>4</sup> M.G. Pellegriti,<sup>4</sup> R. Wadsworth<sup>10</sup>

<sup>1</sup>DAPNIA/SPhN, CEA Saclay

<sup>2</sup>Oliver Lodge Laboratory, University of Liverpool

<sup>3</sup>GSI Darmstadt

<sup>4</sup>GANIL

<sup>5</sup>Heavy Ion Laboratory, Warsaw

<sup>6</sup>Institut für Kernphysik, Universität zu Köln

<sup>7</sup>INFN Legnaro

<sup>8</sup>NBI Copenhagen

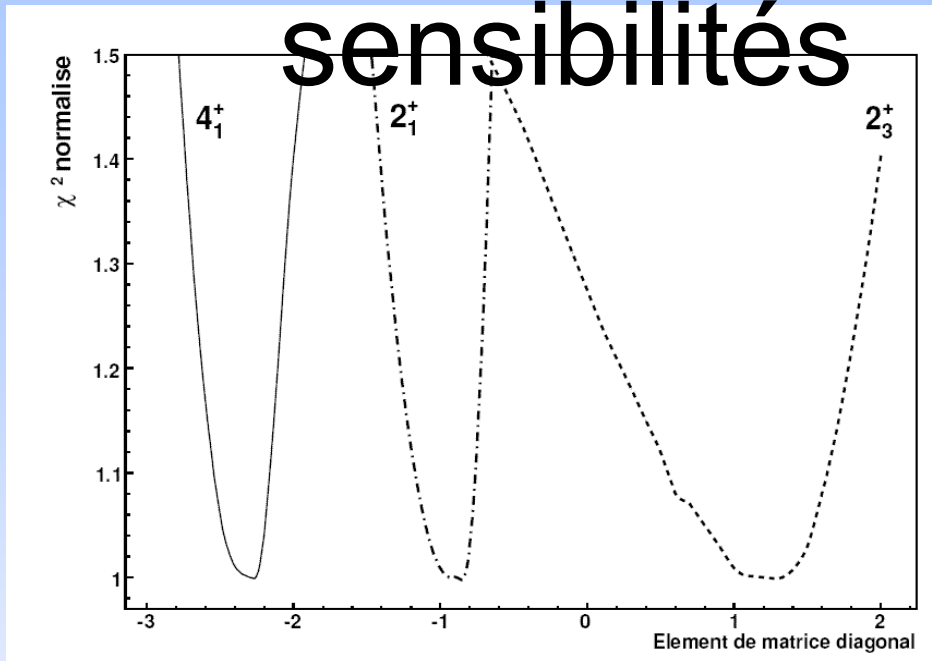
<sup>9</sup>University of Surrey

<sup>10</sup>University of York

<sup>11</sup>Universität zu Bonn



# Comparaison des sensibilités



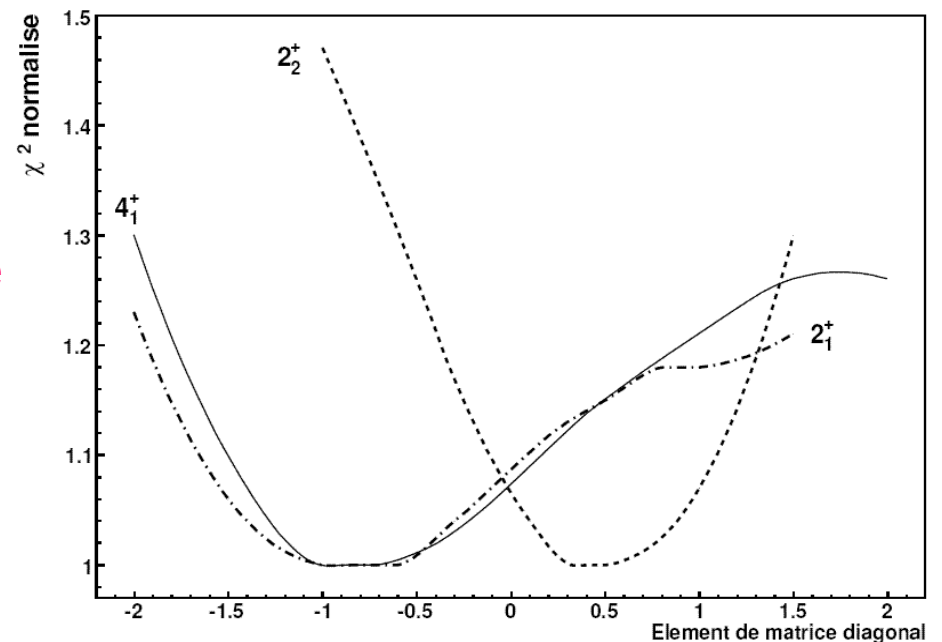
⇔  $^{76}\text{Kr}$

Plus de statistique dans le  $^{76}\text{Kr}$

→ L'augmentation de la sensibilité

→ courbes plus étroites

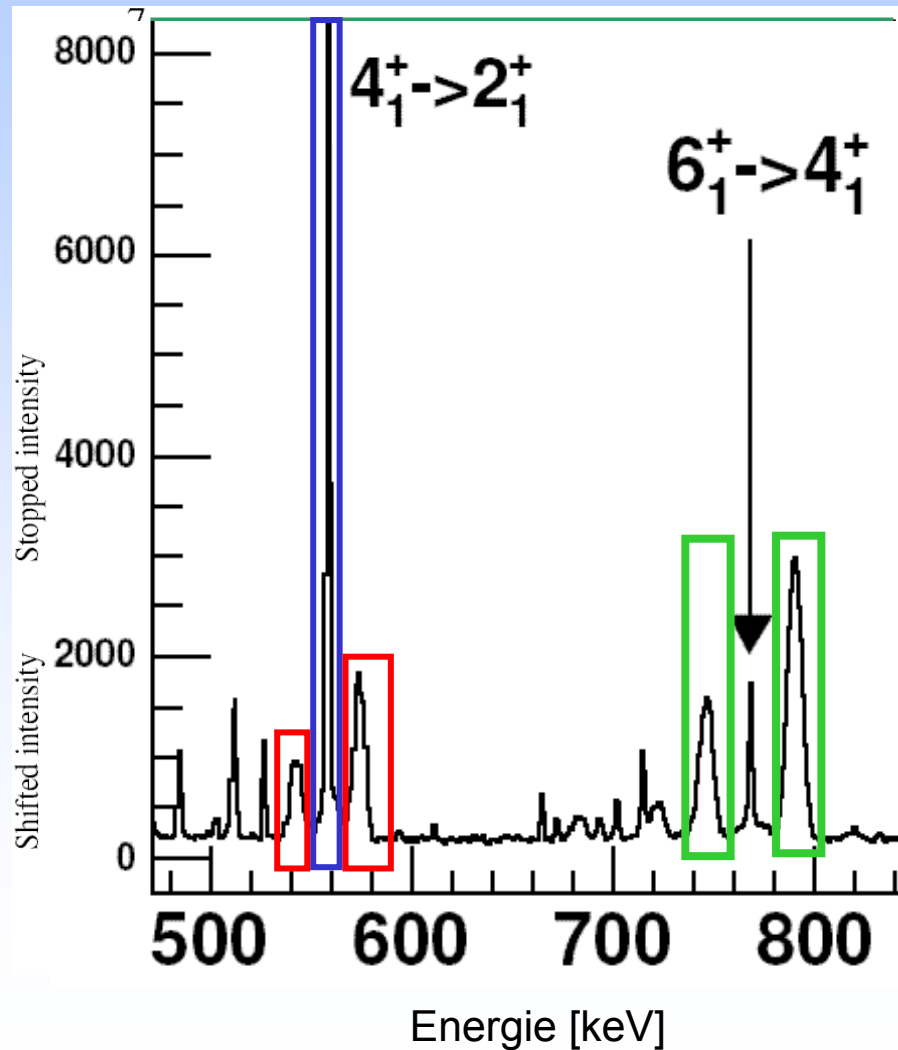
⇔  $^{74}\text{Kr}$



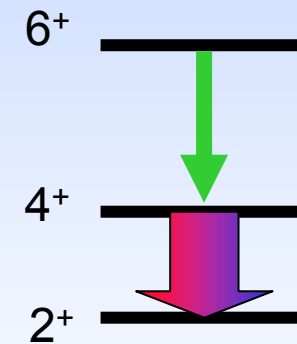
# Mesure de temps de vie



Les contaminations et alimentations parallèles sont supprimées par une analyse en **coïncidences  $\gamma-\gamma$**



Extraction du temps de vie :  
exemple de l'état  $4^+$  du  $^{74}\text{Kr}$



$$\tau(x) = \frac{\frac{1}{N(x)} I(\gamma_1^{sh}, \gamma_2^{st}, x)}{v_{Kr} \frac{d}{dx} \frac{I(\gamma_1^{sh}, \gamma_2^{sh}, x)}{N(x)}}$$

# transition réduite: B(E2)

Au premier ordre de l'excitation Coulombienne :

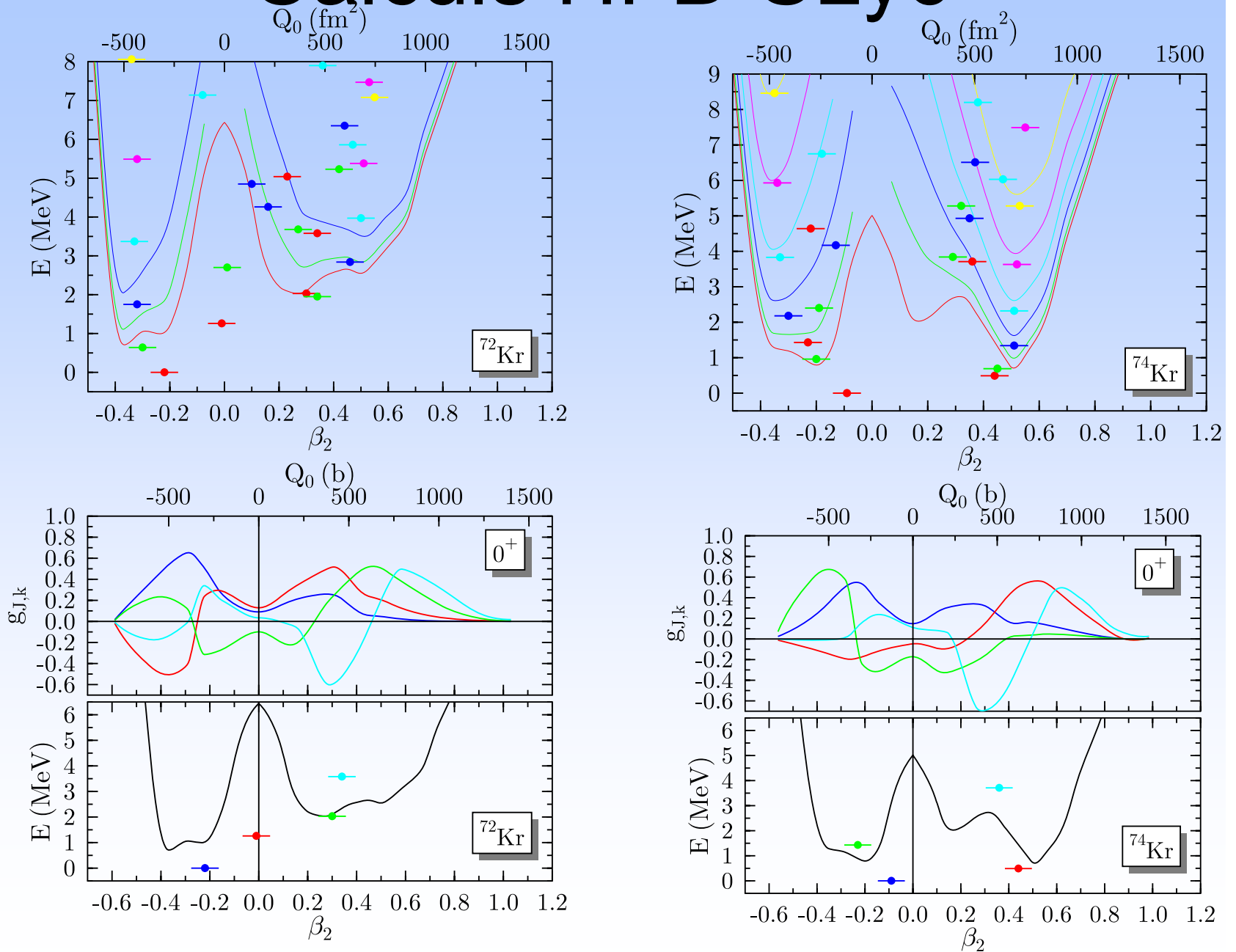
$$\sigma_{E2} \simeq \left( \frac{Z_c e^2}{\hbar c} \right)^2 \frac{\pi}{e^2 b_0^2} B(E2)$$

$$\sigma_{E2} = \frac{N_{\gamma}^{coulex}}{N_{inc} N_{cible/cm^2}}$$

$$B(E2, X) = B(E2, Ref) \frac{\epsilon_{E\gamma}^{rel}(Ref) N_{particule}^{Detecte}(Ref)}{N_{\gamma}^{Det}(Ref)} \frac{N_{\gamma}^{Det}(X)}{\epsilon_{E\gamma}^{rel}(X) N_{particule}^{Detecte}(X)} \mathcal{F}_{cinematique}$$

Noyau	B(E2) Référence	B(E2) déduit [W.u]
$^{66}\text{Ge}$	12.0 (23)	11.7 (1.5)
$^{62}\text{Zn}$	11.7 (9)	10.2 (2.1)
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$^{64}\text{Zn}$	19.5 (6)	21.7 (2.8)

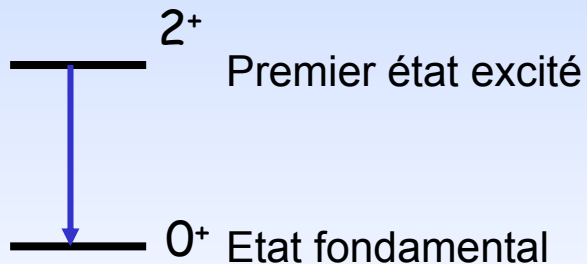
# Calculs HFB-SLy6



# Résultats expérimentaux

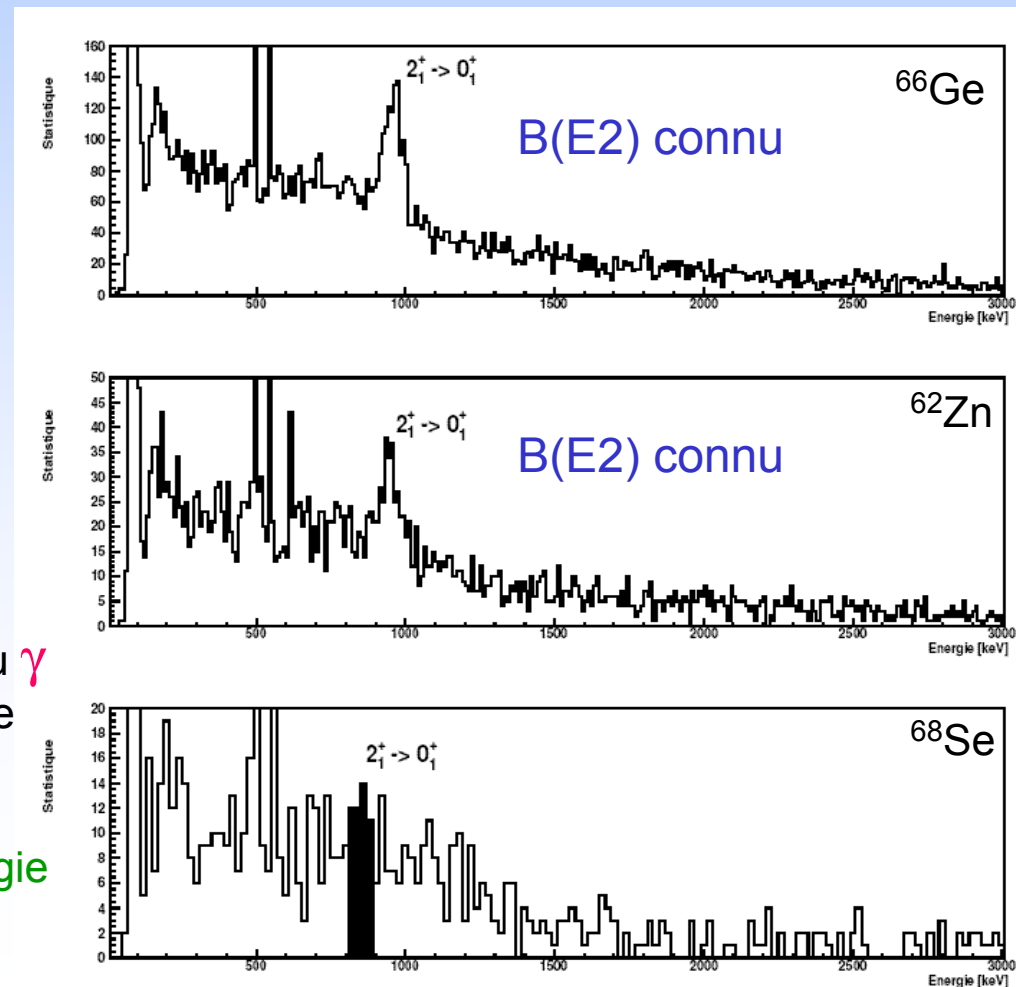
- Excitation Coulombienne des noyaux de  $^{78}\text{Kr}$ ,  $^{72}\text{Ge}$  et  $^{64}\text{Zn}$  pour la **normalisation**
- Intensité du  $^{72}\text{Kr}$  trop faible (**< 54 pps**) pour réaliser l'expérience

- Excitation coulombienne des noyaux radioactifs de  $^{62}\text{Zn}$ ,  $^{66}\text{Ge}$  et  $^{68}\text{Se}$



- Aucune transition **électron** ou  $\gamma$  correspondant à la décroissance de l'état  $0^+_2$  n'a été observée

⇒ Pas d'état  $0^+_2$  à basse énergie



# Faisceaux de normalisation

Le B(E2) mesuré est normalisé à une valeur connue

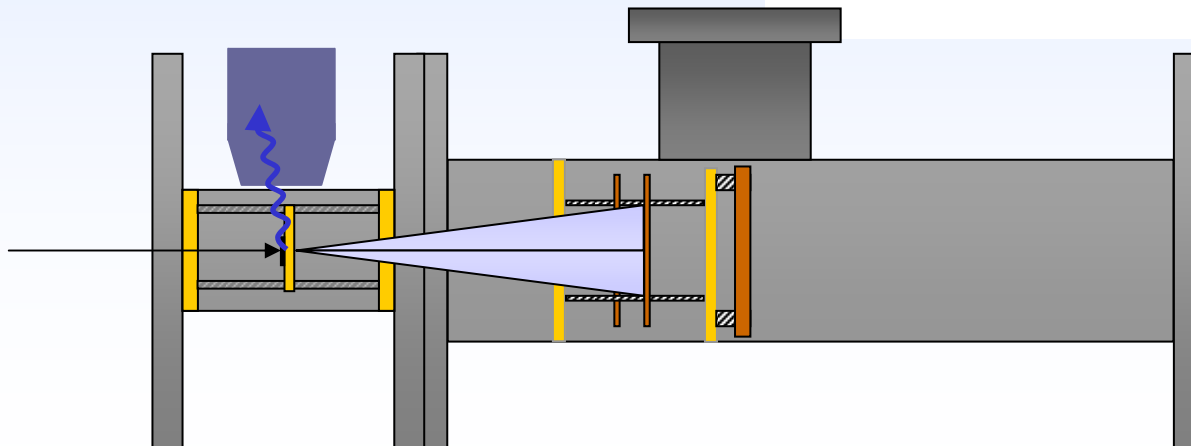
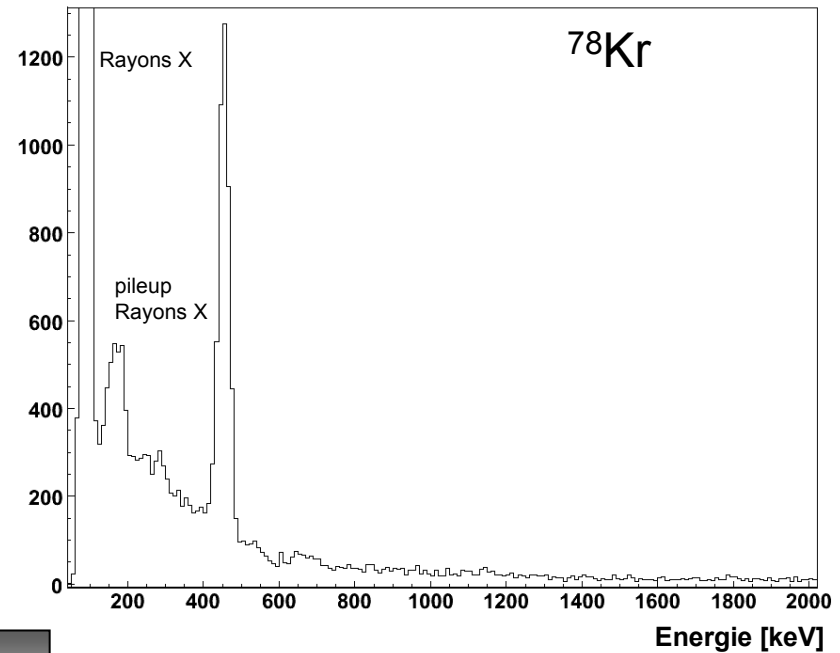
→ « Calibration » du B(E2) en faisceaux stables de  $^{78}\text{Kr}$ ,  $^{72}\text{Ge}$  et  $^{64}\text{Zn}$

Excitation coulombienne

4+ ———

2+ ———

0+ ———



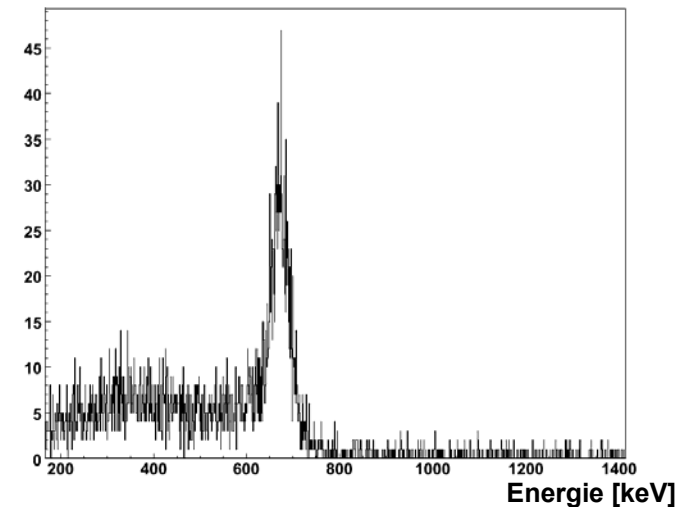
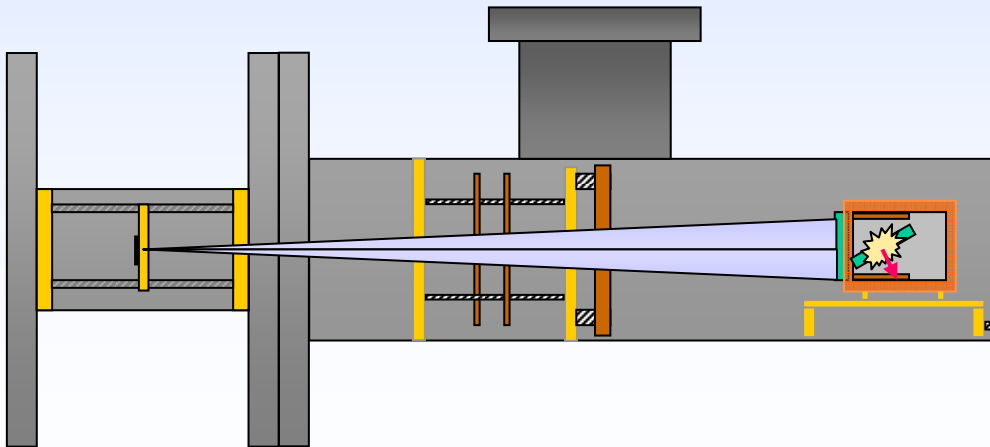
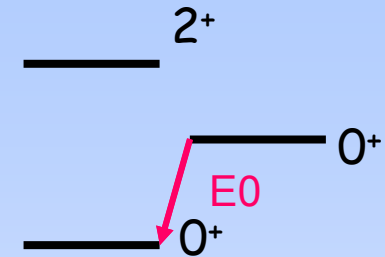
# Spectroscopie isomérique

Isomère  $E_0$  du  $^{72}\text{Ge}$

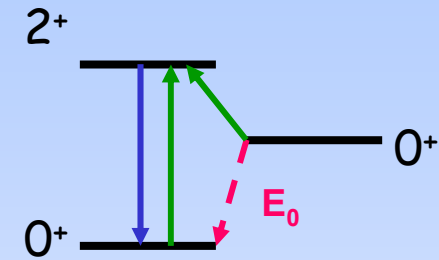
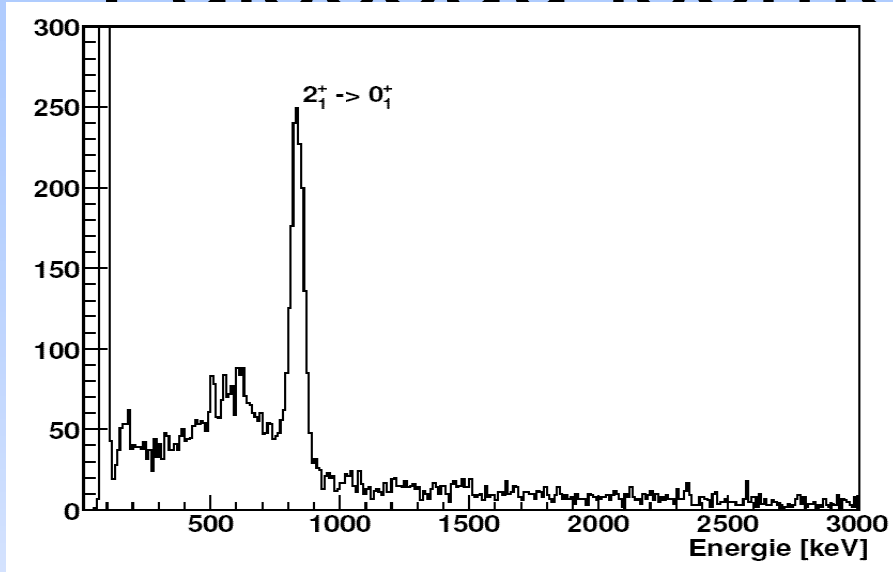
Le premier état excité du  $^{72}\text{Ge}$  est un état  $0^+$ , scénario connu pour le  $^{72}\text{Kr}$  et attendu pour le  $^{68}\text{Se}$

La transition directe entre 2 états  $0^+$  ( $E_0$ ) ne peut se faire par  $\gamma$  mais uniquement par **électrons de conversion**

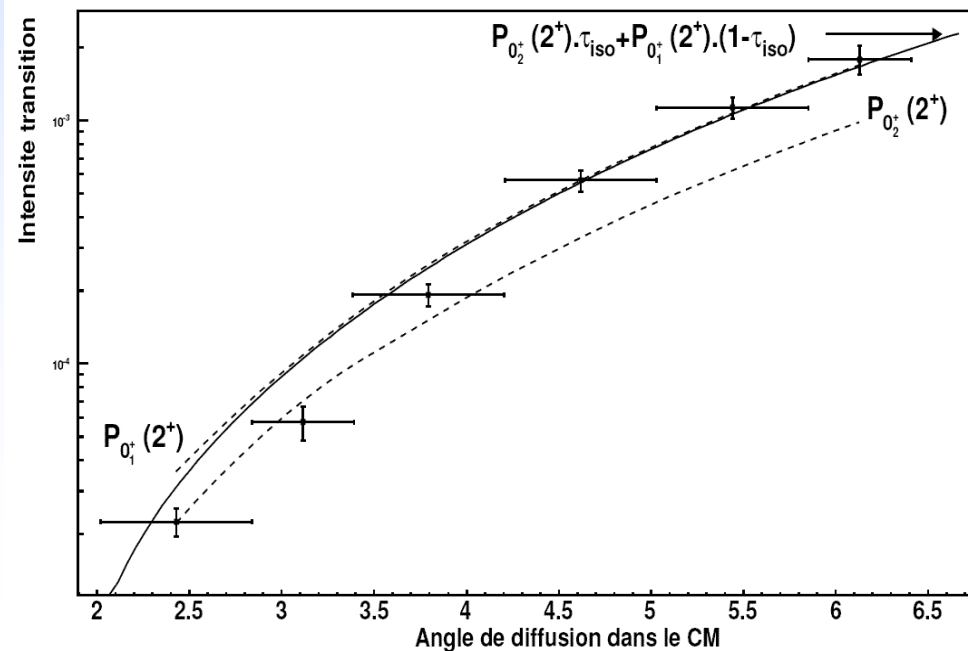
A travers le spectromètre les ions sont complétement **épluchés** de leurs électrons atomiques:  
→ transition  $E_0$  **bloquée** !



# Faisceau isomérique de $^{72}\text{Ge}$

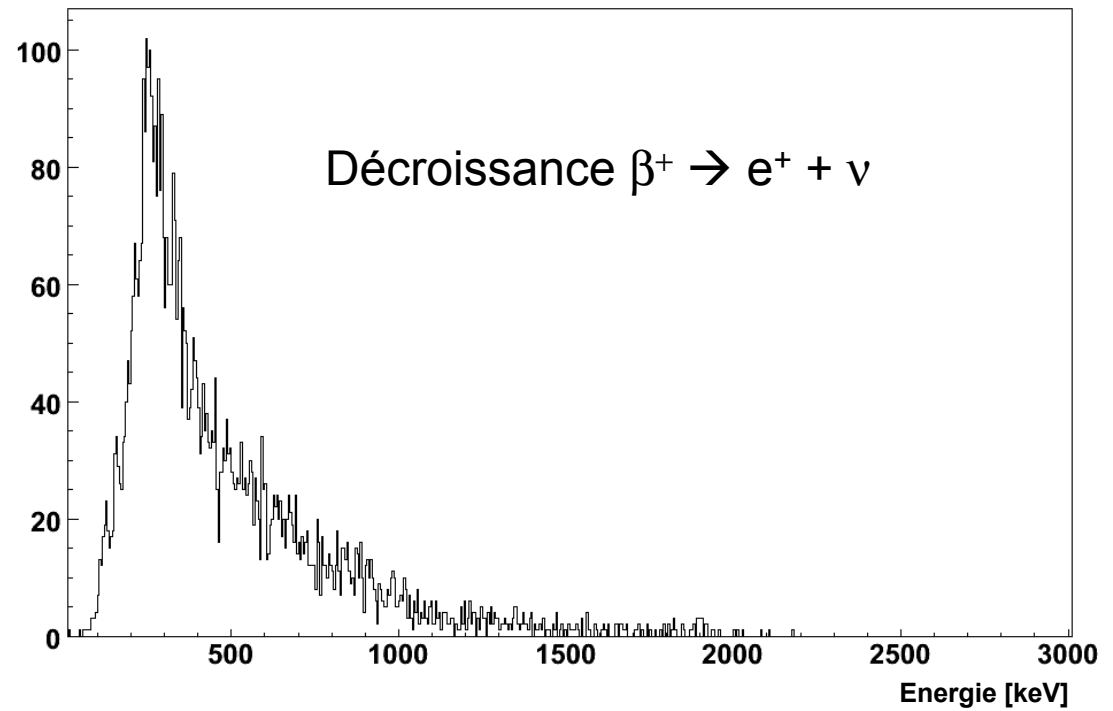
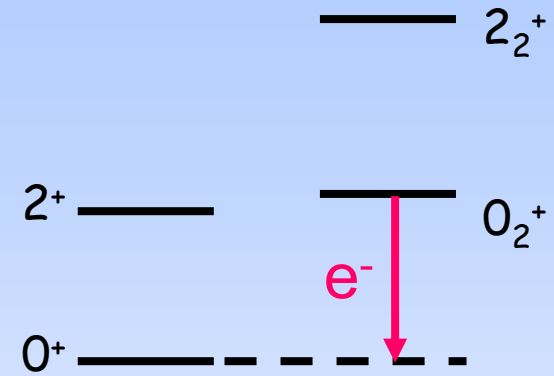
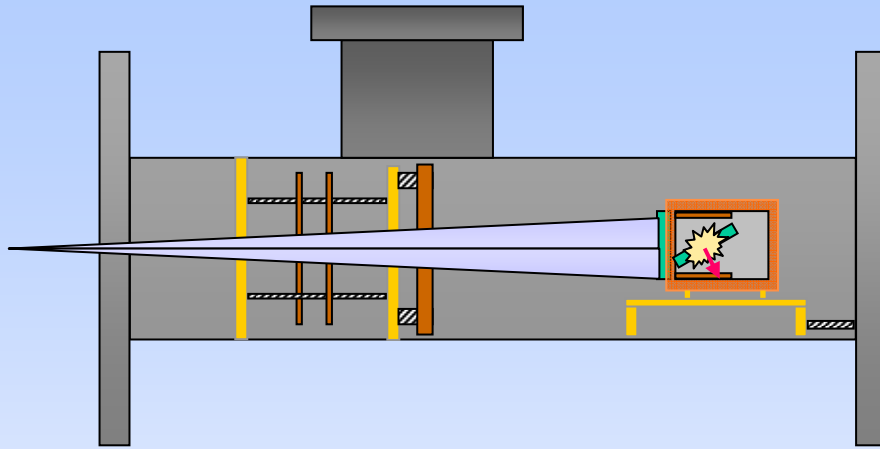


$$\sigma(E2)^{Tot.} = x \cdot \sigma(E2; 0_2^+ \rightarrow 2^+) + (1 - x) \cdot \sigma(E2; 0_1^+ \rightarrow 2^+)$$

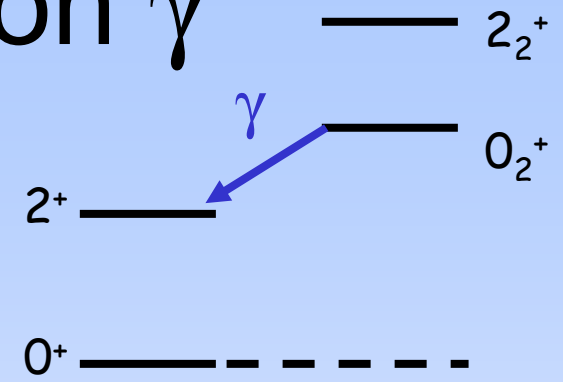
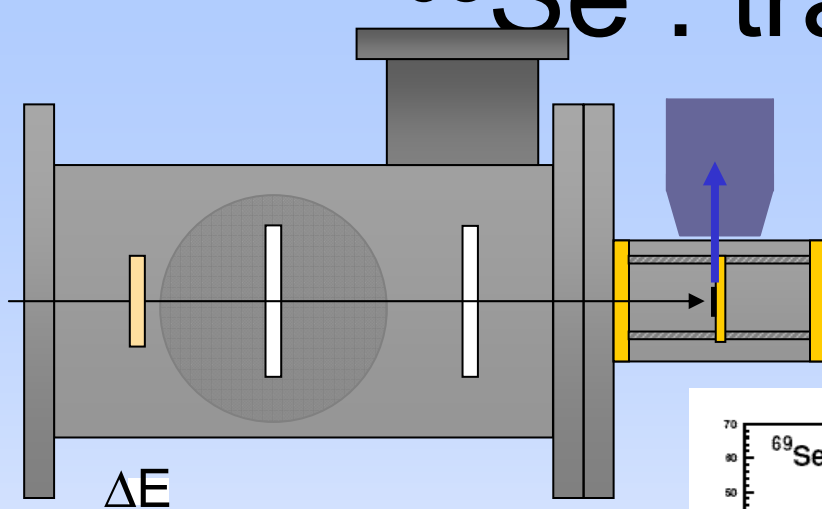




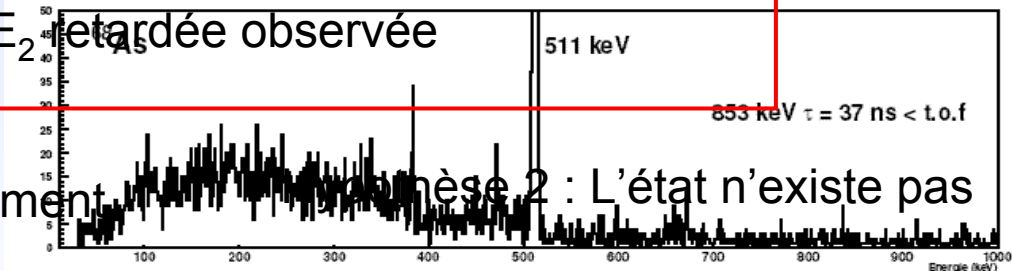
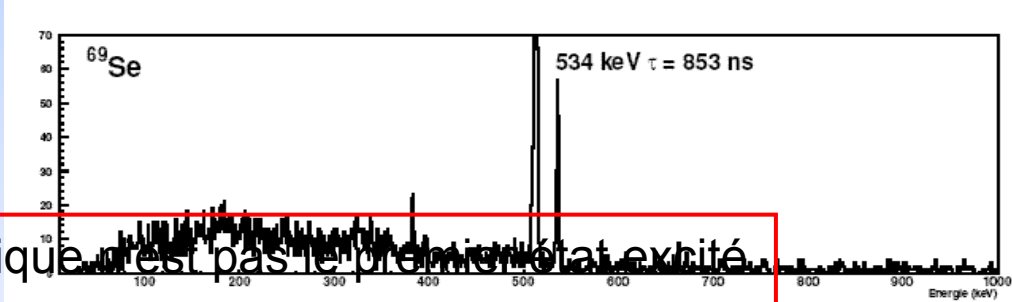
# Spectroscopie nucléaire de $^{68}\text{Se}$ : transition $E_0$



# $^{68}\text{Se}$ : transition $\gamma$



- L'état  $0_2^+$  hypothétique n'est pas le premier état excité
- Aucune transition  $E_2$  retardée observée



Hypothèse 1 : L'état existe vraiment

Hypothèse 2 : L'état n'existe pas

- Temps de vie inférieur au temps de vol dans le spectromètre  $< 1 \mu\text{s}$
- 100 keV au dessus du  $2_1^+$

➤ Pas de coexistence de formes dans les Se légers au delà du  $^{72}\text{Se}$

